

CS388: Natural Language Processing

Lecture 12: Text rationales, Chain-of-thought

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Administrivia

- ▶ Project proposals due today
- ▶ Project 3 released today



Recap: Zero-shot/Few-shot prompting

- ▶ Single unlabeled datapoint \mathbf{x} , want to predict label y

\mathbf{x} = *The movie's acting could've been better, but the visuals and directing were top-notch.*

- ▶ Wrap \mathbf{x} in a template we call a **verbalizer** \mathbf{v}

Review: The movie's acting could've been better, but the visuals and directing were top-notch.

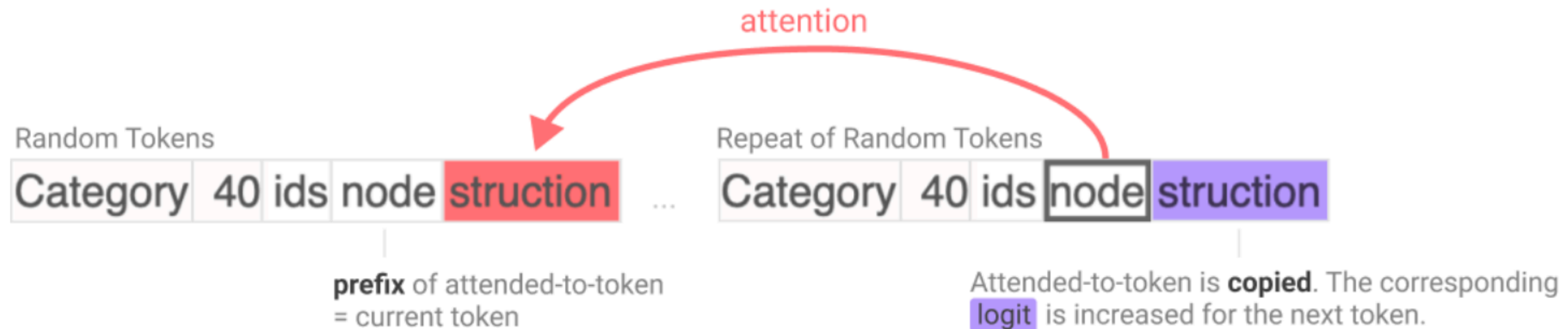
Out of positive, negative, or neutral, this review is — **GPT-3** → neutral

- ▶ Need the right prompt (but there is a “plateau” of prompts that work)
- ▶ Few-shot: add one or more examples. Typically works better! Particularly with rich examples like we'll see today



Recap: Understanding ICL

- ▶ ICL can learn a strategy like ordinary least-squares (Akyurek et al., 2022)
- ▶ We can identify *induction heads* in Transformers; these emerge when ICL performance improves (Olsson et al., 2022)





This Lecture

- ▶ Text rationales: text explanations of answers
- ▶ Chain-of-thought prompting (zero- and few-shot)
- ▶ Extensions
- ▶ Analysis of explanations

Text Rationales



Example from Vision

Laysan Albatross



Description: This is a large flying bird with black wings and a white belly.

Class Definition: The *Laysan Albatross* is a large seabird with a hooked yellow beak, black back and white belly.

Visual Explanation: This is a *Laysan Albatross* because this bird has a large wingspan, hooked yellow beak, and white belly.

Laysan Albatross

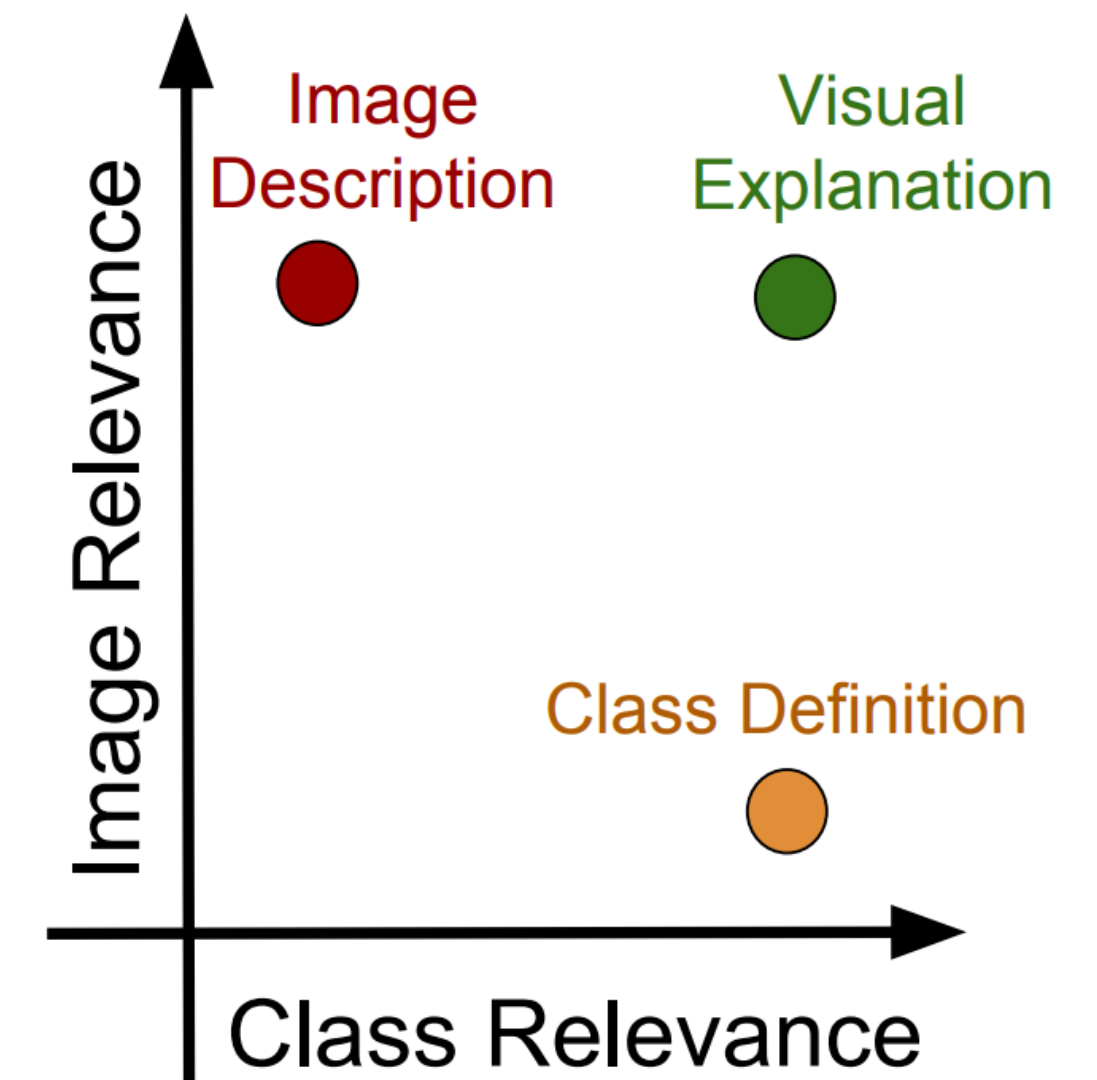


Description: This is a large bird with a white neck and a black back in the water.

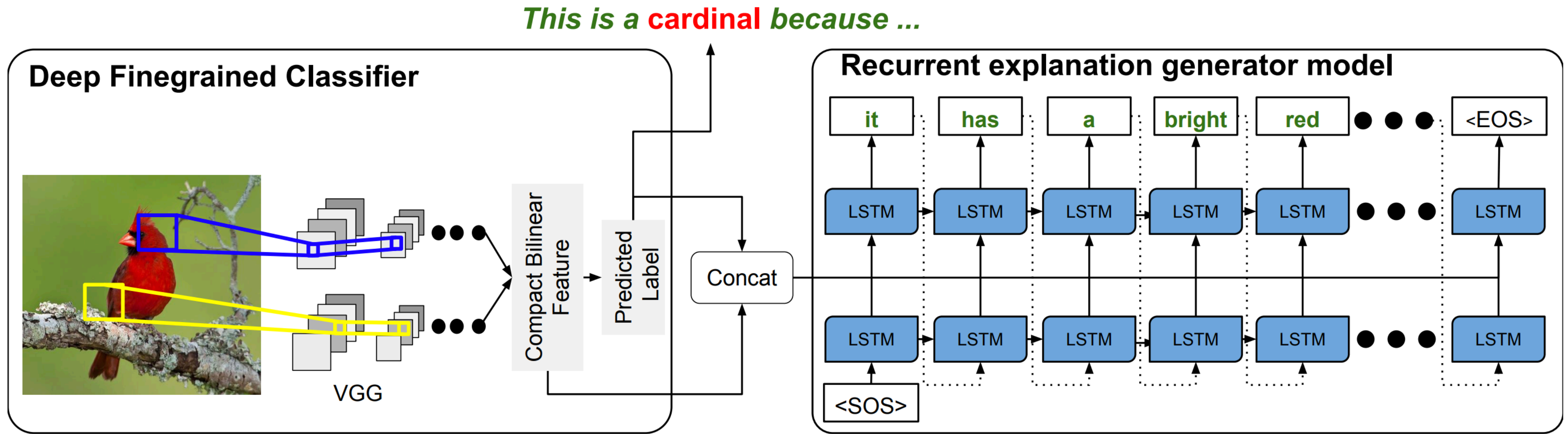
Class Definition: The *Laysan Albatross* is a large seabird with a hooked yellow beak, black back and white belly.

Visual Explanation: This is a *Laysan Albatross* because this bird has a hooked yellow beak white neck and black back.

- ▶ What makes a visual explanation? Should be relevant to the class and the image
- ▶ Are these features *really* what the model used?



Generating Explanations: Birds



- ▶ LSTM decoder looks at a feature vector and predicted label, then generates an explanation from those
- ▶ It's trained on human explanations — so it will likely produce explanations that look good (it learns to be a language model)



E-SNLI

Premise: An adult dressed in black holds a stick.

Hypothesis: An adult is walking away, empty-handed.

Label: contradiction

Explanation: Holds a stick implies using hands so it is not empty-handed.

Premise: A child in a yellow plastic safety swing is laughing as a dark-haired woman in pink and coral pants stands behind her.

Hypothesis: A young mother is playing with her daughter in a swing.

Label: neutral

Explanation: Child does not imply daughter and woman does not imply mother.

Premise: A man in an orange vest leans over a pickup truck.

Hypothesis: A man is touching a truck.

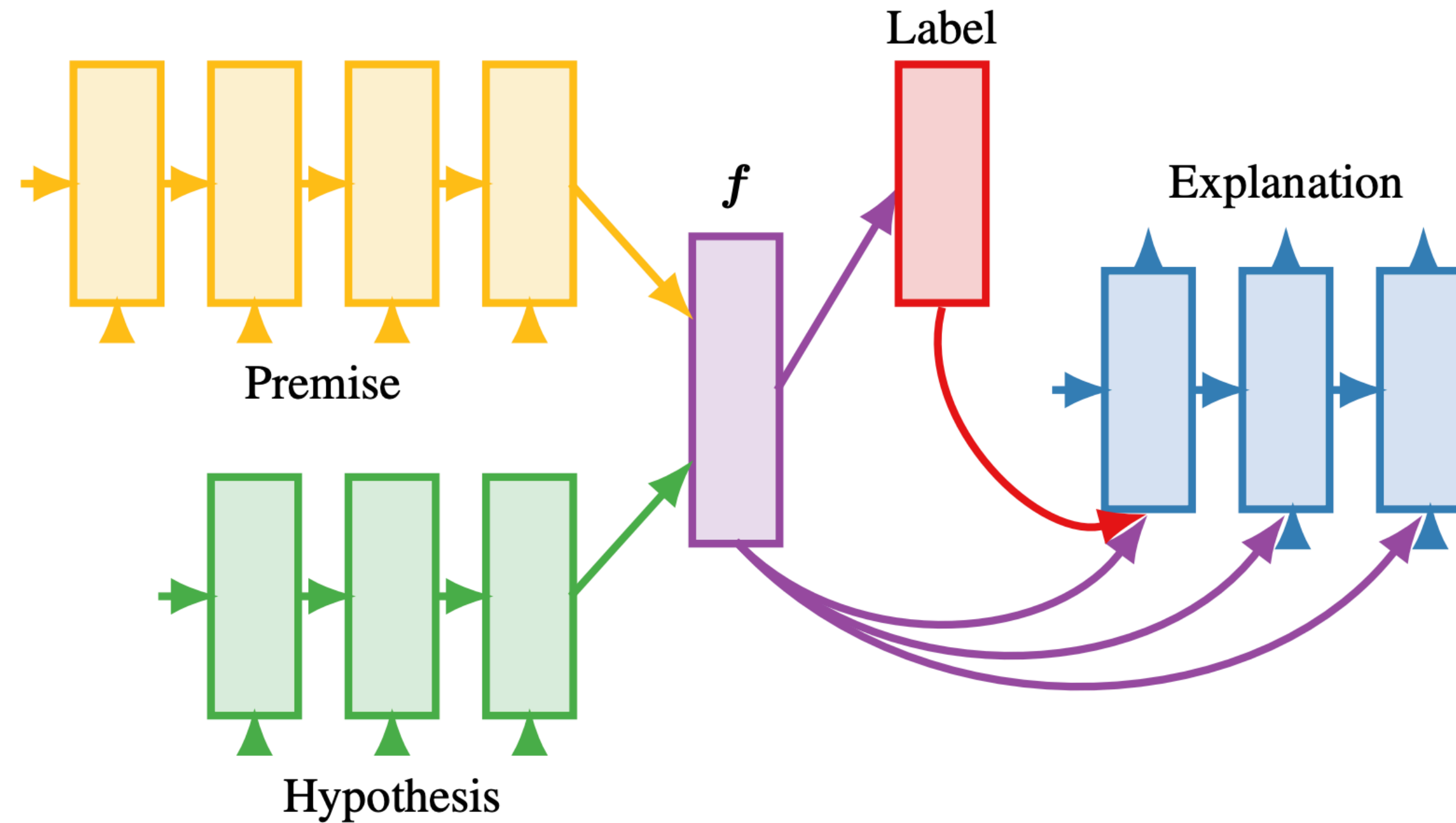
Label: entailment

Explanation: Man leans over a pickup truck implies that he is touching it.

- Two formats: highlights and text



Generating Explanations: E-SNLI



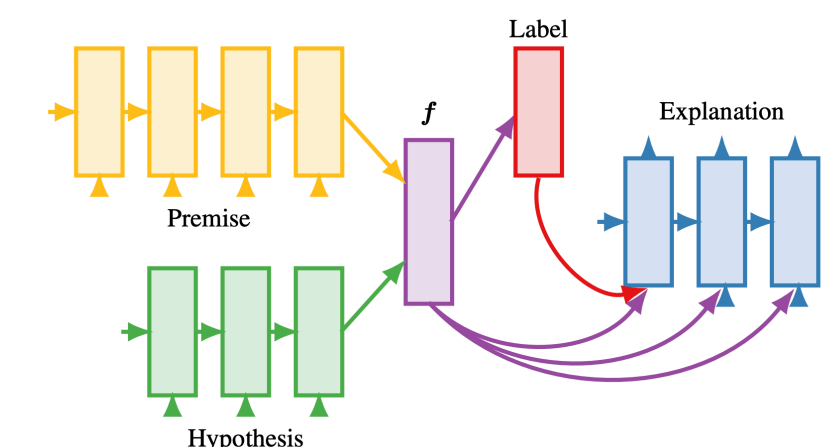
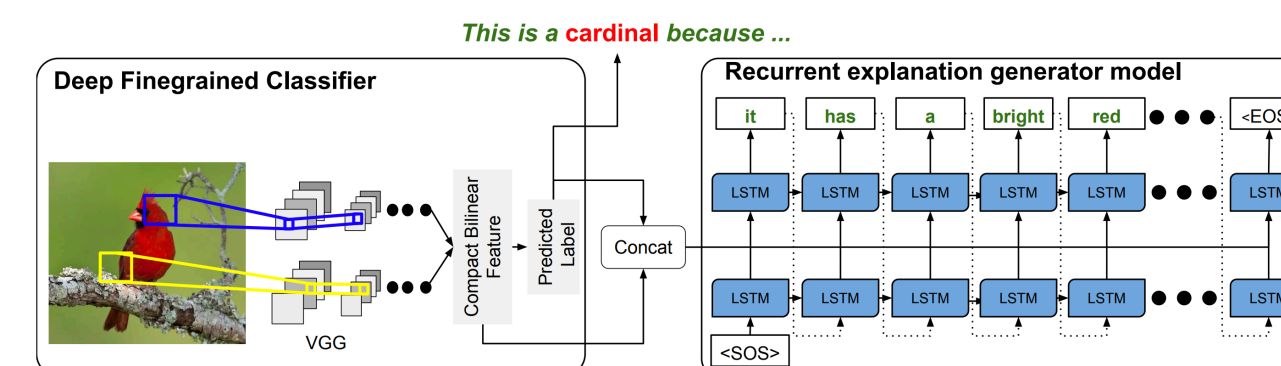
f = function of premise and hypothesis vectors

- ▶ Similar to birds: explanation is conditioned on the label + network state f
- ▶ Information from f is fed into the explanation LSTM, although we don't know how that information is being used



Text Rationales

- ▶ Can we generate a natural language explanation of a model's behavior?
- ▶ What are some advantages to this?
 - ▶ Easy for untrained users to understand
 - ▶ Multitasking to produce human-written explanations may help us learn
- ▶ What are some risks/disadvantages?





Text Explanations

- ▶ Issues with text explanations:
 - ▶ Hard to produce/consume (these models are sort of clunky)
 - ▶ Hard to know if they faithfully reflect what a model is doing
 - ▶ More broadly, hard to evaluate
- ▶ However, writing such explanations comes naturally to us...so that means that they reflect some kind of underlying reasoning process that we're doing?
- ▶ Pre-2021: this process would usually be captured structurally in a model.
2022 and beyond: chain of thought

Chain-of-thought



Text rationales vs. programs

Problem 2:

Question: From a pack of 52 cards, two cards are drawn together at random. What is the probability of both the cards being kings?

Options: A) $2/1223$ B) $1/122$ C) $1/221$ D) $3/1253$ E) $2/153$

Rationale: Let s be the sample space.

Then $n(s) = 52C2 = 1326$

E = event of getting 2 kings out of 4

$n(E) = 4C2 = 6$

$P(E) = 6/1326 = 1/221$

Answer is C

Correct Option: C

- ▶ Rationales are most useful for problems where some computation is required. They can articulate the intermediate steps needed to solve it
- ▶ Some of the earliest work: math word problems



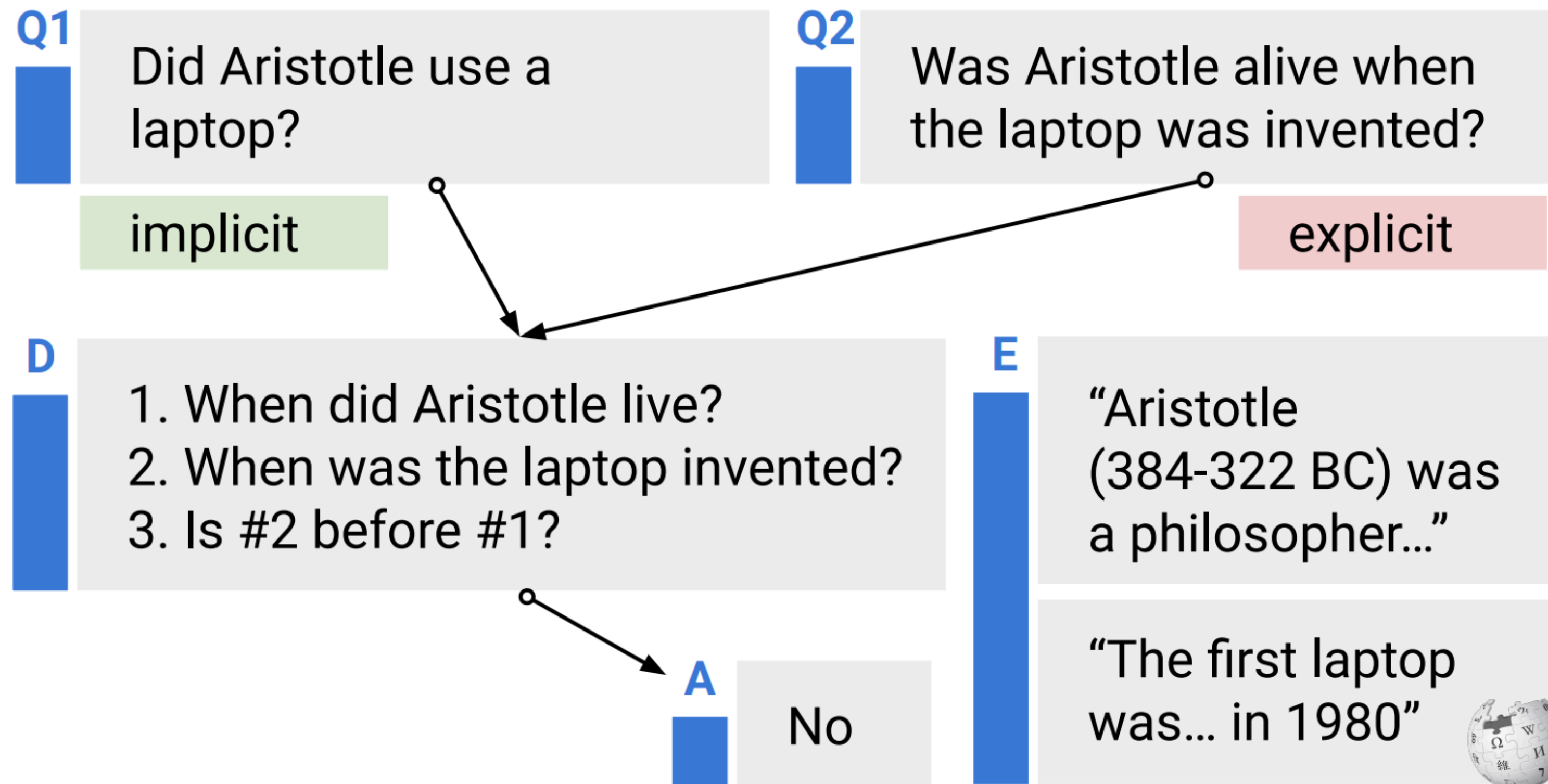
Text rationales vs. programs

9	cards	Id("Then")	<i>Then</i>	y_9
10	are	Id("n")	<i>n</i>	y_{10}
11	drawn	Id("(")	(y_{11}
12	together	Id("s")	<i>s</i>	y_{12}
13	at	Id(")"))	y_{13}
14	random	Id("=")	=	y_{14}
15	.	Str_to_Float(x_5)	52	$\underline{m_1}$
16	What	Float_to_Str(m_1)	52	y_{15}
17	is	Id("C")	<i>C</i>	y_{16}
18	the	Id("2")	2	y_{17}
19	probability	Id("=")	=	y_{18}
20	of	Str_to_Float(y_{17})	2	$\underline{m_2}$
21	both	Choose(m_1, m_2)	1326	$\underline{m_3}$
22	cards	Float_to_Str(m_3)	1326	y_{19}
23	being	Id("E")	<i>E</i>	y_{20}
24	kings	Id("=")	=	y_{21}

- Symbolic computation represented as a latent variable: intermixes computation with production of the string explanation



QA



- ▶ “StrategyQA”: dataset where different reasoning strategies are needed
- ▶ Related to multi-hop QA: “*What’s the capital of the country where Aristotle lived?*” (but these are easy with current models)



Chain-of-thought

- ▶ For these kinds of problems, do “computation” entirely in natural language
- ▶ Unifies several ideas:
 - ▶ For math: relies on the fact that LLMs can at least do single steps of arithmetic okay
 - ▶ For QA: many problems involve reasoning decompositions
E.g., *What’s the capital of the country where Aristotle lived?* ->
ans = “*country where Aristotle lived*”
return *What’s the capital of [ans]*
 - ▶ For other tasks: capture the kinds of behavior written in rationales



Chain-of-thought

- ▶ Typically a few-shot prompting technique where the in-context examples now contain explanations
- ▶ Answer is not generated in one go, but comes after an explanation that “talks through” the reasoning

Input:

Q: Roger has 5 tennis balls. He buys 2 more cans of tennis balls. Each can has 3 tennis balls. How many tennis balls does he have now?

A: Roger started with 5 balls. 2 cans of 3 tennis balls each is 6 tennis balls. $5 + 6 = 11$. The answer is 11.

...

Q: John takes care of 10 dogs. Each dog takes .5 hours a day to walk and take care of their business. How many hours a week does he spend taking care of dogs?

A:

Model output:

John takes care of 10 dogs. Each dog takes .5 hours a day to walk and take care of their business. So that is $10 \times .5 = 5$ hours a day. 5 hours a day $\times 7$ days a week = 35 hours a week. The answer is 35 hours a week. ✓



Chain-of-thought

From our work: a synthetic test of multi-hop reasoning with extractive explanations:

Context: *Christopher agrees with Kevin. Tiffany agrees with Matthew. Mary hangs out with Danielle. James hangs out with Thomas. Kevin is a student. Matthew is a plumber. Danielle is a student. Thomas is a plumber.*

Q: *Who hangs out with a student?*

A: *Mary.*

- ▶ What kind of explanation would you write here?

Explanation: *because Mary hangs out with Danielle and Danielle is a student.*



Chain-of-thought

Context: *Christopher agrees with Kevin. [...]* **Q:** *Who hangs out with a student?*

Mary

Standard few-shot learning, no explanation

Context: *Christopher agrees with Kevin. [...]* **Q:** *Who hangs out with a student?*

Mary, because Mary hangs out with Danielle and Danielle is a student.

Predict-explain: answer **is not** conditioned on output explanation (original E-SNLI LSTM)

Context: *Christopher agrees with Kevin. [...]* **Q:** *Who hangs out with a student?*

Because Mary hangs out with Danielle and Danielle is a student, the answer is Mary.

Explain-predict: answer is conditioned on output explanation (Chain of Thought)



Chain-of-thought

Prompt

Input
Label+
Explanation

Context: *Christopher agrees with Kevin. [...]* **Q:** *Who hangs out with a student?*
Mary, because Mary hangs out with Danielle and Danielle is a student.

Train Ex

Train Ex

Test Input

Context: *Adam plays with Ellen. [...]* **Q:** *Who plays with a doctor?*

GPT-3

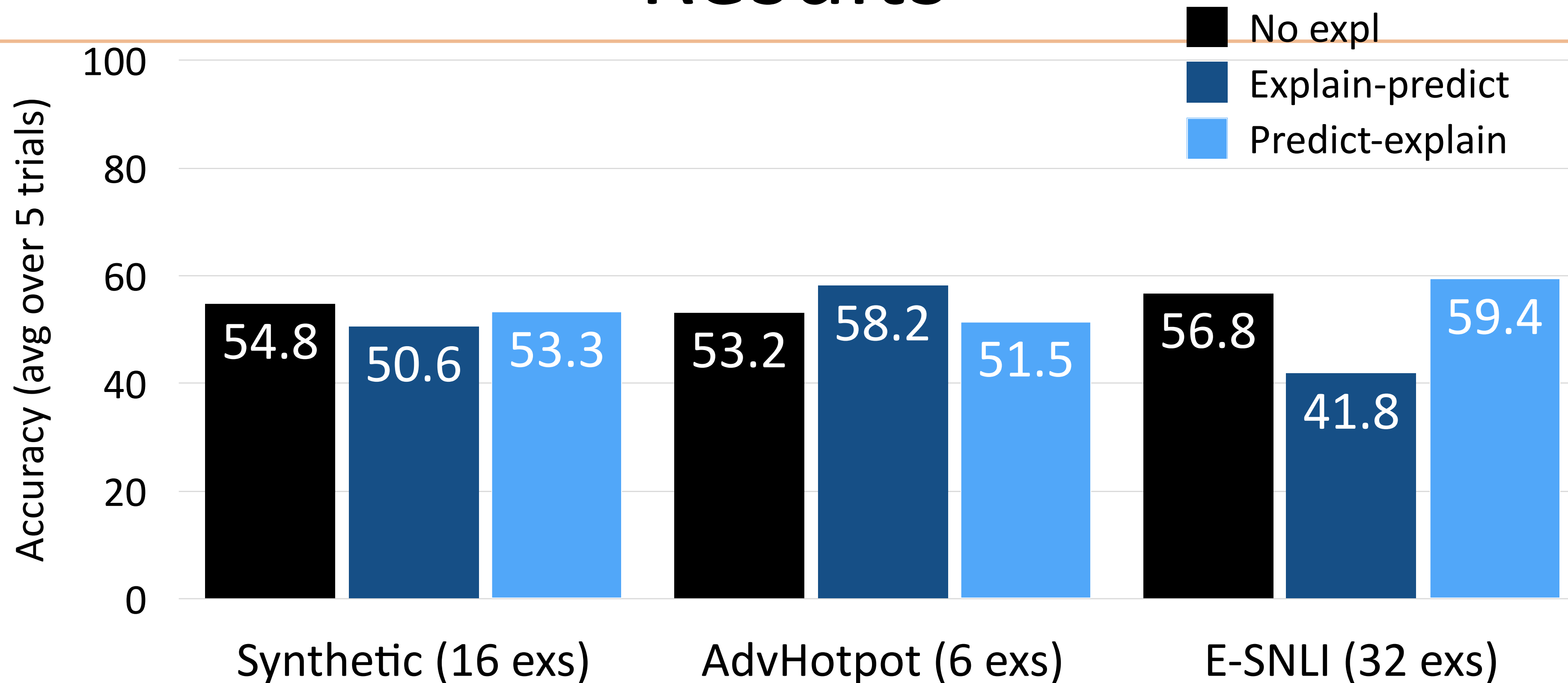
Output

Adam, because Adam plays with Ellen and Ellen is a doctor.

greedy decoding from GPT-3



Results



Does GPT-3 (text-davinci-001) work well without explanations?

- ▶ **Not well.** On Synthetic, surface heuristics give 50%.

Q1: Do these explanations help?

- ▶ **Not really.** Small gains on AdvHotpot and E-SNLI. No one technique dominates

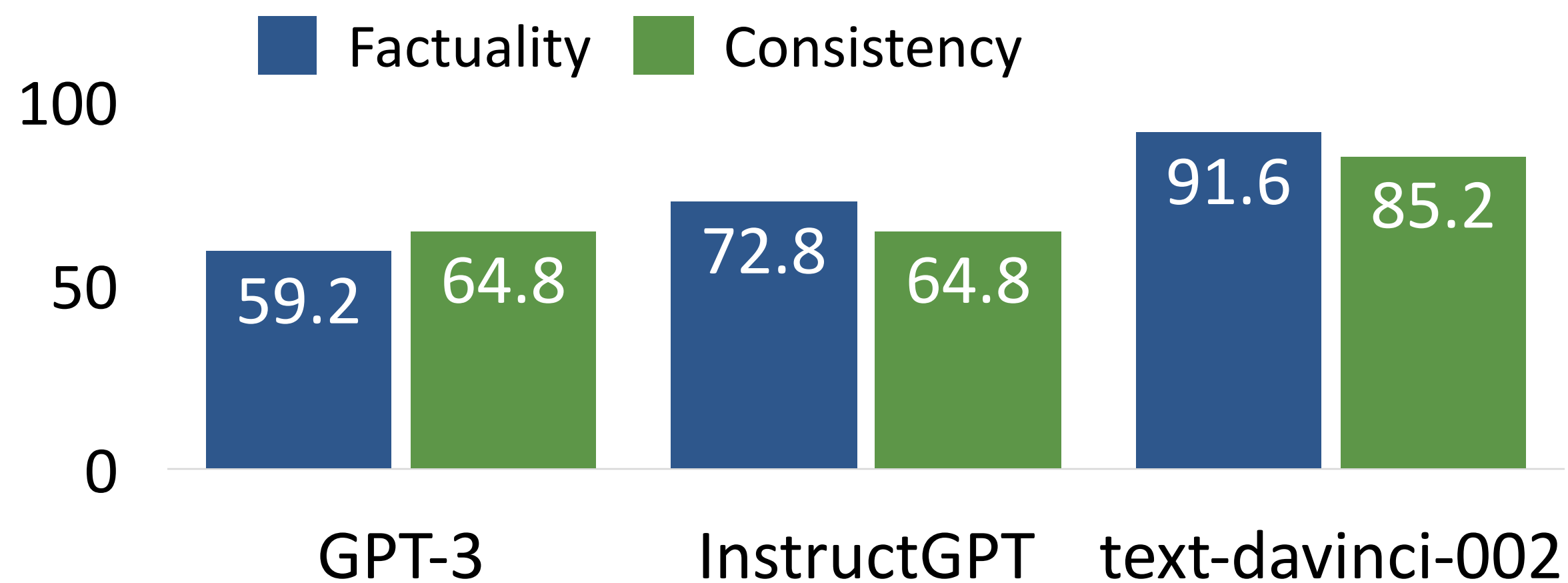
Ye and Durrett (NeurIPS 2022)



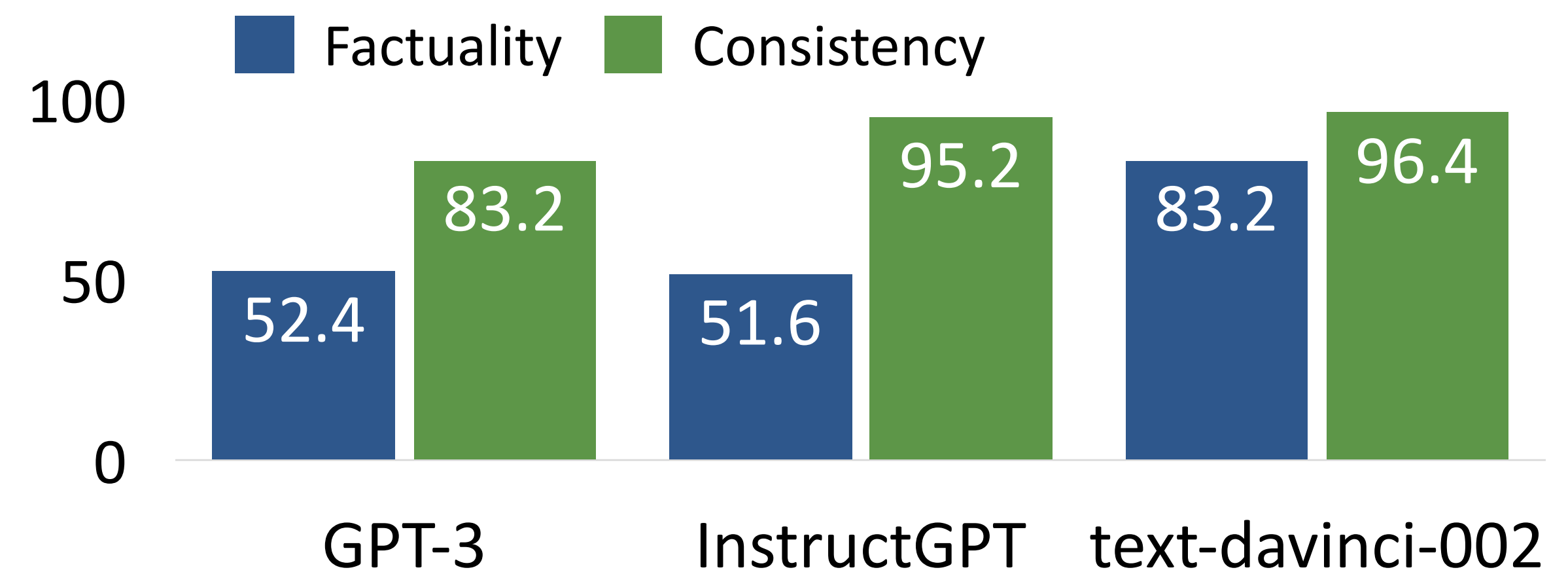
Results

- ▶ Can language models generate reliable explanations?
 - ▶ **Factuality:** whether an explanation is factually grounded in the input context
 - ▶ **Consistency:** whether an explanation entails the answer
- ▶ Model-generated explanations are not always **reliable**

**Explain-Predict
on SYNTH**



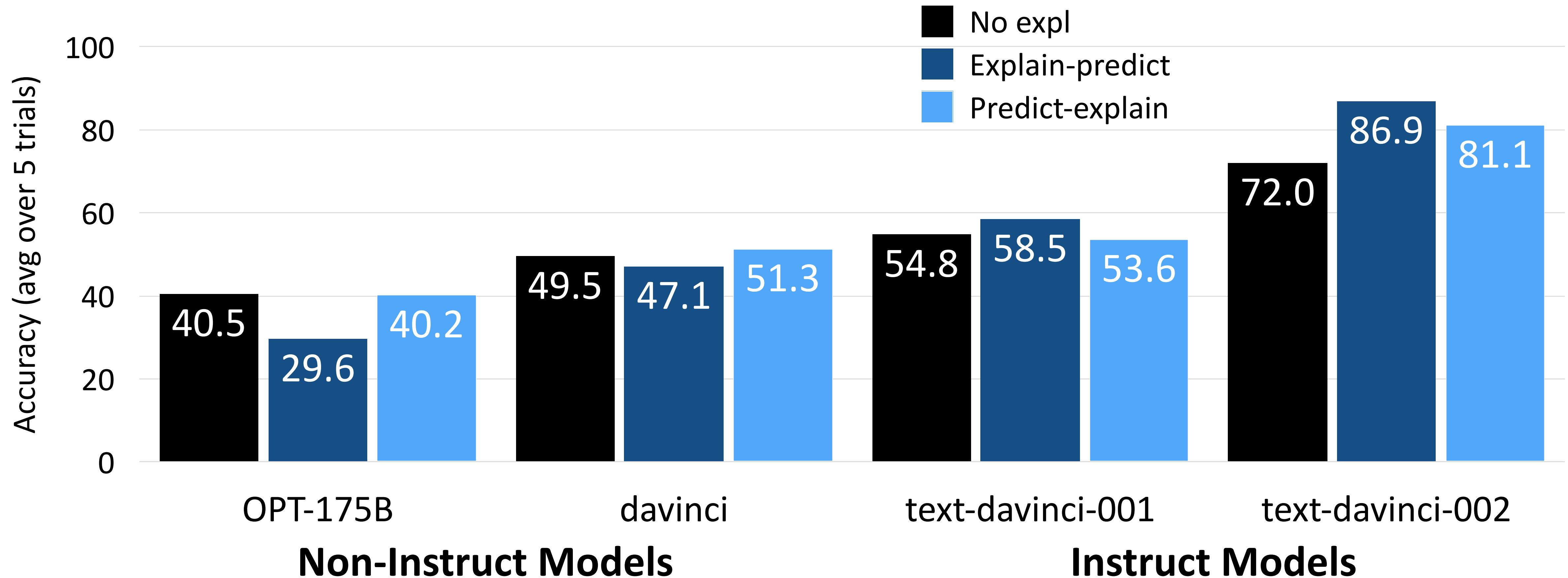
**Predict-Explain
on SYNTH**





Results

Results on SYNTH data



- ▶ Instruct tuning helps but it seems to be not quite sufficient
- ▶ **text-davinci-002 is far ahead of other models on this task**

Chain-of-thought extensions



Step-by-Step

(d) Zero-shot-CoT (Ours)

Q: A juggler can juggle 16 balls. Half of the balls are golf balls, and half of the golf balls are blue. How many blue golf balls are there?

A: **Let's think step by step.**

(Output) There are 16 balls in total. Half of the balls are golf balls. That means that there are 8 golf balls. Half of the golf balls are blue. That means that there are 4 blue golf balls. ✓

- ▶ Prompt for step-by-step reasoning: produces chains of thought without including demonstrations
- ▶ Separate prompt to extract the answer ("Therefore, the answer is ____")



Step-by-Step

	Arithmetic					
	SingleEq	AddSub	MultiArith	GSM8K	AQUA	SVAMP
zero-shot	74.6/78.7	72.2/77.0	17.7/22.7	10.4/12.5	22.4/22.4	58.8/58.7
zero-shot-cot	78.0/78.7	69.6/74.7	78.7/79.3	40.7/40.5	33.5/31.9	62.1/63.7
	Common Sense		Other Reasoning Tasks		Symbolic Reasoning	
	Common SenseQA	Strategy QA	Date Understand	Shuffled Objects	Last Letter (4 words)	Coin Flip (4 times)
zero-shot	68.8/72.6	12.7/54.3	49.3/33.6	31.3/29.7	0.2/-	12.8/53.8
zero-shot-cot	64.6/64.0	54.8/52.3	67.5/61.8	52.4/52.9	57.6/-	91.4/87.8

- text-davinci-002 (fine-tuned model)



Step-by-Step

No.	Category	Template	Accuracy
1	instructive	Let's think step by step.	78.7
2		First, (*1)	77.3
3		Let's think about this logically.	74.5
4		Let's solve this problem by splitting it into steps. (*2)	72.2
5		Let's be realistic and think step by step.	70.8
6		Let's think like a detective step by step.	70.3
7		Let's think	57.5
8		Before we dive into the answer,	55.7
9		The answer is after the proof.	45.7
10	misleading	Don't think. Just feel.	18.8
11		Let's think step by step but reach an incorrect answer.	18.7
12		Let's count the number of "a" in the question.	16.7
13		By using the fact that the earth is round,	9.3
14	irrelevant	By the way, I found a good restaurant nearby.	17.5
15		AbraKadabra!	15.5
16		It's a beautiful day.	13.1
-		(Zero-shot)	17.7

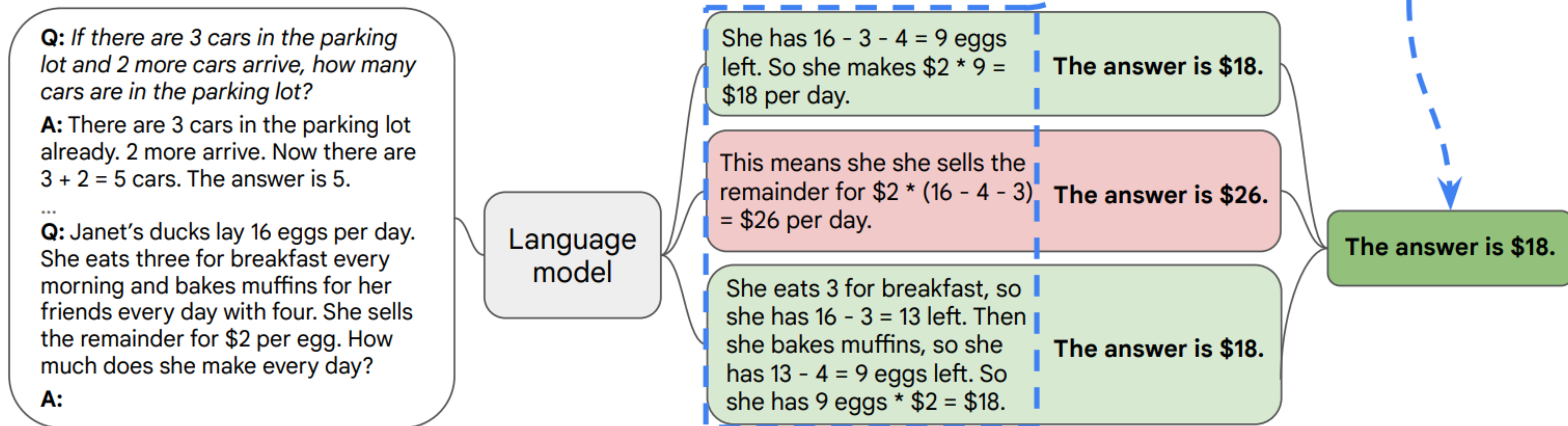


Demo: Step-by-Step (Math QA, StrategyQA)



Self-Consistency

Self-consistency



- ▶ Ensembling across multiple outputs (either zero-shot or few-shot)
- ▶ GSM8k: 56.5 -> 74.4, 5% gains on several other math datasets, lower gains on text tasks



Program-aided Language Models

- ▶ For math: why are we doing the arithmetic in the LLM itself?
- ▶ Instead: generate code fragments and actually execute them to get an answer (how most earlier math word problem systems worked)
- ▶ Many flavors of this:
“Faithful Chain-of-thought”,
“Program-of-thought”,
Toolformer, etc.

Model Output

A: The bakers started with 200 loaves

```
loaves_baked = 200
```

They sold 93 in the morning and 39 in the afternoon

```
loaves_sold_morning = 93
```

```
loaves_sold_afternoon = 39
```

The grocery store returned 6 loaves.

```
loaves_returned = 6
```

The answer is

```
answer = loaves_baked - loaves_sold_morning  
        - loaves_sold_afternoon + loaves_returned
```

```
>>> print(answer)
```

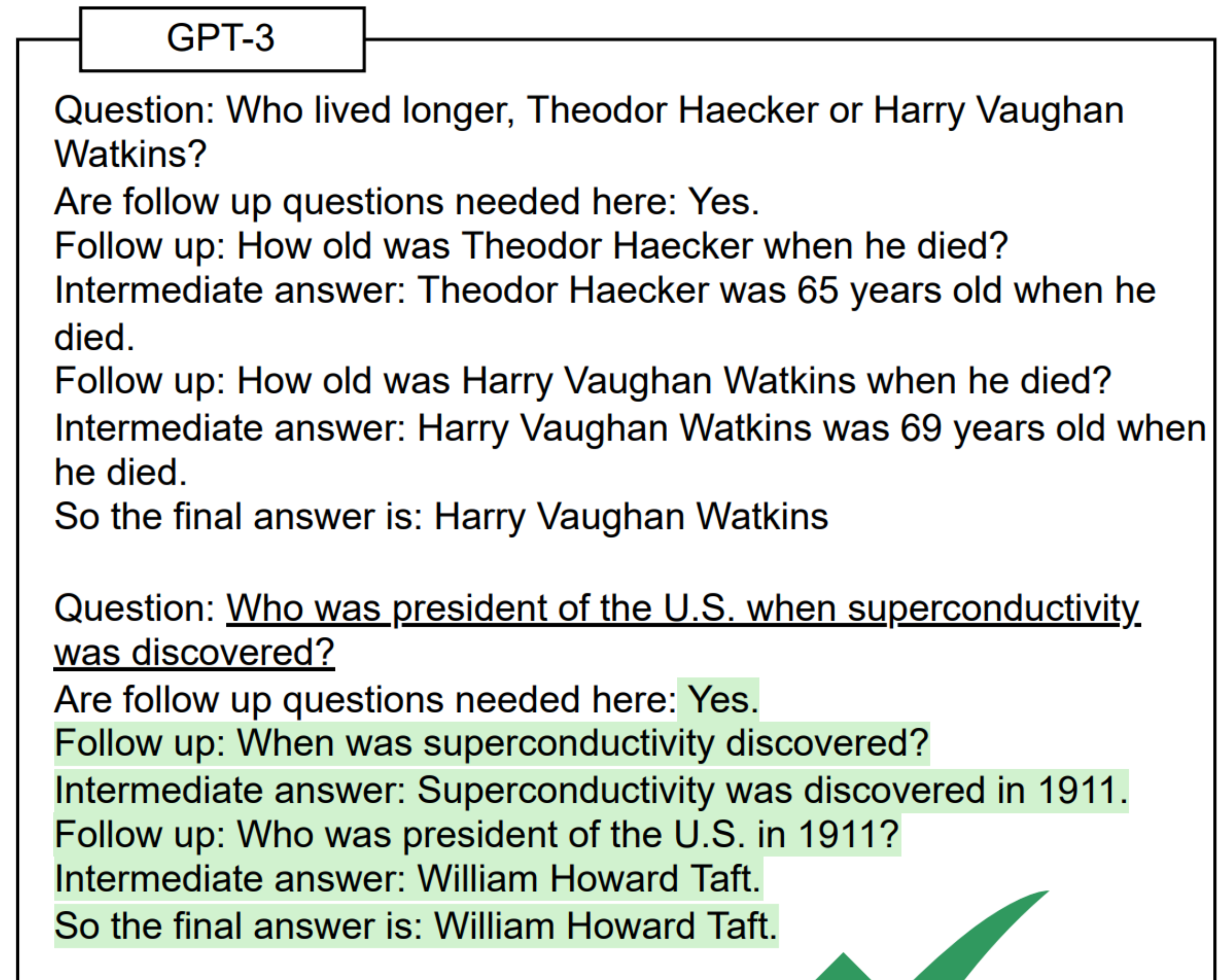
```
74
```





Self-ask

- ▶ Similar idea but with QA/a search engine in the loop
- ▶ Demonstration shows sub-questions and sub-answers, can potentially do search at these intermediate points
- ▶ Bing's "Sydney" agent has some capabilities around this



Press et al. (2022)



Other ideas

- ▶ For math: can having various other ways of doing programmatic verification
- ▶ For natural language reasoning: missing component of search and planning, discussed in “Language Model Cascades”
- ▶ For problems like fact-checking or QA involving complex reasoning, its difficult to verify all of the individual steps...so if CoT goes wrong, it may even be hard for a human to spot

Analysis of Explanations



What Makes Explanations Effective?

- ▶ Do LMs “follow” explanations?
- ▶ Probing LLMs with perturbed explanations
 - ▶ Perturbing **Computation Trace**
 - ▶ Perturbing **Natural Language**

Question

Take the last letters of the words in "Bill Gates" and concatenate them.

Gold Explanation

Trace

NL

The last letter of "Bill" is letter "l". The last of "Gates" is "s". Concatenating "l" and "s" is "ls". So the answer is ls.

Perturbing Trace

The last letter of "Bill" is letter ". The last of "Gates" is ". Concatenating "l" and "s" is "ls". So the answer is ls.

Perturbing NL

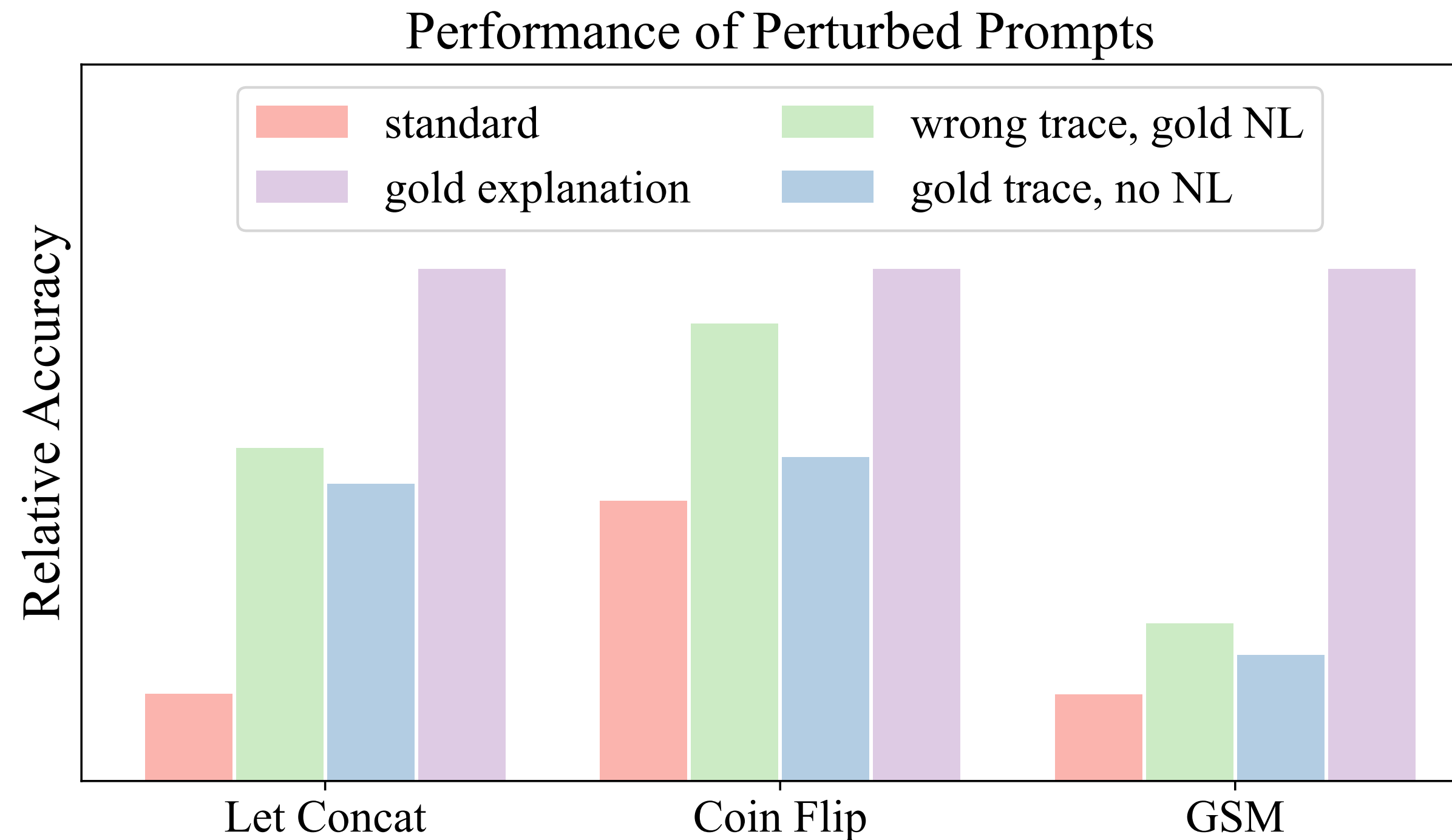
"Bill", "l", "Gates", "s", "l", "s", "ls". So the answer is ls.



What Makes Explanations Effective?



- ▶ Do LMs “follow” explanations? How do explanations work for in-context-learning?
- ▶ YES. Perturbing either trace or NL leads to performance degradation.
- ▶ But perturbed explanations are still beneficial compared to not using explanations at all





What Makes A Good Set of Explanations?

- ▶ Given a test query , we study how to form a maximally effective **set** of exemplars $T=(q,e,a)$
 - ▶ Interplay between query and exemplar: **relevance** (using more relevant examples)
 - ▶ Interplay between exemplars in the set: **complementarity**

Test Query:

Q: Peter bought 20 popsicles at \$0.25 each. He bought 4 ice cream bars at \$0.50 each. How much did he pay in total?

A: $0.25 * 20 = 5$. $0.5 * 4 = 2$. $5 + 2 = 7$. The answer is 7.

Complementary

Addition Exemplars:

Q: Marion received 20 more turtles than Martha. If Martha received 40 turtles, how many turtles did they receive together?

A: $20 + 40 = 60$. $60 + 40 = 100$. The answer is 100.

Multiplication Exemplars:

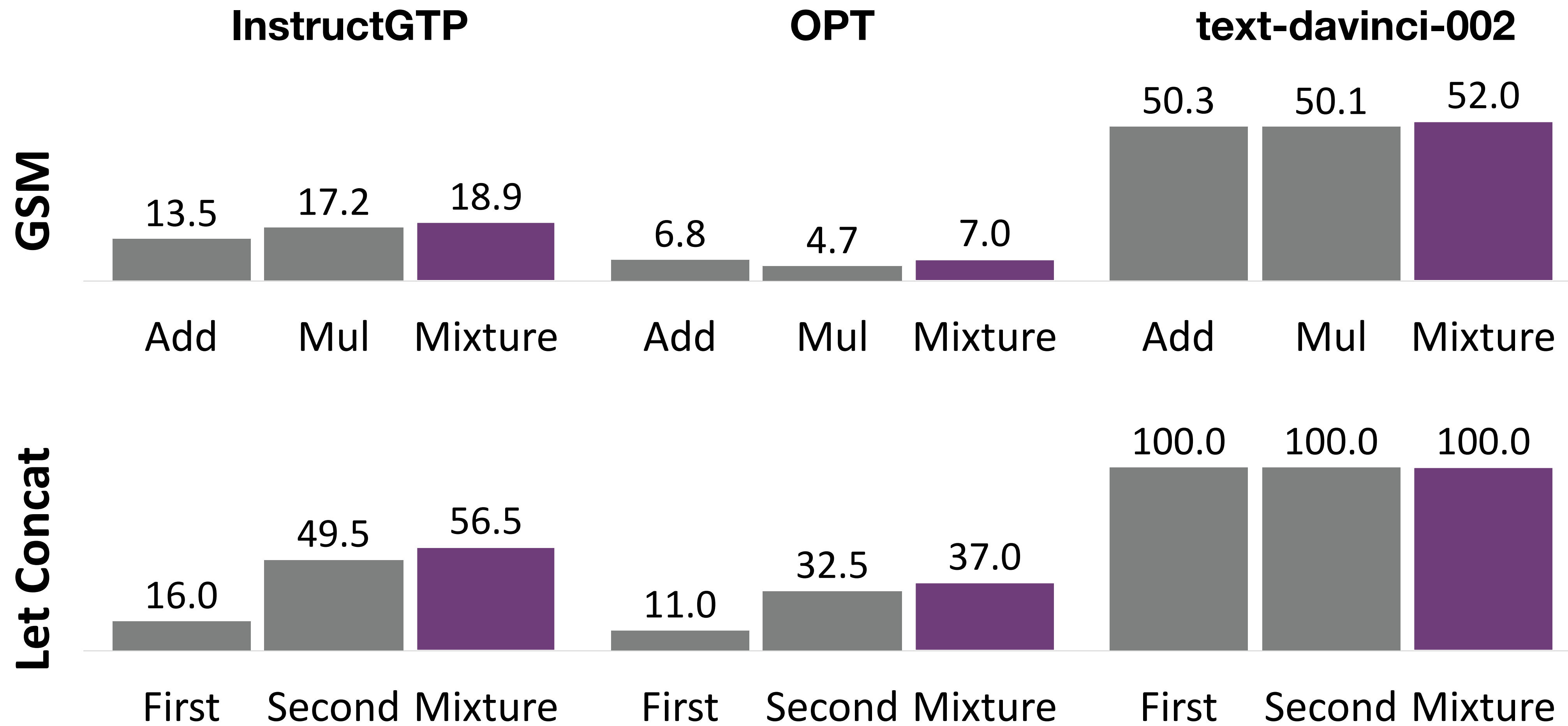
Q: Car Wash Company cleans 80 cars per day. They make \$5 per car washed. How much money will they make in 5 days?

A: $8 * 5 = 40$. $40 * 5 = 2000$. The answer is 2000



What Makes A Good Set of Explanations?

- ▶ We test whether LLMs can benefit from complementarity of exemplars
- ▶ Complementary exemplar sets lead to better performance (in the paper: algorithm for selecting these!)





Takeaways

- ▶ Chain-of-thought prompting (zero- and few-shot) can work well for tasks involving reasoning, especially mathematical reasoning and textual question answering with multiple steps
- ▶ Several things needed to improve them, such as self-consistency and the ability to use other resources like code execution or APIs
- ▶ Next time: RLHF, makes models better at zero-shot prompting and producing well-structured chain-of-thought responses