Midterm for CS378: Natural Language Processing (Fall 2020)

Instructions:

- The exam is due at 5pm CST on Friday, October 16. Leave yourself ample time to upload it.

- **The first thing you do should be to read and sign the honor code. You will upload this with your exam.** This exam is to be completed individually by each student. Again, you may not collaborate with other students! If we find out that you have done so, that will be considered a violation of the course Academic Honesty policy.

- This exam is an open book take-home exam. You are allowed to consult any resources that are helpful, with the exception of other people.

- Partial credit will be given for short-answer and long-answer questions, so please show work in your answers, but avoid writing essays. **You might be penalized for writing too much if it's incorrect.**

- For short-answer and long-answer questions, please box or circle your final answer unless it is an explanation.

- You will scan and upload your exam into Gradescope. You may type your responses, handwrite responses on a printed exam, or a mix of both. If you type your responses, please try to keep the layout of your pages matching the exam to make our grading easier (e.g., put the answers to the first four multiple choice questions on a single page).

- If you have questions during the exam, please use a private Piazza post or directly email the course staff. Important clarifications will be posted as Canvas announcements.

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Name: ____________________________________________
Honor Code (adapted from Dr. Elaine Rich)

The University and the Department are committed to preserving the reputation of your degree. In order to guarantee that every degree means what it says it means, we must enforce a strict policy that guarantees that the work that you turn in is your own and that the grades you receive measure your personal achievements in your classes:

By turning in this exam with your name on it, you are certifying that this is yours and yours alone. You are responsible for complying with this policy in two ways:

1. You must not turn in work that is not yours or work which constitutes any sort of collaborative effort with other students.

2. You must take all reasonable precautions to prevent your work from being stolen. It is important that you do nothing that would enable someone else to turn in work that is not theirs.

The penalty for academic dishonesty will be a course grade of F and a referral of the case to the Dean of Students Office. Further penalties, including suspension or expulsion from the University may be imposed by that office.

Please sign below to indicate that you have read and understood this honor code. If submitting electronically, you can submit any page with a text version of the honor code and a scanned or drawn signature.

Signature: ________________________________
Part 1: Multiple Choice (10 points)

1. (10 points) Answer these questions by writing the answer in the provided blank (2 points each).

(1) What is the big-O runtime of a single forward pass through a Deep Averaging Network? The size of the hidden layer is $D$, the number of words is $S$, the size of the embedding space is $E$, and the number of classes is $K$.

A. $O(S + ED + K)$
B. $O(SEDK)$
C. $O(SE + ED + DK)$
D. $O(D + S)$
E. None of the above

(2) Suppose you remove the nonlinearity from our standard FFNN and replace it with the identity function. Circle or list all that apply (there may be multiple correct choices):
I. Any model represented by this neural network can be represented with a multiclass logistic regression model.
II. The model is no longer mathematically well-defined (i.e., your code would crash if you ran it).
III. The model will need a higher learning rate to train effectively.

(3) Assume you are implementing a simplified DAN with a single weight matrix $W = \begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}$ and no hidden layer. That is, your model is $P(y|x) = \text{softmax}(W(\sum_{i=1}^{n} E(x_i)))$, where $E(x_i)$ is the word embedding of the $i$th word. Suppose $y = 0$ means negative and $y = 1$ means positive.

You have two training sentences: cats and dogs with negative sentiment and dogs and dogs and dogs with positive sentiment. Find the values of $a$ and $b$ such that this training set is fit nearly perfectly by the DAN model (i.e., it fits the training data with negative log likelihood less than 0.01). Assume the network has a single layer and a softmax layer at the end.

$cats = \begin{bmatrix} 0.3 \\ 0.6 \end{bmatrix}$ and $dogs = \begin{bmatrix} -0.4 \\ 0.1 \end{bmatrix}$

A. $[a = -100, b = 100]$  
B. $[a = 100, b = -100]$  
C. $[a = -100, b = -100]$  
D. $[a = 100, b = 100]$  
E. None of the above

(4) Which of the following statements about dependency parses is correct? Circle or list all that apply.

Furthermore, do not count ROOT as a word.
I. Every word has at least one child
II. Every word has at most one child
III. Every word has at least one parent
IV. Every word has exactly one parent
V. ROOT has exactly one child
Consider the skip-gram model

\[ P(\text{context} = y | \text{word} = x) = \frac{\exp(v_x \cdot c_y)}{\sum_{y'} \exp(v_x \cdot c_{y'})} \]

Recall that the choice of which (context, word) pairs to train on is governed by a window size parameter \( k \), which controls how far from a word we look to gather context. **Circle or list all that apply:**

I. If we’re building a neural network classifier for POS tagging, a smaller window size parameter \((k < 4)\) will work better.
II. If we’re building a neural network classifier for POS tagging, a larger window size parameter \((k \geq 4)\) will work better.
III. Skip-gram takes longer to train with a larger window size parameter.
IV. Using a larger window size will cause our vocabulary to be larger.
V. A larger window size will usually work better if the dimension of the skip-gram vectors is larger.

**Part 2: Short Answer (18 points)**

2. (18 points) Answer the following short-answer questions.
   a. (4 points) Suppose you are doing authorship attribution with a multi-class bag-of-words classifier: you have a training set of documents written by several authors, and a test set consisting of a few documents whose authorship you’re unsure of. Authorship attribution relies on distributions of function words, particularly the relative frequencies of common function words in text.

   Given this application, say for each type of preprocessing whether this should **improve** performance, **worsen** performance, or make **no difference**, and write a one-sentence justification of your answer.
   (1) lowercasing

   (2) removing stop words

   (3) applying tf-idf weighting to the words

   (4) applying tokenization
b. (3 points) For part-of-speech tagging in Assignment 3, you were given smoothed emission probabilities that incorporated pseudo-counts: assume we saw every word with every POS tag $\alpha$ times for some very small fractional value of $\alpha$. But smoothing all of the tags’ emission distributions might not be the best assumption. If you were to only apply smoothing to some of the tags, which type of tag is more important to smooth: open-class or closed-class? Justify your answer.

c. (2 points) Name one of the ways in which the Adam optimizer improves over SGD, and state in your own words why this helps optimization of deep networks.

d. (3 points) List three applications you can think of where you could use the bag-of-words classification model from Assignment 1, assuming you retrain this model on new data. Do not include sentiment analysis.

e. (3 points) Your pet ferret walks across your keyboard while you’re working on Assignment 1 and adds a call to shuffle the words in each input sentence before its features are extracted, but after tokenization and other preprocessing. This applies to both training and test time. Recall the three question parts: Q1 (unigram perceptron), Q5 (unigram LR), and Q7 (bigrams). Which of these question parts will have their results impacted by the code change?
f. (3 points) Your ferret is at it again and somehow deleted a random 50% of the words in the Assignment 1 training data; the test data is unchanged. Do you expect the model’s performance to increase, stay the same, decrease slightly, or decrease significantly? Justify your answer.

Part 3: Long Answer (72 points)

3. (14 points) Consider the problem of trying to automatically take words in a tweet and merge them into a hashtag: for example, instead of tweeting going to SXSW2019, you might tweet going to #SXSW2019 to use the event’s hashtag. We are going to approach this as a BIO tagging problem.

Let \( x = (x_1, \ldots, x_n) \) be the sequence of words in the tweet. Let \( y = (y_1, \ldots, y_n) \) be the sequence of BIO labels. Here are some examples of what this looks like:

O O O B I O O O O
gonna go watch Infinity War with the crew tonight
O O O B O O O
Just got back from SXSW2019 and loved it
O O O O O O O O O O B I I I
After watching that football game I can tell you that Texas is not back

A multi-word hashtag would be merged for the final tweet (e.g., #InfinityWar). Also, this task is only about detecting which existing words could be merged into a hashtag, not adding new hashtags to a tweet or changing the wording to conform to existing hashtags.
a. (6 points) First consider a simplified form of the task where we are only trying to detect single-word hashtags like SXSW2020. Imagine that the data is postprocessed so that only the single-B labels remain, and all B-I... sequences are just set to O (e.g., Infinity War is no longer detected).

Suppose we try to do this with a binary classifier, and we are running the classifier over the jth word in the input sentence. Write a piece of pseudocode that extracts indicator or count-based features from the input using three feature templates (that is, do not use skip-gram or neural networks for this question part). For example, the Assignment 1 features could be written as:

```python
for i=1 to n:
    add_feature("Unigram=" + x[i])
```

and this would count as one feature template. (Reminder that n is the length of the sentence.)

**Give your three feature templates and give a one-sentence justification for why each is useful.**

b. (4 points) Now consider the full version of this task. Do you think a standard HMM (using categorical distributions for transitions and emissions, like in Assignment 3) will work well here? Give two reasons to justify your response.

c. (4 points) Suppose you are given a test set of new tweets all from a single day. Your job is to return predictions across all of them. First, you run your model on each tweet in isolation, but you’re not that happy with the consistency of your results. Can you think of a way to postprocess your model’s output to do something smarter and get better results? Put another way, what information could you use across test data points to do better at this problem, and how would you use it? Justify your answer.
4. (14 points) In this question, we are going to consider doing multiclass logistic regression with a very large number of classes \( K > 10000 \). Here’s the multiclass logistic regression update with “different features” as discussed in lecture:

**Algorithm 1 Multiclass logistic regression update**

1: Input: labeled data \((x^{(i)}, y^{(i)})_{i=1}^{D}\), a feature extractor \(f\).
2: Initialize \( w = 0 \), a \( nK \)-dimensional weight vector.
3: for \( t = 1 \) to \( T \) do ▶ Loop over epochs
4: \hspace{1em} for \( i = 1 \) to \( D \) do ▶ Loop over data
5: \hspace{2em} Define local variables \( x = x^{(i)} \), \( y^* = y^{(i)} \) to denote the current example
6: \hspace{2em} Compute \( P(y = y_j | x) = \frac{\exp(w^\top f(x, y_j))}{\sum_{y' \in Y} \exp(w^\top f(x, y'))} \) for all \( j \) in \( 1 \ldots K \)
7: \hspace{2em} for \( j = 1 \) to \( K \) do ▶ Loop over classes
8: \hspace{3em} \( w \leftarrow w - P(y = y_j | x)f(x, y_j) \)
9: \hspace{3em} if \( y^* = y_j \) then
10: \hspace{4em} \( w \leftarrow w + f(x, y_j) \)
11: \hspace{3em} end if
12: \hspace{2em} end for
13: \hspace{1em} end for
14: end for

a. (3 points) Suppose that your “base” feature vector (before conjoining with classes) consists of \( n \) features, but at most \( d \) of these base features are nonzero on any give example. What is the big-O runtime of one iteration of the update (i.e., one pass through the \( i \) loop), assuming an efficient implementation?

b. (7 points) Let’s try to make this update faster. There are two parts that are slow: computing the probabilities for all the classes and then applying the update to all the classes. One way to make this faster is by approximating the denominator and making fewer updates to the weight vector.

Suppose you’ve completed three full passes through the data (three epochs) with the “full” update, and then on the fourth pass you know that the weight vector isn’t changing that dramatically anymore. Describe an approximation to the update you can do on this pass. Feel free to reference the algorithm by line numbers if you’d like. You do not need to provide working code, but you should be clear and specific enough that someone else could implement it given your description.

Hint: record information about the first three passes in some kind of data structure, and try to avoid making very small updates.
c. (4 points) For multiclass perceptron, the algorithm is faster since you don’t need to compute a normalization over $K$ classes; however, you still need to compute $y_{pred}$, which requires computing scores for each class. Describe how you might modify multiclass perceptron in the same setting as part (b) (speeding up the fourth iteration).

5. (14 points) Consider the beam search algorithm as described in lecture. The algorithm we described maintained a beam of $k$ hypotheses at each timestep, with others being disregarded as possible predecessors for the next state in search. However, another way to implement beam search is to have the beam instead store all the hypotheses which are no more than $\alpha$ worse than the optimal in terms of score. Put another way, if the current best hypothesis in the beam has score $s_{\text{max}}$, then any hypothesis with score at least $s_{\text{max}} - \alpha$ will get added to the beam, even if this means every hypothesis gets added. When a hypothesis with score $s’ > s_{\text{max}}$ gets added to the beam, hypotheses that are now too low-ranking must be evicted.

a. (7 points) Assume you have the HMM parameters $E$ and $T$ as described in the lecture notes (you won’t need the start parameters $S$). Using pseudocode, write the loop of the algorithm to take a previous beam $b_p$ for timestep $i – 1$ in the sentence and efficiently produce the new beam $b_n$ for timestep $i$. You may use a beam data structure (call it Beam) implemented with a min-heap: insertion is logarithmic in the number of elements, changing a value for a key is logarithmic, and removal of the “worst” element is constant time.

```plaintext
initialize b_n as a list
for each tag_curr in the tag set:
    track tag_prev_best with tag_prev_best_score
    for each tag_prev in b_p:
        compute score = transition(tag_prev, tag_curr) + emission(tag_curr)
        update tag_prev_best = tag_prev if score > tag_prev_best_score
        add tag_curr to b_n with score tag_prev_best_score
    compute s_max in b_n
drop all elements in b_n less than s_max - alpha
```
b. (5 points) Suppose over the $n$ steps of inference each beam ends up being size $B_i$ for $i = 1$ to $n$. Let $B_{\text{max}}$ be the largest of these. What is the worst-case runtime in big-O notation in terms of the sentence length $n$, the number of tags $|T|$, and these beam sizes? Note that the worst case ranges over both possible HMMs (maximally confusing/tricky ones) as well as orders of visiting the states.

Write a brief (2-3 sentence) justification of your response, referencing your algorithm from part (a) if you’d like.

c. (2 points) Suppose you have a sentence with mostly unambiguous words, where the emission probability of the word given one tag is substantially higher than those from all other tags (by at least $\alpha$ in terms of log probability). 10% of the words are highly ambiguous and these are spread uniformly at random throughout the sentence. Which do you think is more efficient: normal beam search or this modified version? Justify your answer.
6. (14 points) Suppose you have a dataset containing movie reviews. Each movie review is annotated with two different labels, $y_S$ and $y_G$, one corresponding to the sentiment (+ or -) and the other to the genre (action, comedy, or romance) of the movie. Consider the following neural network, which models both tasks at the same time (a multi-task model). The two classification tasks share the parameters at the lower layers of the network and have independent classifiers at the last layer. The network is then trained jointly to minimize the negative log likelihood of both tasks (these terms are added together). Such networks are useful when you have two related tasks and shared representations $z$ might be helpful.

\[ P(y_S|x)P(y_G|x) \]

a. (7 points) Given below is the \texttt{nn.Module} initialization and forward function of a single-task network. Modify this appropriately for the multi-task case. Your forward function should return a tuple with log probabilities from task $S$ and task $G$.

```python
class FFNN(nn.Module):
    def __init__(self, input_size, hidden_size, output_size):
        self.V = nn.Linear(input_size, hidden_size)
        self.nonlin = nn.Tanh()
        self.W = nn.Linear(hidden_size, output_size)
        self.log_sm = nn.LogSoftmax(dim=0)

        # Assume f_x is the averaged embeddings.
        def forward(self, f_x, y_gold):
            return self.log_sm(self.W(self.nonlin(self.V(x)))))
```

b. (3 points) Suppose you take these logits and use them to compute $\text{loss}_S$, the loss for the sentiment analysis task, and $\text{loss}_G$ for the genre classification task. What parameters does the following code update? List all parameters that get updated.

```python
lossS.backward()
optimizer.step()
```
c. (4 points) You are given the model trained using the multi-task objective, but do not have access to the training data anymore. Suppose you get 1000 additional reviews, but annotated only with the sentiment (+/-). What is the best strategy for using this data to further improve your sentiment classification without harming the performance on the genre prediction task?
7. (17 points) Suppose you have the following NPs provided to your as your treebank:

- **NP**
  - NML
  - JJ heavy
  - NN truck

- **NP**
  - JJ small
  - JJ red
  - NNS rentals

- **NP**
  - JJ dark
  - JJ red
  - NNS cars

- **NP**
  - NML
  - JJ strong
  - NN defense
  - NNS agencies

You will construct a PCFG from these trees with NP as the start symbol in this grammar. To binarize the trees, you will introduce a NP symbol to turn the ternary rules into binary rules (you can write NP-B for “NP bar” if you’re typing your answer). This will be described in the following questions.

For all question parts, assume that Greg comes along with a great part-of-speech tagger and tags these sentences. So: (a) do not write down any grammar rules in the lexicon; only include the rules above the part-of-speech tag layer; (b) when doing CKY, assume the gold tag has a score of 0.0 and all other tags have a score of $-\infty$. In this case, each word’s tag is unambiguous anyway, so this does not actually change your answer, just reduces the amount of writing.

a. (5 points) Write the grammar (rules and probabilities) you get if you use right-binarization: that is, NP is introduced as a right child under the NP symbol for ternary-branching rules. (So NP $\rightarrow$ JJ NP-B is introduced for the *small red cars* example).

b. (4 points) Now parse the phrase *large red cars* with the tags JJ JJ NNS. Show your work and write out every parse with nonzero probability and its probability.
c. (4 points) Write the grammar you get if you use right-binarization on *strong defense agencies* but left-binarization on *small red cars*. That is, for that one tree, make the \( \text{NP} \) the left child of the root \( \text{NP} \).

d. (4 points) Now parse *large red cars* with tags JJ JJ NNS using this new grammar. Show your work, write out every parse with nonzero probability and its probability.