Hierarchical Modeling



Reading

Angel, sections 9.1 - 9.6 [reader pp. 169-185] *OpenGL Programming Guide*, chapter 3
Focus especially on section titled "Modelling Transformations".



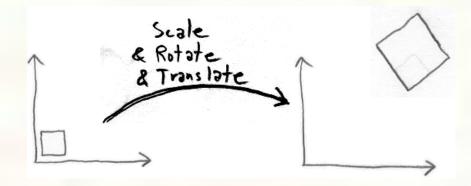
Hierarchical Modeling

Consider a moving automobile, with 4 wheels attached to the chassis, and lug nuts attached to each wheel:



Symbols and instances

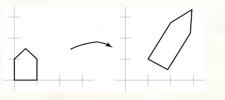
- Most graphics APIs support a few geometric primitives:
 - spheres
 - cubes
 - triangles
- These symbols are instanced using an instance transformation.



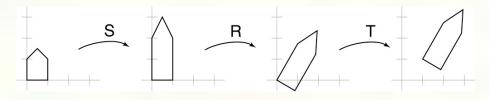


Use a series of transformations

Ultimately, a particular geometric instance is transformed by one combined transformation matrix:



But it's convenient to build this single matrix from a series of simpler transformations:



We have to be careful about how we think about composing these transformations.

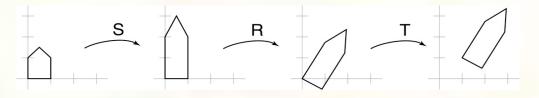
(Mathematical reason: Transformation matrices don't commute under matrix multiplication)



Two ways to compose xforms

Method #1:

Express every transformation with respect to global coordinate system:



Method #2:

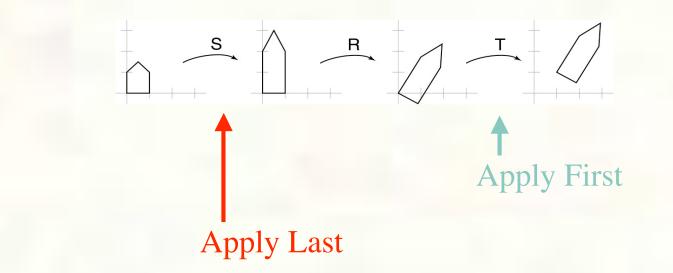
Express every transformation with respect to a "parent" coordinate system created by earlier transformations:



The goal of this second approach is to build a series of transforms. Once they exist, we can think of points as being "processed" by these xforms as in Method #1



#1: Xform for global coordinates



FinalPosition = $M_1 * M_2 * ... * M_n * InitialPosition$

Note: Positions are column vectors:

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yz



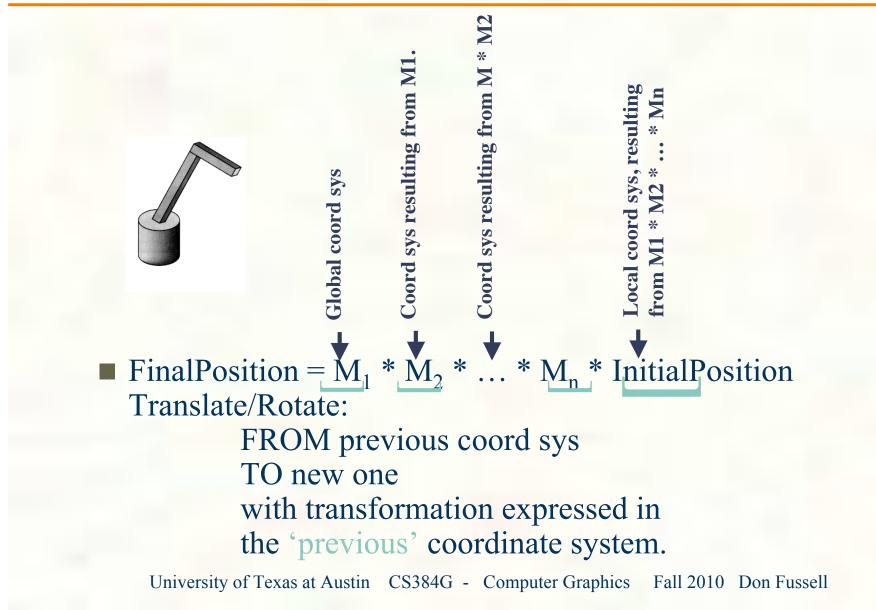
#2: Xform for coordinate system



FinalPosition = $M_1 * M_2 * ... * M_n *$ InitialPosition



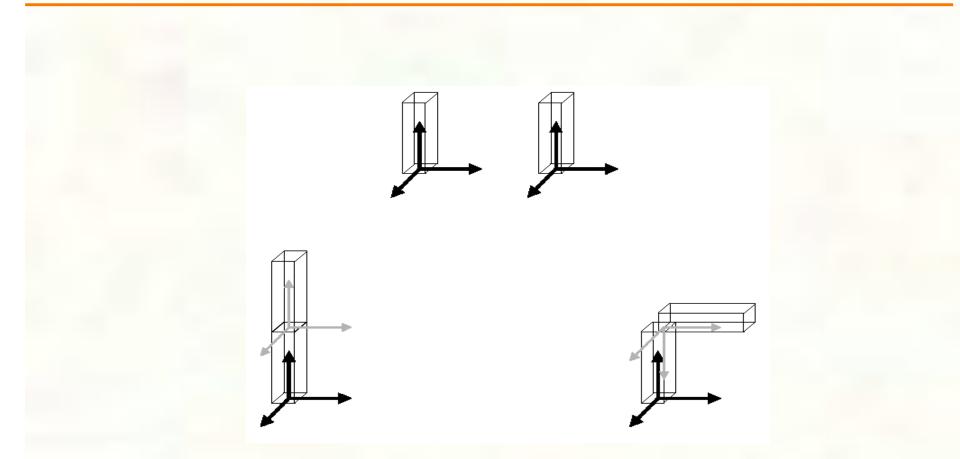
Xform direction for coord. sys



9



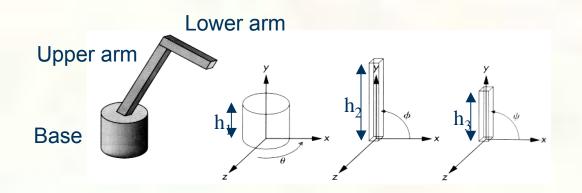
Connecting primitives





3D Example: A robot arm

- Consider this robot arm with 3 degrees of freedom:
 - Base rotates about its vertical axis by θ
 - Upper arm rotates in its xy-plane by \$\phi\$
 - Lower arm rotates in its *xy*-plane by ψ



Q: What matrix do we use to transform the base?
Q: What matrix for the upper arm?
Q: What matrix for the lower arm?
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Robot arm implementation

The robot arm can be displayed by keeping a global matrix and computing it at each step:

```
Matrix M model;
main()
    robot_arm();
robot_arm()
    M \mod l = R y(theta);
    base();
    M_model = R_y(theta) *T(0,h1,0) *R_z(phi);
    upper_arm();
    M_model = R_y(theta) *T(0,h1,0) *R_z(phi)
                           *T(0,h2,0)*R z(psi);
    lower arm();
}
```

Do the matrix computations seem wasteful?



Robot arm implementation, better

Instead of recalculating the global matrix each time, we can just update it *in place* by concatenating matrices on the right:

```
Matrix M model;
main()
    M_model = Identity();
    robot_arm();
robot_arm()
    M_model *= R_y(theta);
    base();
    M_{model} *= T(0, h1, 0) * R_z(phi);
    upper_arm();
    M_{model} *= T(0, h2, 0) * R_z(psi);
    lower_arm();
```

Robot arm implementation, OpenGL

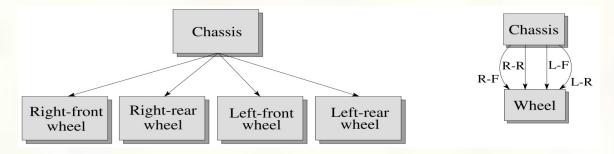
 OpenGL maintains a global state matrix called the model-view matrix, which is updated by concatenating matrices on the *right*.

```
main()
{
    glMatrixMode( GL MODELVIEW );
    glLoadIdentity();
    robot_arm();
robot arm()
{
    glRotatef( theta, 0.0, 1.0, 0.0 );
    base();
    glTranslatef( 0.0, h1, 0.0 );
    glRotatef( phi, 0.0, 0.0, 1.0 );
    lower_arm();
    glTranslatef( 0.0, h2, 0.0 );
    glRotatef( psi, 0.0, 0.0, 1.0 );
    upper arm();
}
```



Hierarchical modeling

Hierarchical models can be composed of instances using trees or DAGs:

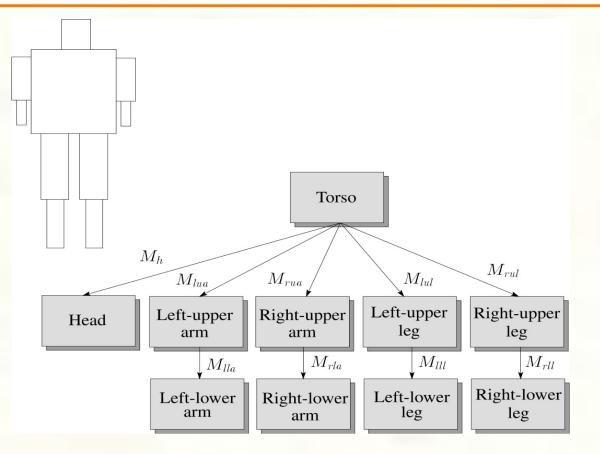


edges contain geometric transformations
 nodes contain geometry (and possibly drawing attributes)

How might we draw the tree for the robot arm?



A complex example: human figure



Q: What's the most sensible way to traverse this tree?



Human figure implementation, OpenGL

figure()

{

}

```
torso();
glPushMatrix();
    glTranslate( ... );
    glRotate( ... );
    head();
glPopMatrix();
glPushMatrix();
    glTranslate( ... );
    glRotate( ... );
    left upper arm();
    glPushMatrix();
        glTranslate( ... );
        glRotate( ... );
        left lower arm();
    glPopMatrix();
 glPopMatrix();
```



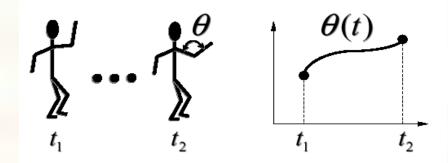
The above examples are called articulated models:

- rigid parts
- connected by joints
- They can be animated by specifying the joint angles (or other display parameters) as functions of time.



Key-frame animation

- The most common method for character animation in production is key-frame animation.
 - Each joint specified at various key frames (not necessarily the same as other joints)
 - System does interpolation or **in-betweening**
- Doing this well requires:
 - A way of smoothly interpolating key frames: **splines**
 - A good interactive system
 - A lot of skill on the part of the animator





Scene graphs

- The idea of hierarchical modeling can be extended to an entire scene, encompassing:
 many different objects
 lights
 camera position
- This is called a scene tree or scene graph.

