CS388: Natural Language Processing

Lecture 3: Multiclass Classification

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Some slides adapted from Vivek Srikumar, University of Utah



Administrivia

- ▶ Course enrollment
- Mini 1 due Thursday at midnight (submit writeup on Gradescope + code/output on Canvas)



Recall: Feature Extraction

O O PER O PER O O O O O O O O Sunday, Thomas and Mary went to the farmer's market

i=0 1 2 3 4 5 6 7 8 9

- ► Feature extractor: function from (sentence, position) => sparse feature vector describing that position in the sentence
 - "Current word": what is the word at this index?
 - "Previous word": what is the word that precedes the index?
 [currWord=Thomas] [currWord=Mary] [prevWord = and]

f(x, i=4) = [0 1

- ▶ Feature vector only has 2 nonzero entries out of 10k+ possible
- ▶ All features coexist in the same space! Other feats (char level, ...) possible



Recall: Binary Classification

 $\text{Logistic regression: } P(y=1|x) = \frac{\exp\left(\sum_{i=1}^n w_i x_i\right)}{\left(1 + \exp\left(\sum_{i=1}^n w_i x_i\right)\right)} \quad \text{these sums are sparse!}$

Decision rule: $P(y=1|x) \geq 0.5 \Leftrightarrow w^{\top}x \geq 0$

Gradient: differentiate the log likelihood: x(y - P(y = 1|x))

- This is the gradient of a single example. Can then apply stochastic gradient (or related optimization methods like Adagrad, etc.)
- ML pipeline: input -> feature representation, train model on labeled data (with stochastic gradient methods), then test on new data



This Lecture

- ▶ Sentiment analysis
- Multiclass fundamentals
- ▶ Feature extraction
- ▶ Multiclass logistic regression

Sentiment Analysis



Sentiment Analysis

this movie was great! would watch again

+

the movie was gross and overwrought, but I liked it

+

this movie was <mark>not</mark> really very <mark>enjoyable</mark>



- ▶ Bag-of-words doesn't seem sufficient (discourse structure, negation)
- ▶ There are some ways around this: extract bigram feature for "not X" for all X following the not

Bo Pang, Lillian Lee, Shivakumar Vaithyanathan (2002)

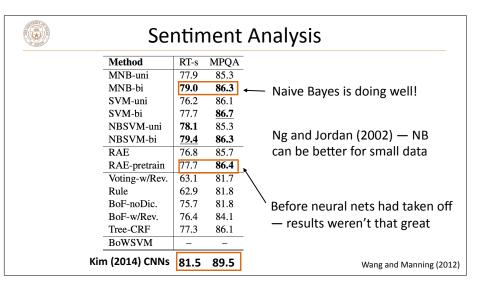


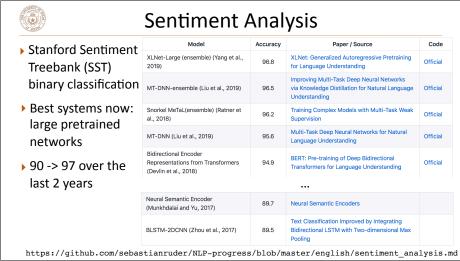
Sentiment Analysis

	Features	# of	frequency or	NB	ME	SVM
		features	presence?			
(1)	unigrams	16165	freq.	78.7	N/A	72.8
(2)	unigrams	"	pres.	81.0	80.4	82.9
(3)	unigrams+bigrams	32330	pres.	80.6	80.8	82.7
(4)	bigrams	16165	pres.	77.3	77.4	77.1
(5)	unigrams+POS	16695	pres.	81.5	80.4	81.9
(6)	adjectives	2633	pres.	77.0	77.7	75.1
(7)	top 2633 unigrams	2633	pres.	80.3	81.0	81.4
(8)	unigrams+position	22430	pres.	81.0	80.1	81.6

▶ Simple feature sets can do pretty well!

Bo Pang, Lillian Lee, Shivakumar Vaithyanathan (2002)





Multiclass Fundamentals

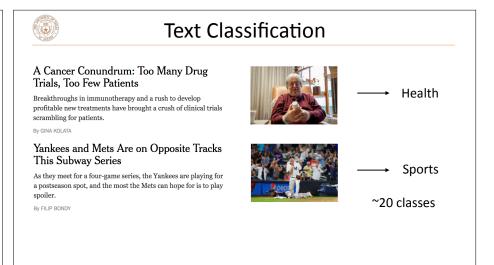
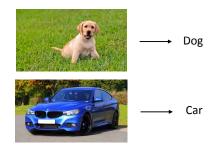




Image Classification



▶ Thousands of classes (ImageNet)



Entailment

Three-class task over sentence pairs

 Not clear how to do this with simple bag-ofwords features A soccer game with multiple males playing. ENTAILS

Some men are playing a sport.

A black race car starts up in front of a crowd of people.

CONTRADICTS

A man is driving down a lonely road

A smiling costumed woman is holding an umbrella.

NEUTRAL

A happy woman in a fairy costume holds an umbrella.

Bowman et al. (2015)



Entity Linking

Although he originally won the event, the United States Anti-Doping Agency announced in August 2012 that they had disqualified (Armstrong) from his seven consecutive Tour de France wins from 1999–2005.





Lance Edward Armstrong is an American former professional road cyclist





Armstrong County is a county in Pennsylvania...

.....

▶ 4,500,000 classes (all articles in Wikipedia)



Reading Comprehension

One day, James thought he would go into town and see what kind of trouble he could get into. He went to the grocery store and pulled all the pudding off the shelves and ate two jars. Then he walked to the fast food restaurant and ordered 15 bags of fries. He didn't pay, and instead headed home.

- 3) Where did James go after he went to the grocery store?
- A) his deck
- B) his freezer
- C) a fast food restaurant
- D) his room

After about a month, and after getting into lots of trouble, James finally made up his mind to be a better turtle.

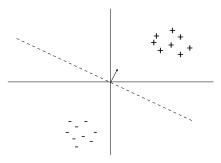
▶ Multiple choice questions, 4 classes (but classes change per example)

Richardson (2013)



Binary Classification

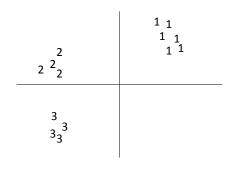
▶ Binary classification: one weight vector defines positive and negative classes





Multiclass Classification

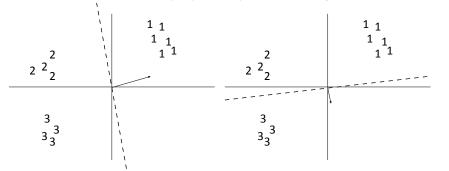
▶ Can we just use binary classifiers here?





Multiclass Classification

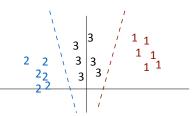
- ▶ One-vs-all: train k classifiers, one to distinguish each class from all the rest
- ▶ How do we reconcile multiple positive predictions? Highest score?





Multiclass Classification

Not all classes may even be separable using this approach

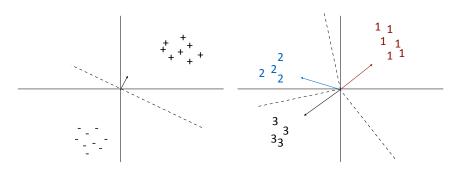


► Can separate 1 from 2+3 and 2 from 1+3 but not 3 from the others (with these features)



Multiclass Classification

- ▶ Binary classification: one weight vector defines both classes
- Multiclass classification: different weights and/or features per class





Multiclass Classification

- \blacktriangleright Formally: instead of two labels, we have an output space $\mathcal Y$ containing a number of possible classes
- ▶ Same machinery that we'll use later for exponentially large output spaces, including sequences and trees
- features depend on choice of label now! note: this isn't the gold label
- ▶ Multiple feature vectors, one weight vector
- lacktriangle Can also have one weight vector per class: $\operatorname{argmax}_{y\in\mathcal{Y}}w_y^{\top}f(x)$



Different Weights vs. Different Features

- lacktriangleright Different features: $rgmax_{y\in\mathcal{Y}}w^{ op}f(x,y)$
 - ▶ Suppose \mathcal{Y} is a structured label space (part-of-speech tags for each word in a sentence). f(x,y) extracts features over shared parts of these
- ightharpoonup Different weights: $\operatorname{argmax}_{y \in \mathcal{Y}} w_y^{\top} f(x)$
 - ▶ Generalizes to neural networks: f(x) is the first n-1 layers of the network, then you multiply by a final linear layer at the end
- For linear multiclass classification with discrete classes, these are identical

Feature Extraction



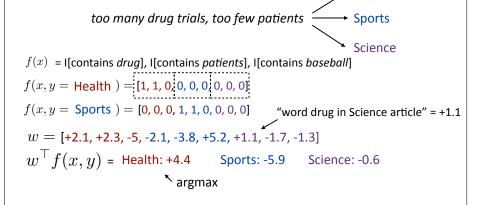
Block Feature Vectors

- Decision rule: $\operatorname{argmax}_{y \in \mathcal{V}} w^{\top} f(x, y)$ Health too many drug trials, too few patients Sports Science Base feature function: f(x) = I[contains drug], I[contains patients], I[contains baseball] = [1, 1, 0]feature vector blocks for each label
- f(x, y = Health) = [1, 1, 0, 0, 0, 0, 0, 0] I[contains drug & label = Health] f(x, y = Sports) = [0, 0, 0, 1, 1, 0, 0, 0, 0]
- ▶ Equivalent to having three weight vectors in this case
- ▶ We are NOT looking at the gold label! Instead looking at the candidate label



Making Decisions

Health





Part-of-speech tagging as multiclass

- the router | blocks | the packets ▶ Classify blocks as one of 36 POS tags **NNS** \blacktriangleright Example is a (sentence, index) pair (x,i=2): the **VBZ**
- word blocks in this sentence
- Extract features with respect to this word:

- tagged as VBZ! saying that Next two lectures: sequence labeling the follows the VBZ word

not saying that the is

NN

DT

Multiclass Logistic Regression



Multiclass Logistic Regression

$$P_w(y|x) = \frac{\exp\left(w^\top f(x,y)\right)}{\sum_{y' \in \mathcal{Y}} \exp\left(w^\top f(x,y')\right)} \quad \text{Compare to binary:} \\ P(y=1|x) = \frac{\exp(w^\top f(x))}{1 + \exp(w^\top f(x))}$$

sum over output space to normalize

exp/sum(exp): also called softmax

Training: maximize
$$\mathcal{L}(x,y) = \sum_{i=1}^n \log P(y_j^*|x_j)$$

$$= \sum_{j=1}^{n} \left(w^{\top} f(x_j, y_j^*) - \log \sum_{y} \exp(w^{\top} f(x_j, y)) \right)$$

negative class implicitly had

f(x, y=0) = the zero vector



Training

- $\text{ Multiclass logistic regression } P_w(y|x) = \frac{\exp\left(w^\top f(x,y)\right)}{\sum_{x' \in \mathcal{V}} \exp\left(w^\top f(x,y')\right)}$
- Likelihood $\mathcal{L}(x_j, y_j^*) = w^\top f(x_j, y_j^*) \log \sum_{x_j} \exp(w^\top f(x_j, y))$ $\frac{\partial}{\partial w_i} \mathcal{L}(x_j, y_j^*) = f_i(x_j, y_j^*) - \frac{\sum_y f_i(x_j, y) \exp(w^\top f(x_j, y))}{\sum_y \exp(w^\top f(x_j, y))}$

$$\begin{split} \frac{\partial}{\partial w_i} \mathcal{L}(x_j, y_j^*) &= f_i(x_j, y_j^*) - \sum_y f_i(x_j, y) P_w(y|x_j) \\ \frac{\partial}{\partial w_i} \mathcal{L}(x_j, y_j^*) &= f_i(x_j, y_j^*) - \mathbb{E}_y[f_i(x_j, y)] \text{ model's expectation of } \\ \text{gold feature value} \end{split}$$



Training

$$\frac{\partial}{\partial w_i} \mathcal{L}(x_j, y_j^*) = f_i(x_j, y_j^*) - \sum_{y} f_i(x_j, y) P_w(y|x_j)$$

too many drug trials, too few patients

$$P_w(y|x) = [0.2, 0.5, 0.3]$$

$$f(x, y = Sports) = [0, 0, 0, 1, 1, 0, 0, 0, 0]$$

gradient:

$$= [0.8, 0.8, 0, -0.5, -0.5, 0, -0.3, -0.3, 0]$$

"towards gold feature value, away from what the model thinks"



Multiclass Logistic Regression: Summary

$$\text{Model: } P_w(y|x) = \frac{\exp\left(w^\top f(x,y)\right)}{\sum_{y' \in \mathcal{Y}} \exp\left(w^\top f(x,y')\right)}$$

- Inference: $\operatorname{argmax}_{y} P_{w}(y|x)$
- Learning: gradient ascent on the discriminative log-likelihood

$$f(x, y^*) - \mathbb{E}_y[f(x, y)] = f(x, y^*) - \sum_y [P_w(y|x)f(x, y)]$$

"towards gold feature value, away from expectation of feature value"

Generative vs. Discriminative Models



Learning in Probabilistic Models

- ▶ So far we have talked about discriminative classifiers (e.g., logistic regression which models P(y|x))
- Cannot analytically compute optimal weights for such models, need to use gradient descent
- ▶ What about generative models?



Naive Bayes

- ullet Data point $\,x=(x_1,...,x_n)$, label $y\in\{0,1\}$
- ullet Formulate a probabilistic model that places a distribution P(x,y)
- ightharpoonup Compute P(y|x), predict $\operatorname{argmax}_y P(y|x)$ to classify

$$P(y|x) = \frac{P(y)P(x|y)}{P(x)} \qquad \text{Bayes' Rule} \\ \propto P(y)P(x|y) \qquad \text{for finding the max} \\ = P(y)\prod^n P(x_i|y) \qquad \text{``Naive'' assumption:}$$



Maximum Likelihood Estimation

- ightharpoonup Data points (x_j, y_j) provided (j indexes over examples)
- Find values of P(y), $P(x_i|y)$ that maximize data likelihood (generative):

$$\prod_{j=1}^m P(y_j,x_j) = \prod_{j=1}^m P(y_j) \left[\prod_{i=1}^n P(x_{ji}|y_j) \right]$$
 data points (j) features (i) ith feature of jth example

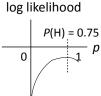


Maximum Likelihood Estimation

- ▶ Imagine a coin flip which is heads with probability p
- ▶ Observe (H, H, H, T) and maximize likelihood: $\prod_{j=1}^m P(y_j) = p^3(1-p)$
- ▶ Easier: maximize log likelihood

$$\sum_{j=1}^{m} \log P(y_j) = 3 \log p + \log(1 - p)$$

Maximum likelihood parameters for binomial/ multinomial = read counts off of the data + normalize





Maximum Likelihood Estimation

- ightharpoonup Data points (x_j, y_j) provided (j indexes over examples)
- lacktriangleright Find values of $P(y),\ P(x_i|y)$ that maximize data likelihood (generative):

$$\prod_{j=1}^{m} P(y_j, x_j) = \prod_{j=1}^{m} P(y_j) \left[\prod_{i=1}^{n} P(x_{ji}|y_j) \right]$$
data points (j) features (i) ith feature of jth example

▶ Equivalent to maximizing log of data likelihood:

$$\sum_{j=1}^{m} \log P(y_j, x_j) = \sum_{j=1}^{m} \left[\log P(y_j) + \sum_{i=1}^{n} \log P(x_{ji}|y_j) \right]$$

▶ Can do this by counting and normalizing distributions!



Summary

- Next time: HMMs / POS tagging
 - ▶ Locally-normalized generative models, so easy to estimate from data
 - ▶ First thing we have that we could plausibly sample real sentences from
- ▶ In 2 lectures: CRFs (NER)
- ▶ You've now seen everything you need to implement multi-class classification models