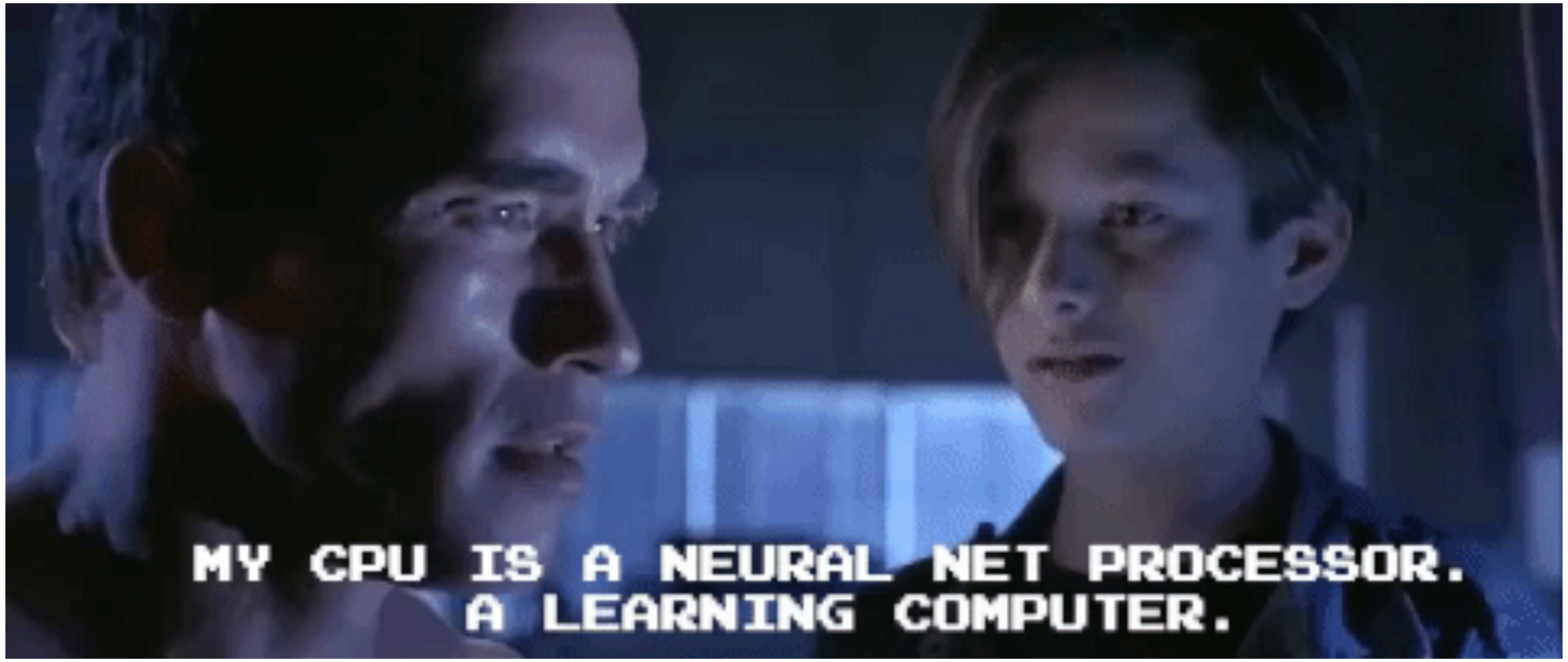
CS388: Natural Language Processing

Lecture 4: Neural Networks

Greg Durrett

TEXAS
The University of Texas at Austin



Recall: Multiclass Classification

- Two views of multiclass classification:
  - Different features: $\text{argmax}_{y \in \mathcal{Y}} w^\top f(x, y)$
  - Different weights: $\text{argmax}_{y \in \mathcal{Y}} w_y^\top f(x)$
- Logistic regression: $P_{\mathbf{w}}(y = \hat{y} \mid \mathbf{x}) = \dfrac{\exp\left(\mathbf{w}_{\hat{y}}^\top \mathbf{f}(\mathbf{x})\right)}{\sum_{y'} \exp\left(\mathbf{w}_{y'}^\top \mathbf{f}(\mathbf{x})\right)}$

Gradient of log likelihood:

"increase value for gold weight vector, decrease for other weight vectors"

$$\frac{\partial}{\partial \mathbf{w}_{y^{(i)}}} \mathcal{L}(\mathbf{x}^{(i)}, y^{(i)}) = \mathbf{f}(\mathbf{x}^{(i)})(P_{\mathbf{w}}(y^{(i)} \mid \mathbf{x}^{(i)}) - 1)$$

$$\frac{\partial}{\partial \mathbf{w}_{\tilde{y}}} \mathcal{L}(\mathbf{x}^{(i)}, y^{(i)}) = \mathbf{f}(\mathbf{x}^{(i)}) P_{\mathbf{w}}(y^{(i)} \mid \mathbf{x}^{(i)})$$

This Lecture

- Neural network history
- Neural network basics
- Feedforward neural networks + backpropagation
- Applications
- Implementing neural networks (if time)

Neural Net Basics

Neural Networks

- Linear classification: $\text{argmax}_y w^\top f(x, y)$
- Want to learn intermediate conjunctive features of the input

the movie was ***not*** *all that* ***good***

I[contains *not* & contains *good*]

- How do we learn this if our feature vector is just the unigram indicators?

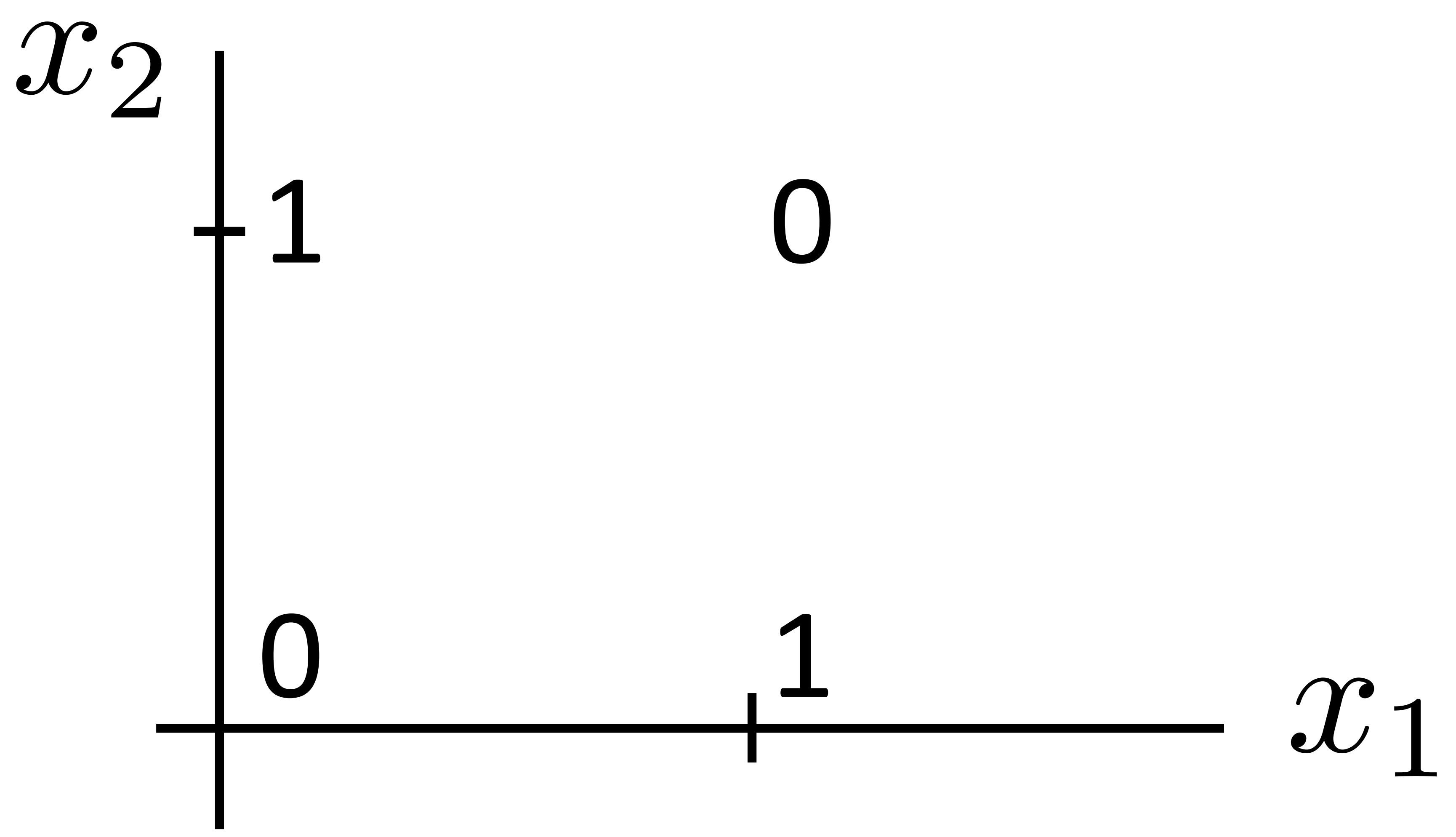
I[contains *not*], I[contains *good*]

Neural Networks: XOR

- Let's see how we can use neural nets to learn a simple nonlinear function
- Inputs $x_1, \ x_2$

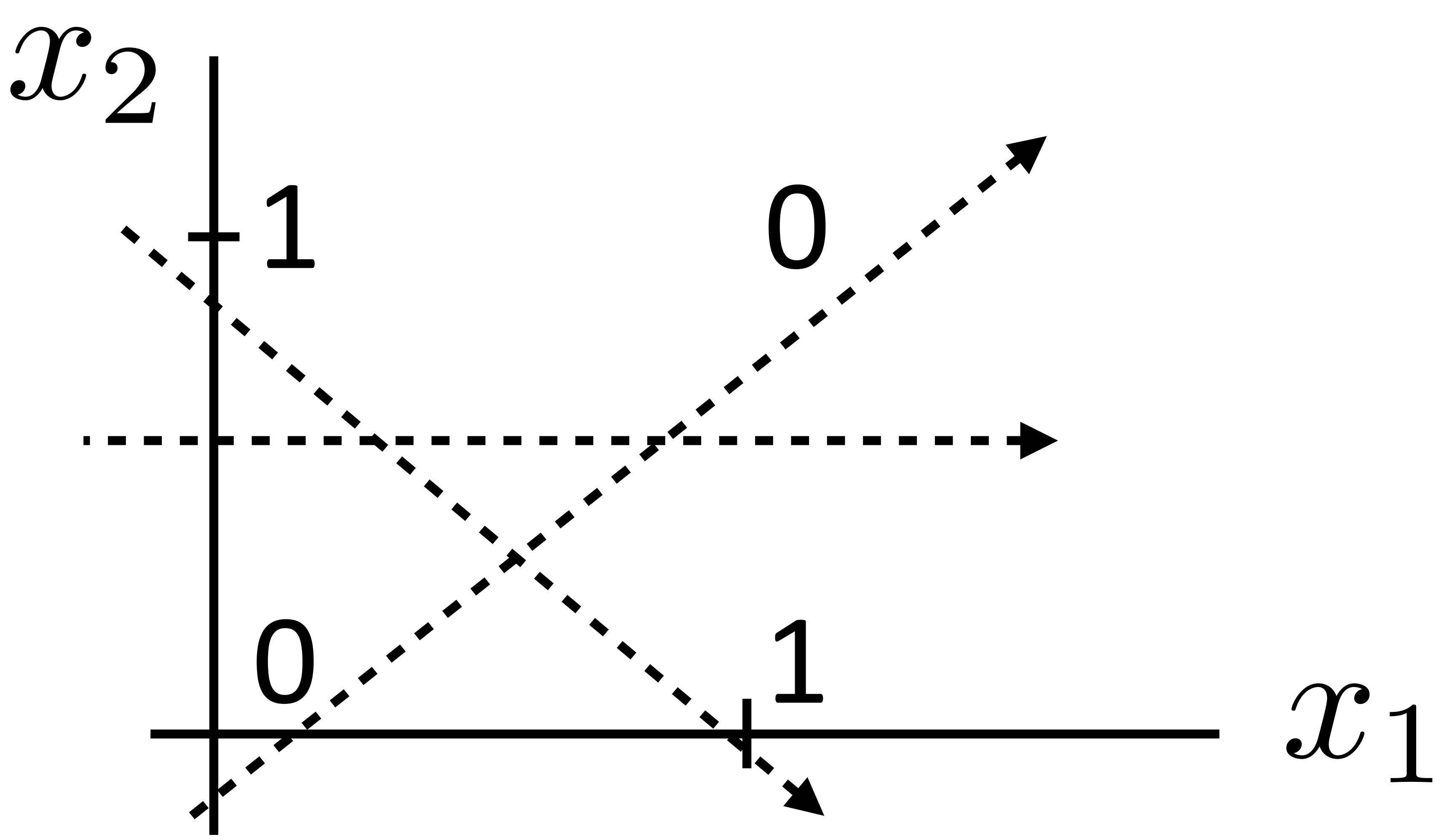
  $(\text{generally } \mathbf{x} = (x_1, \ldots, x_m))$
- Output y

  $(\text{generally } \mathbf{y} = (y_1, \ldots, y_n))$



x_1	x_2	$y = x_1 \text{ XOR } x_2$
0	0	0
0	1	1
1	0	1
1	1	0

Neural Networks: XOR



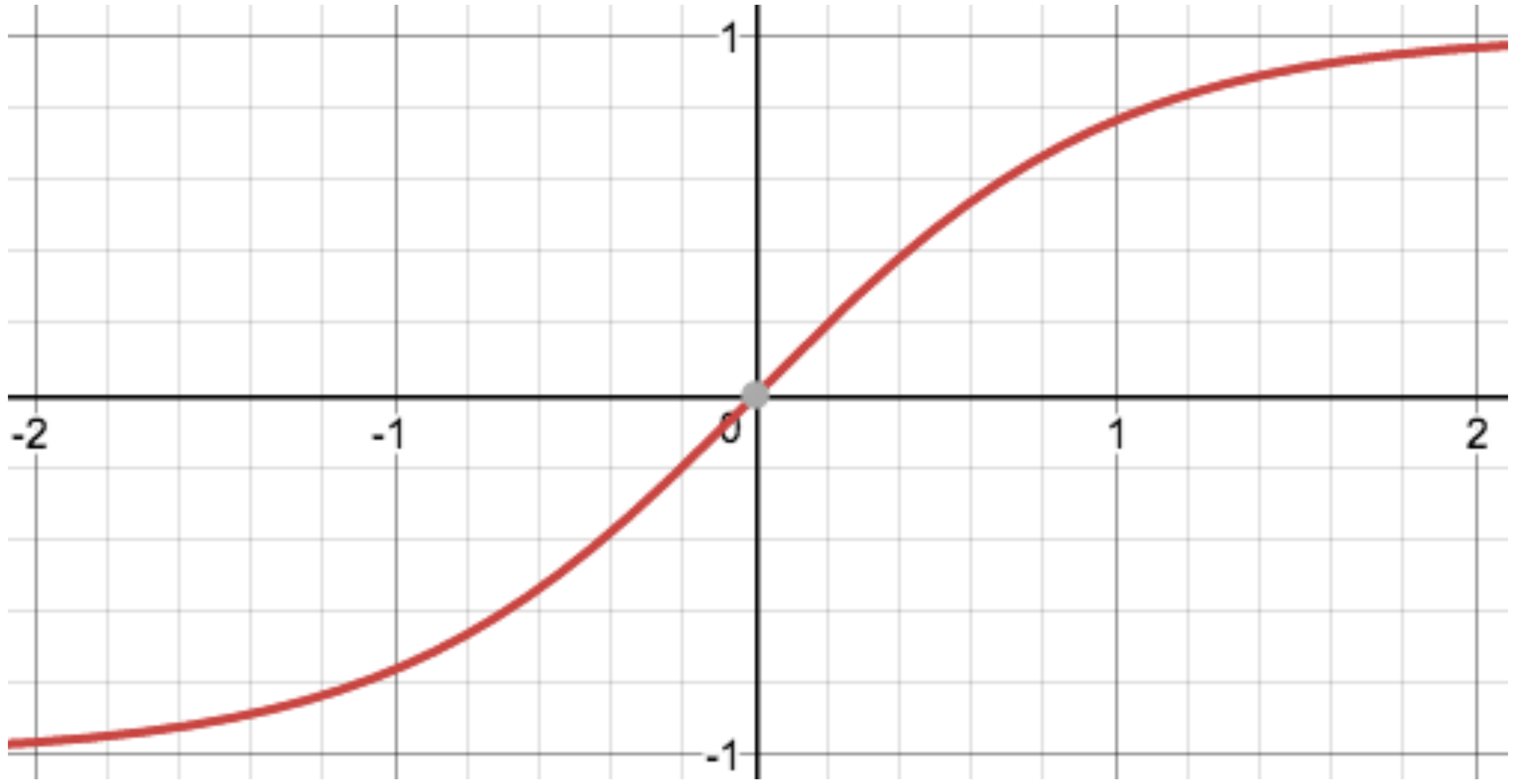
$$y = a_1 x_1 + a_2 x_2$$ X

$$y = a_1 x_1 + a_2 x_2 + a_3 \tanh(x_1 + x_2)$$ ✓

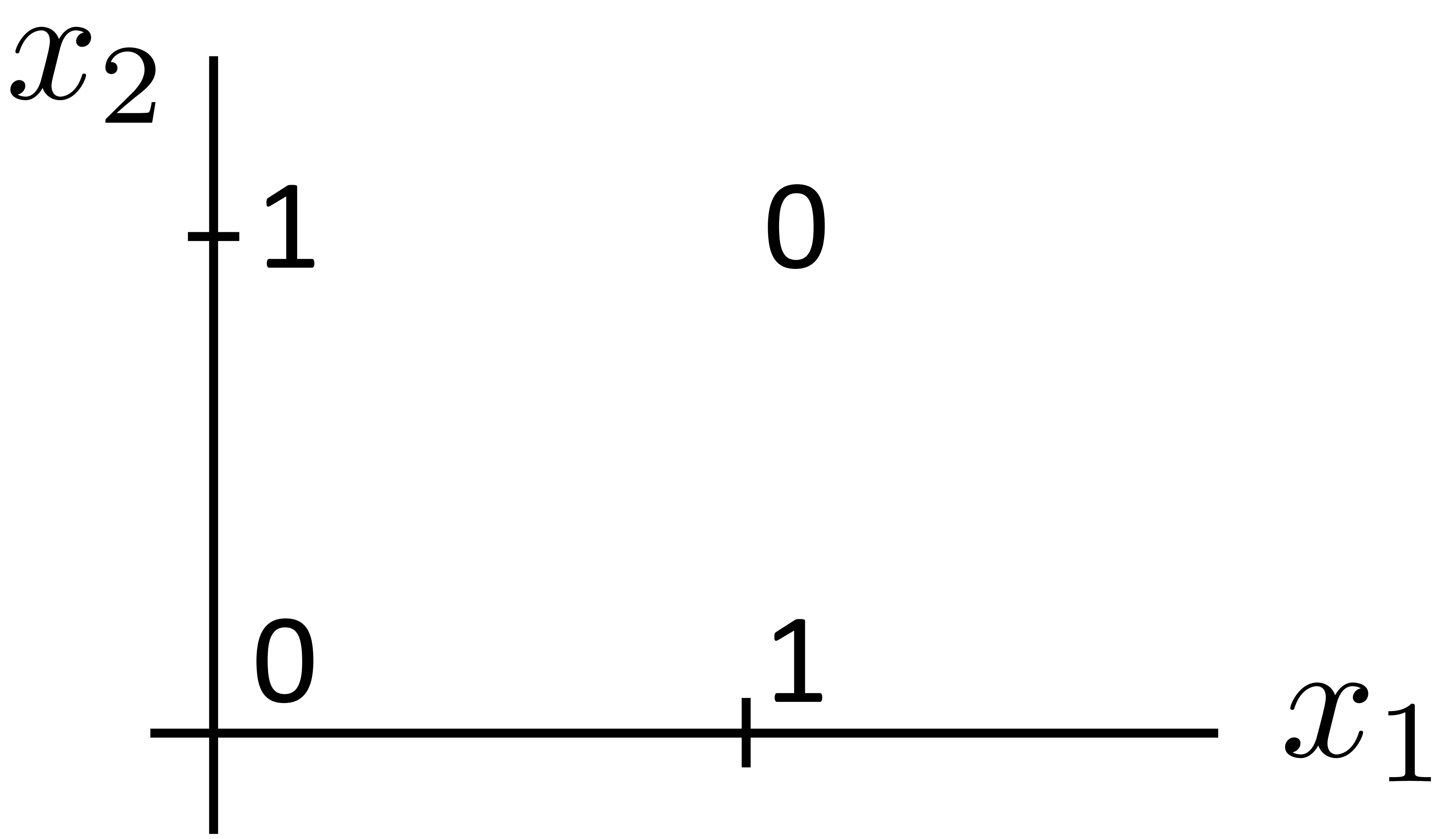
"or"

(looks like action potential in neuron)

x_1	x_2	$x_1 \text{ XOR } x_2$
0	0	0
0	1	1
1	0	1
1	1	0



Neural Networks: XOR



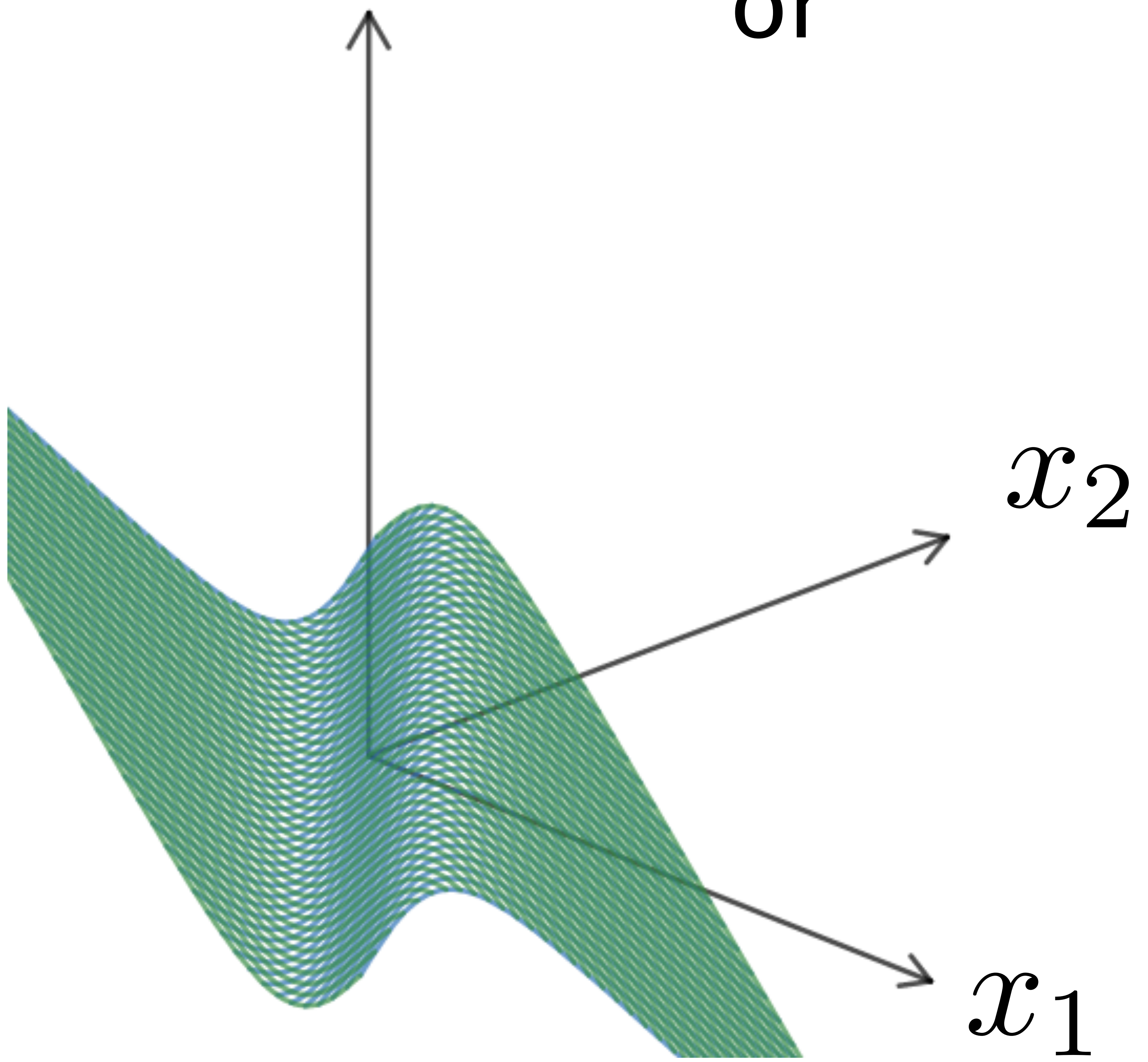
x_1	x_2	$x_1 \text{ XOR } x_2$
0	0	0
0	1	1
1	0	1
1	1	0

$$y = a_1 x_1 + a_2 x_2$$ ✗

$$y = a_1 x_1 + a_2 x_2 + a_3 \tanh(x_1 + x_2)$$ ✓

$$y = -x_1 - x_2 + 2 \tanh(x_1 + x_2)$$

"or"



Neural Networks

Linear model: $y = \mathbf{w} \cdot \mathbf{x} + b$

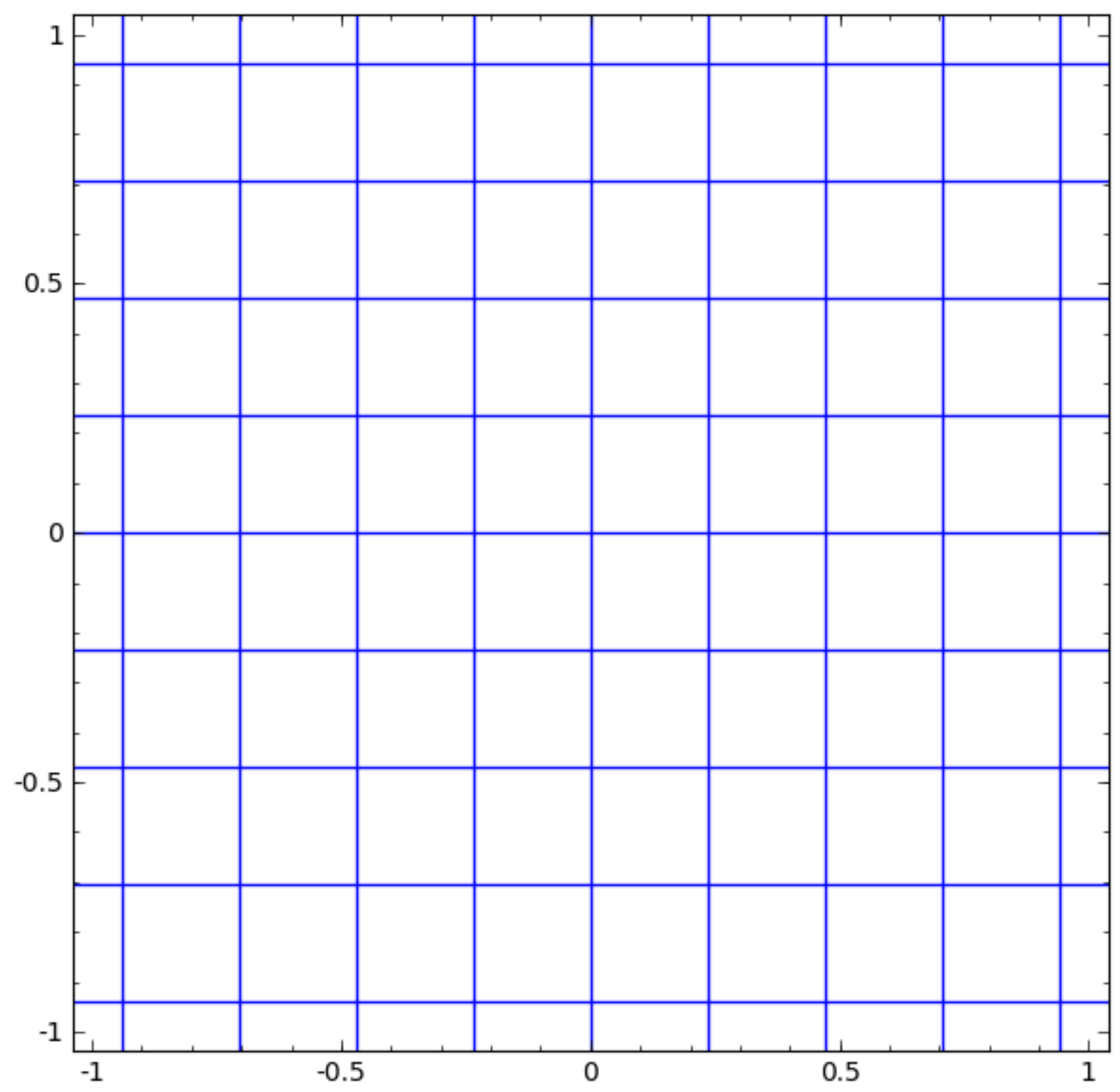
$$y = g(\mathbf{w} \cdot \mathbf{x} + b)$$

$$\mathbf{y} = g(\mathbf{W}\mathbf{x} + \mathbf{b})$$

Nonlinear transformation

Warp space

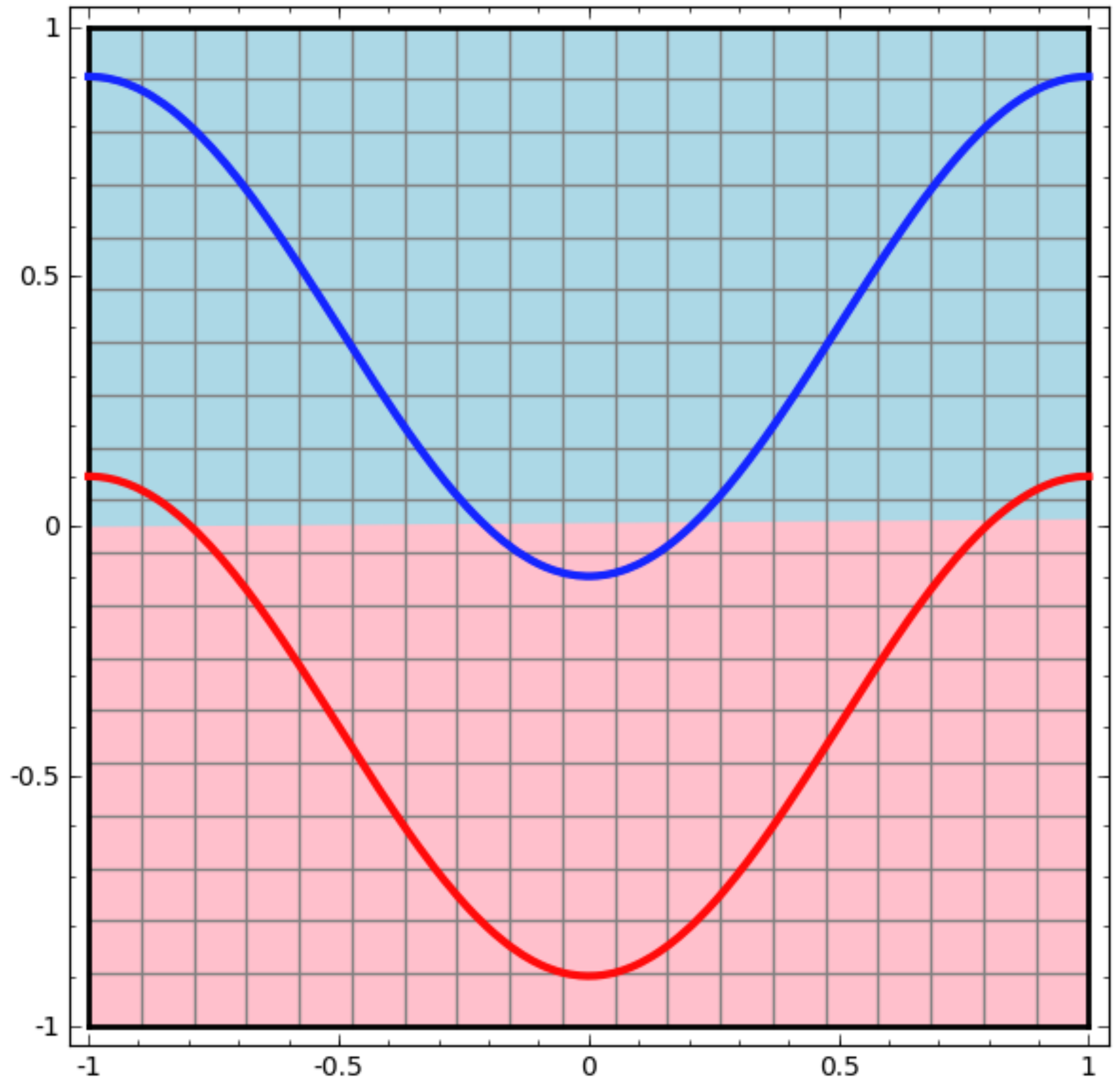
Shift



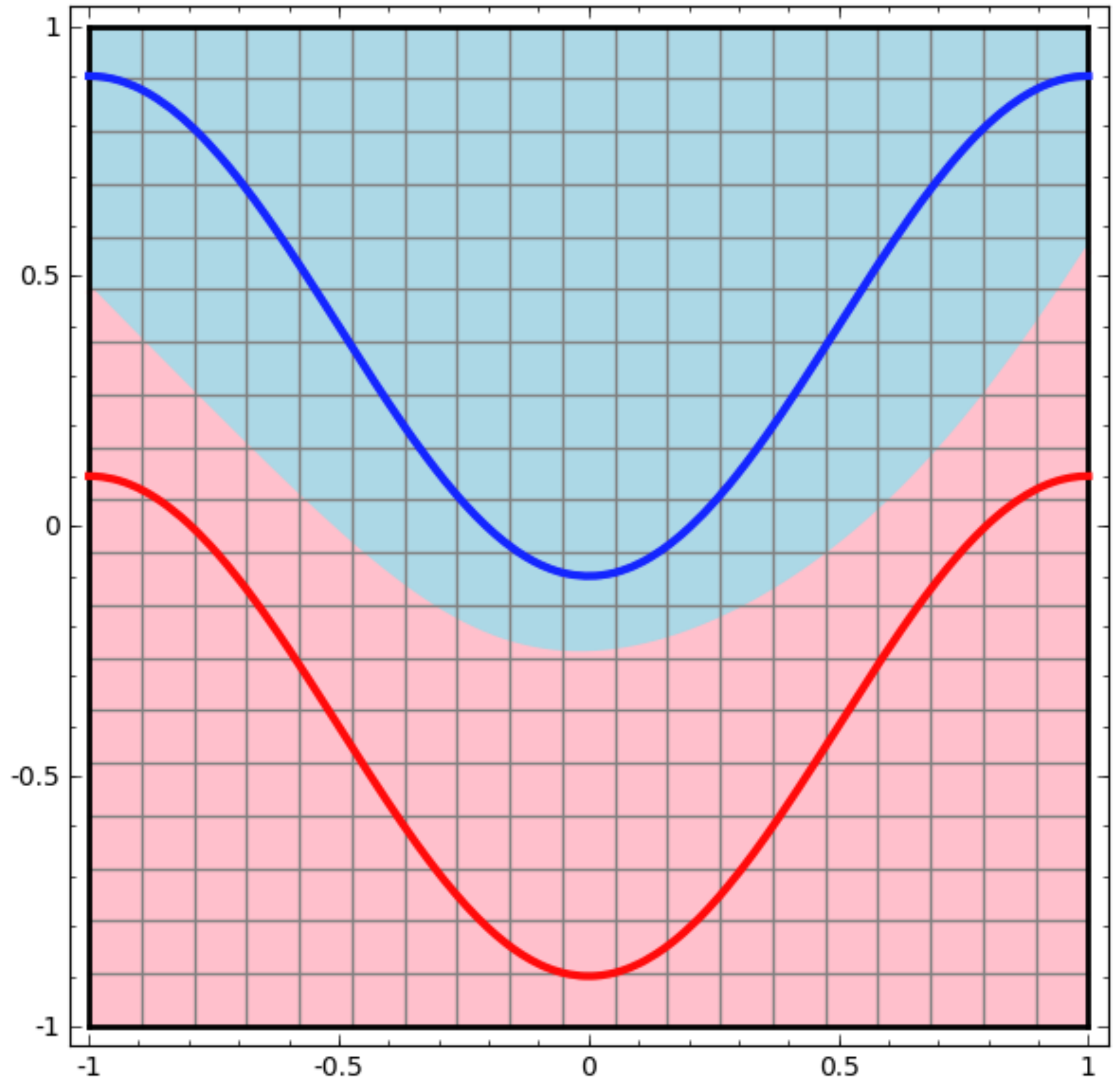
Taken from http://colah.github.io/posts/2014-03-NN-Manifolds-Topology/

Neural Networks

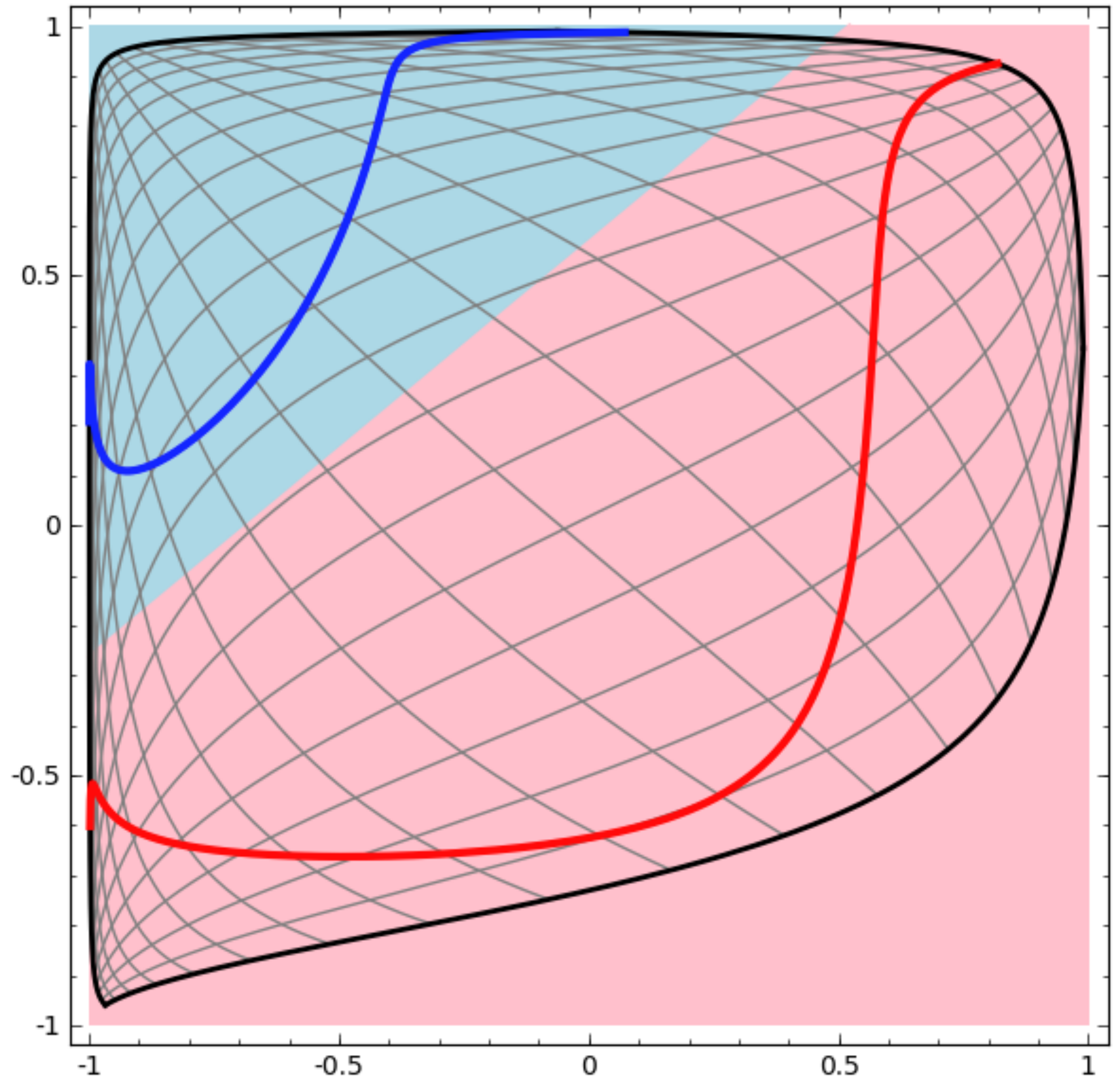
Linear classifier



Neural network



…possible because we transformed the space!



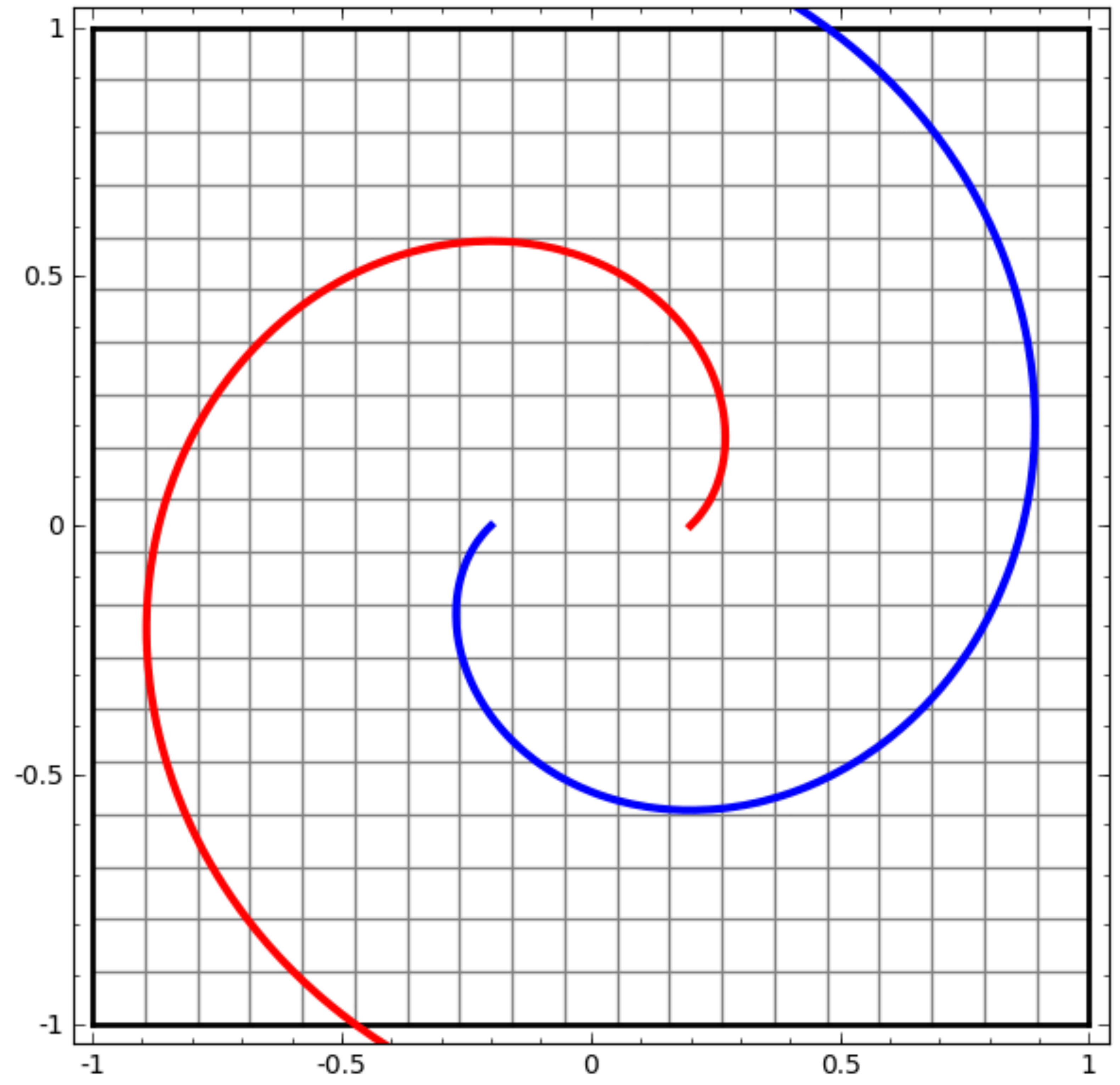
Taken from http://colah.github.io/posts/2014-03-NN-Manifolds-Topology/

Deep Neural Networks

$$\boldsymbol{y} = g(\mathbf{W}\boldsymbol{x} + \boldsymbol{b})$$

$$\mathbf{z} = g(\mathbf{V}\mathbf{y} + \mathbf{c})$$

$$\mathbf{z} = g(\mathbf{V}\underbrace{g(\mathbf{W}\mathbf{x} + \mathbf{b})}_{\text{output of first layer}} + \mathbf{c})$$



Check: what happens if no nonlinearity?

More powerful than basic linear models?

$$\mathbf{z} = \mathbf{V}(\mathbf{W}\mathbf{x} + \mathbf{b}) + \mathbf{c}$$

Taken from http://colah.github.io/posts/2014-03-NN-Manifolds-Topology/

Feedforward Networks, Backpropagation

Logistic Regression with NNs

$$P_{\mathbf{w}}(y = \hat{y} \mid \mathbf{x}) = \frac{\exp\left(\mathbf{w}_{\hat{y}}^\top \mathbf{f}(\mathbf{x})\right)}{\sum_{y'} \exp\left(\mathbf{w}_{y'}^\top \mathbf{f}(\mathbf{x})\right)}$$

- Single scalar probability

$$P(\mathbf{y} \mid \mathbf{x}) = \text{softmax}([\mathbf{w}_{\hat{y}}^\top \mathbf{f}(\mathbf{x})]_{y \in \mathcal{Y}})$$

- Compute scores for all possible labels at once (returns vector)

$$\text{softmax}(p)_i = \frac{\exp(p_i)}{\sum_{i'} \exp(p_{i'})}$$

- softmax: exps and normalizes a given vector

$$P(\mathbf{y}|\mathbf{x}) = \text{softmax}(Wf(\mathbf{x}))$$

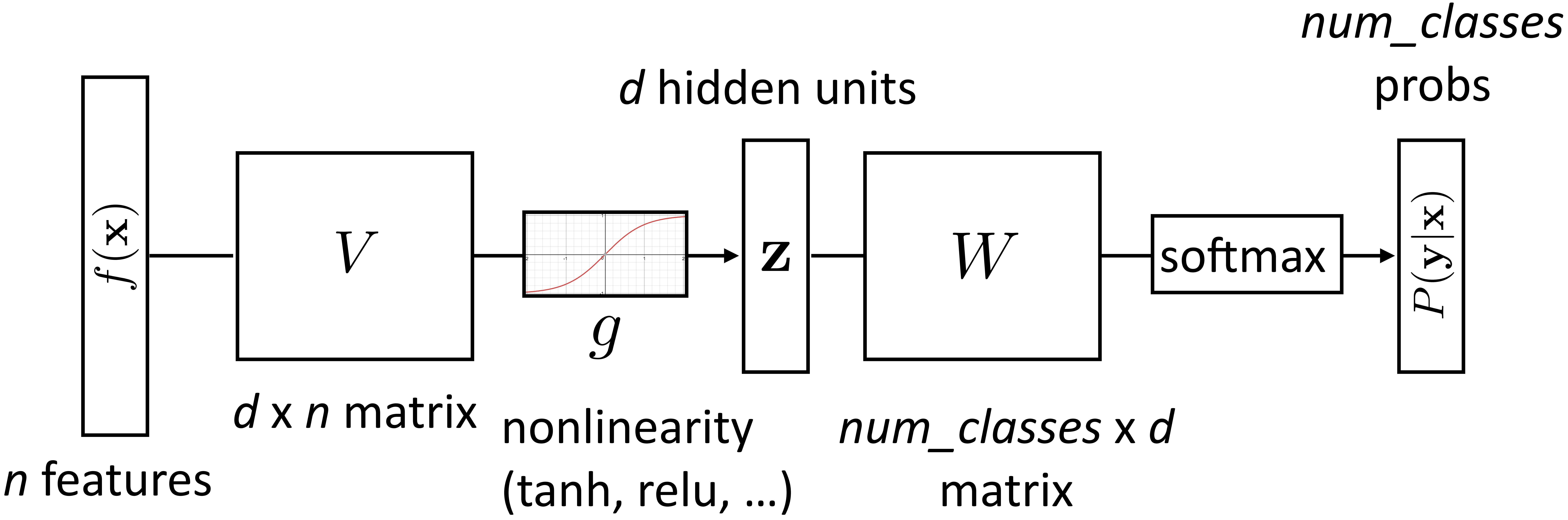
- Weight vector per class;
  W is [num classes x num feats]

$$P(\mathbf{y}|\mathbf{x}) = \text{softmax}(Wg(Vf(\mathbf{x})))$$

- Now one hidden layer

Neural Networks for Classification

$$P(\mathbf{y}|\mathbf{x}) = \text{softmax}(Wg(Vf(\mathbf{x})))$$



Training Neural Networks

$$P(\mathbf{y}|\mathbf{x}) = \text{softmax}(W\mathbf{z}) \qquad \mathbf{z} = g(Vf(\mathbf{x}))$$

- Maximize log likelihood of training data

$$\mathcal{L}(\mathbf{x}, i^*) = \log P(y = i^*|\mathbf{x}) = \log\left(\text{softmax}(W\mathbf{z}) \cdot e_{i^*}\right)$$

- $i*$: index of the gold label

- e_i: 1 in the ith row, zero elsewhere. Dot by this = select ith index

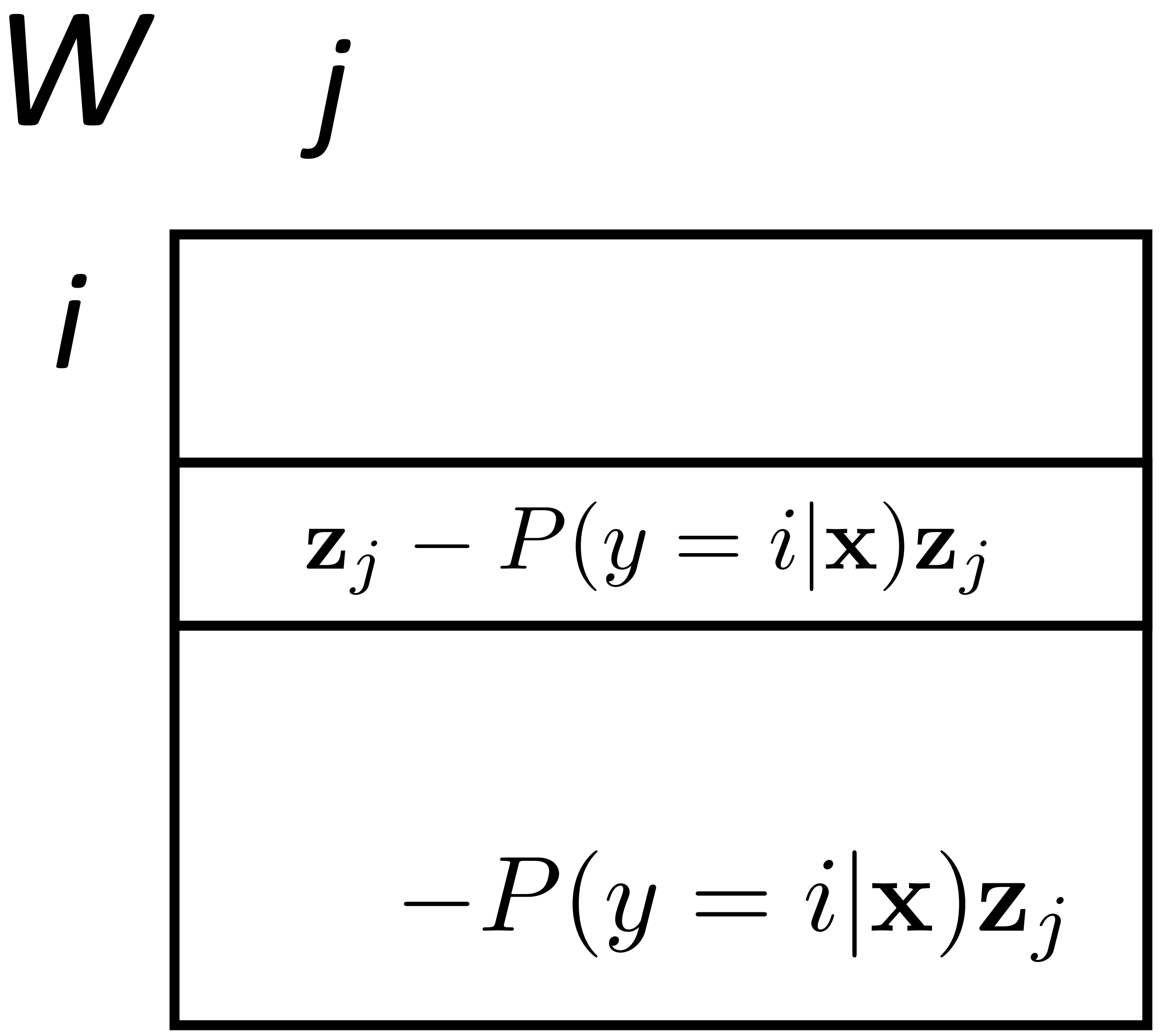
$$\mathcal{L}(\mathbf{x}, i^*) = W\mathbf{z} \cdot e_{i^*} - \log \sum_j \exp(W\mathbf{z}) \cdot e_j$$

Computing Gradients

$$\mathcal{L}(\mathbf{x}, i^*) = W\mathbf{z} \cdot e_{i^*} - \log \sum_j \exp(W\mathbf{z}) \cdot e_j$$

- Gradient with respect to *W*

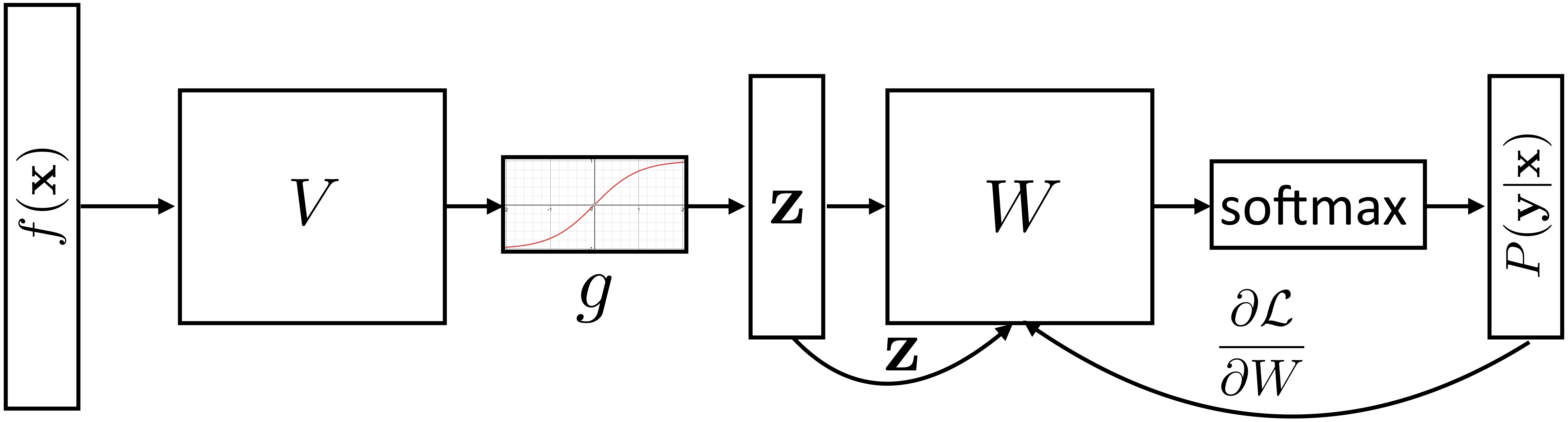
$$\frac{\partial}{\partial W_{ij}} \mathcal{L}(\mathbf{x}, i^*) = \begin{cases} \mathbf{z}_j - P(y = i|\mathbf{x})\mathbf{z}_j & \text{if } i = i^* \\ -P(y = i|\mathbf{x})\mathbf{z}_j & \text{otherwise} \end{cases}$$



- Looks like logistic regression with ***z*** as the features!

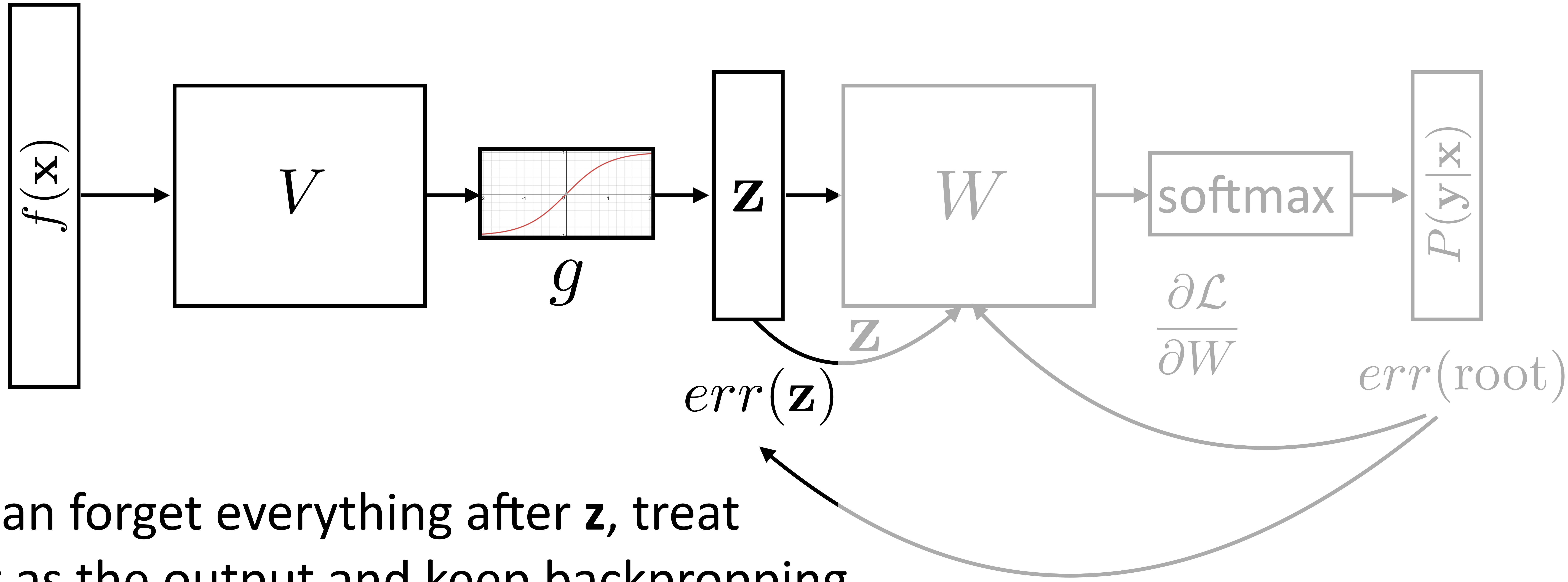
Neural Networks for Classification

$$P(\mathbf{y}|\mathbf{x}) = \mathrm{softmax}(W g(V f(\mathbf{x})))$$



Backpropagation: Picture

$$P(\mathbf{y}|\mathbf{x}) = \text{softmax}(Wg(Vf(\mathbf{x})))$$



- Can forget everything after **z**, treat it as the output and keep backpropping

Backpropagation: Takeaways

- Gradients of output weights W are easy to compute — looks like logistic regression with hidden layer $\mathbf{z}$ as feature vector

- Can compute derivative of loss with respect to $\mathbf{z}$ to form an "error signal" for backpropagation

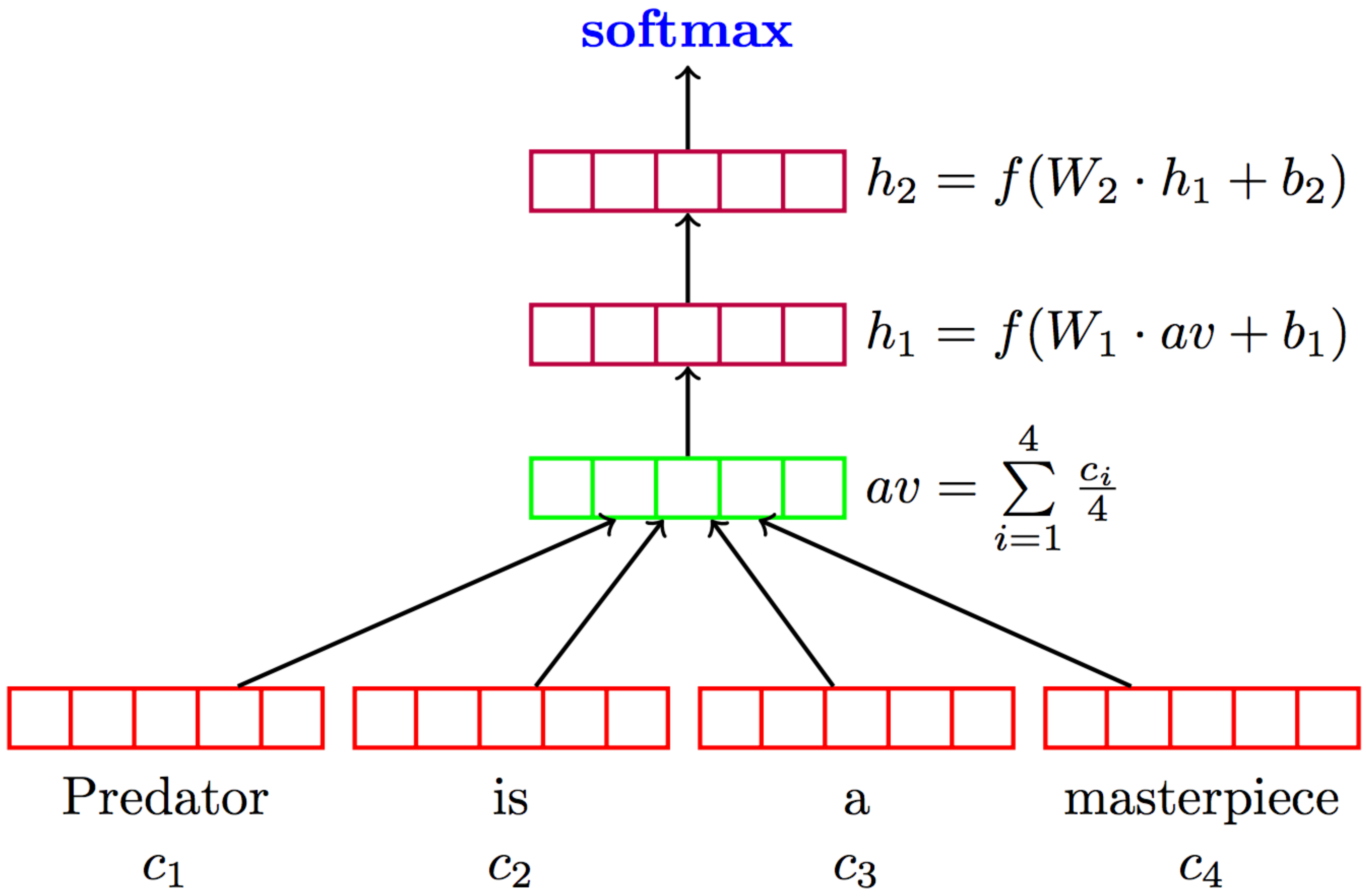
- Easy to update parameters based on "error signal" from next layer, keep pushing error signal back as backpropagation

- Need to remember the values from the forward computation

Applications

Sentiment Analysis (Project 1)

- Deep Averaging Networks: feedforward neural network on average of word embeddings from input



Iyyer et al. (2015)

Sentiment Analysis (Project 1)

Tips:

- Word embedding layer can be either frozen or trained — be attentive to this (torch.nn.Embedding layer from the WordEmbeddings class)
- As with the linear model, most minor tweaks like dropout, etc. will make <1% difference. If you're 10% off the performance target, it's likely due to a mis-sized network, poor optimization, bugs, etc.
- Debugging: follow ffnn_example.py, can use 50-dim embeddings to debug (they're smaller and a bit faster to use)

Iyyer et al. (2015)

Sentiment Analysis

Model	RT	SST fine	SST bin	IMDB	Time (s)
DAN-ROOT	—	46.9	85.7	—	**31**
DAN-RAND	77.3	45.4	83.2	88.8	136
DAN	80.3	47.7	86.3	89.4	136
NBOW-RAND	76.2	42.3	81.4	88.9	91
NBOW	79.0	43.6	83.6	89.0	91
BiNB	—	41.9	83.1	—	—
NBSVM-bi	79.4	—	—	91.2	—
RecNN*	77.7	43.2	82.4	—	—
RecNTN*	—	45.7	85.4	—	—
DRecNN	—	49.8	86.6	—	431
TreeLSTM	—	**50.6**	86.9	—	—
DCNN*	—	48.5	86.9	89.4	—
PVEC*	—	48.7	87.8	**92.6**	—
CNN-MC	**81.1**	47.4	**88.1**	—	2,452
WRRBM*	—	—	—	89.2	—

Iyyer et al. (2015)

Bag-of-words

Wang and Manning (2012)

Tree RNNs / CNNS / LSTMS

Kim (2014)

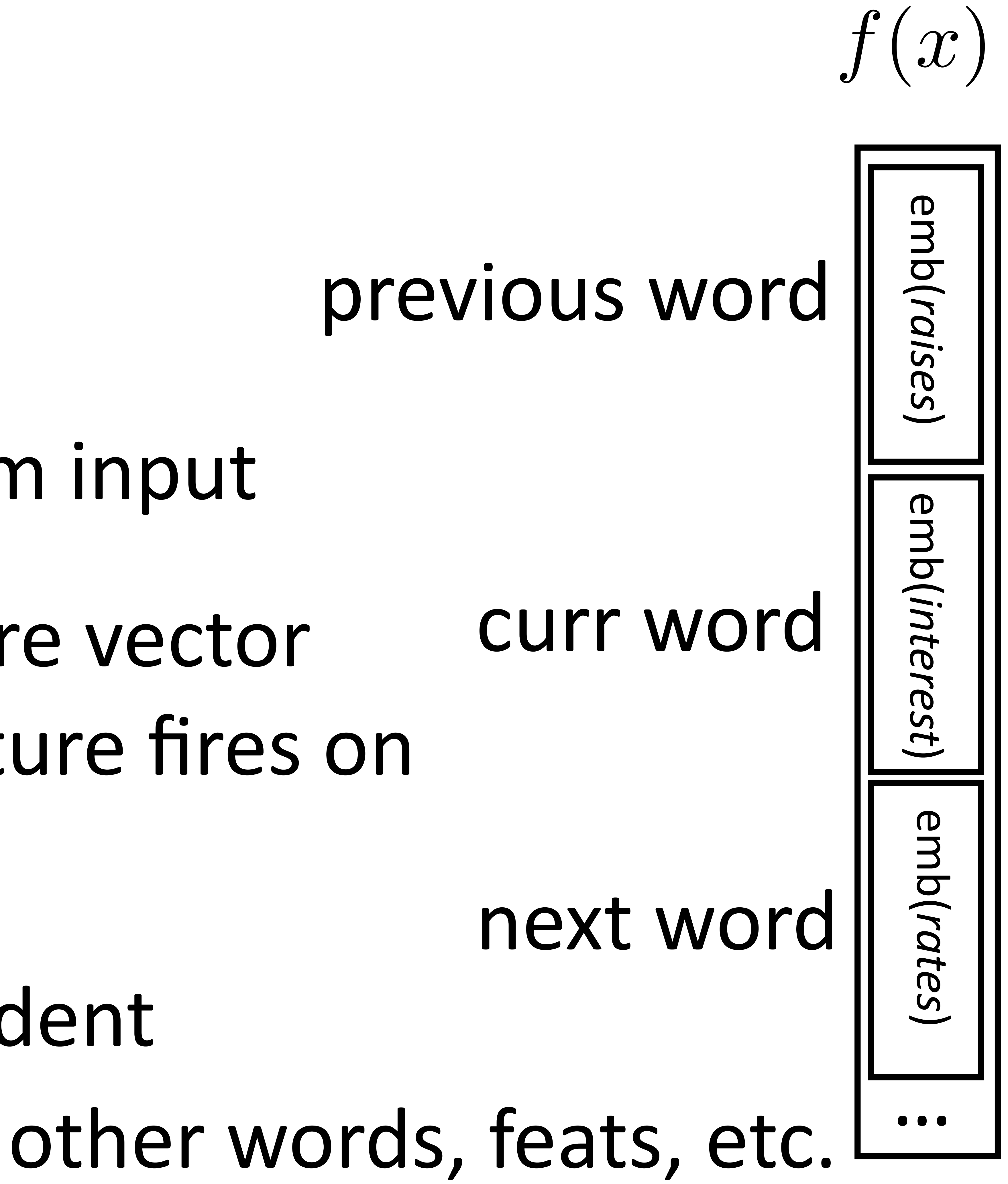
NLP with Feedforward Networks

- Part-of-speech tagging with FFNNs

??

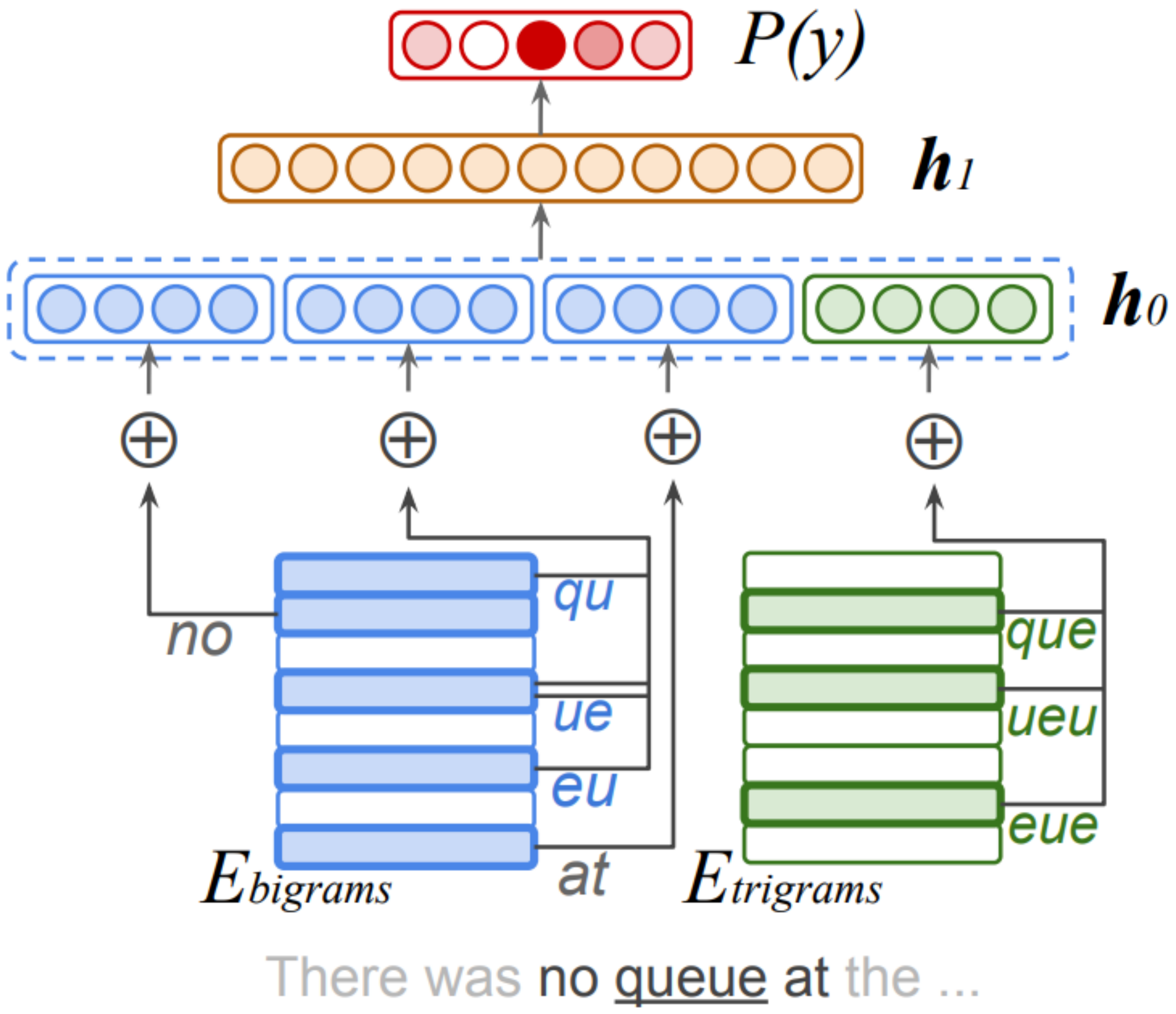
*Fed raises **interest** rates in order to …*

- Word embeddings for each word form input
- ~1000 features here — smaller feature vector than in sparse models, but every feature fires on every example
- Weight matrix learns position-dependent processing of the words



Botha et al. (2017)

NLP with Feedforward Networks



- Hidden layer mixes these different signals and learns feature conjunctions

Botha et al. (2017)

NLP with Feedforward Networks

- Multilingual tagging results:

Model	Acc.	Wts.	MB	Ops.
Gillick et al. (2016)	95.06	900k	-	6.63m
Small FF	94.76	241k	0.6	0.27m
+Clusters	95.56	261k	1.0	0.31m
$\frac{1}{2}$ Dim.	95.39	143k	0.7	0.18m

- Gillick used LSTMs; this is smaller, faster, and better

Botha et al. (2017)

Implementing NNs

(see ffnn_example.py on the course website)

Computation Graphs

- Computing gradients is hard! Computation graph abstraction allows us to define a computation symbolically and will do this for us

- Automatic differentiation: keep track of derivatives / be able to backpropagate through each function:

```
y = x * x   ──codegen──>   (y,dy) = (x * x, 2 * x * dx)
```

- Use a library like Pytorch or Tensorflow. This class: Pytorch

Computation Graphs in Pytorch

- Define forward pass for $P(\mathbf{y}|\mathbf{x}) = \text{softmax}(Wg(Vf(\mathbf{x})))$

```
class FFNN(nn.Module):
    def __init__(self, inp, hid, out):
        super(FFNN, self).__init__()
        self.V = nn.Linear(inp, hid)
        self.g = nn.Tanh()
        self.W = nn.Linear(hid, out)
        self.softmax = nn.Softmax(dim=0)

    def forward(self, x):
        return self.softmax(self.W(self.g(self.V(x))))
```

Computation Graphs in Pytorch

$$P(\mathbf{y}|\mathbf{x}) = \mathrm{softmax}(Wg(Vf(\mathbf{x})))$$

ei*: one-hot vector of the label (e.g., [0, 1, 0])

```
ffnn = FFNN()
def make_update(input, gold_label):
    ffnn.zero_grad() # clear gradient variables
    probs = ffnn.forward(input)
    loss = torch.neg(torch.log(probs)).dot(gold_label)
    loss.backward()
    optimizer.step()
```

Training a Model

Define a computation graph

For each epoch:

  For each batch of data:

    Compute loss on batch

    Autograd to compute gradients

    Take step with optimizer

Decode test set

Training Tips

Batching

- Batching data gives speedups due to more efficient matrix operations
- Need to make the computation graph process a batch at the same time

```
# input is [batch_size, num_feats]
# gold_label is [batch_size, num_classes]
def make_update(input, gold_label)
    ...
    probs = ffnn.forward(input) # [batch_size, num_classes]
    loss = torch.sum(torch.neg(torch.log(probs)).dot(gold_label))
    ...
```

- Batch sizes from 1-100 often work well

Training Basics

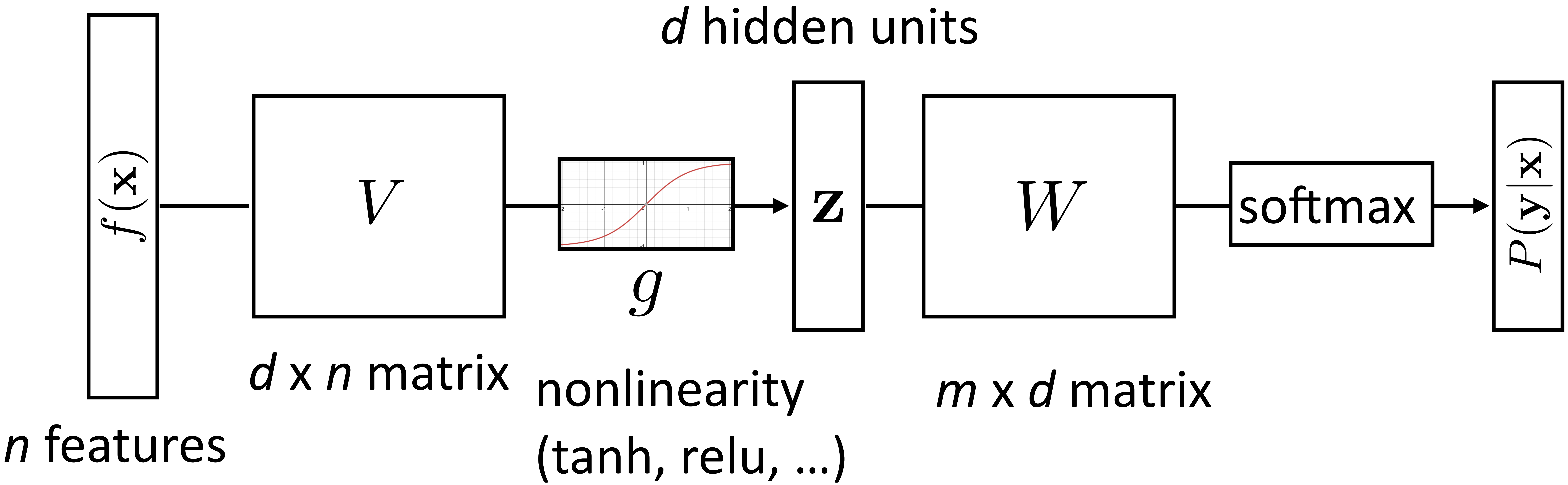
- Basic formula: compute gradients on batch, use first-order optimization method (SGD, Adagrad, etc.)

- How to initialize? How to regularize? What optimizer to use?

- This lecture: some practical tricks. Take deep learning or optimization courses to understand this further

How does initialization affect learning?

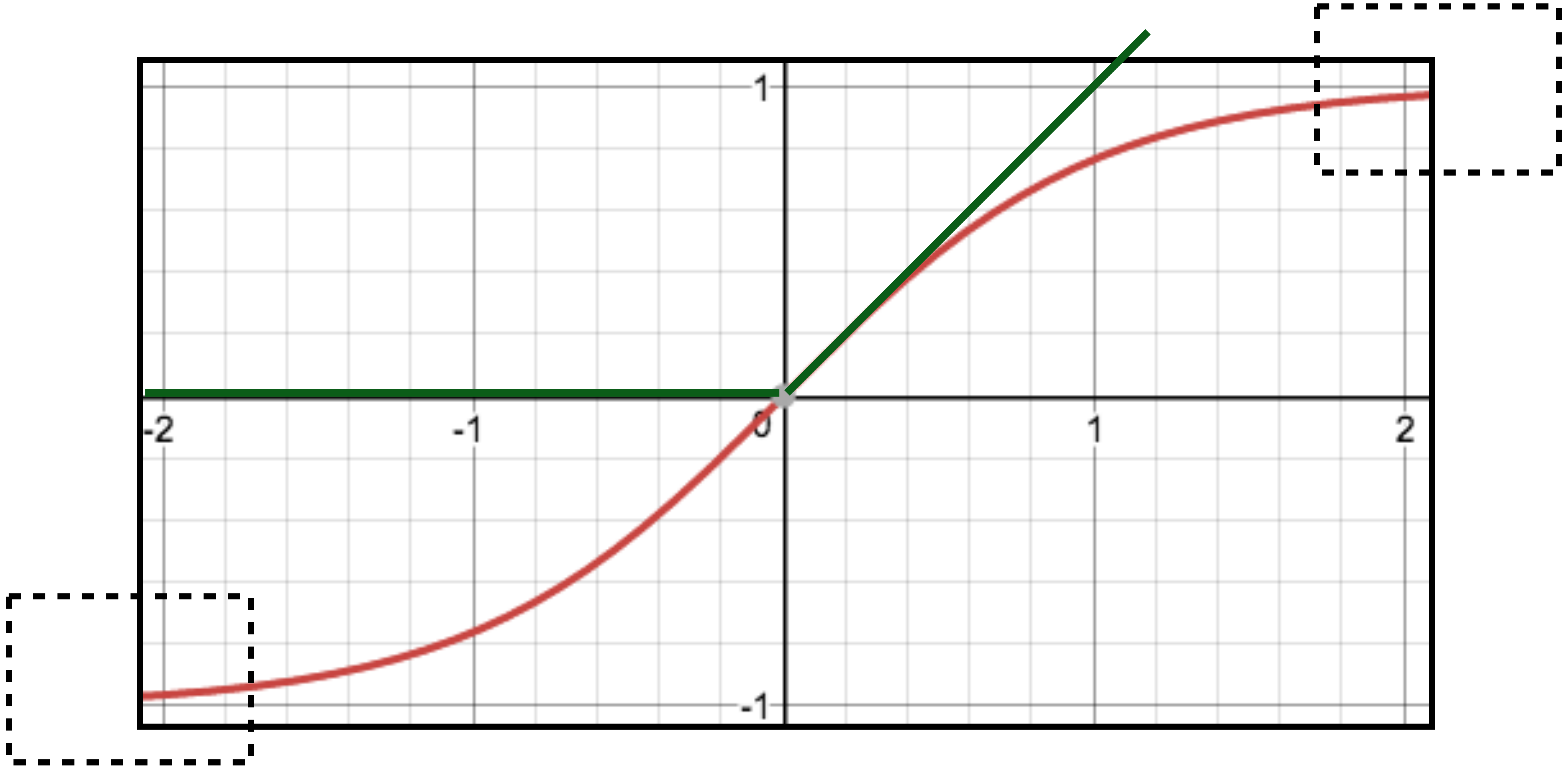
$$P(\mathbf{y}|\mathbf{x}) = \text{softmax}(Wg(Vf(\mathbf{x})))$$



- How do we initialize V and W? What consequences does this have?
- *Nonconvex* problem, so initialization matters!

How does initialization affect learning?

- Nonlinear model…how does this affect things?



- If cell activations are too large in absolute value, gradients are small
- ReLU: larger dynamic range (all positive numbers), but can produce big values, can break down if everything is too negative

Initialization

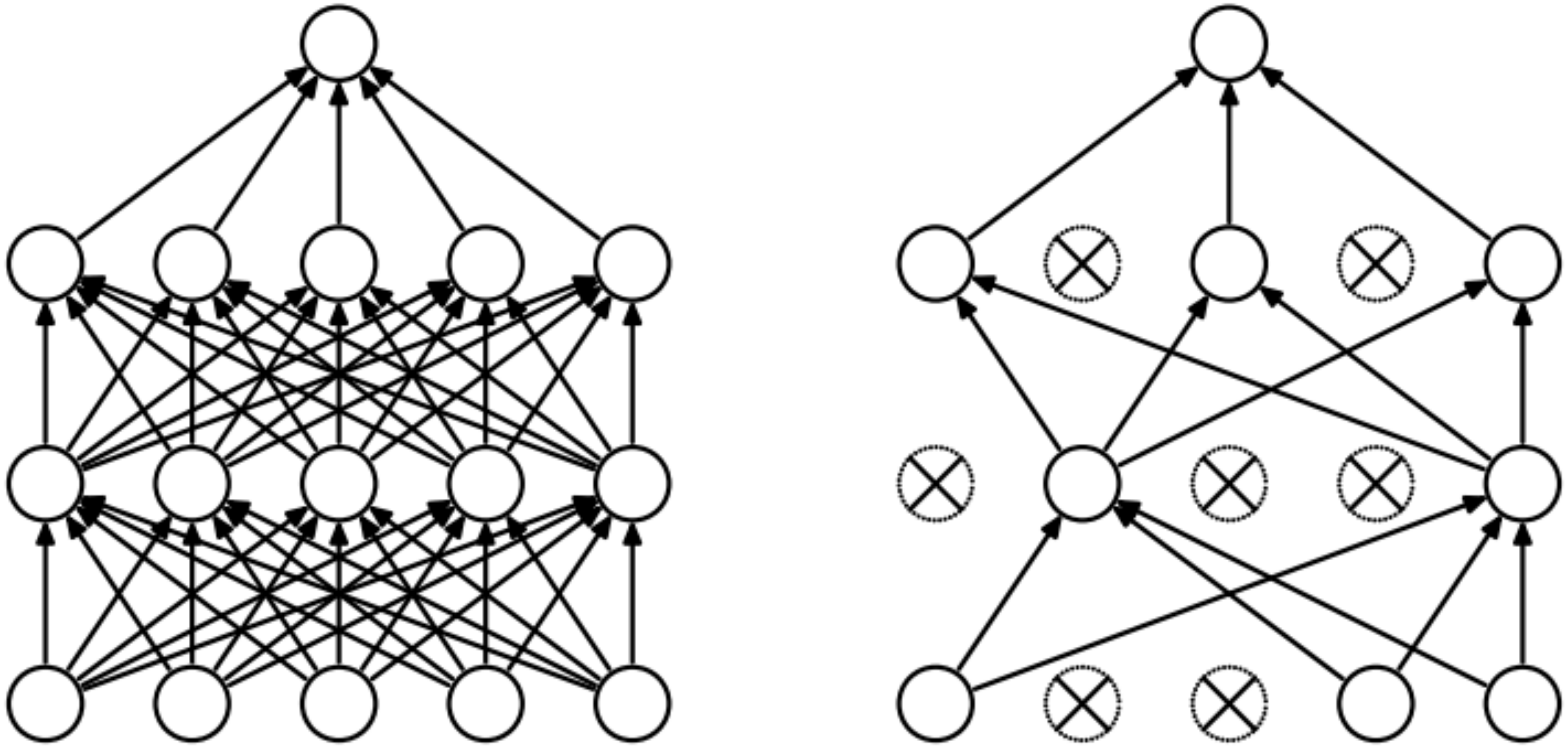
1) Can't use zeroes for parameters to produce hidden layers: all values in that hidden layer are always 0 and have gradients of 0, never change

2) Initialize too large and cells are saturated

- Can do random uniform / normal initialization with appropriate scale
- Glorot initializer: $U\left[-\sqrt{\frac{6}{\text{fan-in}+\text{fan-out}}},+\sqrt{\frac{6}{\text{fan-in}+\text{fan-out}}}\right]$
  - Want variance of inputs and gradients for each layer to be the same
- Batch normalization (Ioffe and Szegedy, 2015): periodically shift+rescale each layer to have mean 0 and variance 1 over a batch (useful if net is deep)

Dropout

- Probabilistically zero out parts of the network during training to prevent overfitting, use whole network at test time
- Form of stochastic regularization
- Similar to benefits of ensembling: network needs to be robust to missing signals, so it has redundancy



(a) Standard Neural Net (b) After applying dropout.

- One line in Pytorch/Tensorflow

Srivastava et al. (2014)

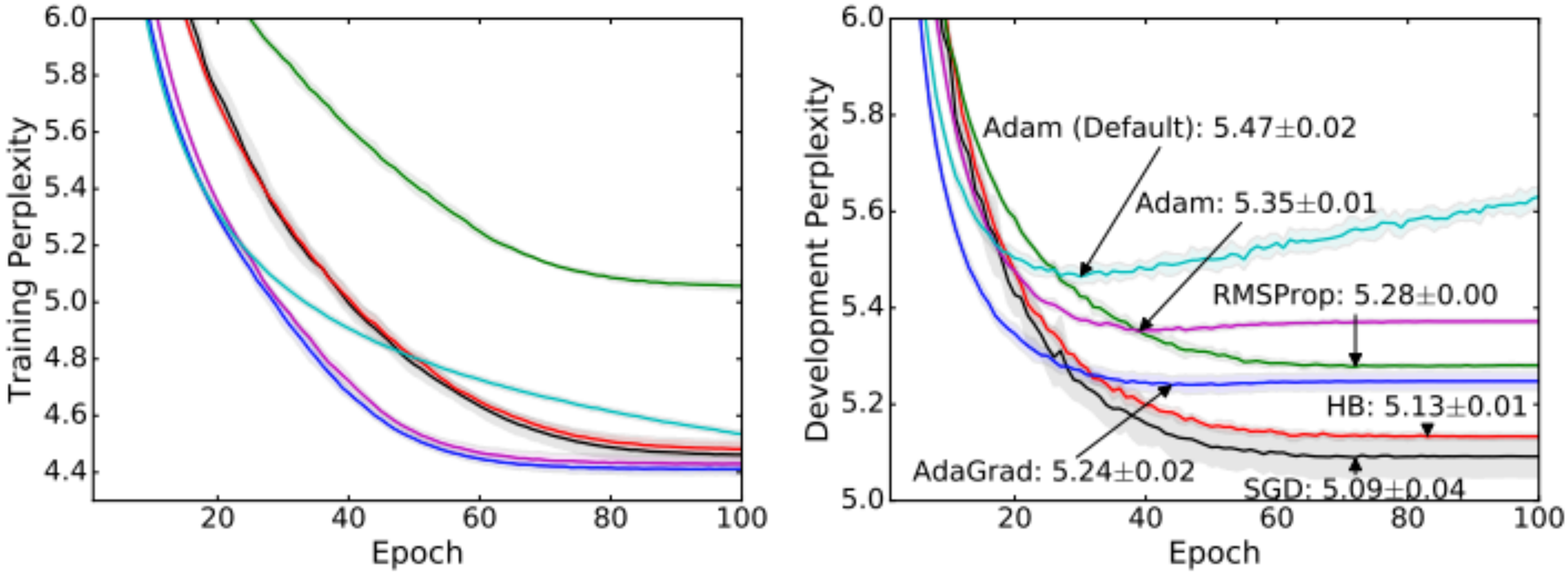
Adam

$$g_t \leftarrow \nabla_\theta f_t(\theta_{t-1}) \text{ (Get gradients w.r.t. stochastic objective at timestep } t\text{)}$$
$$m_t \leftarrow \beta_1 \cdot m_{t-1} + (1 - \beta_1) \cdot g_t \text{ (Update biased first moment estimate)}$$
$$v_t \leftarrow \beta_2 \cdot v_{t-1} + (1 - \beta_2) \cdot g_t^2 \text{ (Update biased second raw moment estimate)}$$
$$\widehat{m}_t \leftarrow m_t / (1 - \beta_1^t) \text{ (Compute bias-corrected first moment estimate)}$$
$$\widehat{v}_t \leftarrow v_t / (1 - \beta_2^t) \text{ (Compute bias-corrected second raw moment estimate)}$$
$$\theta_t \leftarrow \theta_{t-1} - \alpha \cdot \widehat{m}_t / (\sqrt{\widehat{v}_t} + \epsilon) \text{ (Update parameters)}$$

- *m*: exponentially-weighted moving average of gradients
- *v*: exponentially-weighted moving average of gradients squared
- $\beta_1 = 0.9$, $\beta_2 = 0.999$, so these average over many steps
- Update is based on normalized corrected mean, incorporates *momentum*

Kingma and Ba (2015)

Optimizer



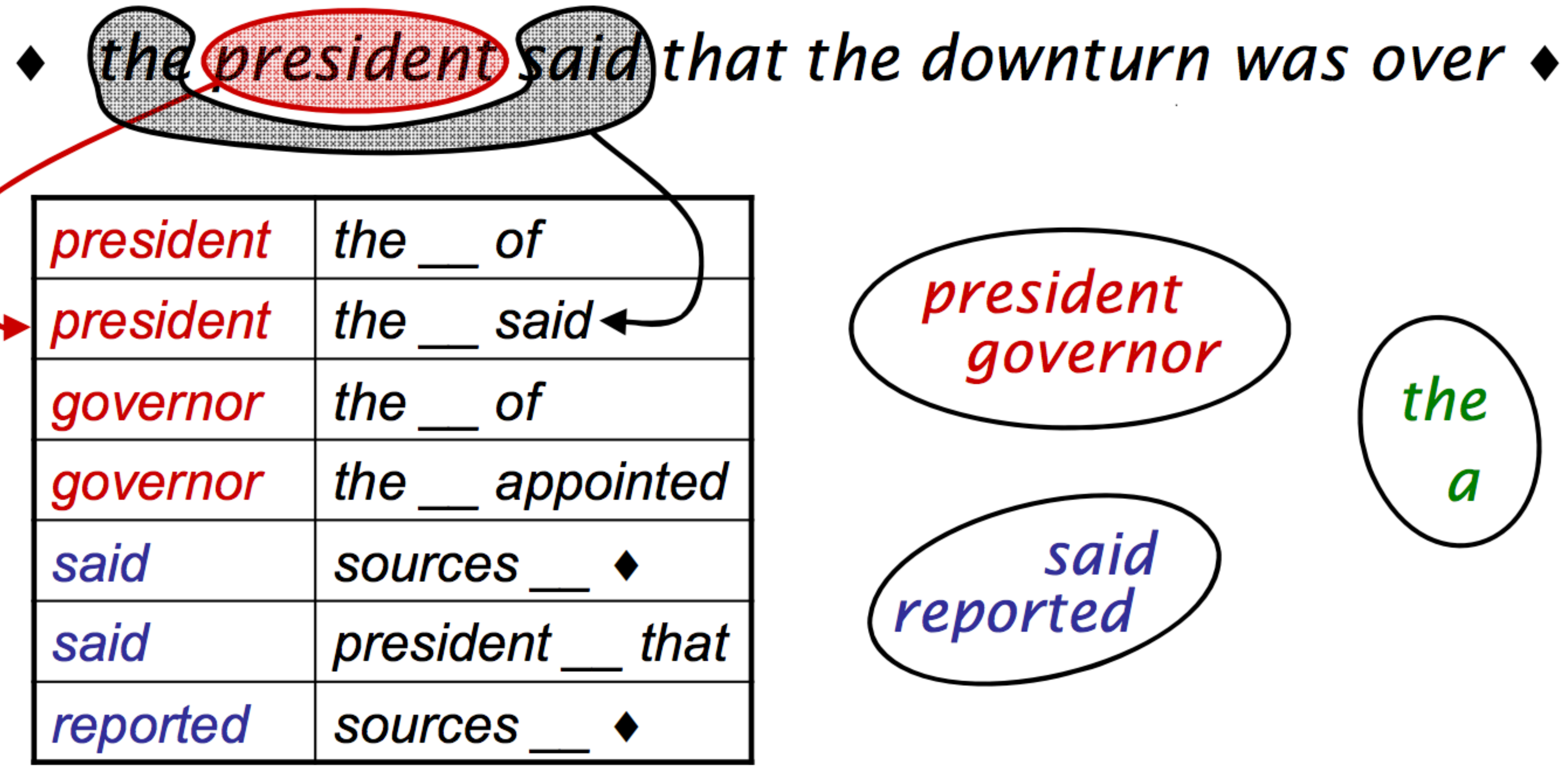
(e) Generative Parsing (Training Set) (f) Generative Parsing (Development Set)

- Wilson et al. NeurIPS 2017: adaptive methods can sometimes perform badly at test time (Adam is in pink, SGD in black)
- One more trick: **gradient clipping** (set max value for your gradients)

Next Time: Word Representations

Word Representations

- Neural networks work very well at continuous data, but words are discrete
- Continuous model <-> expects continuous semantics from input
- "You shall know a word by the company it keeps" Firth (1957)



[Finch and Chater 92, Shuetze 93, many others]

slide credit: Dan Klein

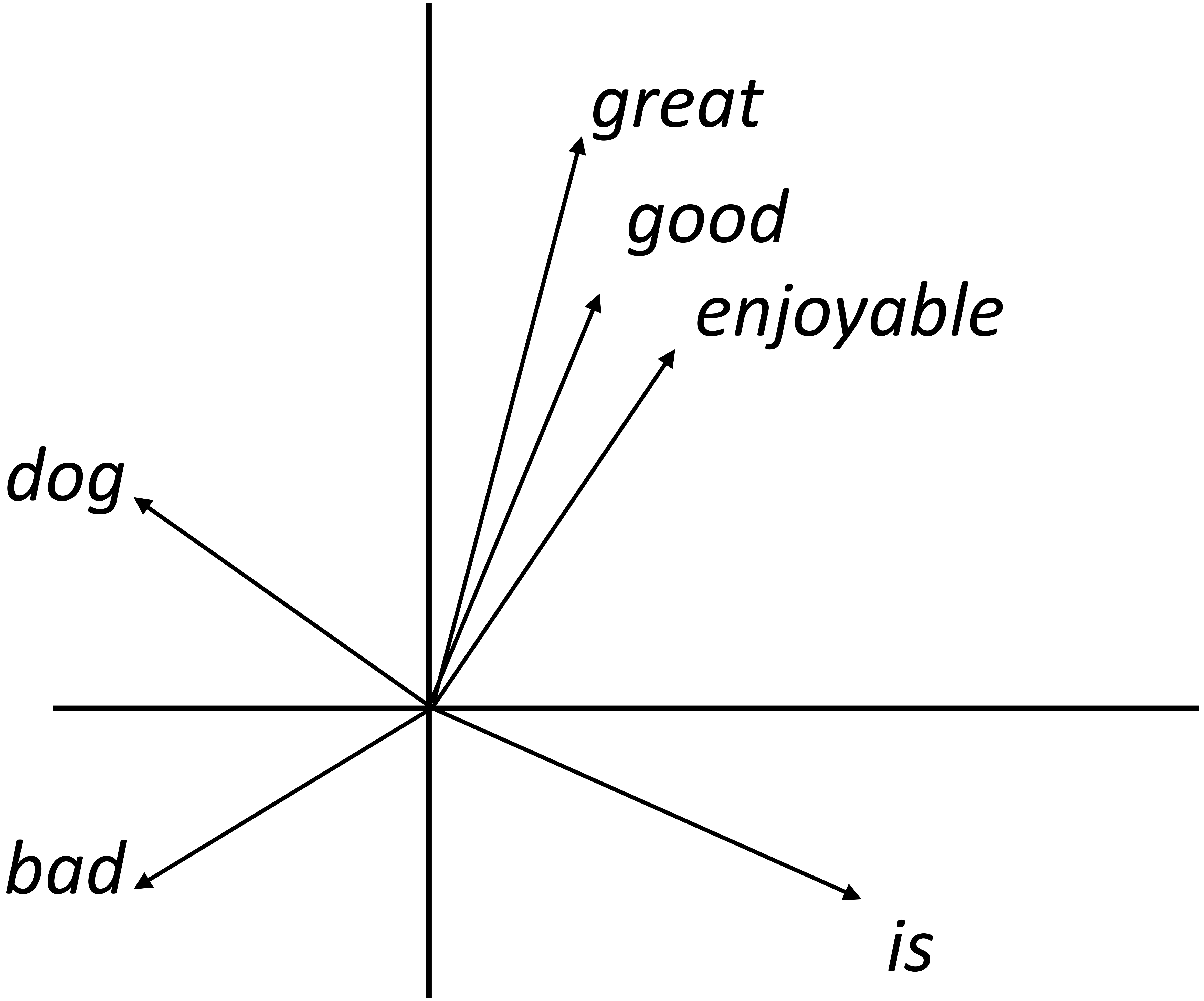
Word Embeddings

- Want a vector space where similar words have similar embeddings

the movie was great

≈

the movie was good



- Goal: come up with a way to produce these embeddings
- For each word, want "medium" dimensional vector (50-300 dims) representing it

Takeaways

- Feedforward neural networks can be implemented easily in PyTorch
  - We saw that these are basically logistic regression
  - Easy to implement backpropagation (you don't have to do anything!) and use the standard tricks to get good performance
- Next class: thinking about the feature representations: word representations / word vectors (word2vec and GloVe)