

Step	Annotated Algorithm: $B := L^{-1}B$
1a	$\left\{ B = \hat{B} \right\}$
4	<p>Partition $L \rightarrow \begin{pmatrix} L_{TL} & 0 \\ L_{BL} & L_{BR} \end{pmatrix}$, $B \rightarrow \begin{pmatrix} B_T \\ B_B \end{pmatrix}$,</p> <p>and $\hat{B} \rightarrow \begin{pmatrix} \hat{B}_T \\ \hat{B}_B \end{pmatrix}$</p> <p>where L_{TL} is 0×0, and B_T and \hat{B}_T have 0 rows</p>
2	$\left\{ \left(\frac{B_T}{B_B} \right) = \left(\frac{L_{TL}^{-1} \hat{B}_T}{\hat{B}_B - L_{BL} L_{TL}^{-1} \hat{B}_T} \right) \right\}$
3	while $n(L_{TL}) \neq n(L)$ do
2,3	$\left\{ \left(\left(\frac{B_T}{B_B} \right) = \left(\frac{L_{TL}^{-1} \hat{B}_T}{\hat{B}_B - L_{BL} L_{TL}^{-1} \hat{B}_T} \right) \right) \wedge (n(L_{TL}) \neq n(L)) \right\}$
5a	<p>Repartition</p> <p>$\begin{pmatrix} L_{TL} & 0 \\ L_{BL} & L_{BR} \end{pmatrix} \rightarrow \begin{pmatrix} L_{00} & 0 & 0 \\ l_{10}^T & \lambda_{11} & 0 \\ L_{20} & l_{21} & L_{22} \end{pmatrix}$, $\begin{pmatrix} B_T \\ B_B \end{pmatrix} \rightarrow \begin{pmatrix} B_0 \\ b_1^T \\ B_2 \end{pmatrix}$,</p> <p>and $\begin{pmatrix} \hat{B}_T \\ \hat{B}_B \end{pmatrix} \rightarrow \begin{pmatrix} \hat{B}_0 \\ \hat{b}_1^T \\ \hat{B}_2 \end{pmatrix}$</p> <p>where λ_{11} is a scalar and b_1^T and \hat{b}_1^T are rows</p>
6	$\left\{ \left(\frac{B_0}{b_1^T} \right) = \left(\frac{L_{00}^{-1} \hat{B}_0}{\hat{b}_1^T - l_{10}^T L_{00}^{-1} \hat{B}_0} \right) \right\}$
8	$b_1^T := \hat{b}_1^T / \lambda_{11}$ $\hat{B}_2 := \hat{B}_2 - l_{21} b_1^T$
5b	<p>Continue with</p> <p>$\begin{pmatrix} L_{TL} & 0 \\ L_{BL} & L_{BR} \end{pmatrix} \leftarrow \begin{pmatrix} L_{00} & 0 & 0 \\ l_{10}^T & \lambda_{11} & 0 \\ L_{20} & l_{21} & L_{22} \end{pmatrix}$, $\begin{pmatrix} B_T \\ B_B \end{pmatrix} \leftarrow \begin{pmatrix} B_0 \\ b_1^T \\ B_2 \end{pmatrix}$,</p> <p>and $\begin{pmatrix} \hat{B}_T \\ \hat{B}_B \end{pmatrix} \leftarrow \begin{pmatrix} \hat{B}_0 \\ \hat{b}_1^T \\ \hat{B}_2 \end{pmatrix}$</p>
7	$\left\{ \left(\frac{B_0}{b_1^T} \right) = \left(\frac{L_{00}^{-1} \hat{B}_0}{\lambda_{11}^{-1} (\hat{b}_1^T - l_{10}^T L_{00}^{-1} \hat{B}_0)} \right) \right\}$
2	$\left\{ \left(\frac{B_T}{B_B} \right) = \left(\frac{L_{TL}^{-1} \hat{B}_T}{\hat{B}_B - L_{BL} L_{TL}^{-1} \hat{B}_T} \right) \right\}$
	enddo
2,3	$\left\{ \left(\left(\frac{B_T}{B_B} \right) = \left(\frac{L_{TL}^{-1} \hat{B}_T}{\hat{B}_B - L_{BL} L_{TL}^{-1} \hat{B}_T} \right) \right) \wedge \neg (n(L_{TL}) \neq n(L)) \right\}$
1b	$\left\{ B = L^{-1} \hat{B} \right\}$

Figure 1: Worksheet for deriving unblocked algorithm for $B := L^{-1}B$ (Variant 2).

Partition $L \rightarrow \left(\begin{array}{c|c} L_{TL} & 0 \\ \hline L_{BL} & \| L_{BR} \end{array} \right)$, and $B \rightarrow \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right)$

where L_{TL} is 0×0 and B_T has 0 rows

while $n(L_{TL}) \neq n(L)$ **do**

Repartition

$$\left(\begin{array}{c|c} L_{TL} & 0 \\ \hline L_{BL} & \| L_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c|c|c} L_{00} & 0 & 0 \\ \hline l_{10}^T & \lambda_{11} & 0 \\ \hline L_{20} & l_{21} & L_{22} \end{array} \right) \text{ and } \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \rightarrow \left(\begin{array}{c} B_0 \\ \hline \frac{b_1^T}{B_2} \end{array} \right)$$

where λ_{11} is a scalar and b_1^T is a row

$$b_1^T := b_1^T / \lambda_{11}$$

$$\hat{B}_2 := B_2 - l_{21} b_1^T$$

Continue with

$$\left(\begin{array}{c|c} L_{TL} & 0 \\ \hline L_{BL} & \| L_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c|c|c} L_{00} & 0 & 0 \\ \hline l_{10}^T & \lambda_{11} & 0 \\ \hline L_{20} & l_{21} & L_{22} \end{array} \right), \quad \left(\begin{array}{c} B_T \\ \hline B_B \end{array} \right) \leftarrow \left(\begin{array}{c} B_0 \\ \hline \frac{b_1^T}{B_2} \end{array} \right),$$

$$\text{and } \left(\begin{array}{c} \hat{B}_T \\ \hline \hat{B}_B \end{array} \right) \leftarrow \left(\begin{array}{c} \hat{B}_0 \\ \hline \frac{\hat{b}_1^T}{\hat{B}_2} \end{array} \right)$$

enddo

Figure 2: Algorithm for deriving unblocked algorithm for $B := L^{-1}B$ (Variant 2).