

# CS388: Natural Language Processing

## Lecture 14: Semantics I

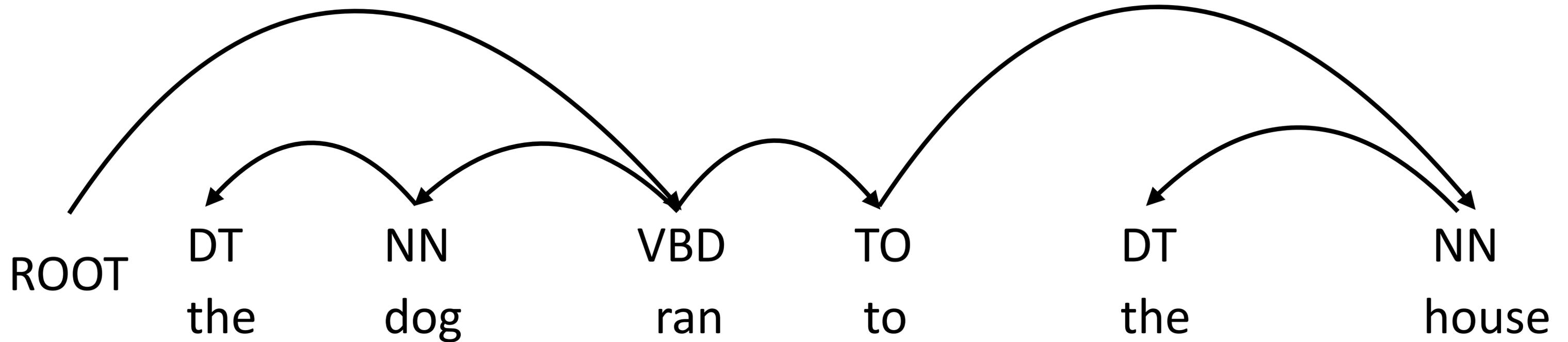
Greg Durrett





# Recall: Dependencies

- ▶ Dependency syntax: syntactic structure is defined by dependencies
  - ▶ Head (parent, governor) connected to dependent (child, modifier)
  - ▶ Each word has exactly one parent except for the ROOT symbol
  - ▶ Dependencies must form a directed acyclic graph





# Recall: Shift-Reduce Parsing

ROOT



▶ State: **Stack:** [ROOT I ate]    **Buffer:** [some spaghetti bolognese]

▶ Left-arc (reduce operation): Let  $\sigma$  denote the stack

▶ “Pop two elements, add an arc, put them back on the stack”

$$\boxed{\sigma | w_{-2}, w_{-1}} \rightarrow \boxed{\sigma | w_{-1}}, \quad w_{-2} \text{ is now a child of } w_{-1}$$

▶ Train a classifier to make these decisions sequentially — that classifier can parse sentences for you



# Where are we now?

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- ▶ Early in the class: bags of word (classifiers) => sequences of words (sequence modeling)
- ▶ Now we can understand sentences in terms of tree structures as well
- ▶ Why is this useful? What does this allow us to do?
- ▶ We're going to see how parsing can be a stepping stone towards more formal representations of language meaning



# Today

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- ▶ Montague semantics:
  - ▶ Model theoretic semantics
  - ▶ Compositional semantics with first-order logic
- ▶ CCG parsing for database queries
- ▶ Lambda-DCS for question answering

# Model Theoretic Semantics



# Model Theoretic Semantics

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- ▶ Key idea: can ground out natural language expressions in set-theoretic expressions called *models* of those sentences
- ▶ Natural language statement  $S \Rightarrow$  interpretation of  $S$  that models it  
*She likes going to that restaurant*
  - ▶ Interpretation: defines who *she* and *that restaurant* are, make it able to be concretely evaluated with respect to a *world*
- ▶ Entailment (statement A implies statement B) reduces to: in all worlds where A is true, B is true
- ▶ Our modeling language is *first-order logic*



# First-order Logic

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- ▶ Powerful logic formalism including things like entities, relations, and quantifications

*Lady Gaga sings*

- ▶ *sings* is a *predicate* (with one argument), function  $f: \text{entity} \rightarrow \text{true/false}$
- ▶  $\text{sings}(\text{Lady Gaga}) = \text{true or false}$ , have to execute this against some database (*world*)
- ▶  $[[\text{sings}]] = \textit{denotation}$ , set of entities which sing (found by executing this predicate on the world — we'll come back to this)



# Quantification

- ▶ Universal quantification: “forall” operator
  - ▶  $\forall x \text{ sings}(x) \vee \text{ dances}(x) \rightarrow \text{ performs}(x)$   
*“Everyone who sings or dances performs”*
- ▶ Existential quantification: “there exists” operator
  - ▶  $\exists x \text{ sings}(x)$       *“Someone sings”*
- ▶ Source of ambiguity! *“Everyone is friends with someone”*
  - ▶  $\forall x \exists y \text{ friend}(x,y)$
  - ▶  $\exists y \forall x \text{ friend}(x,y)$





# Logic in NLP

- ▶ Question answering:

*Who are all the American singers named Amy?*

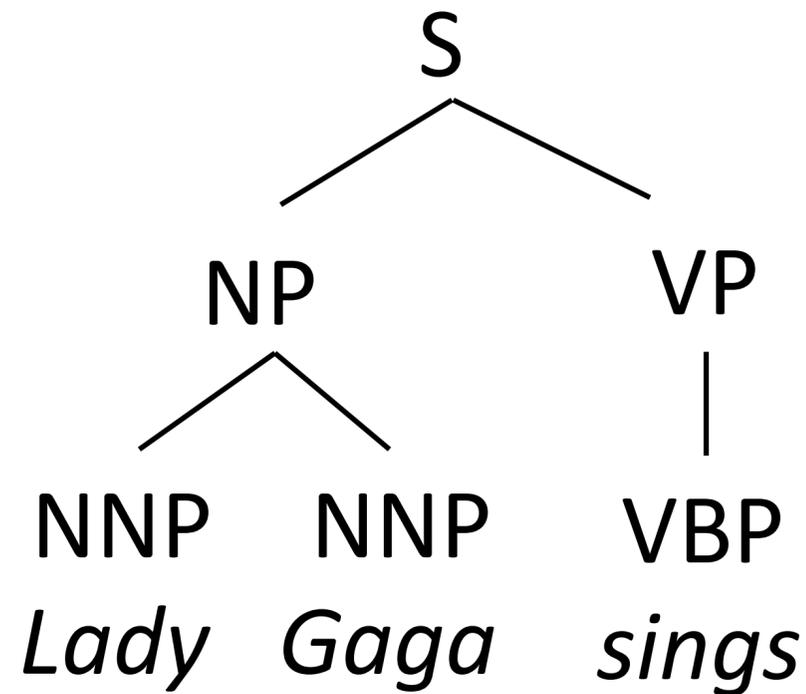
$\lambda x. \text{nationality}(x, \text{USA}) \wedge \text{sings}(x) \wedge \text{firstName}(x, \text{Amy})$

- ▶ Function that maps from  $x$  to true/false, like `filter`. Execute this on the world to answer the question
- ▶ Lambda calculus: powerful system for expressing these functions
- ▶ Information extraction: *Lady Gaga and Eminem are both musicians*  
 $\text{musician}(\text{Lady Gaga}) \wedge \text{musician}(\text{Eminem})$
- ▶ Can now do reasoning. Maybe know:  $\forall x \text{musician}(x) \Rightarrow \text{performer}(x)$   
Then:  $\text{performer}(\text{Lady Gaga}) \wedge \text{performer}(\text{Eminem})$

# Compositional Semantics with First- Order Logic



# Montague Semantics



Id	Name	Alias	Birthdate	Sings?
e470	Stefani Germanotta	Lady Gaga	3/28/1986	T
e728	Marshall Mathers	Eminem	10/17/1972	T

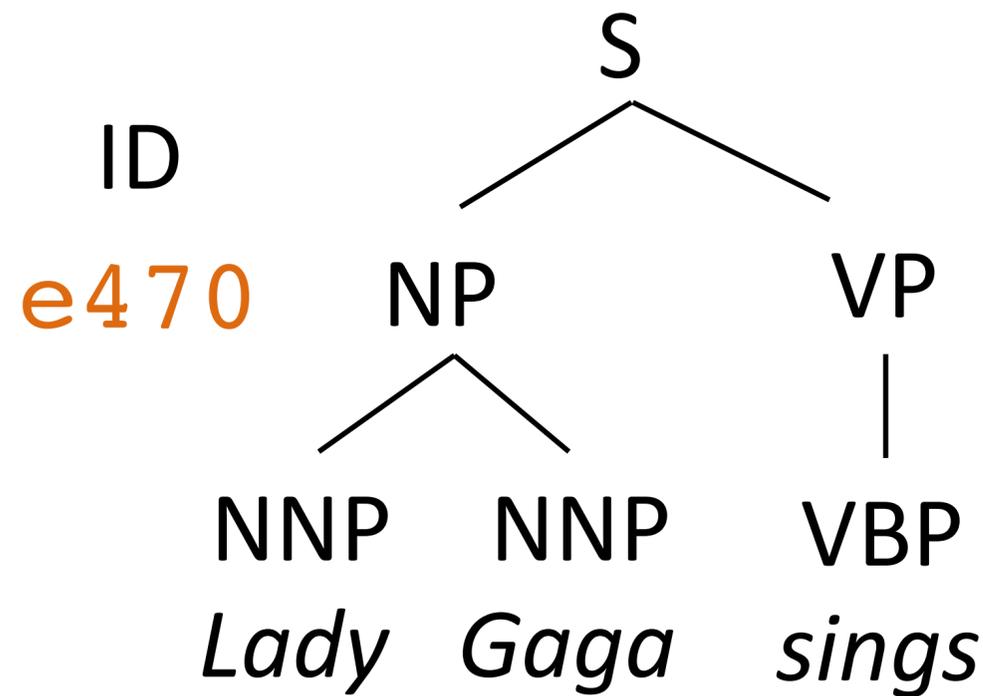
▶ Database containing entities, predicates, etc.

- ▶ Sentence expresses something about the world which is either true or false
- ▶ Denotation: evaluation of some expression against this database
- ▶  $[[ \textit{Lady Gaga} ]]$  = e470  
denotation of this string is an entity
- ▶  $[[ \textit{sings}(\textit{e470}) ]]$  = True  
denotation of this expression is T/F



# Montague Semantics

*sings* (e470)



function application: apply this to e470

$\lambda y. \textit{sings}(y)$

$\lambda y. \textit{sings}(y)$

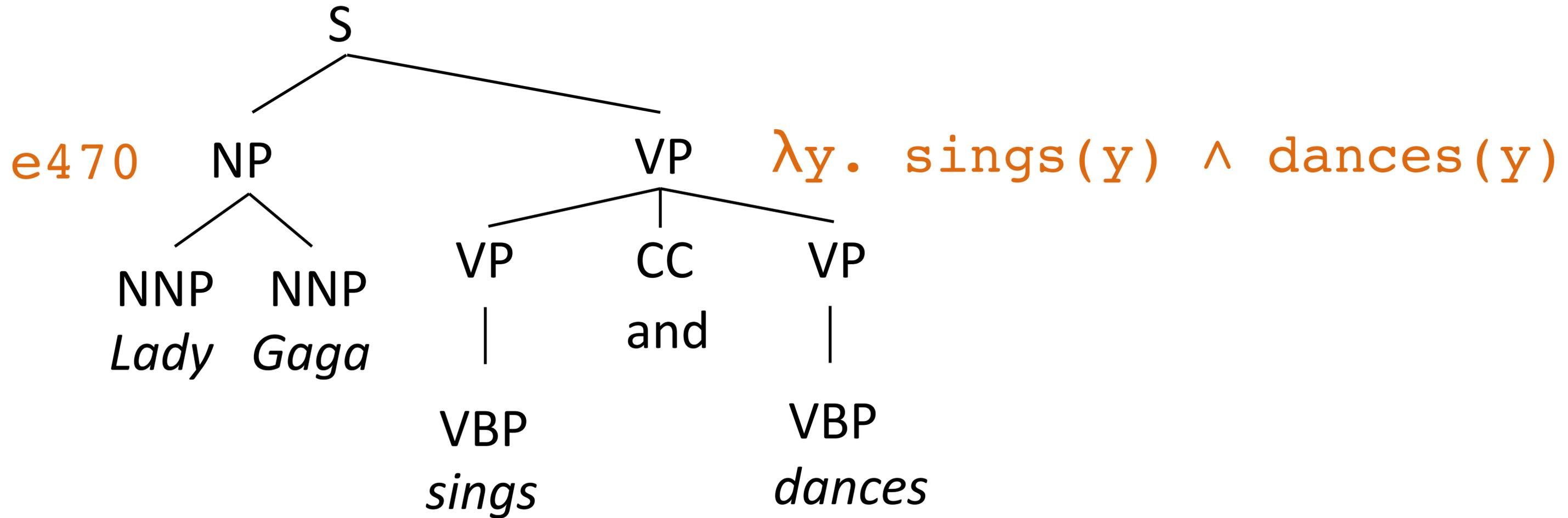
takes one argument ( $y$ , the entity) and returns a logical form  $\textit{sings}(y)$

- ▶ We can use the syntactic parse as a bridge to the lambda-calculus representation, build up a logical form (our model) *compositionally*



# Parses to Logical Forms

$sings(e470) \wedge dances(e470)$



$\lambda y. sings(y) \quad \lambda y. dances(y)$

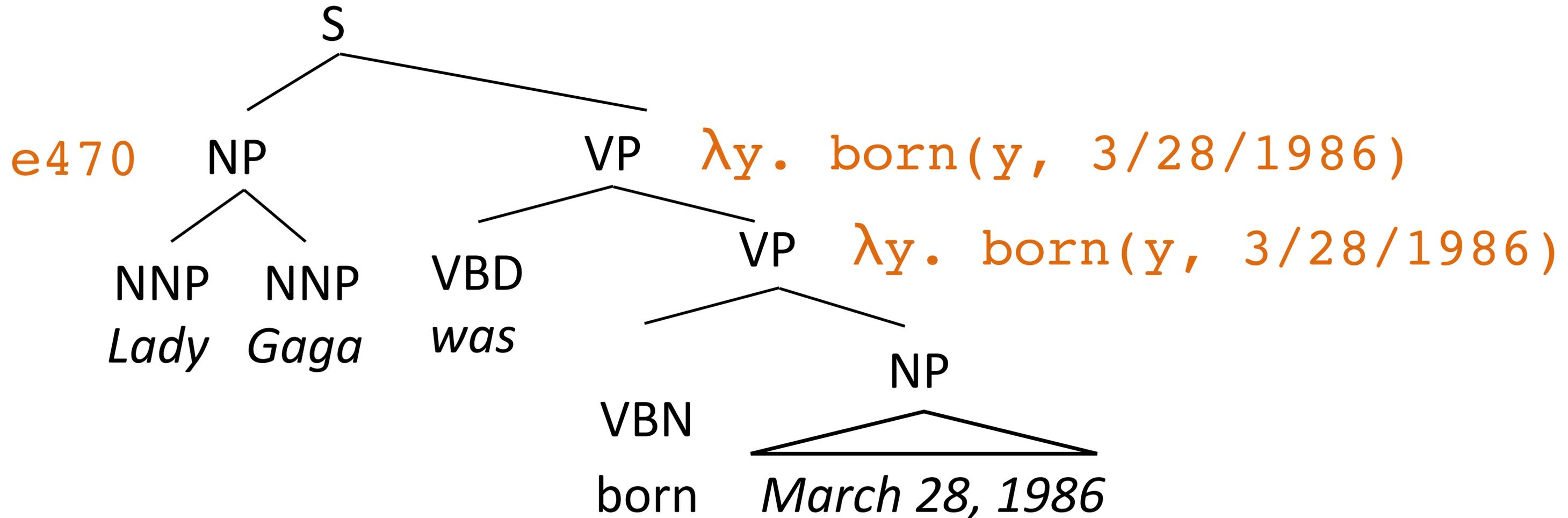
► General rules: VP:  $\lambda y. a(y) \wedge b(y) \rightarrow$  VP:  $\lambda y. a(y)$  CC VP:  $\lambda y. b(y)$

S:  $f(x) \rightarrow$  NP:  $x$  VP:  $f$



# Parses to Logical Forms

$\text{born}(e470, 3/28/1986)$



- ▶ Function takes two arguments: first  $x$  (date), then  $y$  (entity)
- ▶ How to handle tense: should we indicate that this happened in the past?



# Tricky things

- ▶ Adverbs/temporality: *Lady Gaga sang well yesterday*

$\text{sings}(\text{Lady Gaga}, \text{time=yesterday}, \text{manner=well})$

- ▶ “Neo-Davidsonian” view of events: things with many properties:

$\exists e. \text{type}(e, \text{sing}) \wedge \text{agent}(e, e470) \wedge \text{manner}(e, \text{well}) \wedge \text{time}(e, \dots)$

- ▶ Quantification: *Everyone is friends with someone*

$\exists y \forall x \text{friend}(x, y)$        $\forall x \exists y \text{friend}(x, y)$

(one friend)

(different friends)

- ▶ Same syntactic parse for both! So syntax doesn't resolve all ambiguities

- ▶ Indefinite: *Amy ate a waffle*       $\exists w. \text{waffle}(w) \wedge \text{ate}(\text{Amy}, w)$

- ▶ Generic: *Cats eat mice* (all cats eat mice? most cats? some cats?)



# Semantic Parsing

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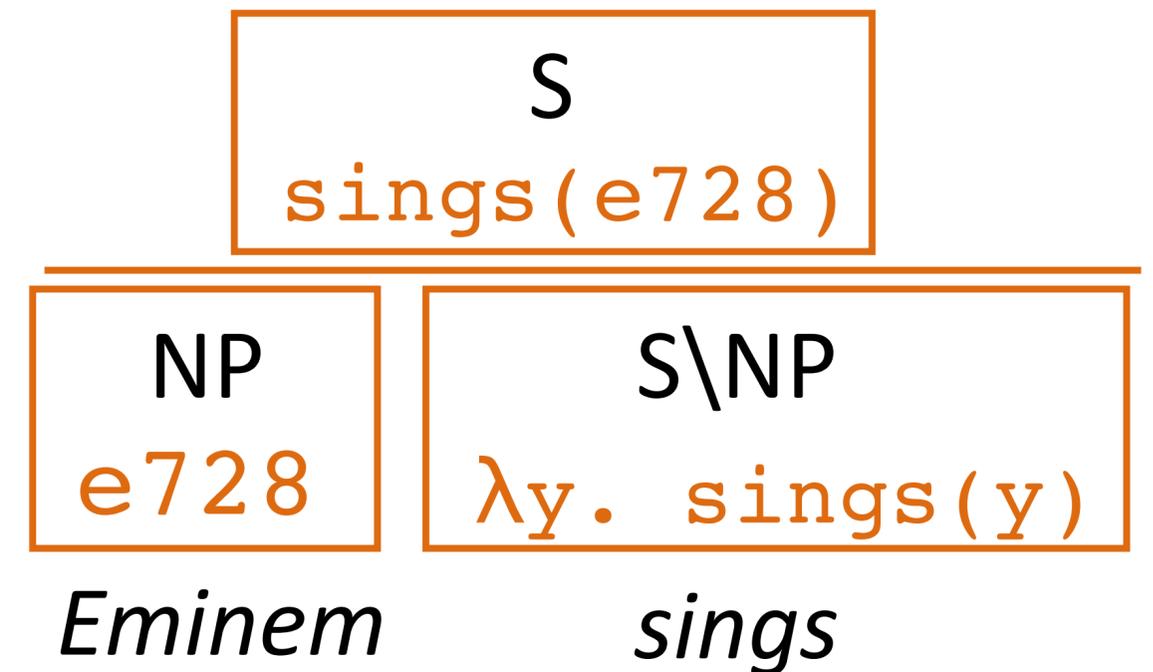
- ▶ For question answering, syntactic parsing doesn't tell you everything you want to know, but indicates the right structure
- ▶ Solution: *semantic parsing*: many forms of this task depending on semantic formalisms
- ▶ Two today: CCG (looks like what we've been doing) and lambda-DCS
- ▶ Applications: database querying/question answer: produce lambda-calculus expressions that can be executed in these contexts

# CCG Parsing



# Combinatory Categorical Grammar

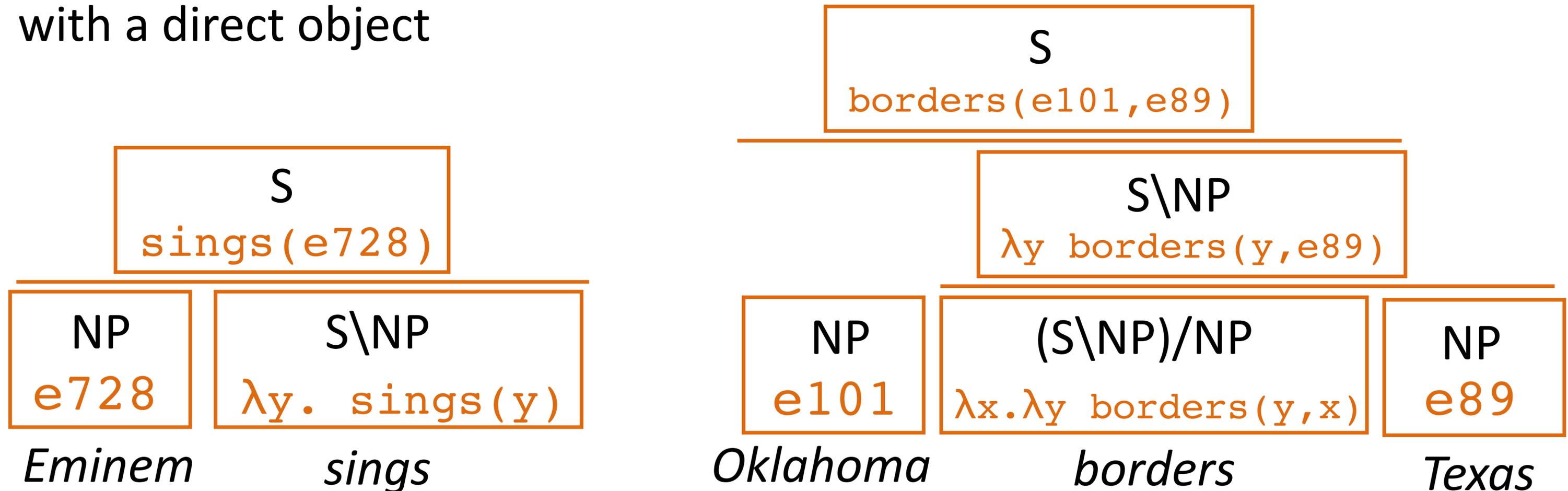
- ▶ Steedman+Szabolcsi (1980s): formalism bridging syntax and semantics
- ▶ Parallel derivations of syntactic parse and lambda calculus expression
- ▶ Syntactic categories (for this lecture): S, NP, “slash” categories
- ▶  $S \backslash NP$ : “if I combine with an NP on my left side, I form a sentence” — verb
- ▶ When you apply this, there has to be a parallel instance of function application on the semantics side





# Combinatory Categorical Grammar

- ▶ Steedman+Szabolcsi 1980s: formalism bridging syntax and semantics
- ▶ Syntactic categories (for this lecture): S, NP, “slash” categories
  - ▶  $S \backslash NP$ : “if I combine with an NP on my left side, I form a sentence” — verb
  - ▶  $(S \backslash NP) / NP$ : “I need an NP on my right and then on my left” — verb with a direct object





# CCG Parsing

What	states	border	Texas
$(S/(S \setminus NP))/N$	$N$	$(S \setminus NP)/NP$	$NP$
$\lambda f. \lambda g. \lambda x. f(x) \wedge g(x)$	$\lambda x. state(x)$	$\lambda x. \lambda y. borders(y, x)$	$texas$
		$(S \setminus NP)$	
		$\lambda y. borders(y, texas)$	

- ▶ “What” is a **very** complex type: needs a noun and needs a  $S \setminus NP$  to form a sentence.  $S \setminus NP$  is basically a verb phrase (*border Texas*)



# CCG Parsing

What	states	border	Texas
$(S/(S \setminus NP))/N$ $\lambda f. \lambda g. \lambda x. f(x) \wedge g(x)$	$N$ $\lambda x. state(x)$	$(S \setminus NP)/NP$ $\lambda x. \lambda y. borders(y, x)$	$NP$ <i>texas</i>
$S/(S \setminus NP)$ $\lambda g. \lambda x. state(x) \wedge g(x)$		$(S \setminus NP)$ $\lambda y. borders(y, texas)$	
$S$ $\lambda x. state(x) \wedge borders(x, texas)$			

- ▶ “What” is a **very** complex type: needs a noun and needs a  $S \setminus NP$  to form a sentence.  $S \setminus NP$  is basically a verb phrase (*border Texas*)
  - ▶ Lexicon is highly ambiguous — all the challenge of CCG parsing is in picking the right lexicon entries
- Zettlemoyer and Collins (2005)



# CCG Parsing

Show me	flights	to	Prague
S/N $\lambda f. f$	N $\lambda x. flight(x)$	(N\N) / NP $\lambda y. \lambda f. \lambda x. f(y) \wedge to(x, y)$	NP PRG
		N\N $\lambda f. \lambda x. f(x) \wedge to(x, PRG)$	
		N $\lambda x. flight(x) \wedge to(x, PRG)$	
		S $\lambda x. flight(x) \wedge to(x, PRG)$	

- ▶ “to” needs an NP (destination) and N (parent)



# CCG Parsing

- ▶ Many ways to build these parsers
- ▶ One approach: run a “supertagger” (tags the sentence with complex labels), then run the parser

What	states	border	Texas
$\frac{(S/(S \setminus NP))/N}{\lambda f. \lambda g. \lambda x. f(x) \wedge g(x)}$	$\frac{N}{\lambda x. state(x)}$	$\frac{(S \setminus NP)/NP}{\lambda x. \lambda y. borders(y, x)}$	$\frac{NP}{texas}$

- ▶ Parsing is easy once you have the tags, so we’ve reduced it to a (hard) tagging problem



# Building CCG Parsers

- ▶ Model: log-linear model over derivations with features on rules:

$$P(d|x) \propto \exp w^\top \left( \sum_{r \in d} f(r, x) \right)$$

$$f \left( \begin{array}{c} \boxed{\text{S}} \\ \text{sings(e728)} \end{array} \right) = \text{Indicator}(S \rightarrow NP \ S \setminus NP)$$

$$f \left( \begin{array}{c} \boxed{\text{NP}} \\ \text{e728} \end{array} \right) \quad f \left( \begin{array}{c} \boxed{\text{S} \setminus \text{NP}} \\ \lambda y. \text{sings}(y) \end{array} \right) = \text{Indicator}(S \setminus NP \rightarrow \text{sings})$$

*Eminem*

*sings*

- ▶ Can parse with a variant of CKY

Zettlemoyer and Collins (2005)



# Building CCG Parsers

- ▶ Training data looks like pairs of sentences and logical forms

*What states border Texas*       $\lambda x. \text{state}(x) \wedge \text{borders}(x, e89)$

- ▶ Problem: we don't know the derivation
  - ▶ *Texas* corresponds to NP |  $e89$  in the logical form (easy to figure out)
  - ▶ *What* corresponds to  $(S/(S \setminus NP))/N$  |  $\lambda f. \lambda g. \lambda x. f(x) \wedge g(x)$
  - ▶ How do we infer that without being told it?



# Lexicon

- ▶ GENLEX: takes sentence  $S$  and logical form  $L$ . Break up logical form into chunks  $C(L)$ , assume any substring of  $S$  might map to any chunk

*What states border Texas*       $\lambda x. \text{state}(x) \wedge \text{borders}(x, e89)$

- ▶ Chunks inferred from the logic form based on rules:
  - ▶ NP:  $e89$       ▶  $(S \setminus NP) / NP: \lambda x. \lambda y. \text{borders}(x, y)$
- ▶ Any substring can parse to any of these in the lexicon
  - ▶ *Texas*  $\rightarrow$  NP:  $e89$  is correct
  - ▶ *border Texas*  $\rightarrow$  NP:  $e89$
  - ▶ *What states border Texas*  $\rightarrow$  NP:  $e89$

...

Zettlemoyer and Collins (2005)



# GENLEX

Rules		Categories produced from logical form
Input Trigger	Output Category	$\arg \max(\lambda x.state(x) \wedge borders(x, texas), \lambda x.size(x))$
constant $c$	$NP : c$	$NP : texas$
arity one predicate $p_1$	$N : \lambda x.p_1(x)$	$N : \lambda x.state(x)$
arity one predicate $p_1$	$S \setminus NP : \lambda x.p_1(x)$	$S \setminus NP : \lambda x.state(x)$
arity two predicate $p_2$	$(S \setminus NP) / NP : \lambda x.\lambda y.p_2(y, x)$	$(S \setminus NP) / NP : \lambda x.\lambda y.borders(y, x)$
arity two predicate $p_2$	$(S \setminus NP) / NP : \lambda x.\lambda y.p_2(x, y)$	$(S \setminus NP) / NP : \lambda x.\lambda y.borders(x, y)$
arity one predicate $p_1$	$N / N : \lambda g.\lambda x.p_1(x) \wedge g(x)$	$N / N : \lambda g.\lambda x.state(x) \wedge g(x)$
literal with arity two predicate $p_2$ and constant second argument $c$	$N / N : \lambda g.\lambda x.p_2(x, c) \wedge g(x)$	$N / N : \lambda g.\lambda x.borders(x, texas) \wedge g(x)$
arity two predicate $p_2$	$(N \setminus N) / NP : \lambda x.\lambda g.\lambda y.p_2(x, y) \wedge g(x)$	$(N \setminus N) / NP : \lambda g.\lambda x.\lambda y.borders(x, y) \wedge g(x)$
an $\arg \max / \min$ with second argument arity one function $f$	$NP / N : \lambda g.\arg \max / \min(g, \lambda x.f(x))$	$NP / N : \lambda g.\arg \max(g, \lambda x.size(x))$
an arity one numeric-ranged function $f$	$S / NP : \lambda x.f(x)$	$S / NP : \lambda x.size(x)$

- Very complex and hand-engineered way of taking lambda calculus expressions and “backsolving” for the derivation

Zettlemoyer and Collins (2005)



# Learning

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- ▶ Iterative procedure like the EM algorithm: estimate “best” parses that derive each logical form, retrain the parser using these parses with supervised learning
- ▶ We’ll talk about a simpler form of this in a few slides



# Applications

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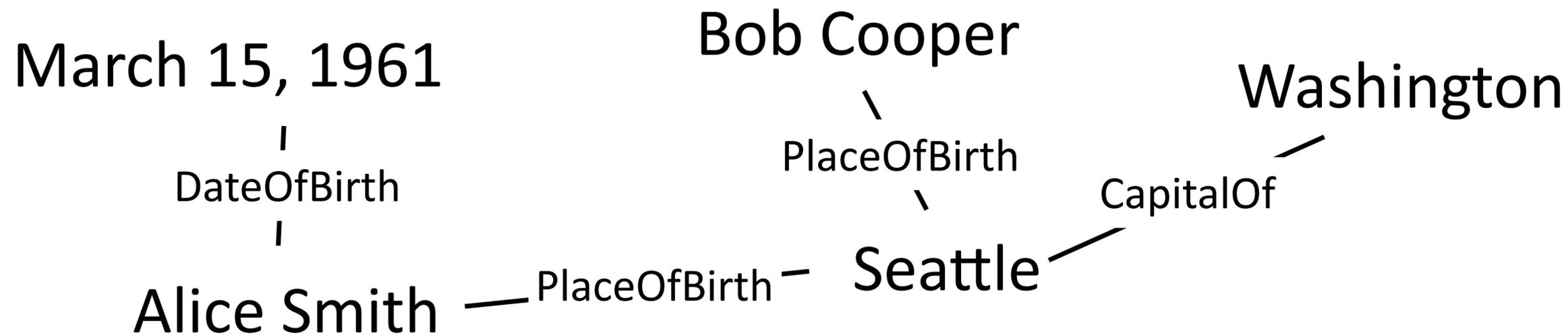
- ▶ GeoQuery: answering questions about states (~80% accuracy)
- ▶ Jobs: answering questions about job postings (~80% accuracy)
- ▶ ATIS: flight search
- ▶ Can do well on all of these tasks if you handcraft systems and use plenty of training data: these domains aren't that rich
- ▶ What about broader QA?

Lambda-DCS



# Lambda-DCS

- ▶ Dependency-based compositional semantics — original version was less powerful than lambda calculus, lambda-DCS is as powerful
- ▶ Designed in the context of building a QA system from Freebase
- ▶ Freebase: set of entities and relations



- ▶  $[[\text{PlaceOfBirth}]] = \text{set of pairs of (person, location)}$



# Lambda-DCS

Lambda-DCS

Seattle

PlaceOfBirth

PlaceOfBirth.Seattle

Lambda calculus

$\lambda x. x = \text{Seattle}$

$\lambda x. \lambda y. \text{PlaceOfBirth}(x, y)$

$\lambda x. \text{PlaceOfBirth}(x, \text{Seattle})$

- ▶ Looks like a tree fragment over Freebase

??? — PlaceOfBirth — Seattle

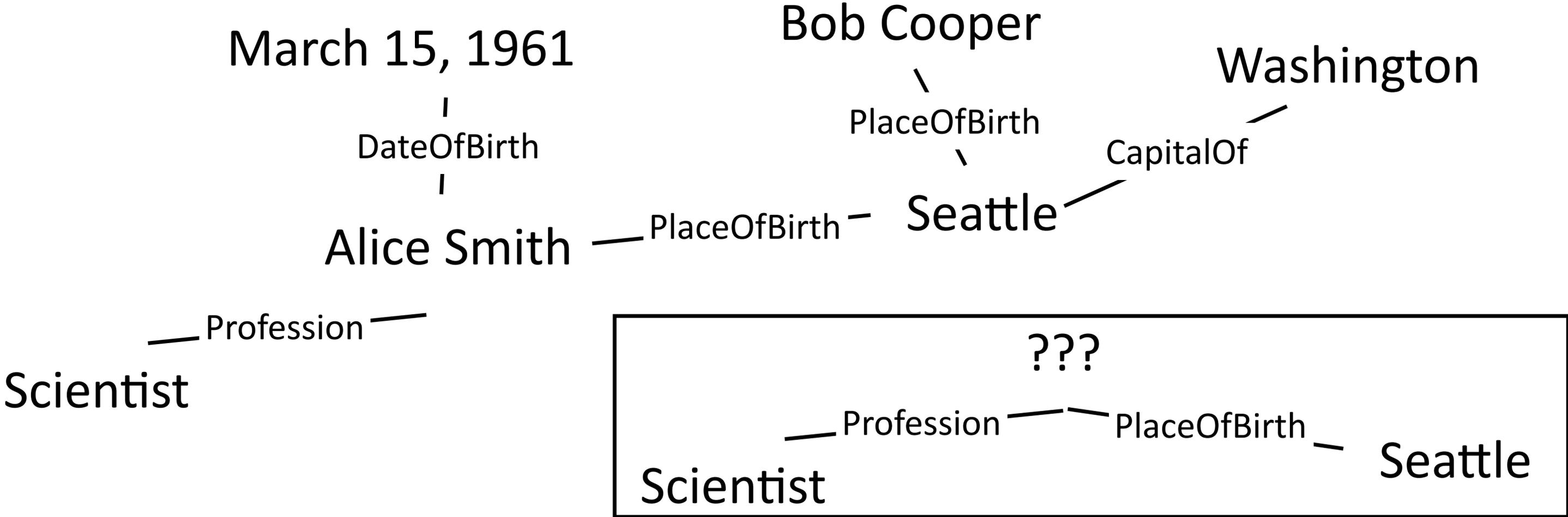
Profession.Scientist  $\wedge$   
PlaceOfBirth.Seattle

$\lambda x. \text{Profession}(x, \text{Scientist})$   
 $\wedge \text{PlaceOfBirth}(x, \text{Seattle})$

Liang et al. (2011), Liang (2013)



# Lambda-DCS



“list of scientists born in Seattle”

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Profession.Scientist ^
PlaceOfBirth.Seattle

```

- ▶ Execute this fragment against Freebase, returns Alice Smith (and others)





# Parsing with Lambda-DCS

- ▶ Learn just from question-answer pairs: maximize the likelihood of the right denotation  $y$  with the derivation  $d$  marginalized out

$$\mathcal{O}(\theta) = \sum_{i=1}^n \log \sum_{d \in D(x) : \llbracket d.z \rrbracket_{\mathcal{K}} = y_i} p_{\theta}(d \mid x_i).$$

sum over derivations  $d$  such that the denotation of  $d$  on knowledge base  $K$  is  $y_i$

For each example:

Run beam search to get a set of derivations

Let  $d$  = highest-scoring derivation in the beam

Let  $d^*$  = highest-scoring derivation in the beam *with correct denotation*

Do a structured perceptron update towards  $d^*$  away from  $d$



# Takeaways

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- ▶ Can represent meaning with first order logic and lambda calculus
- ▶ Can bridge syntax and semantics and create semantic parsers that can interpret language into lambda-calculus expressions
- ▶ Useful for querying databases, question answering, etc.
- ▶ Next time: neural net methods for doing this that rely less on having explicit grammars