

CS378: Natural Language Processing

Lecture 16: Transformers

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Multi-Head Self-Attention



Multi-Head Self Attention

- ▶ Multiple “heads” analogous to different convolutional filters
- ▶ Let $E = [\text{sent len, embedding dim}]$ be the input sentence. This will be passed through three different linear layers to produce three mats:
 - ▶ Query $Q = EW^Q$: these are like the **decoder hidden state** in attention
 - ▶ Keys $K = EW^K$: these control what gets attended to, along with the query
 - ▶ Values $V = EW^V$: these vectors get summed up to form the output

$$\text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)V$$

← dim of keys



Self-Attention

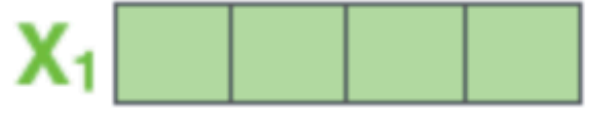
Alammar, *The Illustrated Transformer*

Input

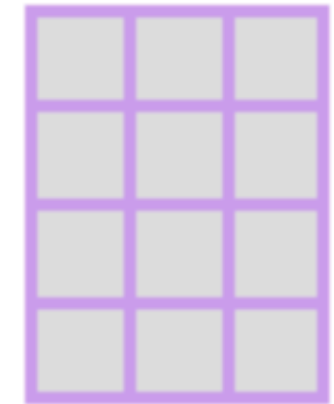
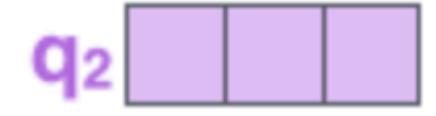
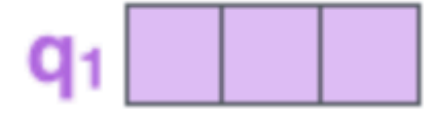
Thinking

Machines

Embedding

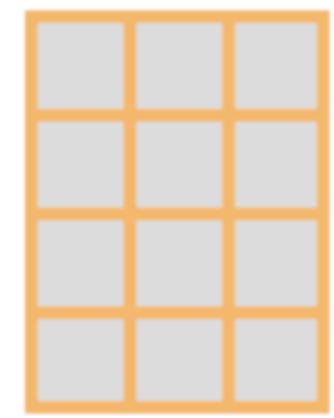
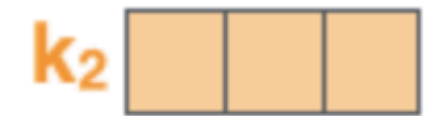
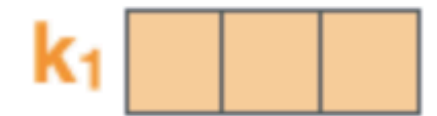


Queries



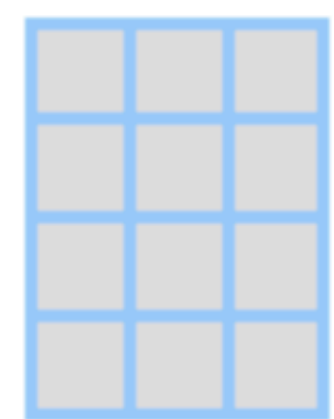
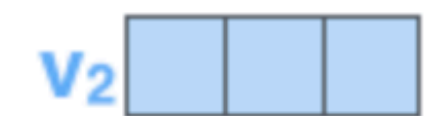
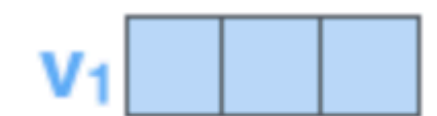
W^Q

Keys



W^K

Values



W^V



Self-Attention

$$X \times W^Q = Q$$

$$X \times W^K = K$$

$$X \times W^V = V$$

Alammar, *The Illustrated Transformer*

sent len x sent len (attn for each word to each other)

$$\text{softmax} \left(\frac{Q \times K^T}{\sqrt{d_k}} \right) \times V$$

sent len x hidden dim

Z is a weighted combination of V rows



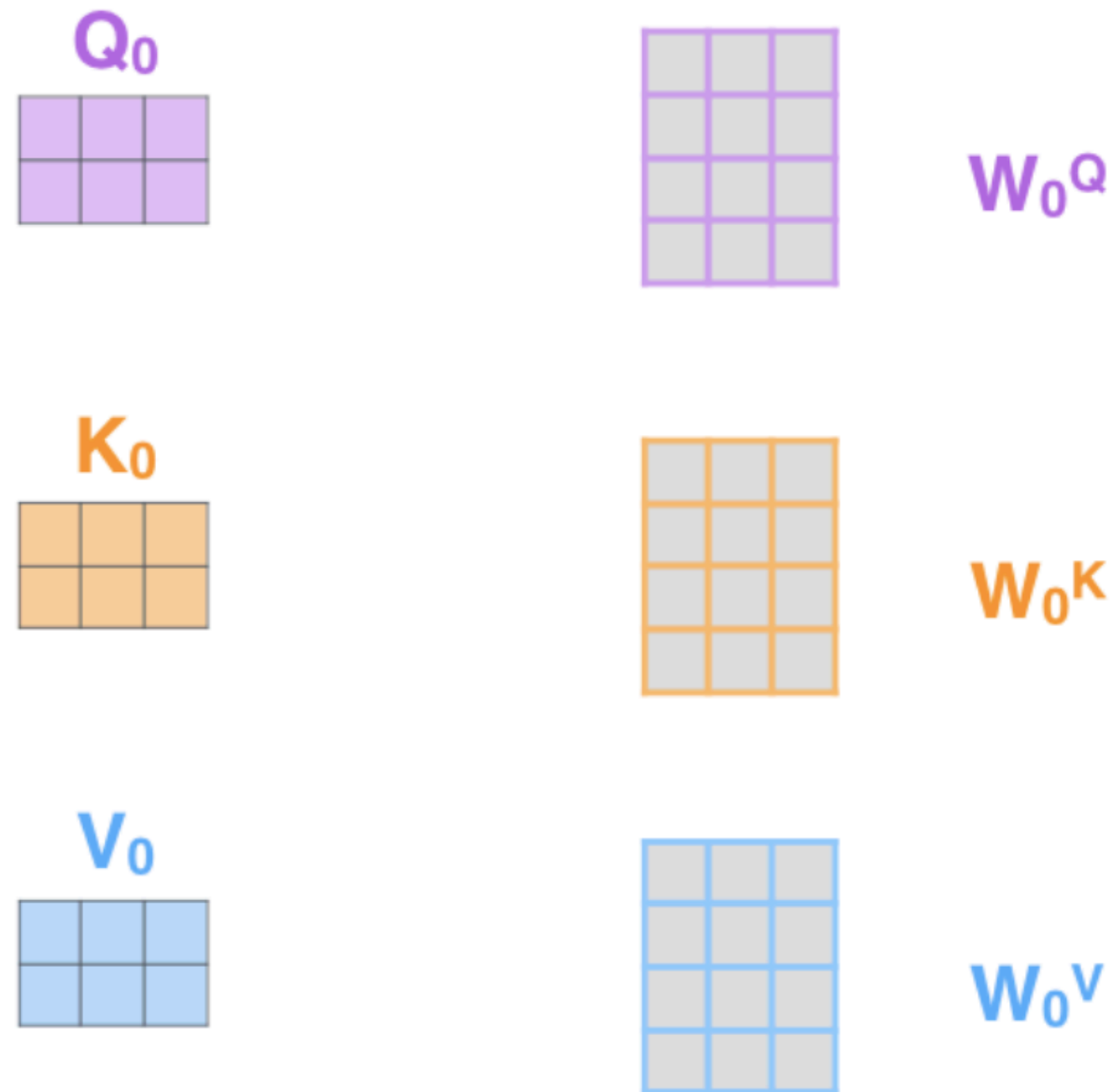
Multi-head Self-Attention

Just duplicate the whole computation with different weights:

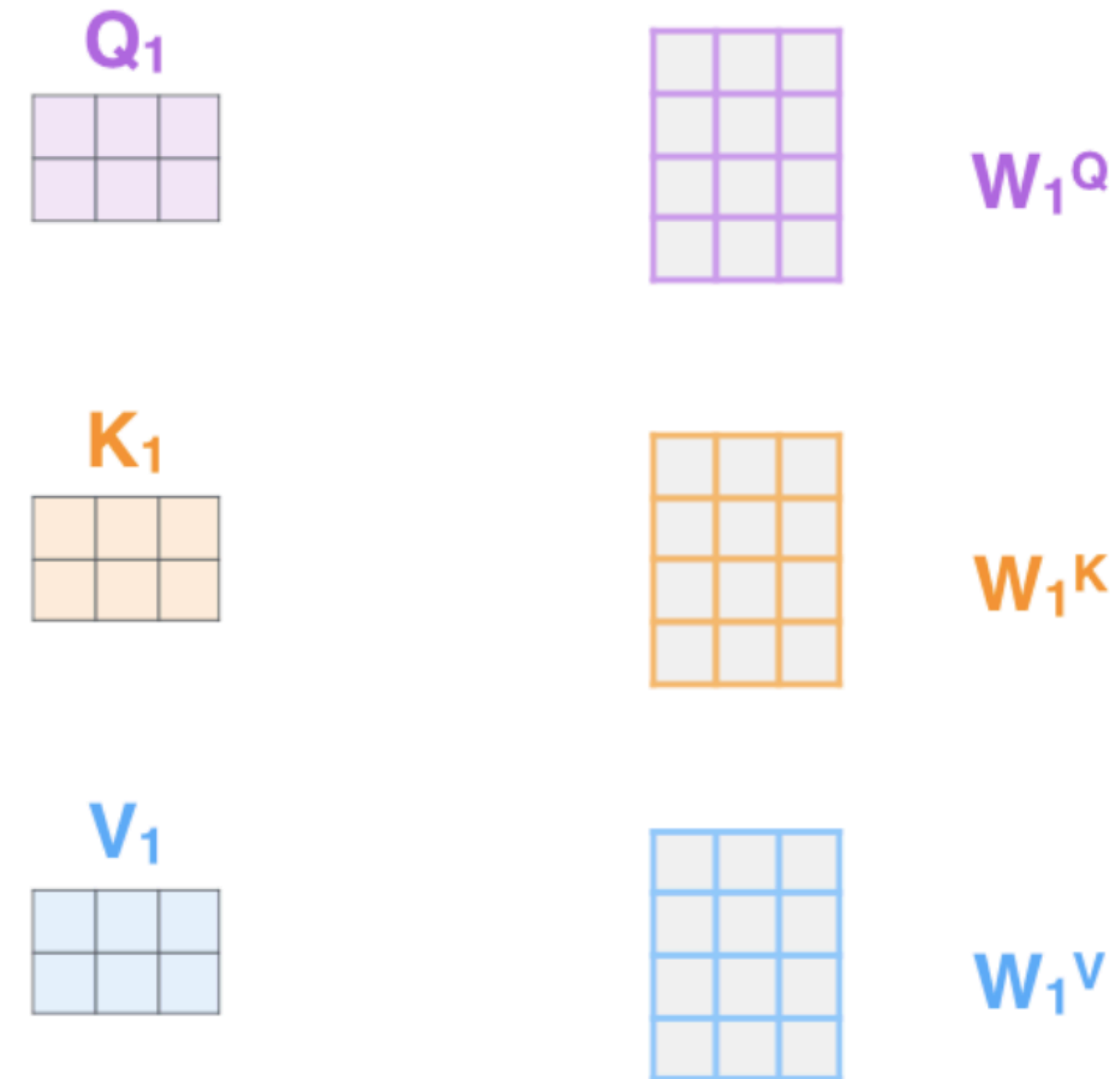
Alammar, *The Illustrated Transformer*



ATTENTION HEAD #0



ATTENTION HEAD #1





Multi-head Self-Attention

1) This is our input sentence*

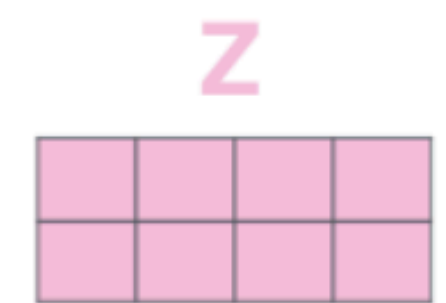
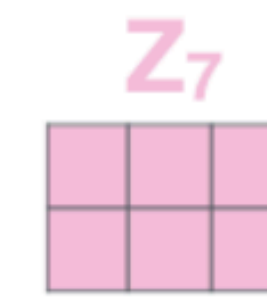
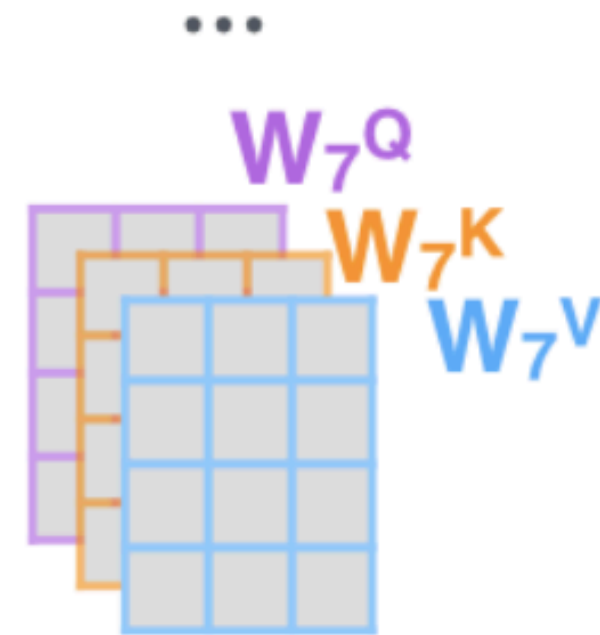
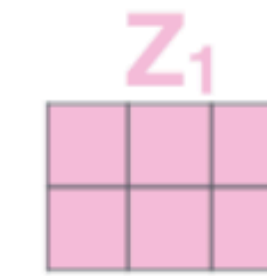
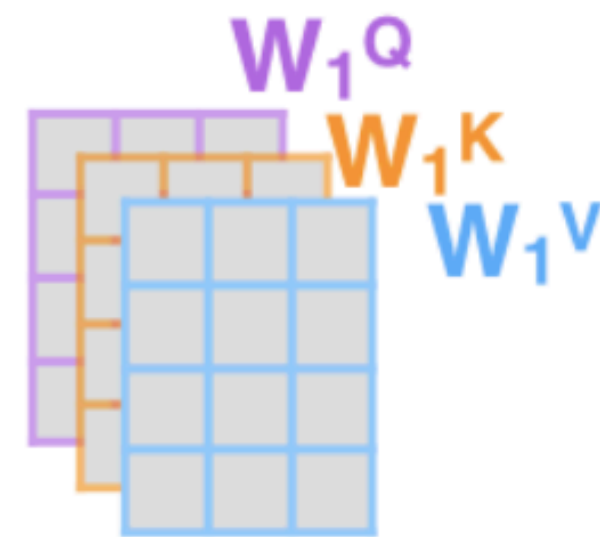
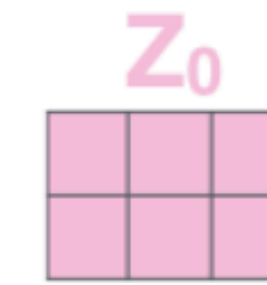
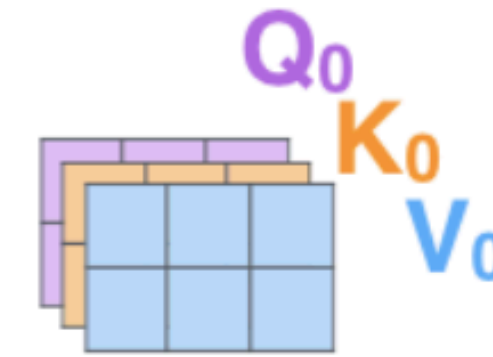
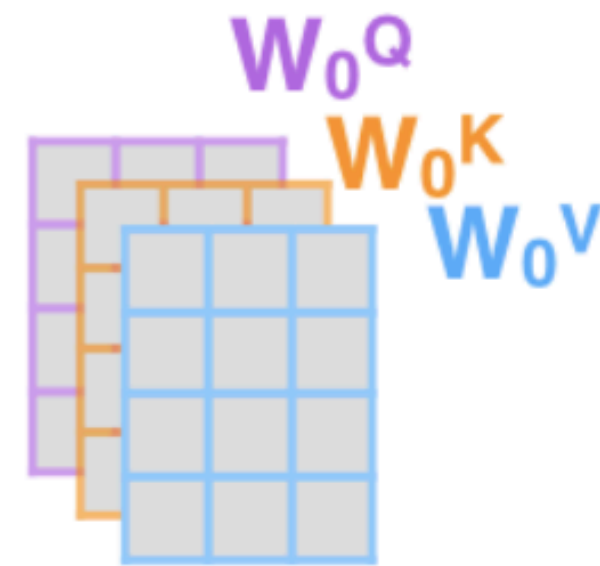
2) We embed each word*

3) Split into 8 heads. We multiply X or R with weight matrices

4) Calculate attention using the resulting $Q/K/V$ matrices

5) Concatenate the resulting Z matrices, then multiply with weight matrix W^O to produce the output of the layer

Thinking Machines



* In all encoders other than #0, we don't need embedding. We start directly with the output of the encoder right below this one





Properties of Self-Attention

Layer Type	Complexity per Layer	Sequential Operations	Maximum Path Length
Self-Attention	$O(n^2 \cdot d)$	$O(1)$	$O(1)$
Recurrent	$O(n \cdot d^2)$	$O(n)$	$O(n)$
Convolutional	$O(k \cdot n \cdot d^2)$	$O(1)$	$O(\log_k(n))$
Self-Attention (restricted)	$O(r \cdot n \cdot d)$	$O(1)$	$O(n/r)$

- ▶ n = sentence length, d = hidden dim, k = kernel size, r = restricted neighborhood size
- ▶ **Quadratic complexity**, but $O(1)$ sequential operations (not linear like in RNNs) and $O(1)$ “path” for words to inform each other

Transformers

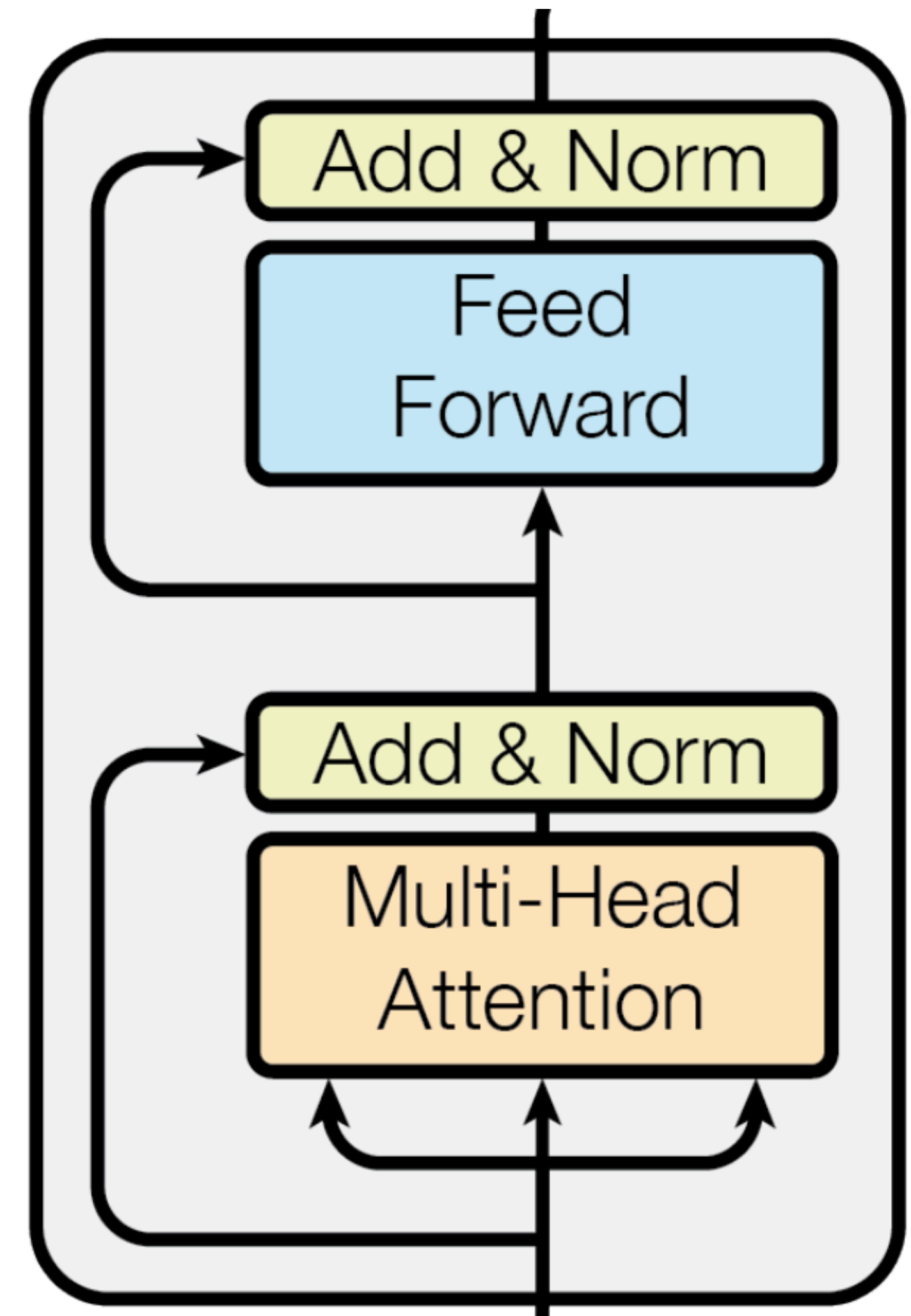


Architecture

- ▶ Alternate multi-head self-attention with feedforward layers that **operate over each word individually**

$$\text{FFN}(x) = \max(0, xW_1 + b_1)W_2 + b_2$$

- ▶ These feedforward layers are where most of the parameters are
- ▶ Residual connections in the model: input of a layer is added to its output
- ▶ Layer normalization: controls the scale of different layers in very deep networks (not needed in A4)



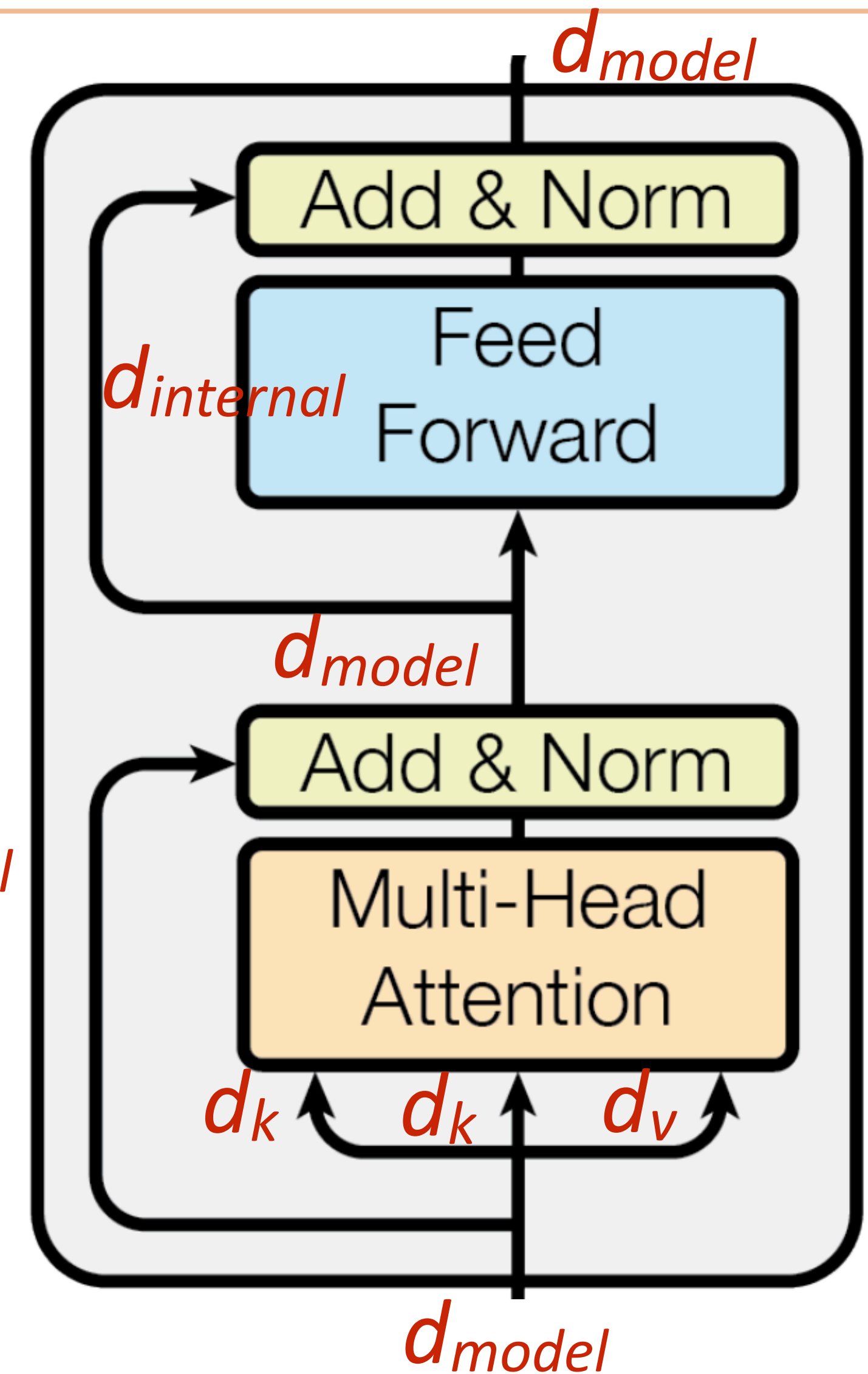


Dimensions

- ▶ Vectors: d_{model}
- ▶ Queries/keys: d_k , always smaller than d_{model}
- ▶ Values: separate dimension d_v , output is multiplied by W^O which is $d_v \times d_{model}$ so we can get back to d_{model} before the residual
- ▶ FFN can explode the dimension with W_1 and collapse it back with W_2

$d_v \rightarrow d_{model}$

$$\text{FFN}(x) = \max(0, xW_1 + b_1)W_2 + b_2$$





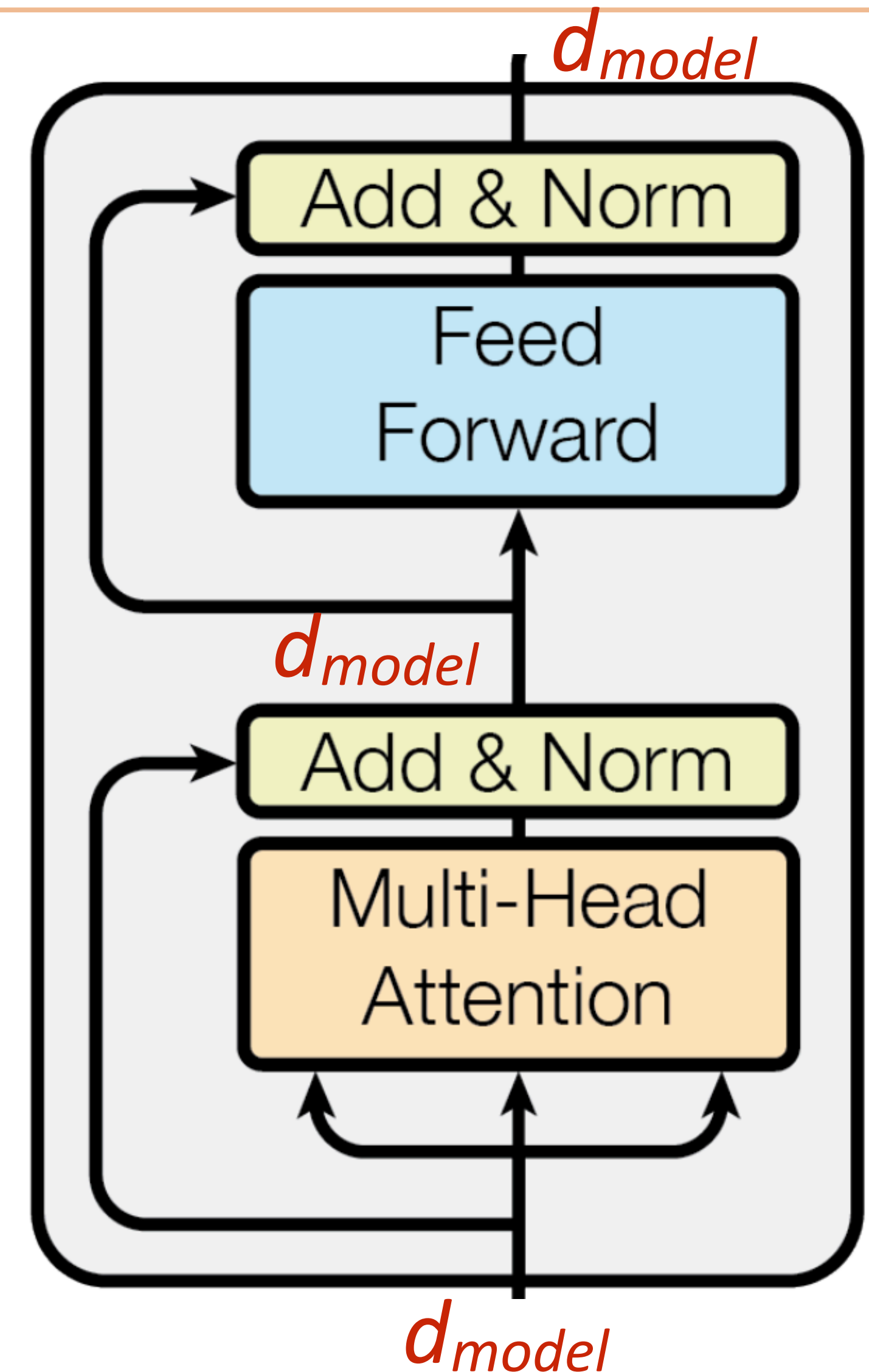
Transformer Architecture

	N	d_{model}	d_{ff}	h	d_k	d_v
base	6	512	2048	8	64	64

► From Vaswani et al.

Model Name	n_{params}	n_{layers}	d_{model}	n_{heads}	d_{head}
GPT-3 Small	125M	12	768	12	64
GPT-3 Medium	350M	24	1024	16	64
GPT-3 Large	760M	24	1536	16	96
GPT-3 XL	1.3B	24	2048	24	128
GPT-3 2.7B	2.7B	32	2560	32	80
GPT-3 6.7B	6.7B	32	4096	32	128
GPT-3 13B	13.0B	40	5140	40	128
GPT-3 175B or “GPT-3”	175.0B	96	12288	96	128

► From GPT-3; d_{head} is our d_k





Transformer Architecture

1	description	FLOPs / update	% FLOPS MHA	% FLOPS FFN	% FLOPS attn	% FLOPS logit
8	OPT setups					
9	760M	4.3E+15	35%	44%	14.8%	5.8%
10	1.3B	1.3E+16	32%	51%	12.7%	5.0%
11	2.7B	2.5E+16	29%	56%	11.2%	3.3%
12	6.7B	1.1E+17	24%	65%	8.1%	2.4%
13	13B	4.1E+17	22%	69%	6.9%	1.6%
14	30B	9.0E+17	20%	74%	5.3%	1.0%
15	66B	9.5E+17	18%	77%	4.3%	0.6%
16	175B	2.4E+18	17%	80%	3.3%	0.3%

Credit: Stephen Roller on Twitter



Transformers: Position Sensitivity

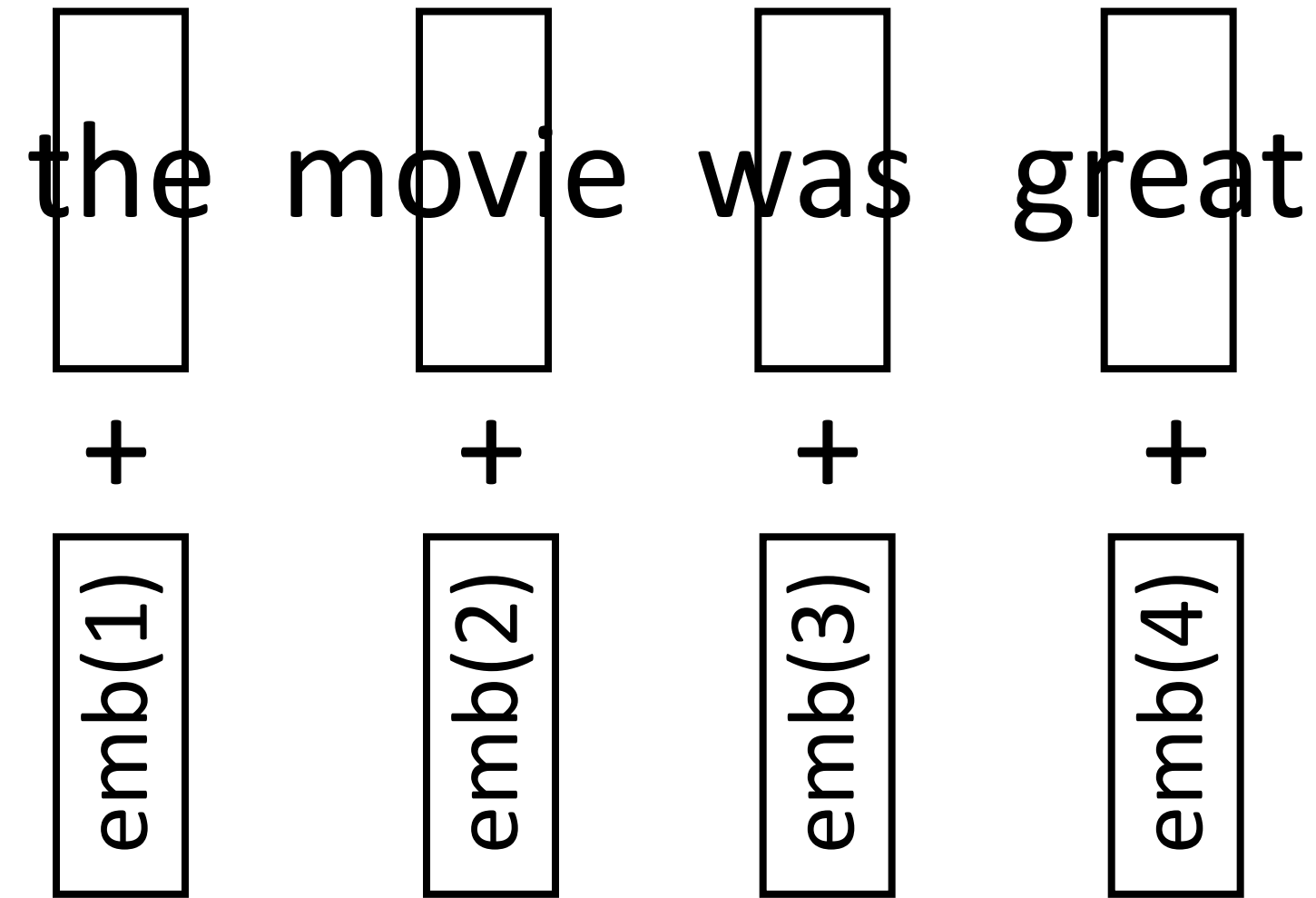
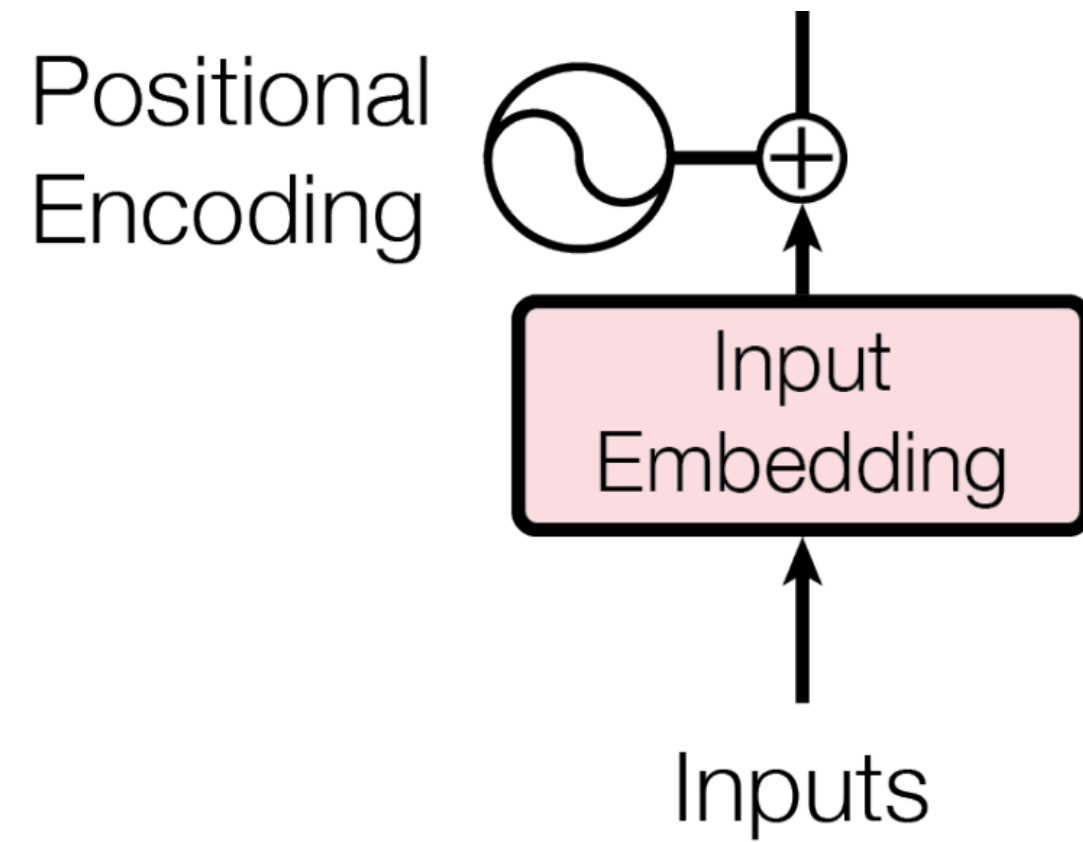
*The ballerina is very excited that **she** will dance in the **show**.*

The diagram illustrates attention weights between the words 'she' and 'show'. A blue arrow points from 'she' to 'The ballerina is very excited that', and another blue arrow points from 'she' to 'show'. A red arrow points from 'show' to 'she'.

- ▶ If this is in a longer context, we want words to attend *locally*
- ▶ But transformers have *no notion of position* by default



Transformers: Position Sensitivity



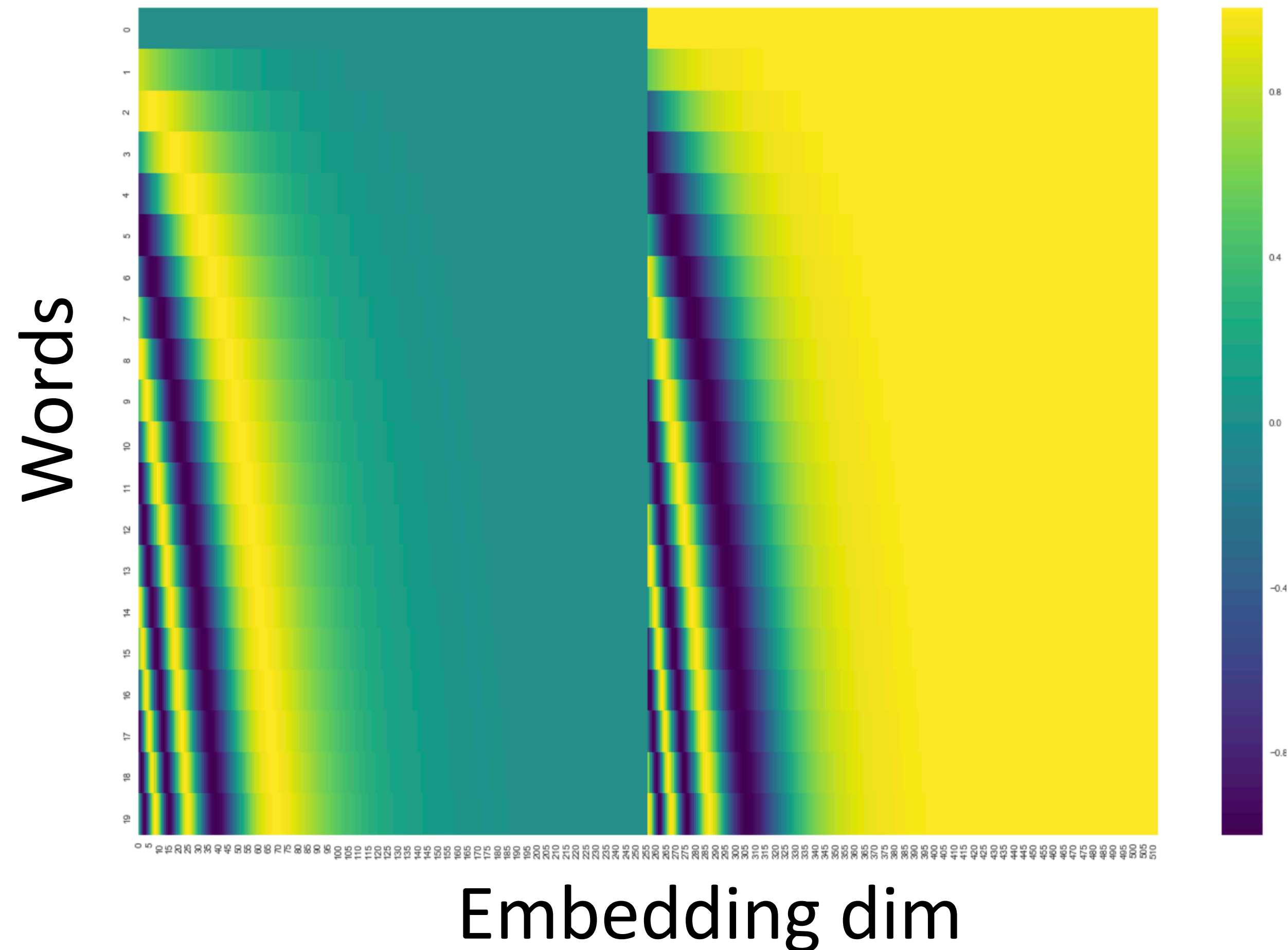
- ▶ Encode each sequence position as an integer, add it to the word embedding vector
- ▶ Why does this work?



Transformers

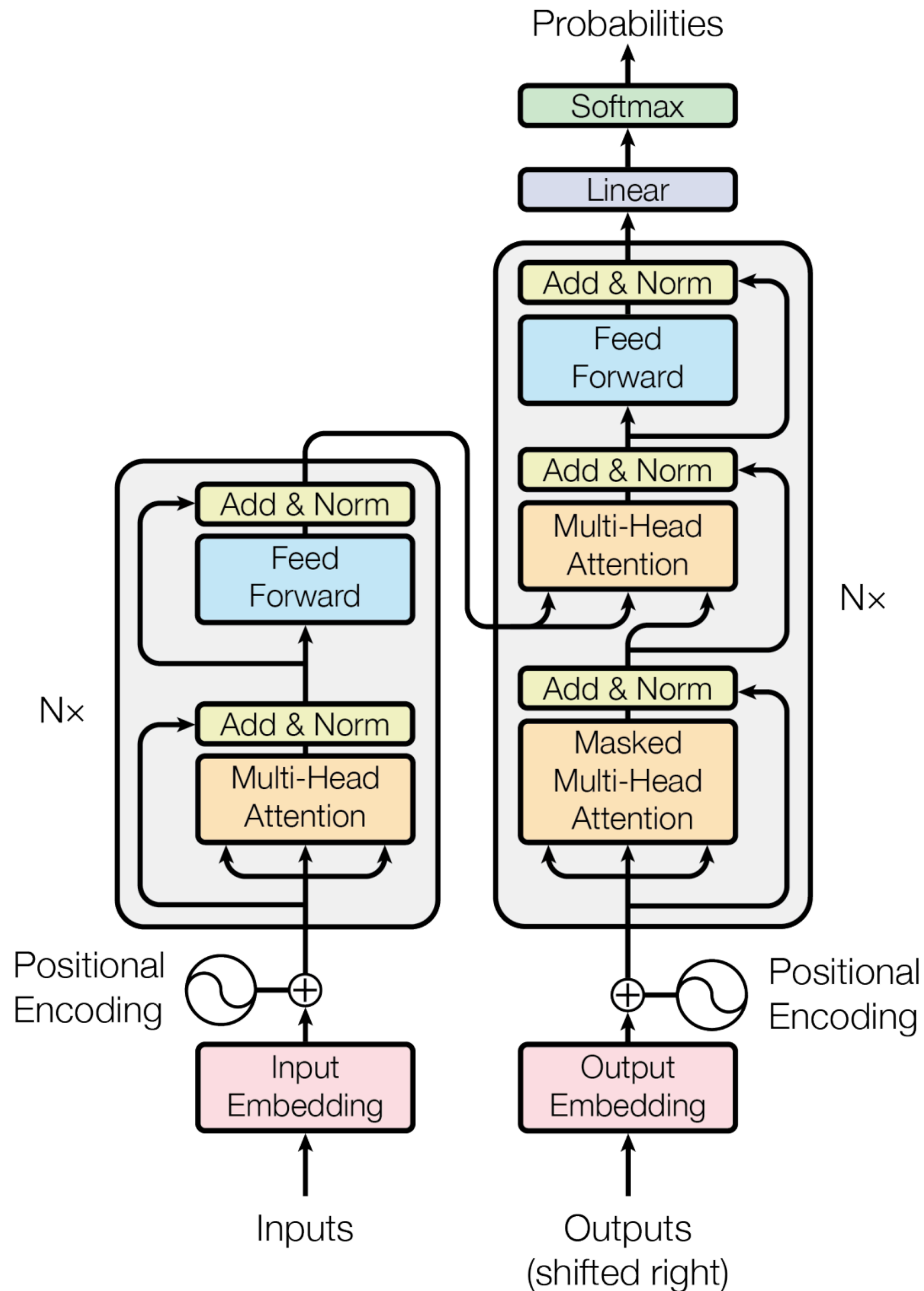
Alammar, *The Illustrated Transformer*

- ▶ Alternative from Vaswani et al.: sines/cosines of different frequencies (closer words get higher dot products by default)





Transformers: Complete Model



- ▶ Original Transformer paper presents an **encoder-decoder** model
- ▶ Right now we don't need to think about both of these parts — will return in the context of MT
- ▶ Can turn the encoder into a decoder-only model through use of a triangular causal attention mask (only allow attention to previous tokens)