

In Expo, algorithm B invoker algorithm A on the string G(S) \$\Omega\$ In where S \in \( \sigma \) \( \sigma \) is random. This is precisely the distribution of Expo fer A. Thus Wo = Pr [B outputs I in Expa] = Pr [A output: I in Expo]

In Exp, algorithm B insokes algorithm A on the string  $t \oplus 1^n$  where  $t \stackrel{R}{\leftarrow} \{o, i\}^n$  is uniformly roudem. The distribution of  $t \oplus 1^n$  is still uniform:

Yue 80,13": Pr[+ = 80,13": + @ 1" = u]

= Pr[t & foils : t = u & 1"] = 1

This means

W, = Pr [B outputs 1 in Exp, ] = Pr [A outputs I in Exp, ]

We carchede then that

PRGAN[B,G]; Wo-W.)

= | Pr [A outputs 1 in Exp.] - Pr [A outputs 1 : Exp.]

which is nonnegligible by assumption. This proves the contrapositive.

The above proof is an example of a security reduction. We show how to reduce the task of breaking G to that of breaking G. This means an attack on G implies an attack on G. Correspondingly, if G is secure (i.e., no efficient attacks receed with non-negligible probability), then the same holds for G.

Refer to the posted notes on the course website as well as the textbook for more examples. We will see more reductions throughout the course as well.

Now we will return to the notion of a secure encryption scheme: Goal is to capture property that no efficient adversary can learn any information about the message given only the ciphertext. Suffices to argue that no efficient adversary can distinguish encryption of message mo from m, even if mo, m, are adversarially-chosen. Let (Encrypt, Decrypt) be a cipher. We define two experiments (parameterized by  $b \in \{0,1\}$ ): adversary mo, m, E m > k & K semantic security experiment Cb 
Encrypt(k,mb) Adversory chooses two messages and receives encryption of one of them. Heels to guess which one (i.e., distinguish encryption of mo from encryption of m,) Let Wo := Pr[b' = 1 | b = 0] } probability that adversary guesses 1 (if adversary is good distinguisher, there two should be very different) W. = Pc[b'=1 | b=1] Define semantic security advantage of adversory A for cipher Tist = (Encrypt, Decrypt) SSALV[A, TSE] = | Wo - WI) <u>Definition</u>. A cipher TSE: (Encrypt, Decrypt) is semantically secure if for all efficient adversaries A, SSAdv[A, TISE] = regl(2) I is a security parameter (here, models the bit-length of the key)