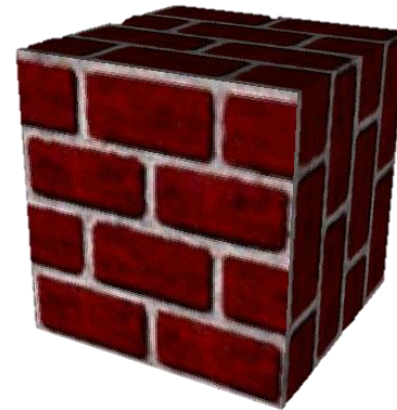


# Texturing

# Basic Idea

Paint pictures on all of your polygons

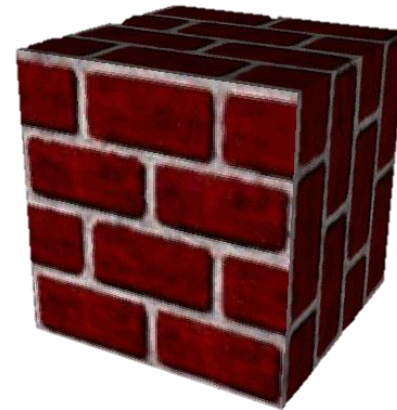
- adds color data
- adds (fake) geometric and texture detail



# Basic Idea

Paint pictures on all of your polygons

- adds color data
- adds (fake) geometric and texture detail



one of **the** basic graphics techniques

- tons of hardware support

# Sprites

Draw object for a few states / from a few viewpoints



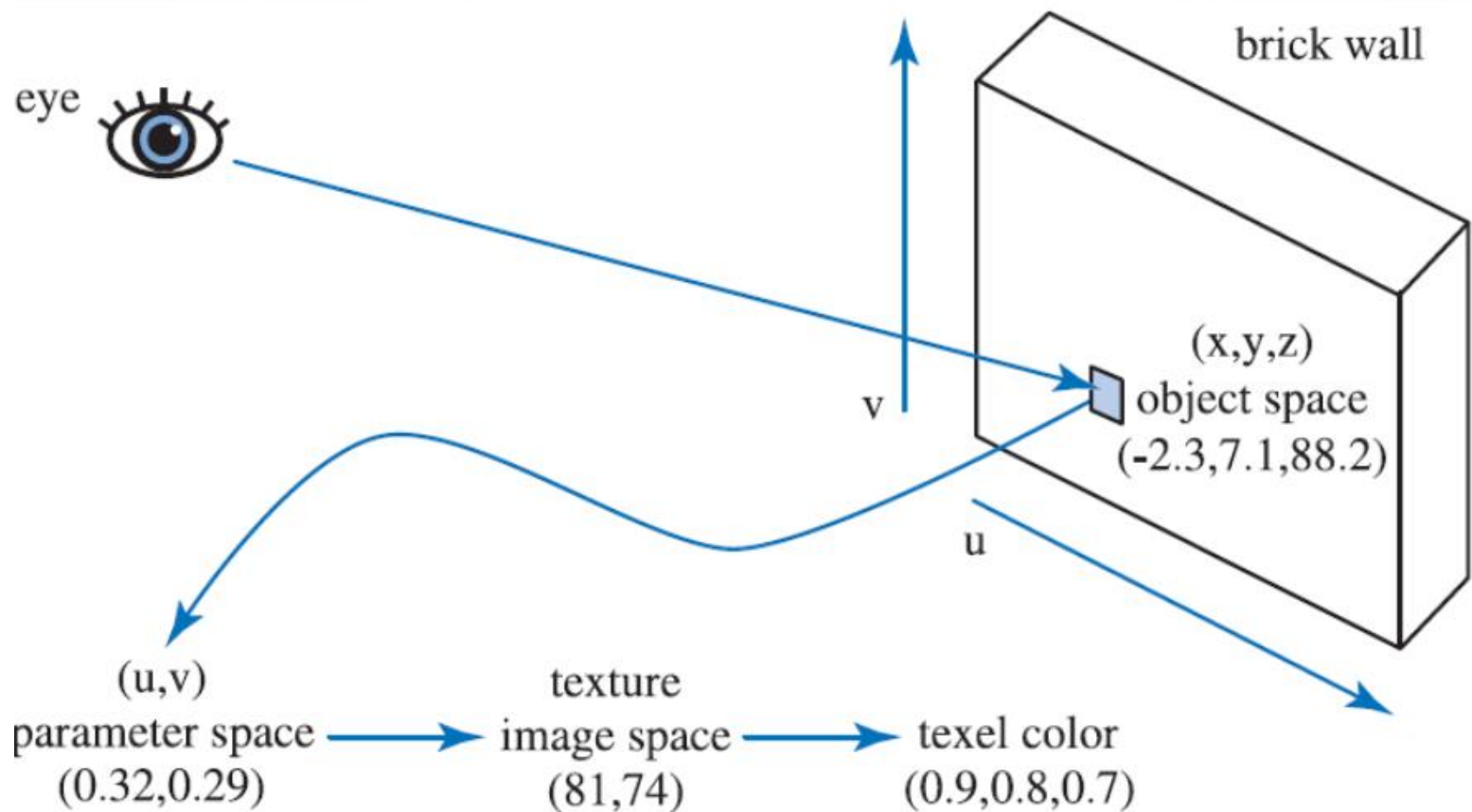
# Sprites

Draw object for a few states / from a few viewpoints

Then copy closest matching image directly to screen



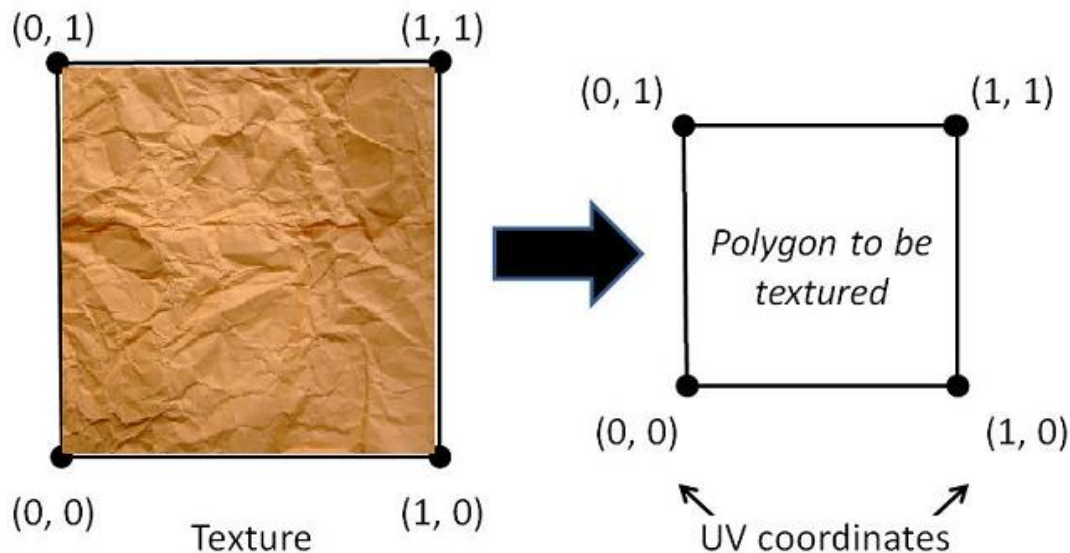
# True Texture Mapping



# True Texture Mapping

Texture map: map from **object** to **texture** coordinates  $(u,v)$  to **bitmap pixels**

- last lecture: how to generate UVs



# Texture Mapping Algorithm

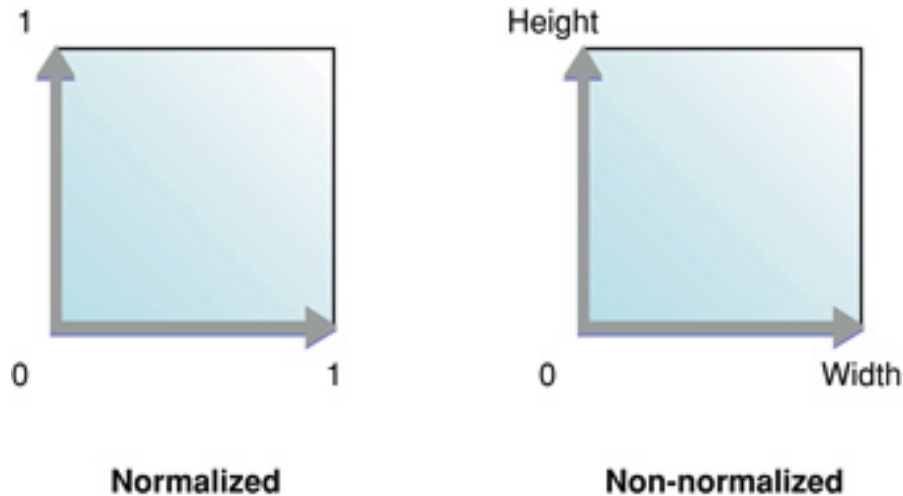
For every pixel:

- compute pixel's  $(u,v)$  using barycentric interpolation
- look up texture pixel (**texel**) at  $(u,v)$
- copy color to pixel
- apply shading



# Texture Mapping: Details

Two texture coordinate conventions:



Doesn't matter which you use, but must be consistent

# Texture Mapping: Details

What if  $(u,v)$  is out of range?



repeat



mirror



clamp



background

# Texture Mapping: Details

What if  $(u,v)$  aren't integers?

Option 1: snap to nearest texel



# Texture Mapping: Details

What if  $(u,v)$  aren't integers?

Option 2: linearly interpolate color



# Texture Mapping: Details

What if  $(u,v)$  is out of range?

What if  $(u,v)$  aren't integers?

These are both parts of **sampling**

- extracting color from bitmap given  $(u,v)$

# Texture Mapping: Details

What if  $(u,v)$  is out of range?

What if  $(u,v)$  aren't integers?

These are both parts of **sampling**

- extracting color from bitmap given  $(u,v)$
- sampling methods (**filters**) can improve quality/jagginess of textured objects

# Texture Mapping: Details

A few more minor details:

- texture sizes traditionally powers of 2

# Texture Mapping: Details

A few more minor details:

- texture sizes traditionally powers of 2
- textures usually compressed on GPU



# Texture Mapping: Details

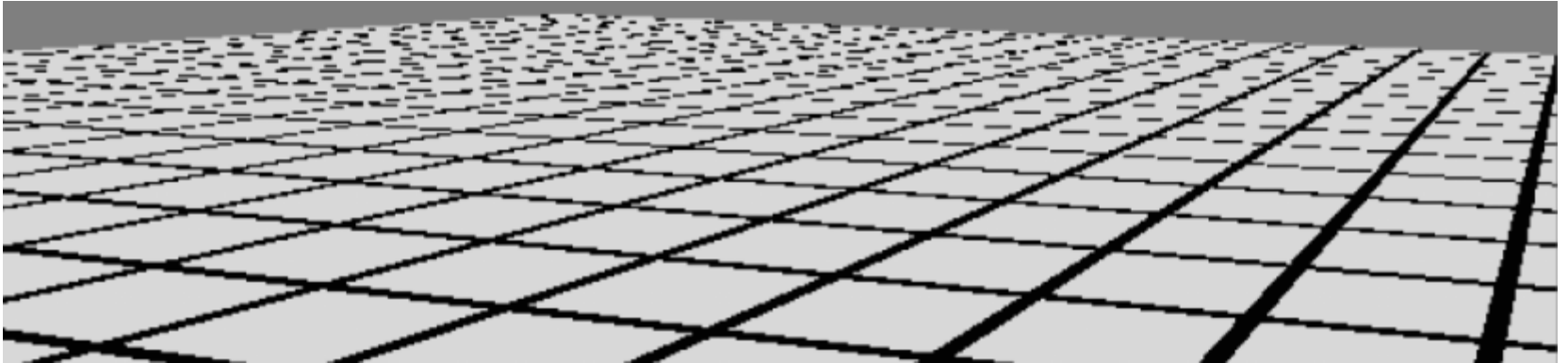
A few more minor details:

- texture sizes traditionally powers of 2
- textures usually compressed on GPU
- textures can be 3D
  - huge memory hog!



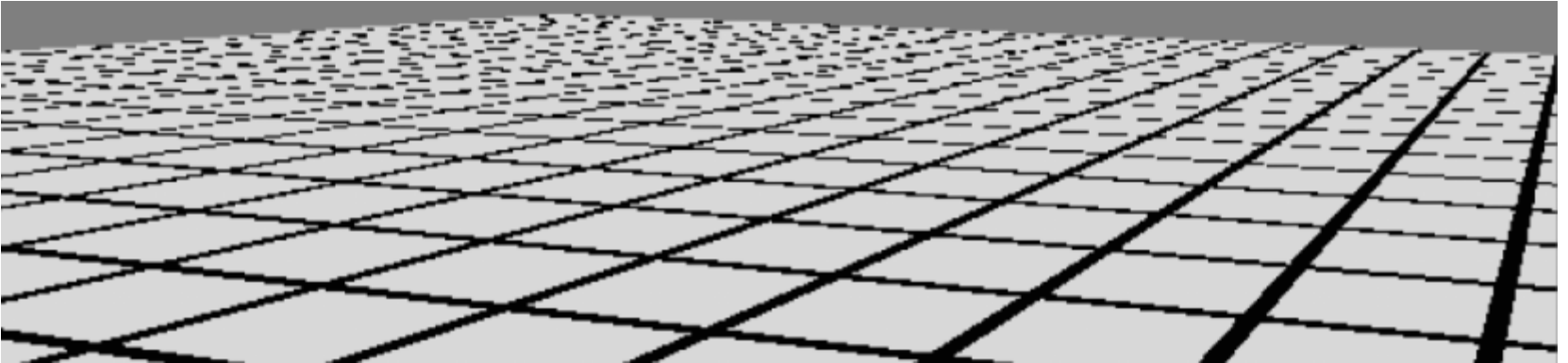
# Advanced Sampling

Problem:



# Advanced Sampling

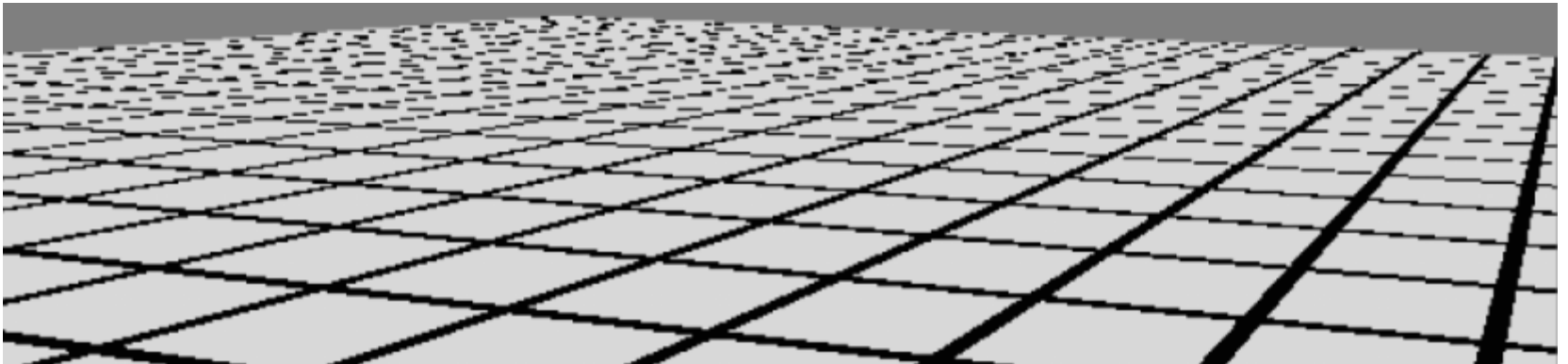
Problem:



No correlation between pixels and texels

# Advanced Sampling

Problem:

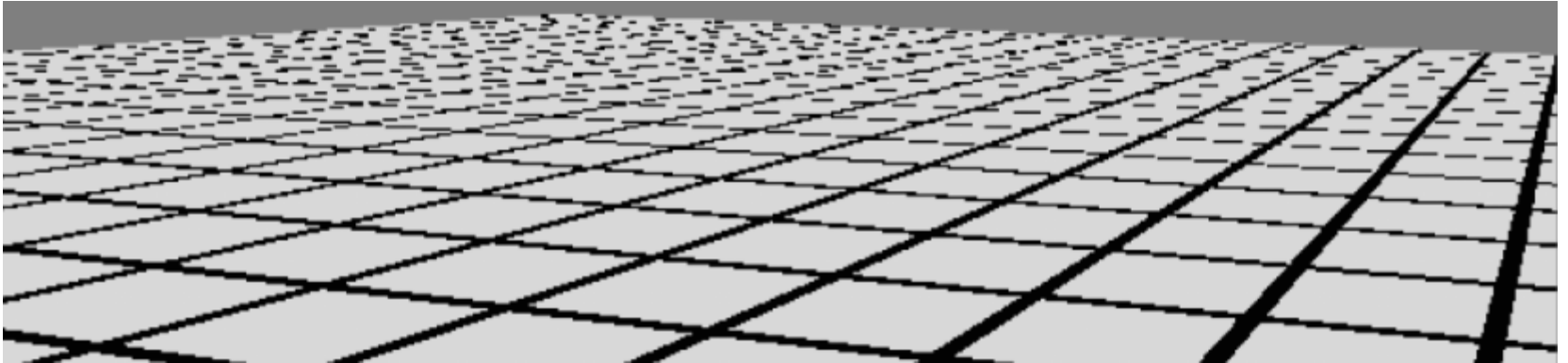


No correlation between pixels and texels

Too many texels per pixel: aliasing

# Advanced Sampling

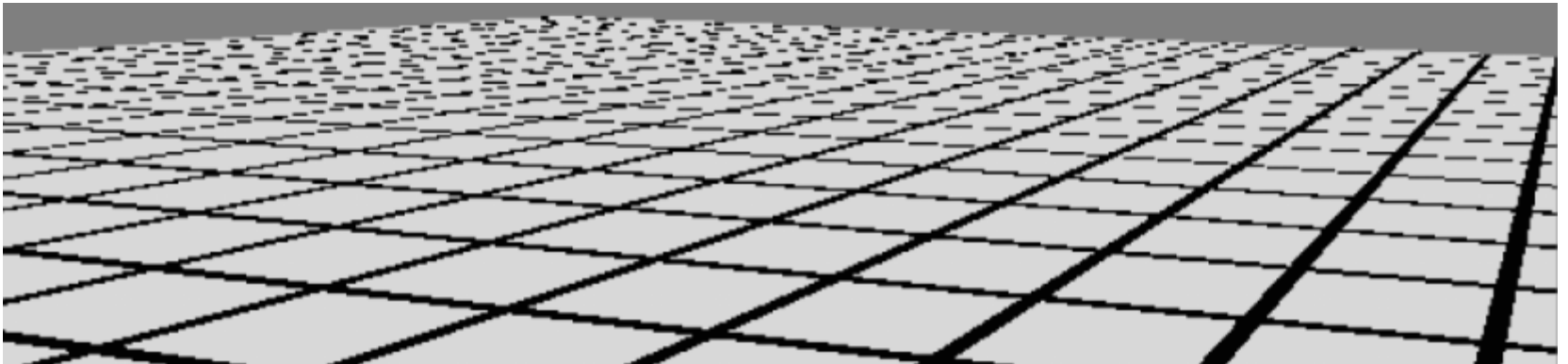
Problem:



No correlation between pixels and texels  
Sample many texels and average?

# Advanced Sampling

Problem:

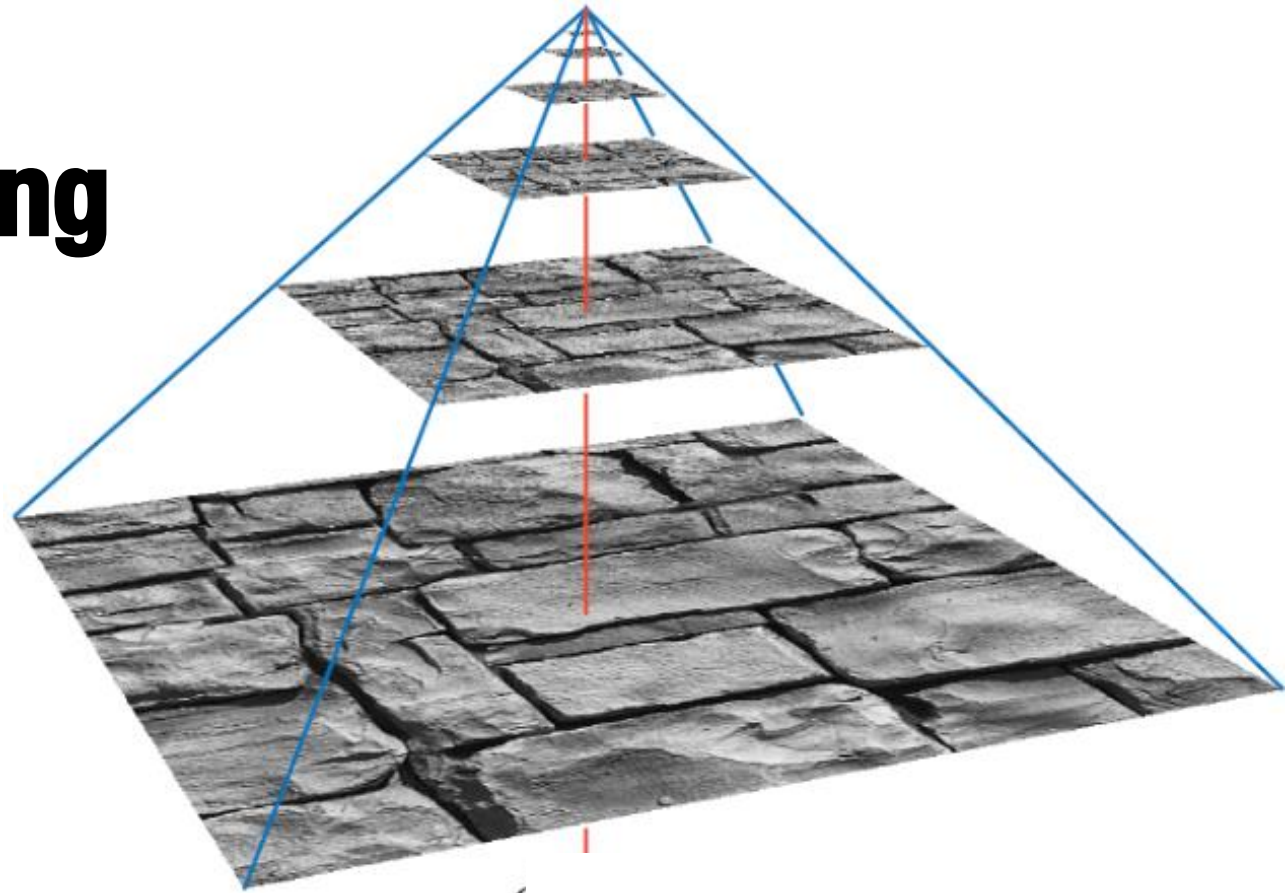


No correlation between pixels and texels

Sample many texels and average?

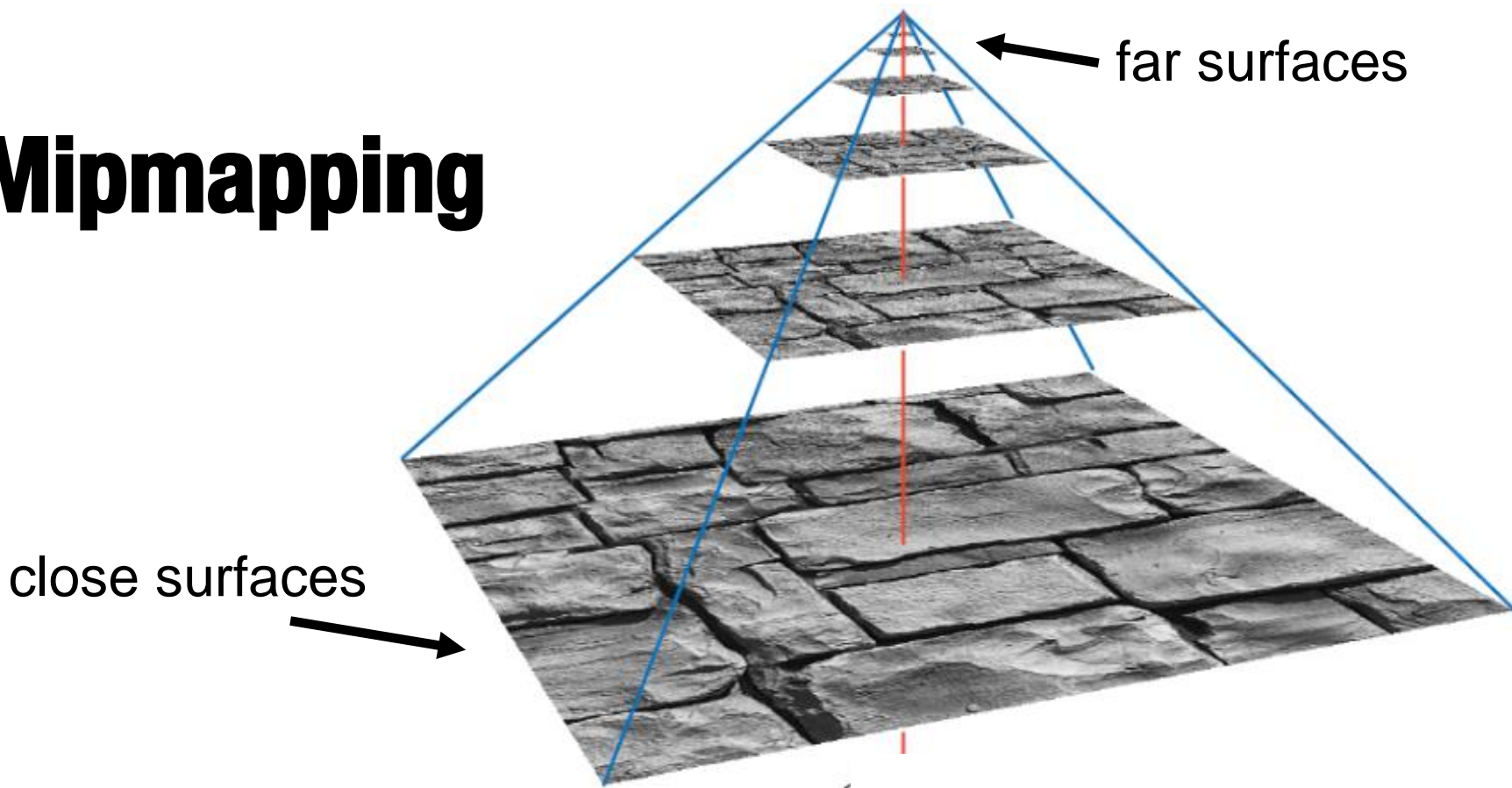
- works but very slow

# Mipmapping



Main idea: store hierarchy of subsampled textures

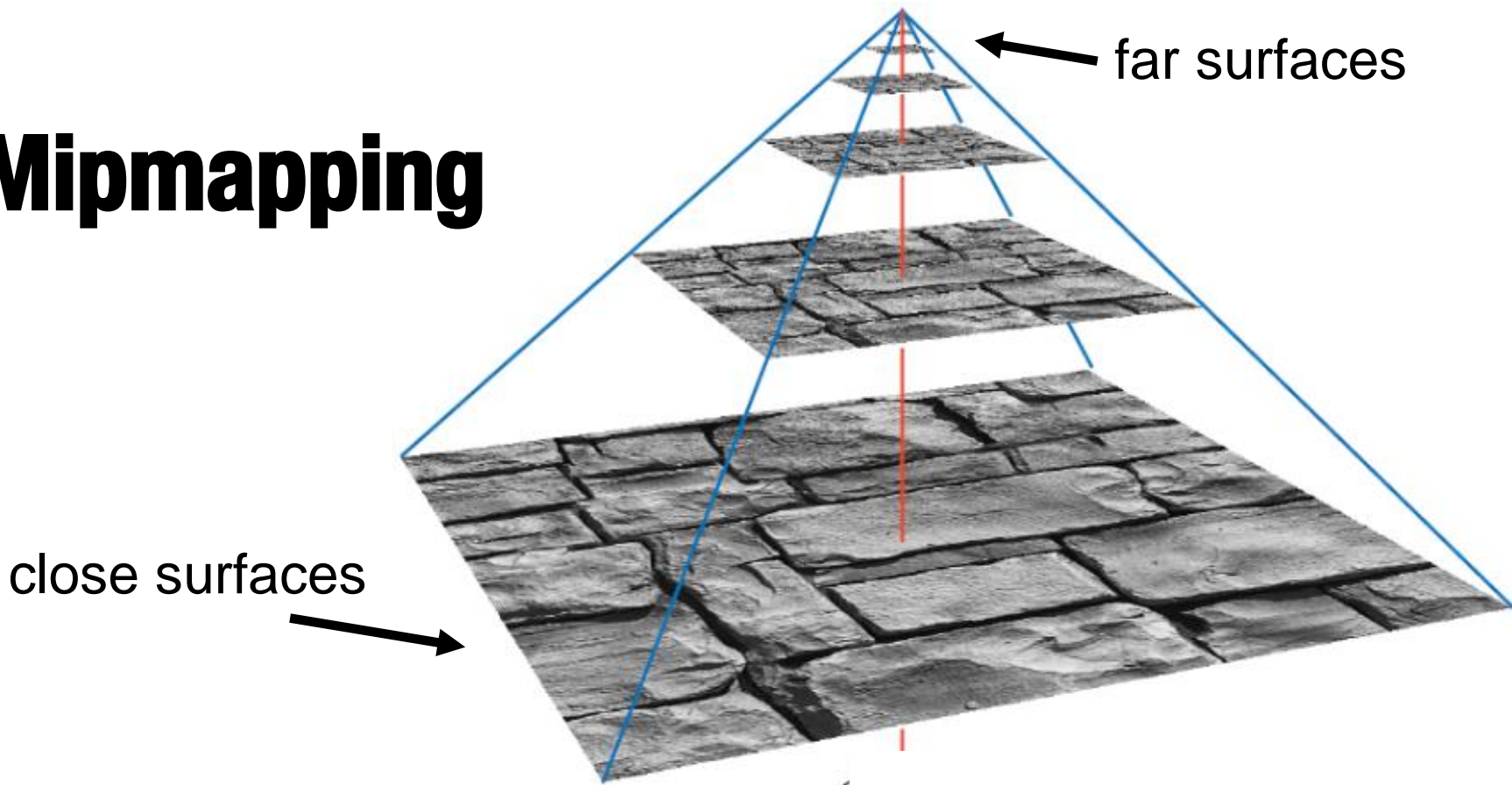
# Mipmapping



Main idea: store hierarchy of subsampled textures

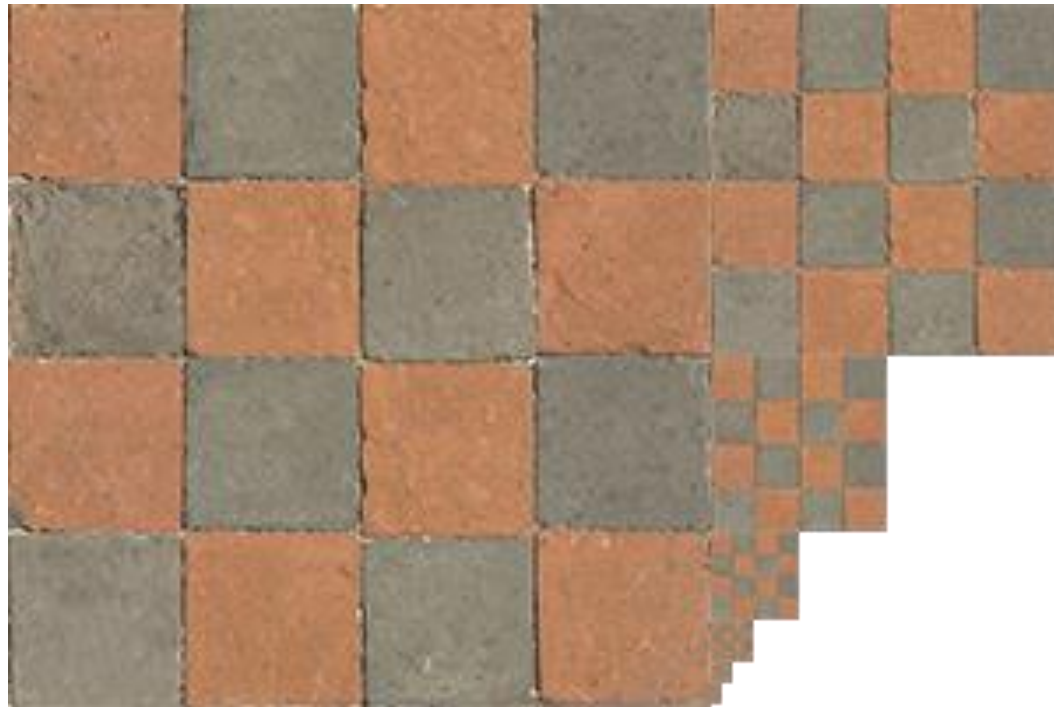


# Mipmapping



How expensive is this?

# Mipmapping



~50% more memory consumed

# Bilinear Filtering

Average four nearest texels



Eliminates “blockiness”/pixellation

# Trilinear Filtering

Classic problem in games: popping



# Trilinear Filtering

Classic problem in games: popping



different mipmap levels

Can fix by averaging neighboring levels

# Anisotropic Filtering

Use non-square pyramid levels



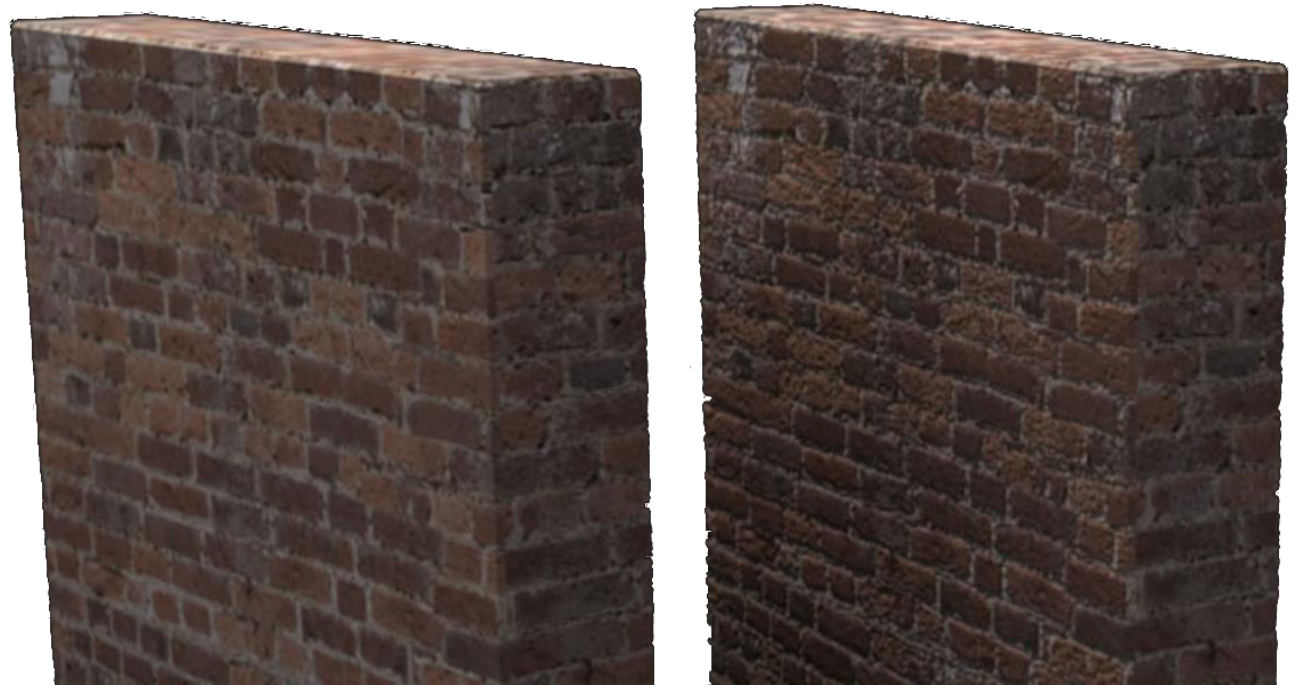
Compute them on the fly

# Texture Mapping Flaws

Texture map adds fake geometric detail

- but still looks **flat**

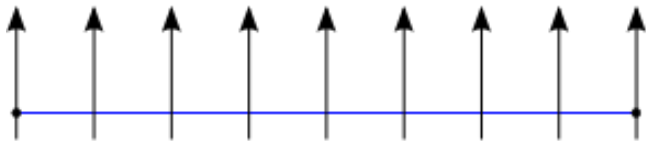
Why?



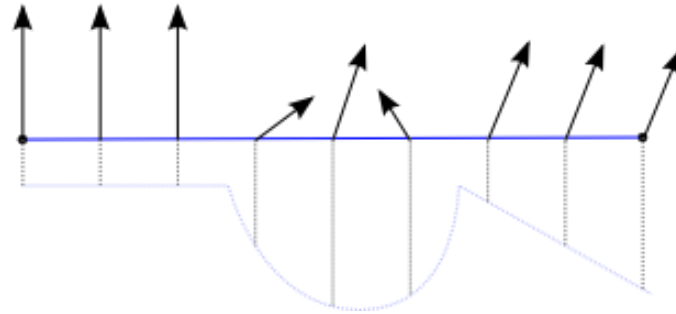
# Normal Map

Key idea: modify normals of flat face

Unmapped face



Normal-mapped face

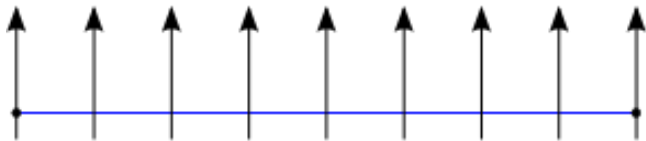




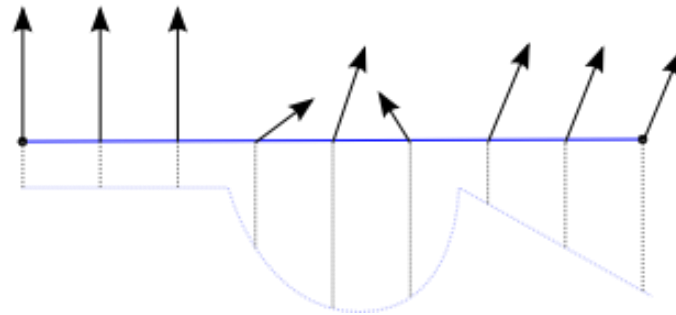
# Normal Map

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Normal-mapped face

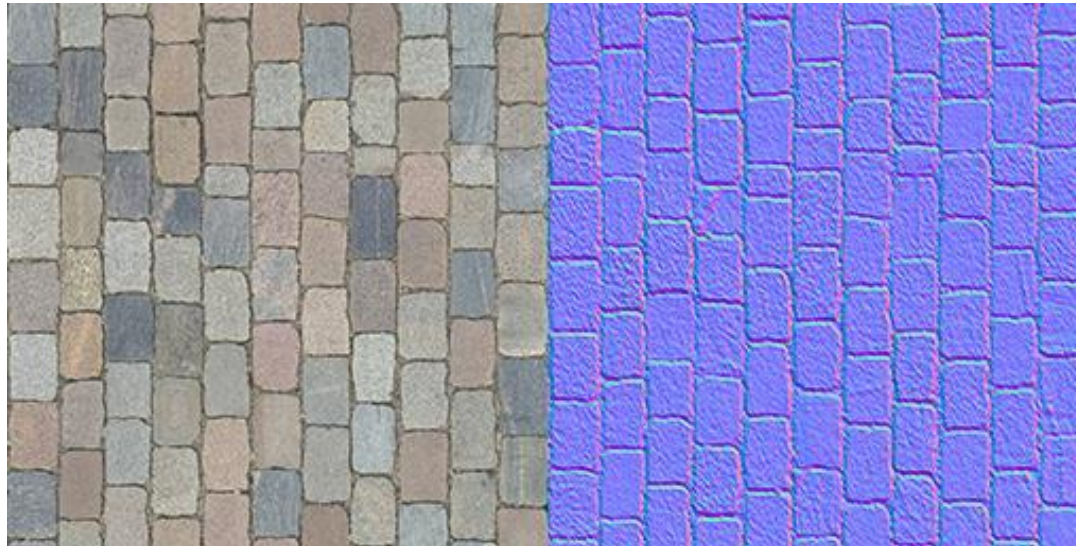


Rendered surface

- **is flat**
- shaded as if it were bumpy

# Normal Map

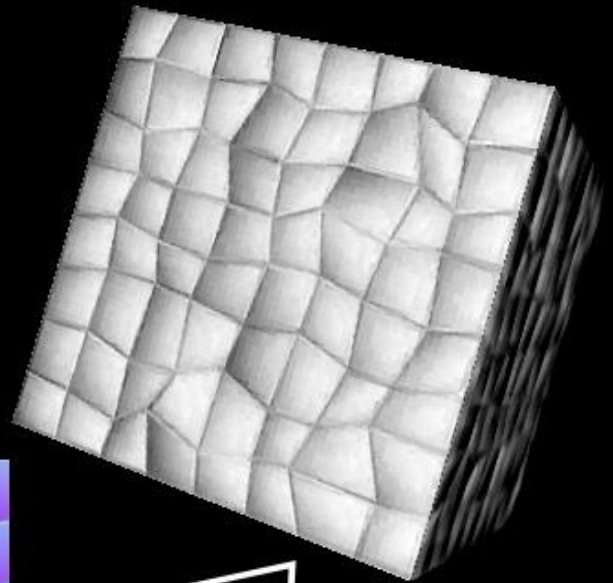
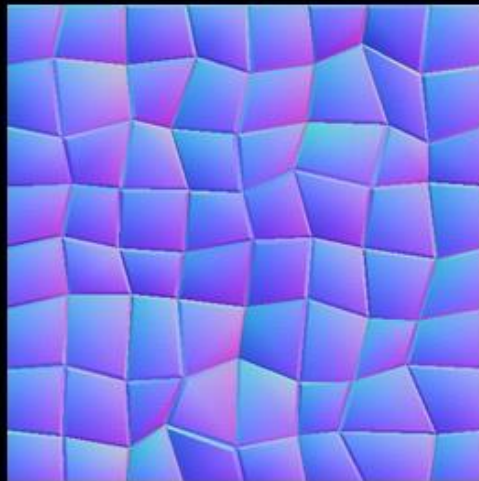
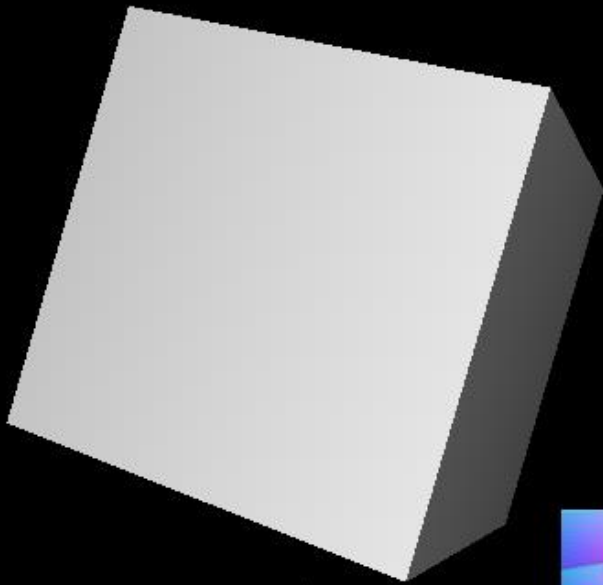
How to represent normals?



Encode as second texture (same size)

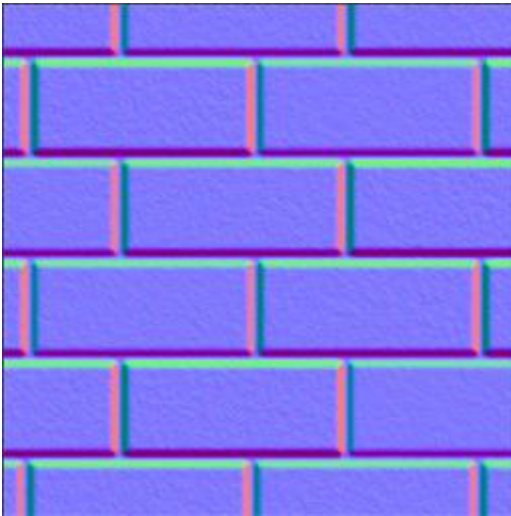
- (r,g,b) encodes coordinates of normal

# Applying Normal Map



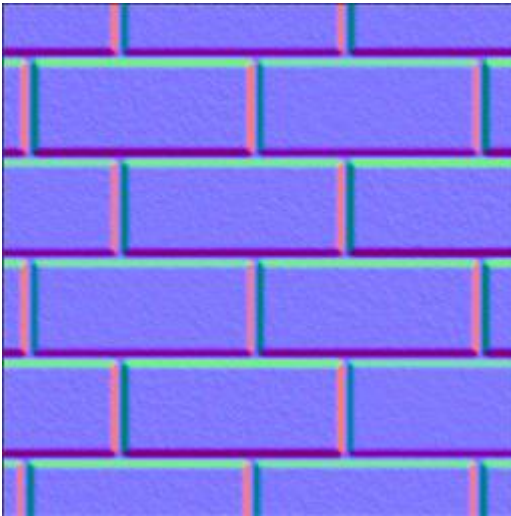
# Hold On

What coordinate system does normal map use?



# Hold On

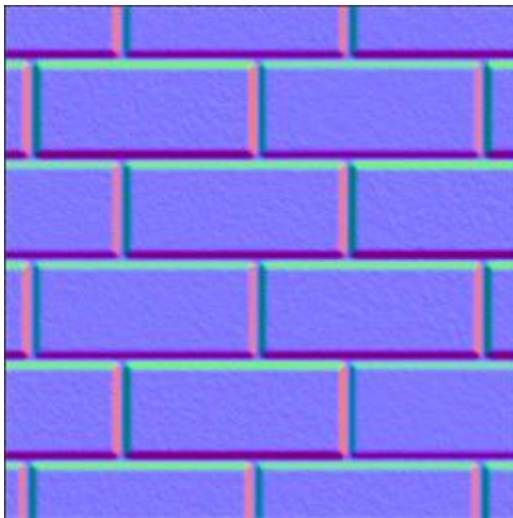
What coordinate system does normal map use?



$$(r, g, b) \mapsto r\hat{u} + g\hat{v} + b\hat{n}$$

# Hold On

What coordinate system does normal map use?



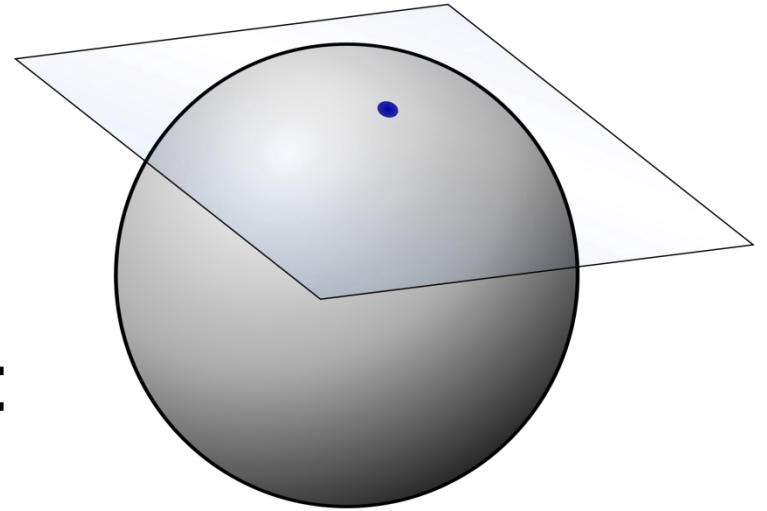
$$(r, g, b) \mapsto r\hat{u} + g\hat{v} + b\hat{n}$$

**texture** or **tangent space** coordinates

# Tangent Space

At every point of surface:

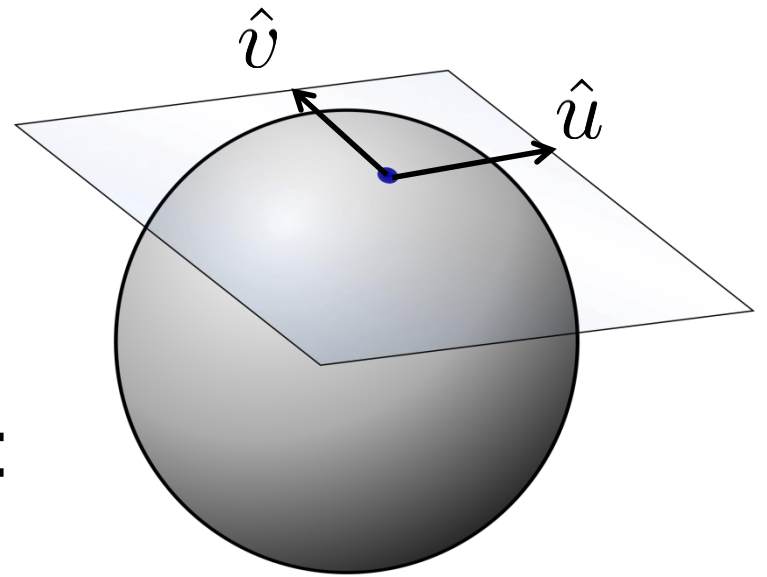
- one **normal** direction
  - (we know how to compute this)



# Tangent Space

At every point of surface:

- one **normal** direction
  - (we know how to compute this)
- two-dimensional **tangent space**
  - how to pick basis vectors?

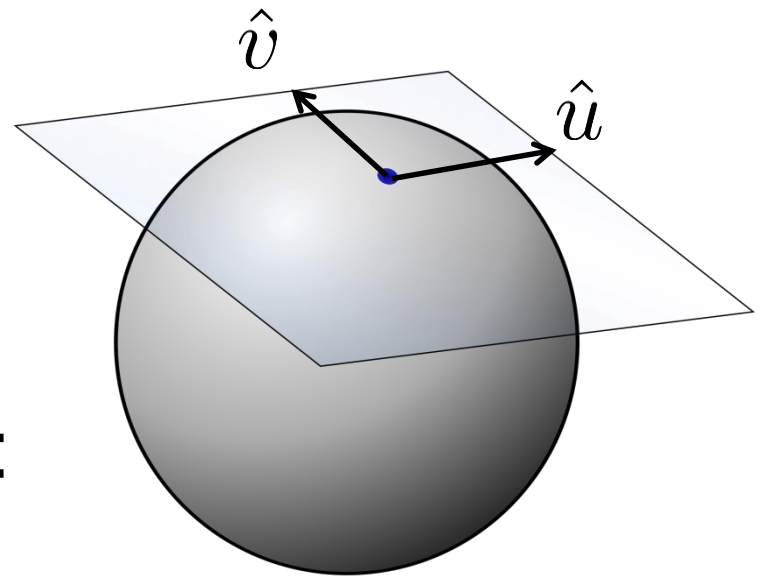




# Tangent Space

At every point of surface:

- one **normal** direction
  - (we know how to compute this)
- two-dimensional **tangent space**
  - how to pick basis vectors?
  - many possible ways (parameterization lecture)



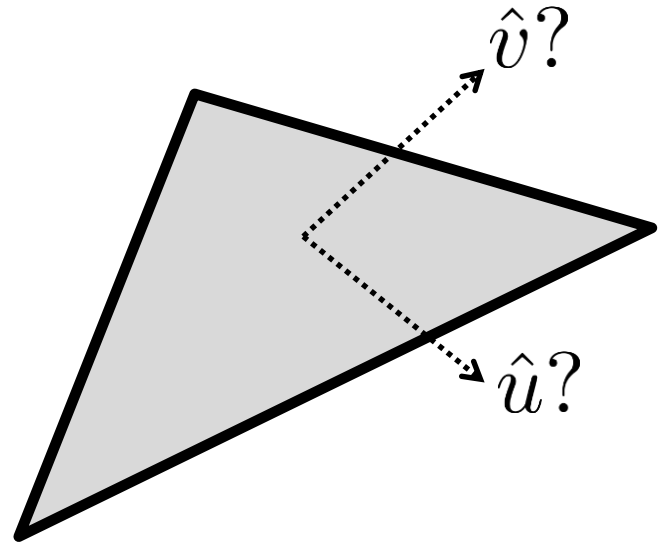
# Texture Coordinates

What are basis vectors  
at each point?



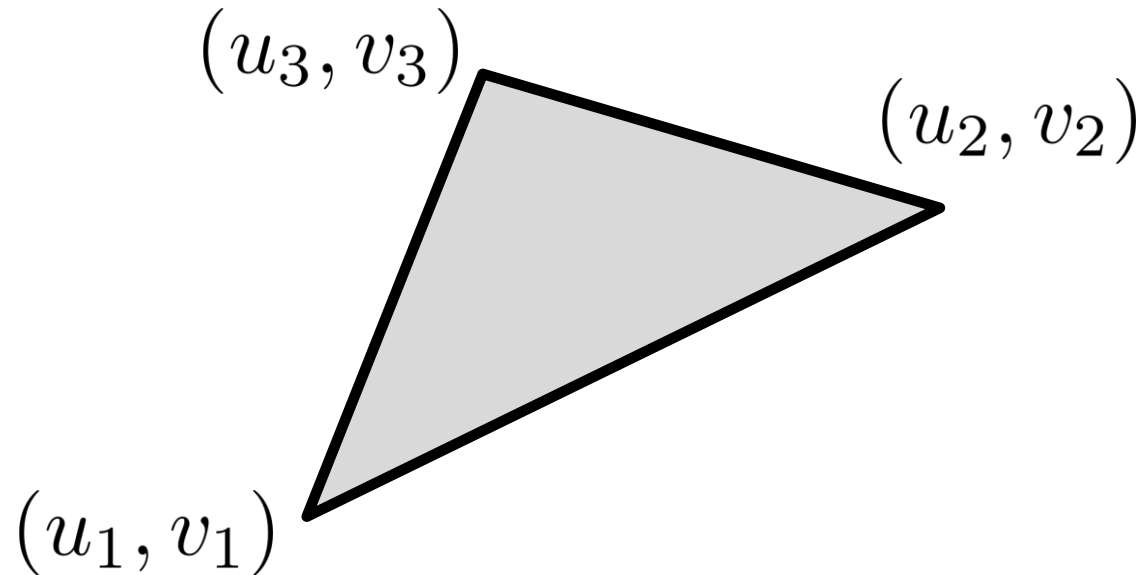
# Computing Tangent Basis

On each triangle, **precompute**  $u$  and  $v$  directions



# Computing Tangent Basis

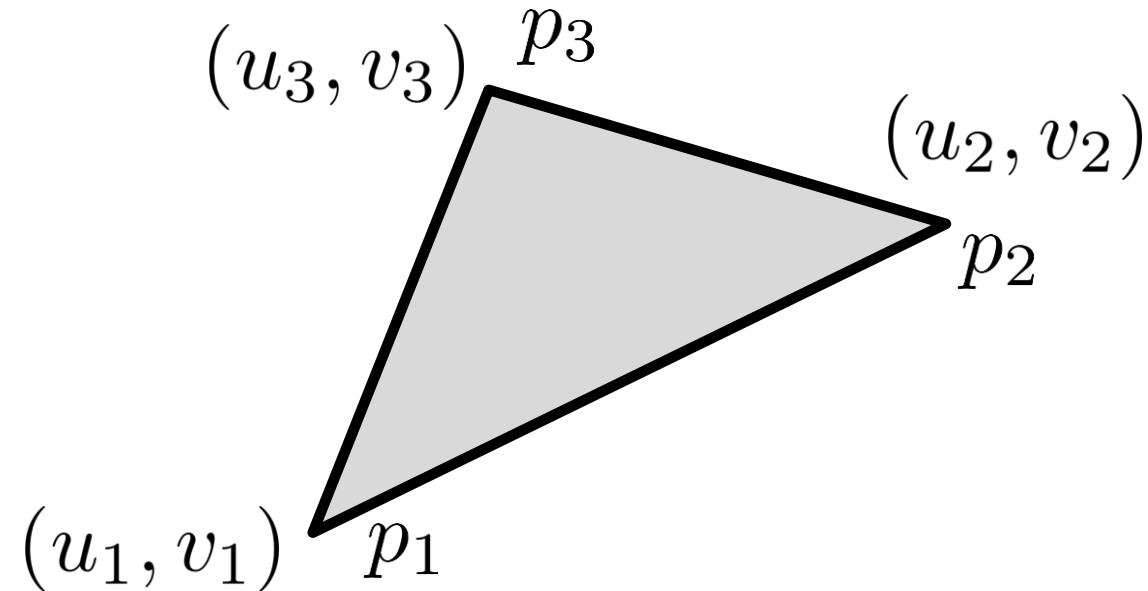
On each triangle, **precompute**  $u$  and  $v$  directions



Already know: three  $(u, v)$  pairs from parameterization

# Computing Tangent Basis

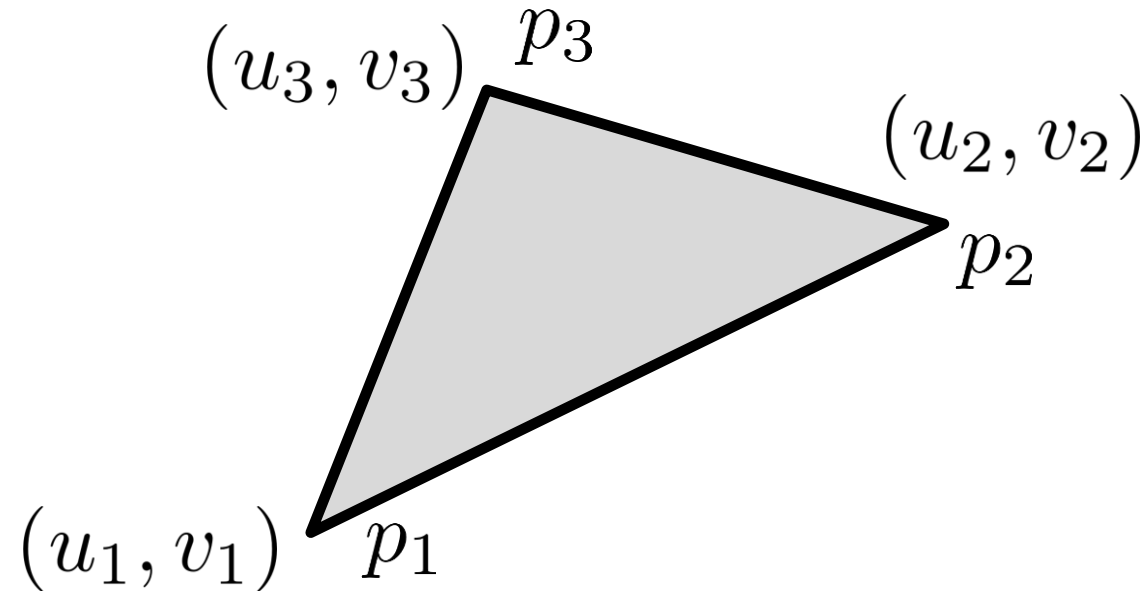
On each triangle, **precompute**  $u$  and  $v$  directions



Already know: vertex positions

# Computing Tangent Basis

On each triangle, **precompute**  $u$  and  $v$  directions



$$p_2 = p_1 + (u_2 - u_1)\hat{u} + (v_2 - v_1)\hat{v}$$

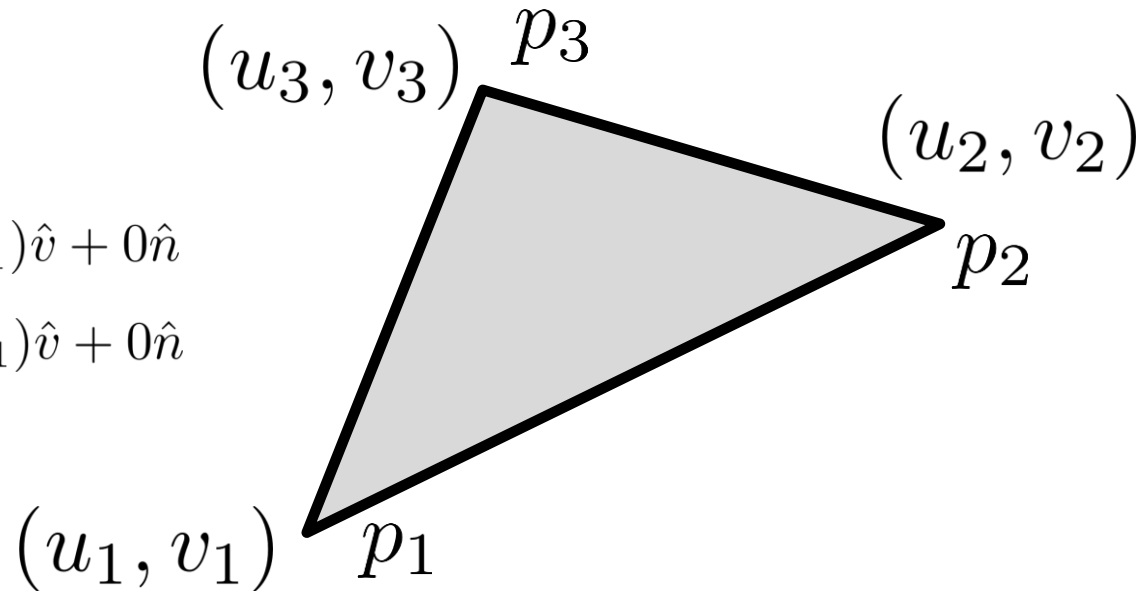
$$p_3 = p_1 + (u_3 - u_1)\hat{u} + (v_3 - v_1)\hat{v}$$

# Computing Tangent Basis

On each triangle, **precompute**  $u$  and  $v$  directions

$$p_2 = p_1 + (u_2 - u_1)\hat{u} + (v_2 - v_1)\hat{v} + 0\hat{n}$$

$$p_3 = p_1 + (u_3 - u_1)\hat{u} + (v_3 - v_1)\hat{v} + 0\hat{n}$$



Need third equation...

# Computing Tangent Basis

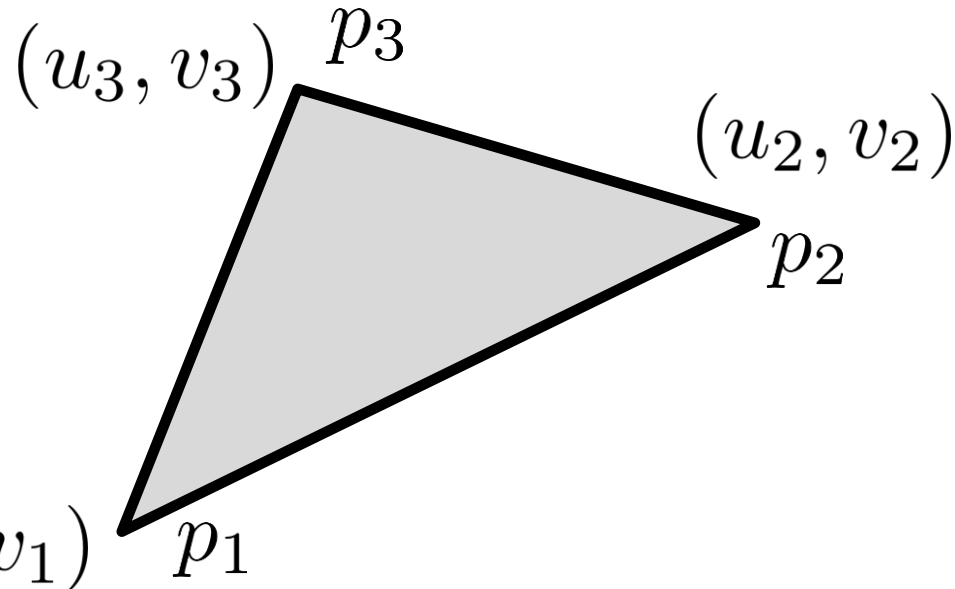
On each triangle, **precompute**  $u$  and  $v$  directions

$$p_2 = p_1 + (u_2 - u_1)\hat{u} + (v_2 - v_1)\hat{v} + 0\hat{n}$$

$$p_3 = p_1 + (u_3 - u_1)\hat{u} + (v_3 - v_1)\hat{v} + 0\hat{n}$$

$$\frac{(p_2 - p_1) \times (p_3 - p_1)}{\|(p_2 - p_1) \times (p_3 - p_1)\|} = 0\hat{u} + 0\hat{v} + \hat{n}$$

$$(u_1, v_1) \quad p_1$$



Need third equation...



# Computing Tangent Basis

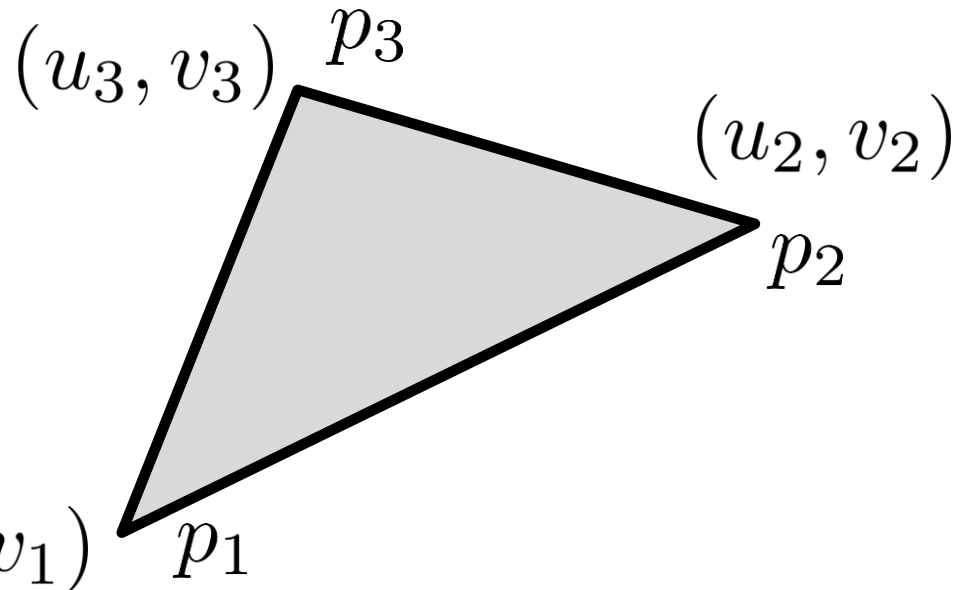
On each triangle, **precompute**  $u$  and  $v$  directions

$$p_2 = p_1 + (u_2 - u_1)\hat{u} + (v_2 - v_1)\hat{v} + 0\hat{n}$$

$$p_3 = p_1 + (u_3 - u_1)\hat{u} + (v_3 - v_1)\hat{v} + 0\hat{n}$$

$$\frac{(p_2 - p_1) \times (p_3 - p_1)}{\|(p_2 - p_1) \times (p_3 - p_1)\|} = 0\hat{u} + 0\hat{v} + \hat{n}$$

$$(u_1, v_1) \quad p_1$$



$$\left[ \begin{array}{c|c|c} p_2 - p_1 & p_3 - p_1 & \frac{(p_2 - p_1) \times (p_3 - p_1)}{\|(p_2 - p_1) \times (p_3 - p_1)\|} \end{array} \right] = \left[ \begin{array}{c|c|c} \hat{u} & \hat{v} & \hat{n} \end{array} \right] \left[ \begin{array}{cc|c} u_2 - u_1 & u_3 - u_1 & 0 \\ v_2 - v_1 & v_3 - v_1 & 0 \\ 0 & 0 & 1 \end{array} \right]$$

# Bump Mapping

Older technique: give **offset height** only



# Bump Mapping

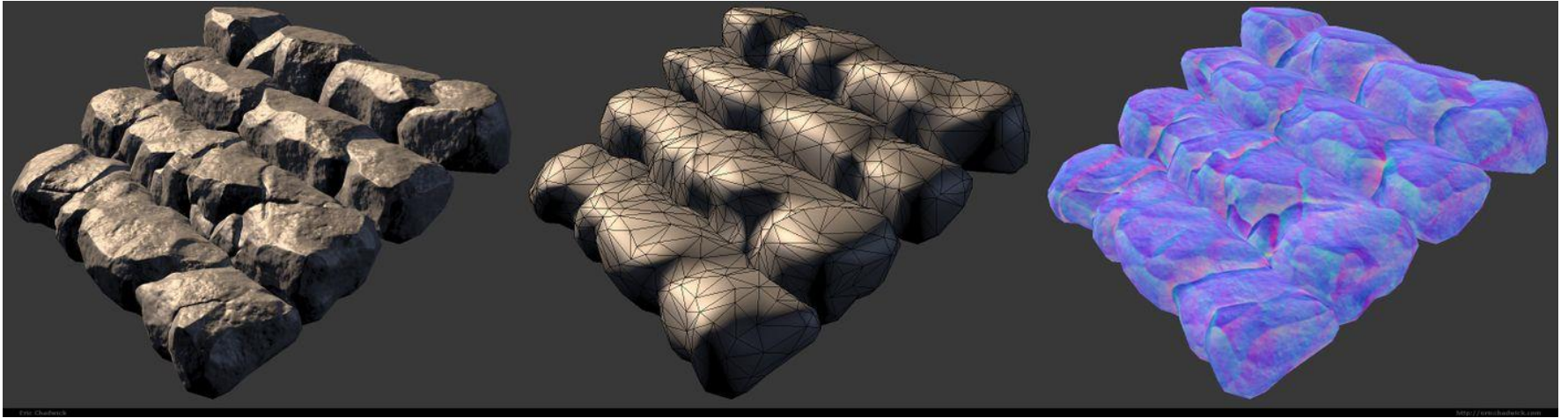
Older technique: give **offset height** only

Less flexible than  
normal map

To use, convert to  
normal map



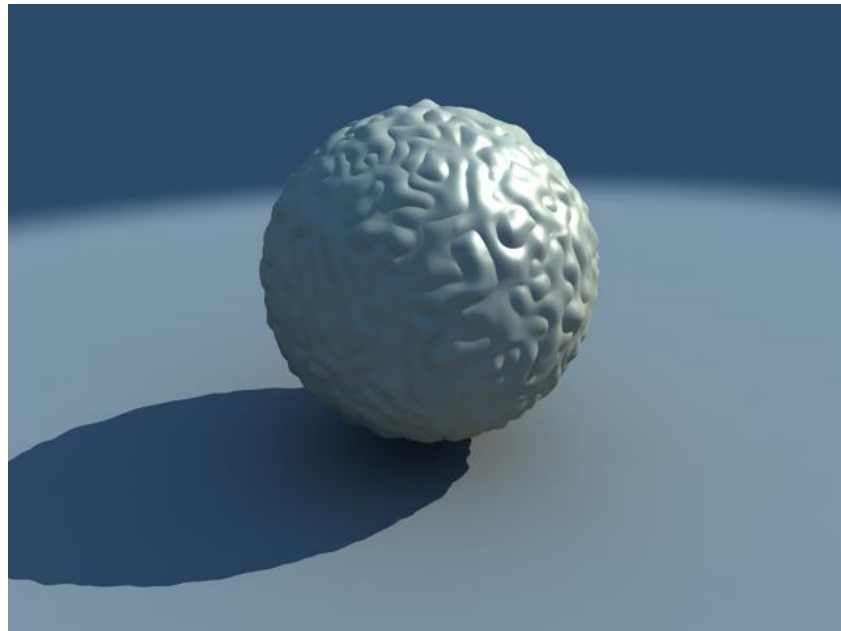
# More Examples



# Displacement Map

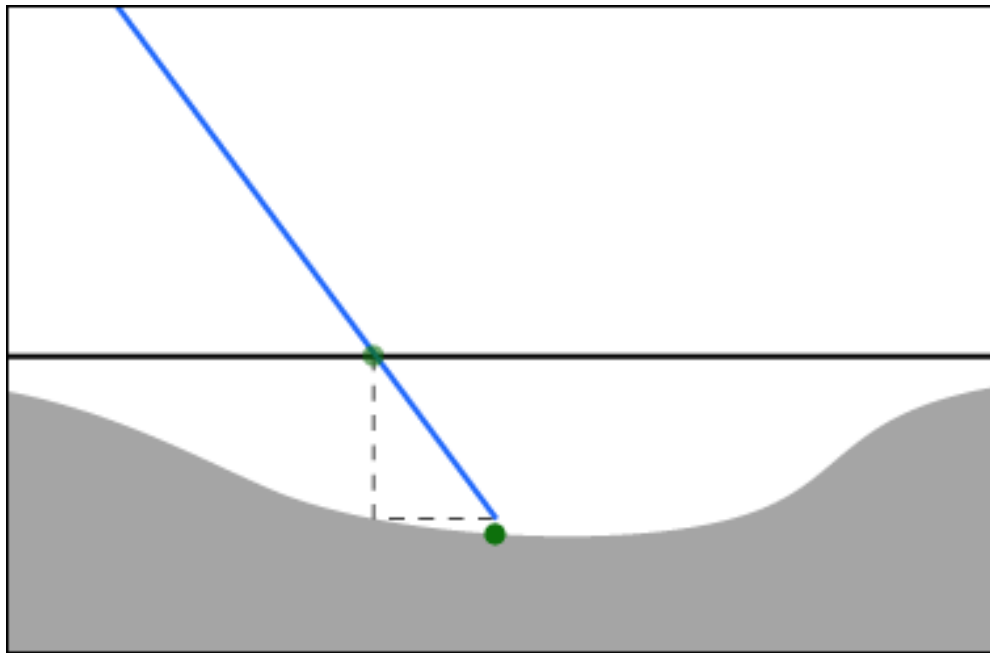
Like normal map, but change normals  
**and** geometry

- Fully correct
- **Slow**



# Parallax Map

Take into account **shift in texture coordinates**



# Parallax Map Example



Texture Mapped



Normal Mapped



Parallax Mapped