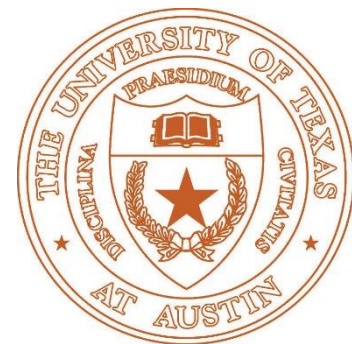


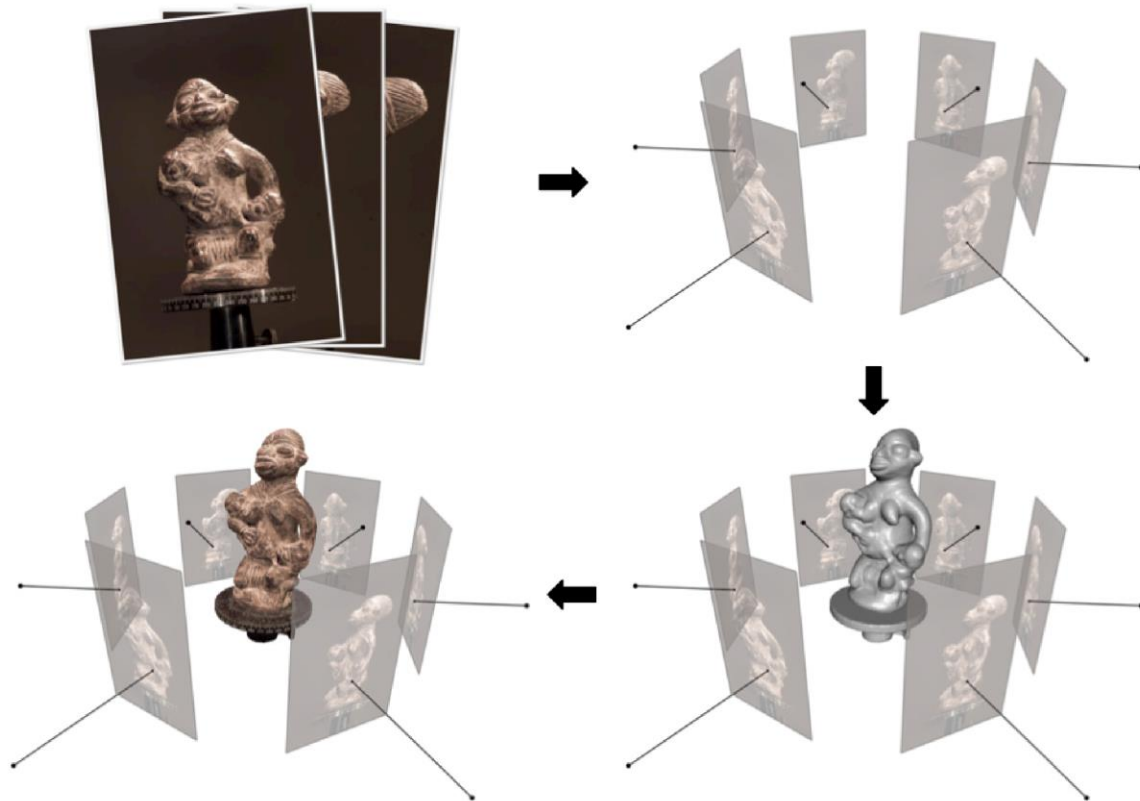
CS395T Lecture 14: Multi-View Stereo

Qixing Huang
Oct. 17th 2018

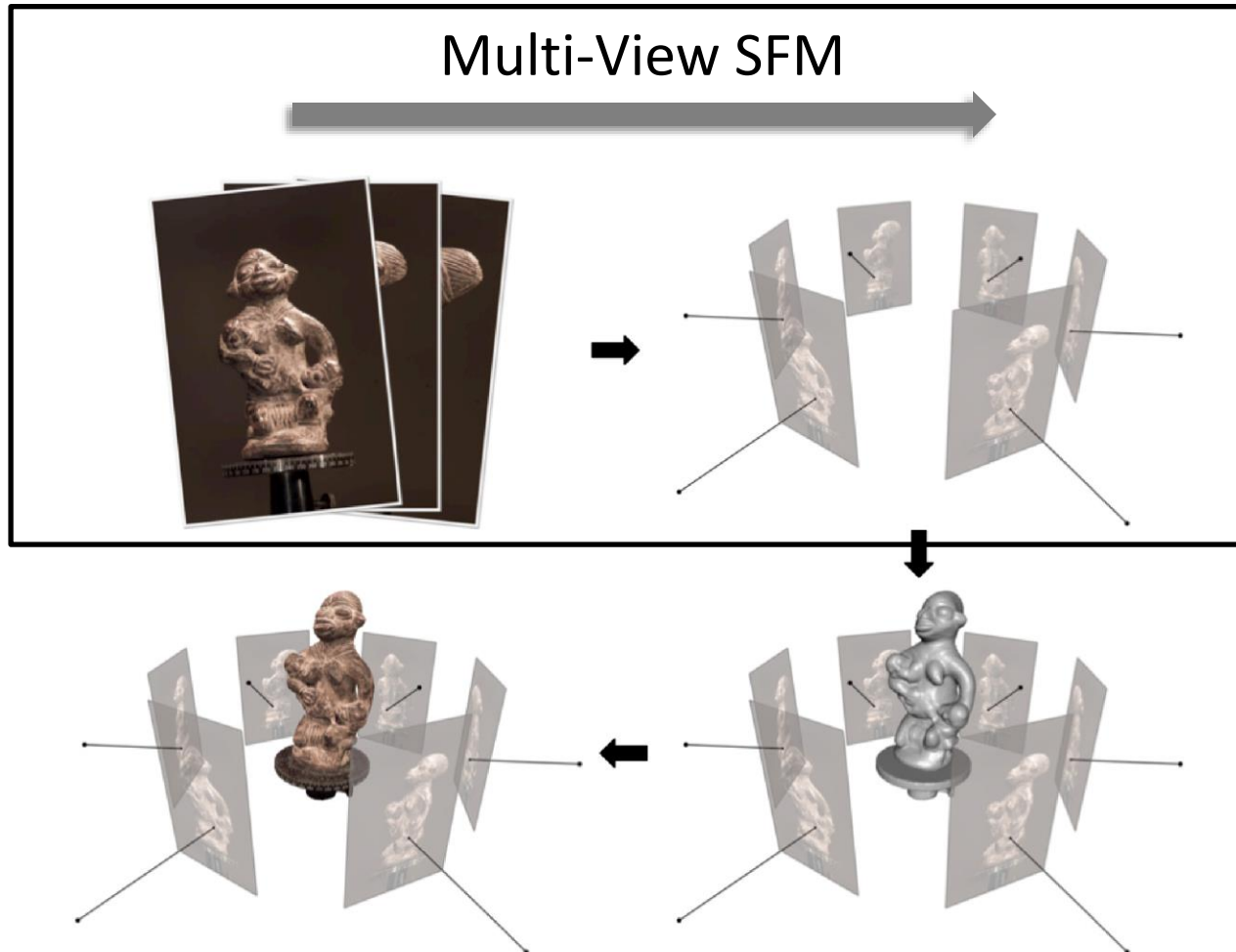


Slide Credit: Yasutaka Furukawa

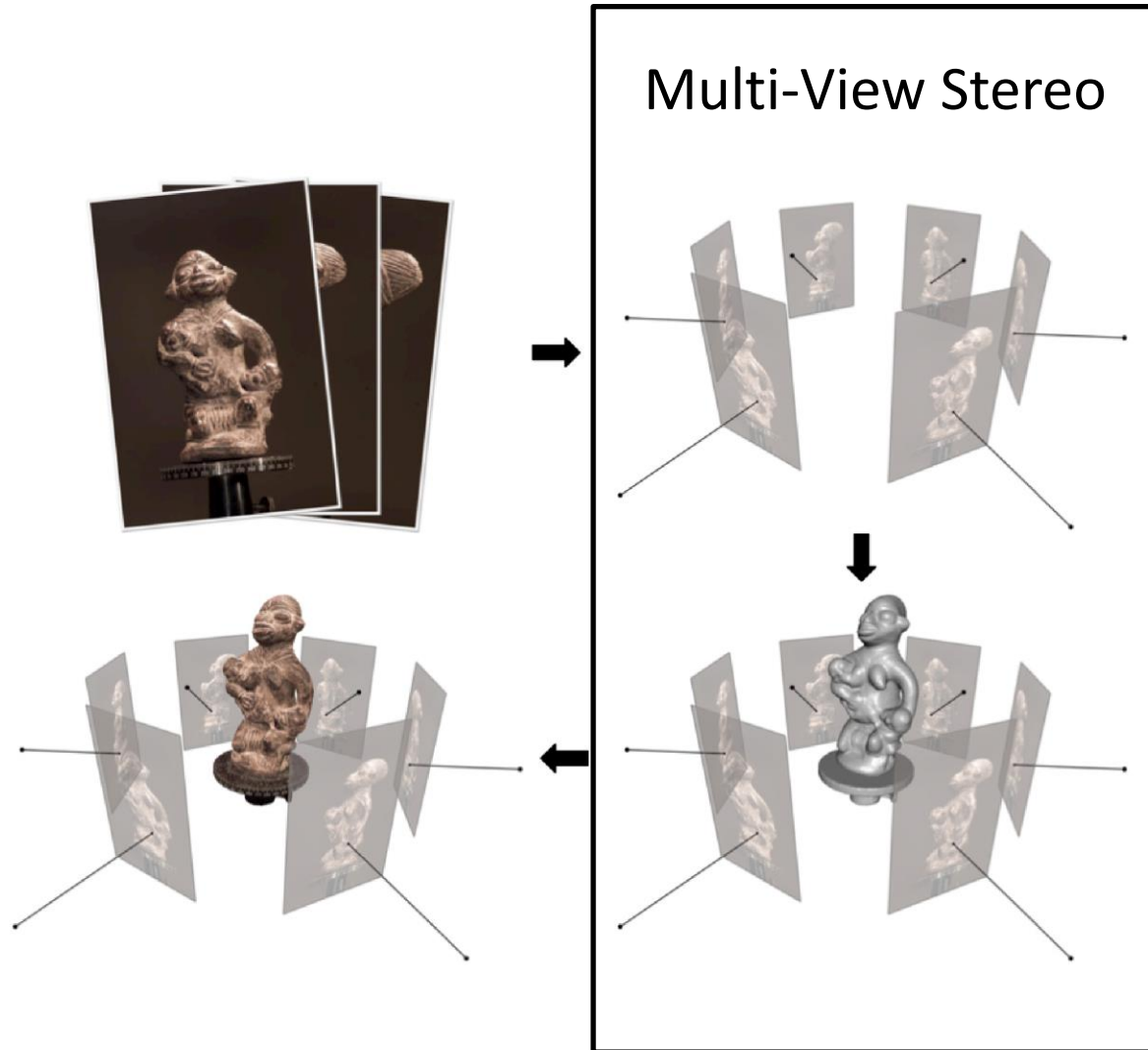
Image-Based Geometry Reconstruction Pipeline



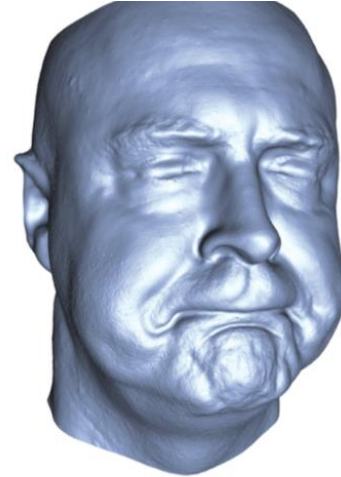
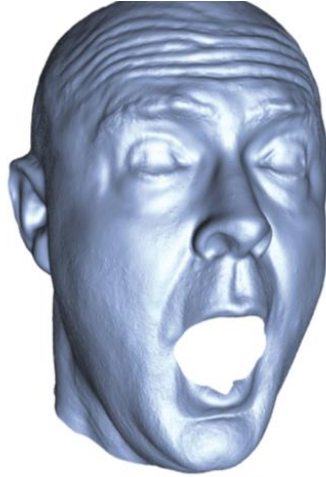
Last Lecture: Multi-View SFM



This Lecture: Multi-View Stereo



Multi-view Stereo for Visual Effects



Input Images

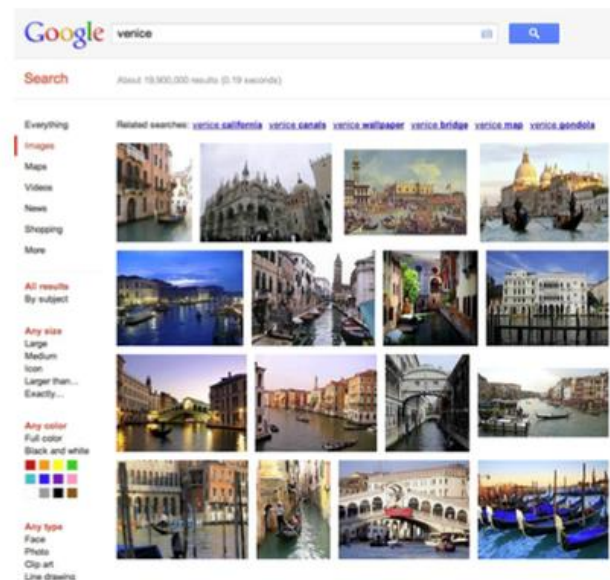


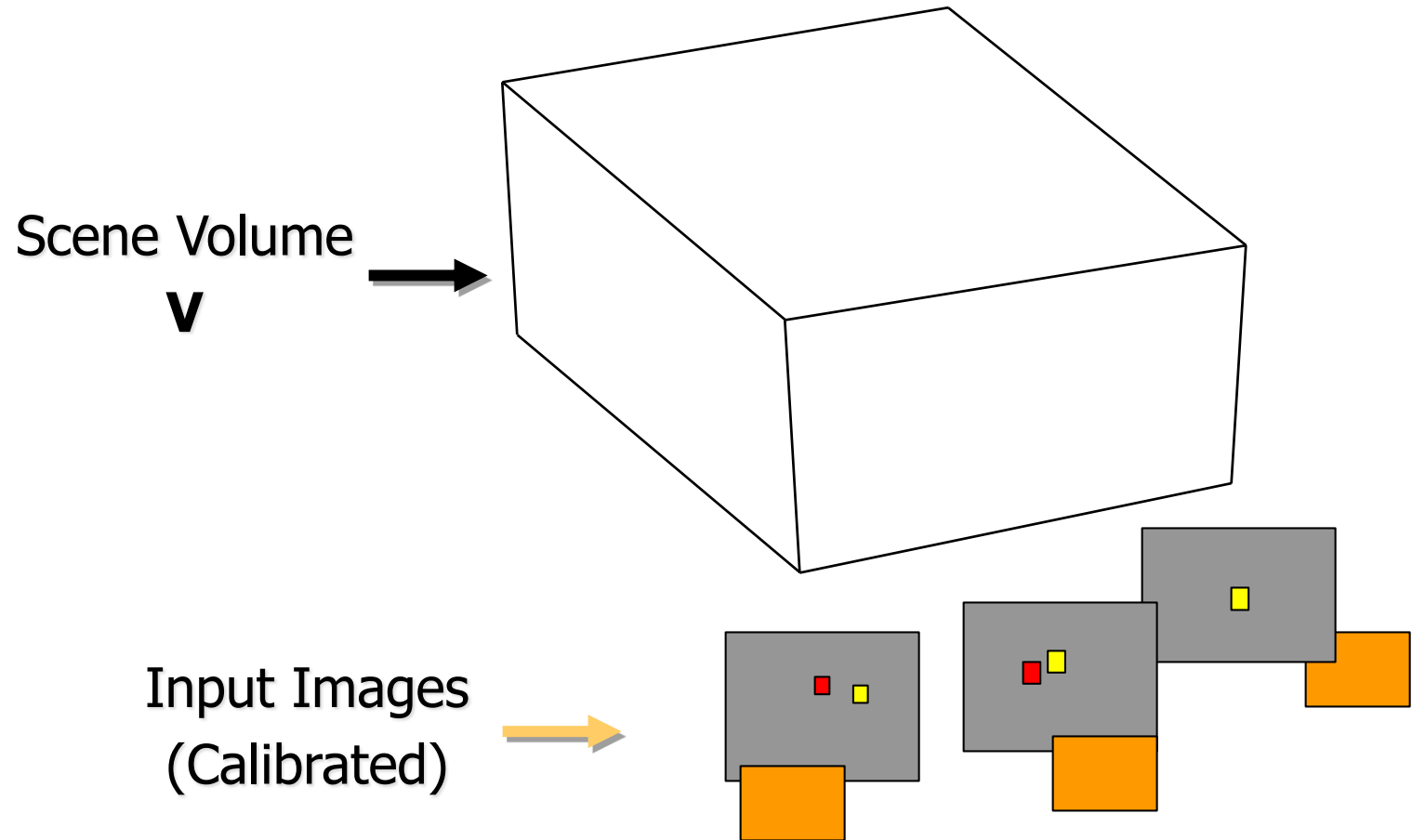
Fig. 1.3 Different MVS capture setups. From left to right: a controlled MVS capture using diffuse lights and a turn table, outdoor capture of small-scale scenes, and crowd-sourcing from online photo-sharing websites.

Volumetric Stereo

Space Carving

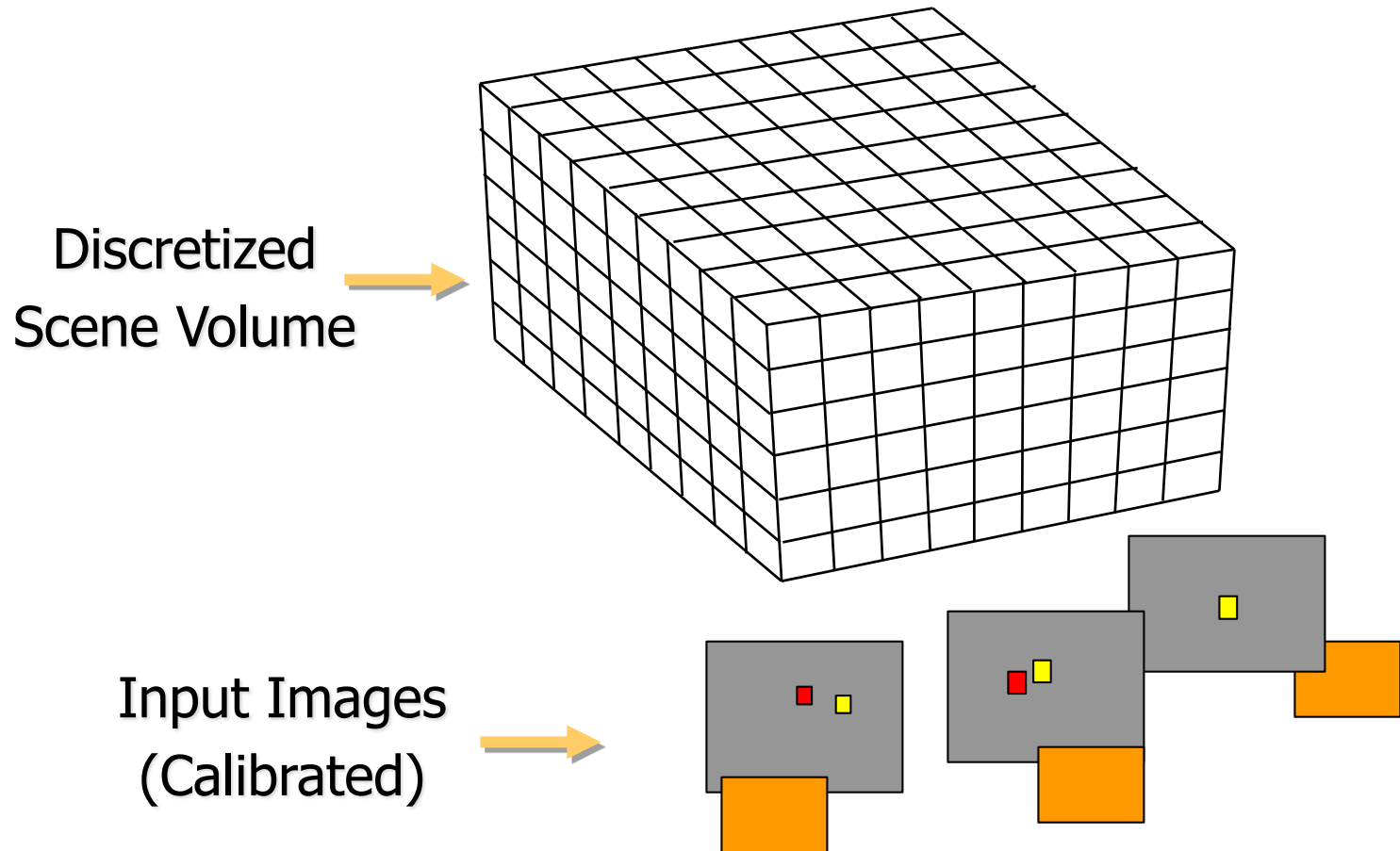
Multi-Baseline Stereo

Volumetric Stereo



Goal: Determine occupancy, “color” of points in V

Discrete formulation: Voxel Coloring



Goal: Assign RGBA values to voxels in V
photo-consistent with images

Voxel Coloring Solutions

1. $C=2$ (shape from silhouettes)

- Volume intersection [Baumgart 1974]

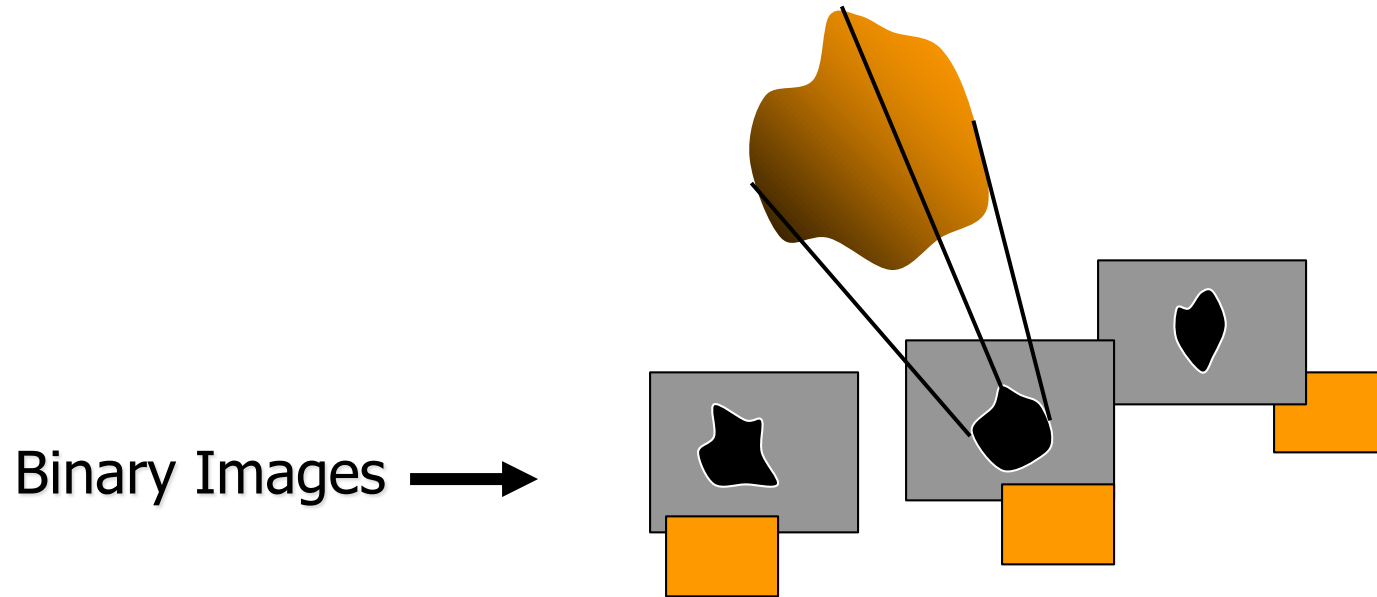
2. C unconstrained, viewpoint constraints

- Voxel coloring algorithm [Seitz & Dyer 97]

3. General Case

- Space carving [Kutulakos & Seitz 98]

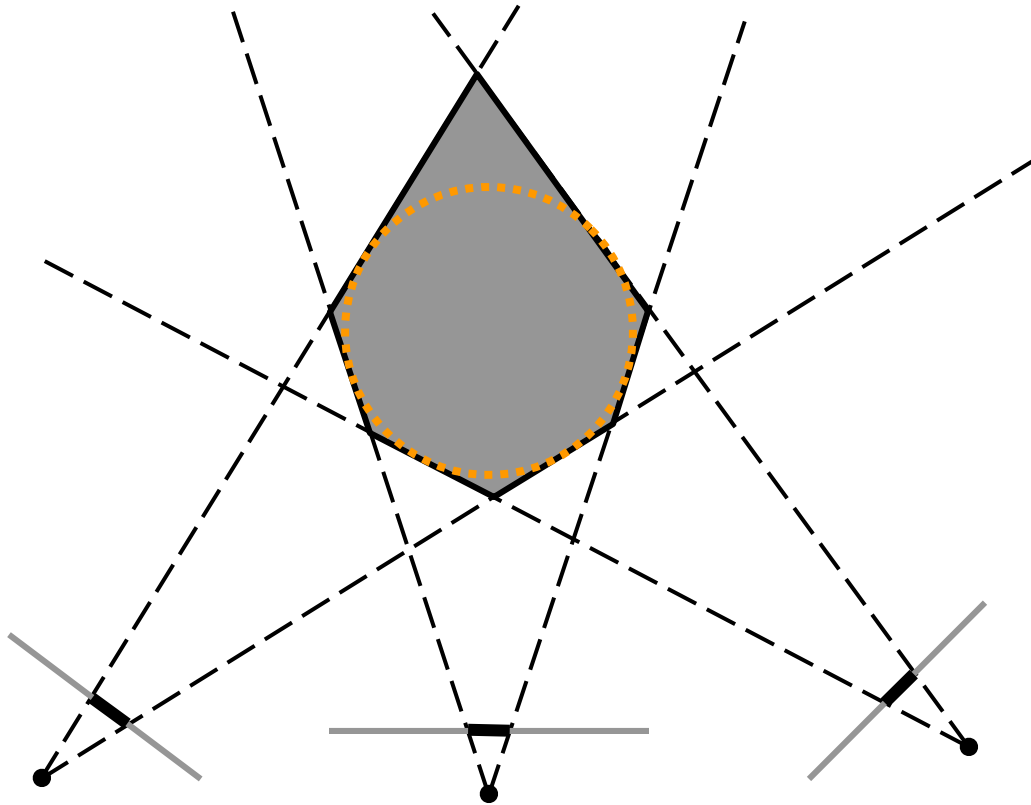
Reconstruction from Silhouettes ($C = 2$)



Approach:

- *Backproject* each silhouette
- Intersect backprojected volumes

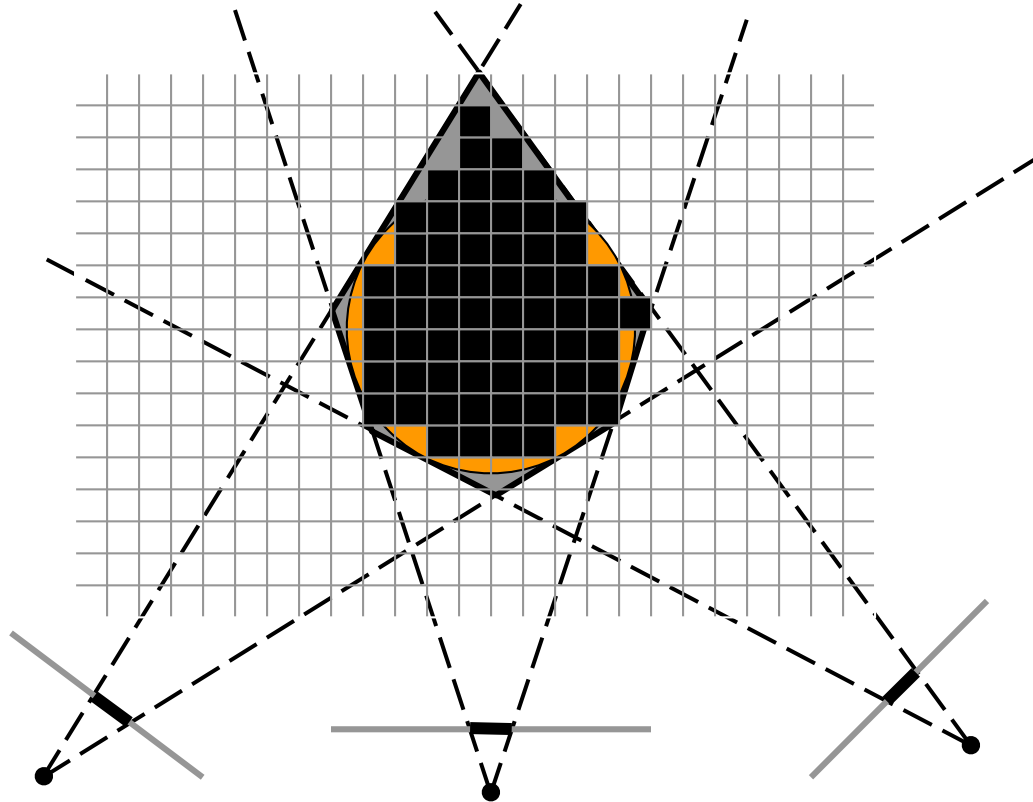
Volume Intersection



Reconstruction Contains the True Scene

- In the limit (all views) get *convex hull*

Voxel Algorithm for Volume Intersection



Color voxel black if on silhouette in every image

Properties of Volume Intersection

- Pros

- Easy to implement, fast
- Accelerated via octrees [Szeliski 1993] or interval techniques [Matusik 2000]

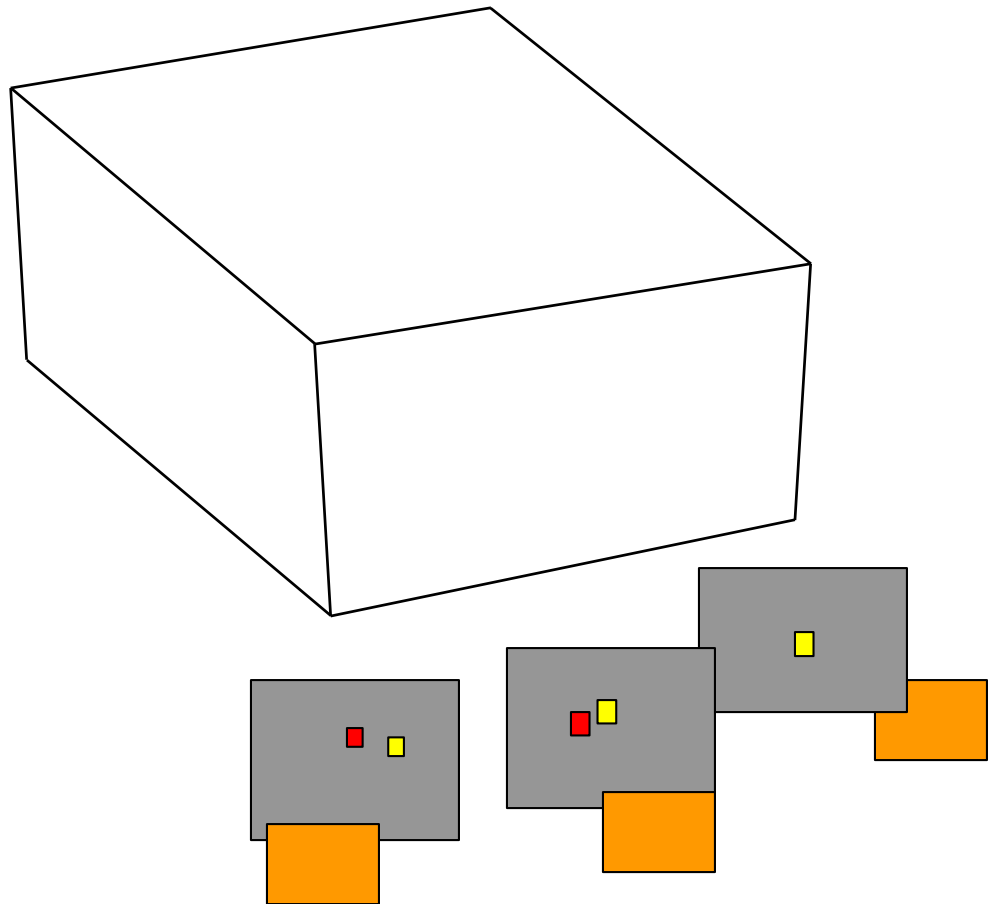
- Cons

- No concavities
- Reconstruction is not photo-consistent
- Requires identification of silhouettes

Voxel Coloring Solutions

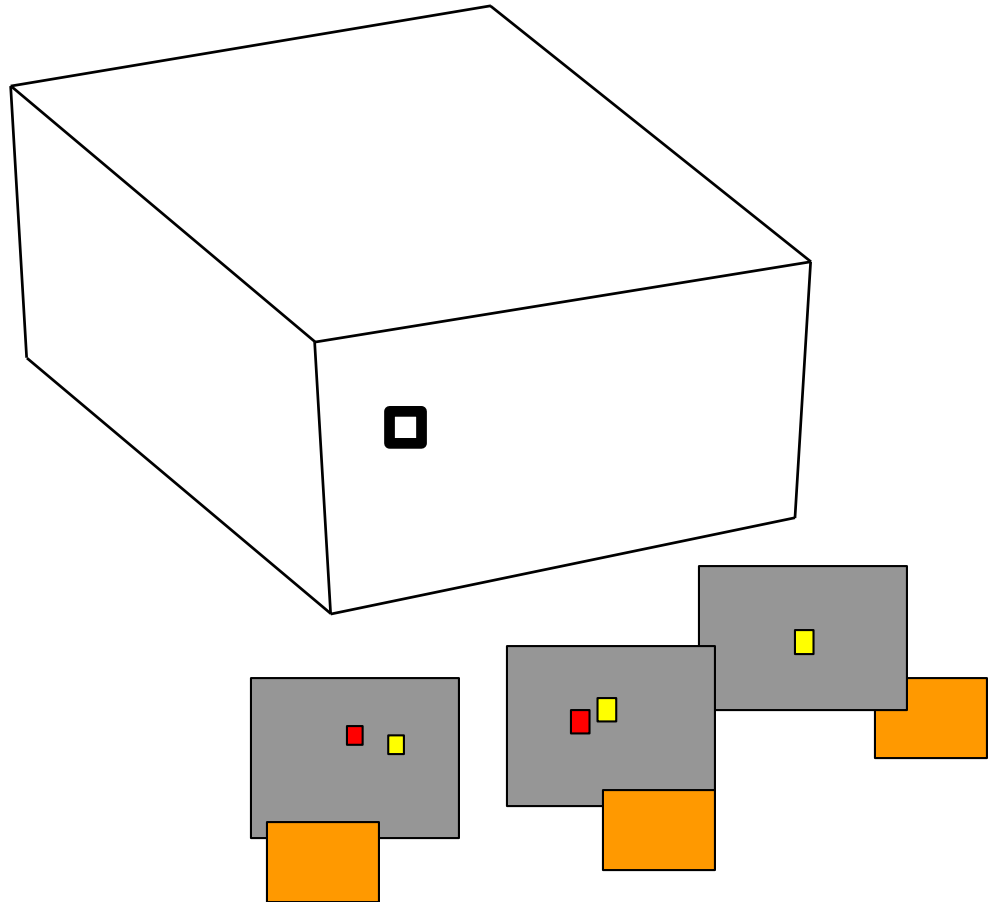
1. $C=2$ (shape from silhouettes)
 - Volume intersection [Baumgart 1974]
2. C unconstrained, viewpoint constraints
 - Voxel coloring algorithm [Seitz & Dyer 97]
3. General Case
 - Space carving [Kutulakos & Seitz 98]

Voxel Coloring Approach



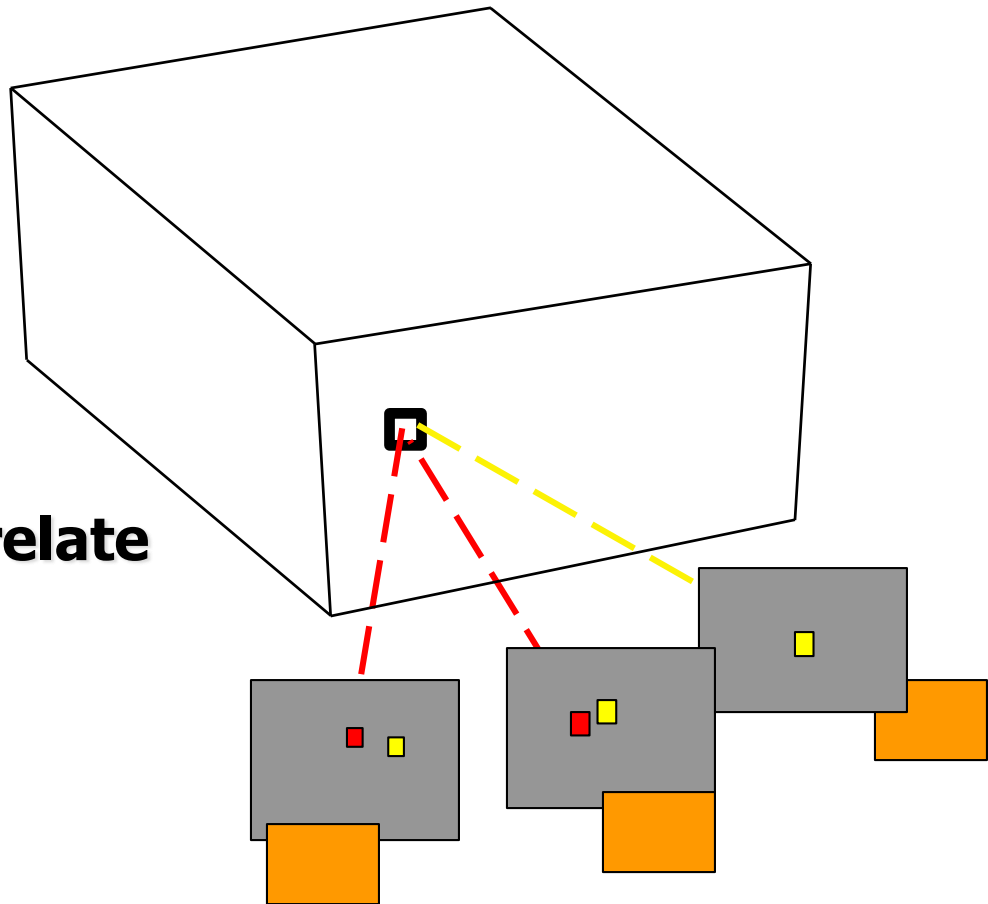
Voxel Coloring Approach

1. Choose voxel



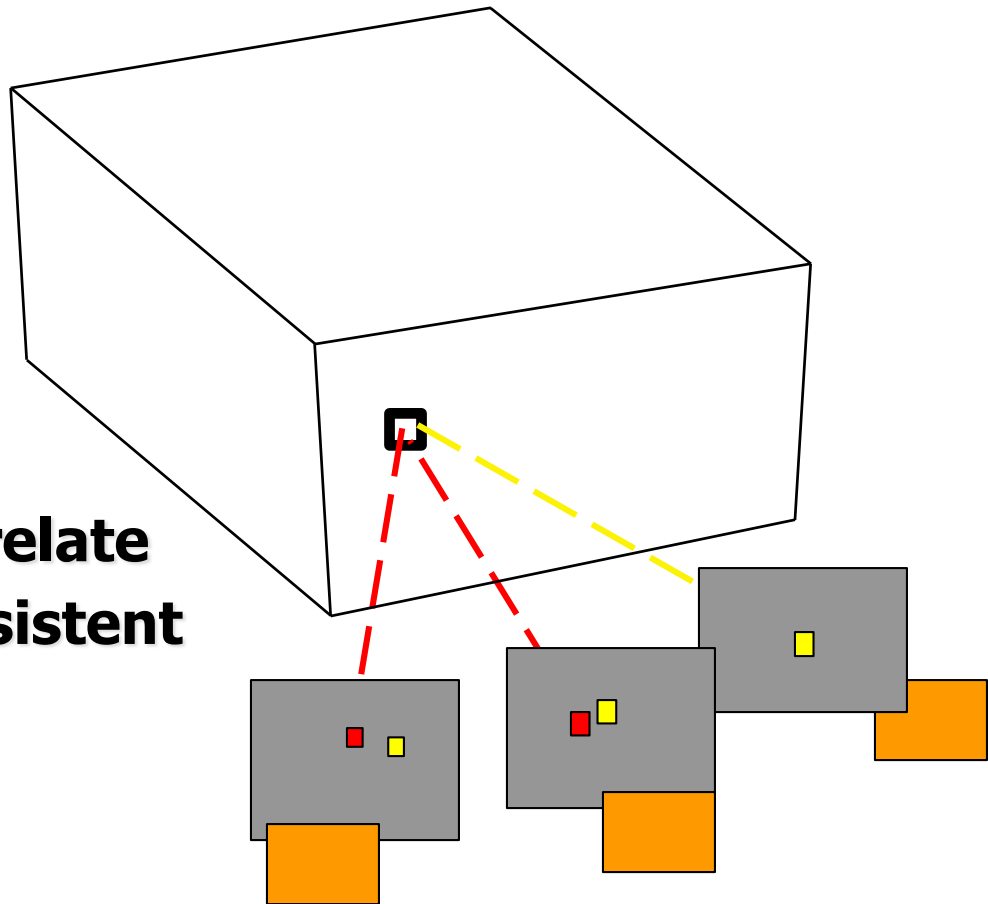
Voxel Coloring Approach

- 1. Choose voxel**
- 2. Project and correlate**



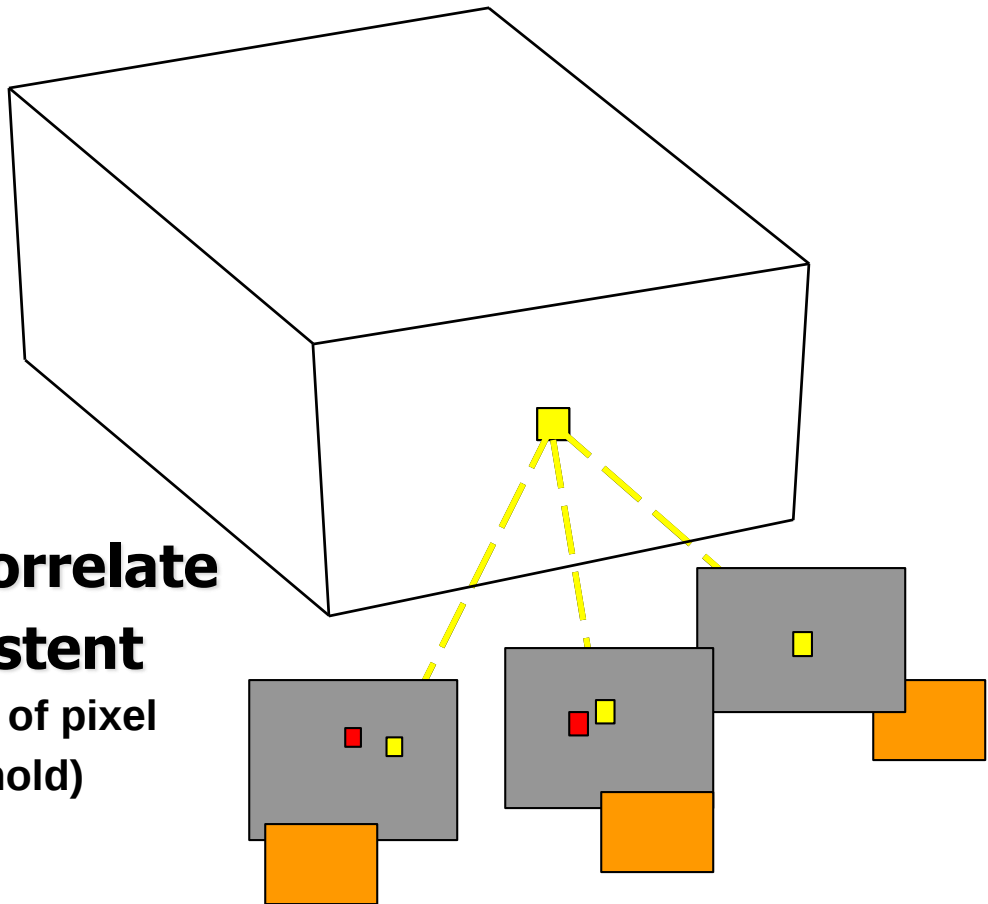
Voxel Coloring Approach

- 1. Choose voxel**
- 2. Project and correlate**
- 3. Discard if inconsistent**



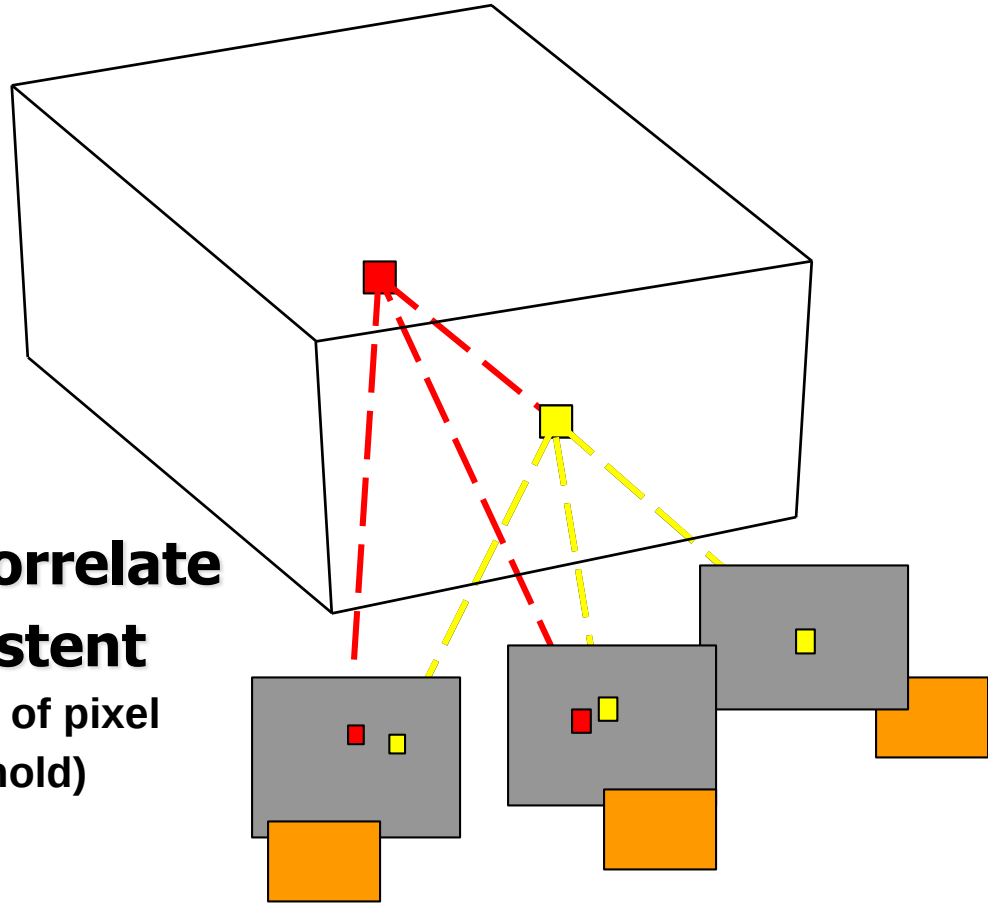
Voxel Coloring Approach

- 1. Choose voxel**
- 2. Project and correlate**
- 3. Color if consistent**
(standard deviation of pixel colors below threshold)



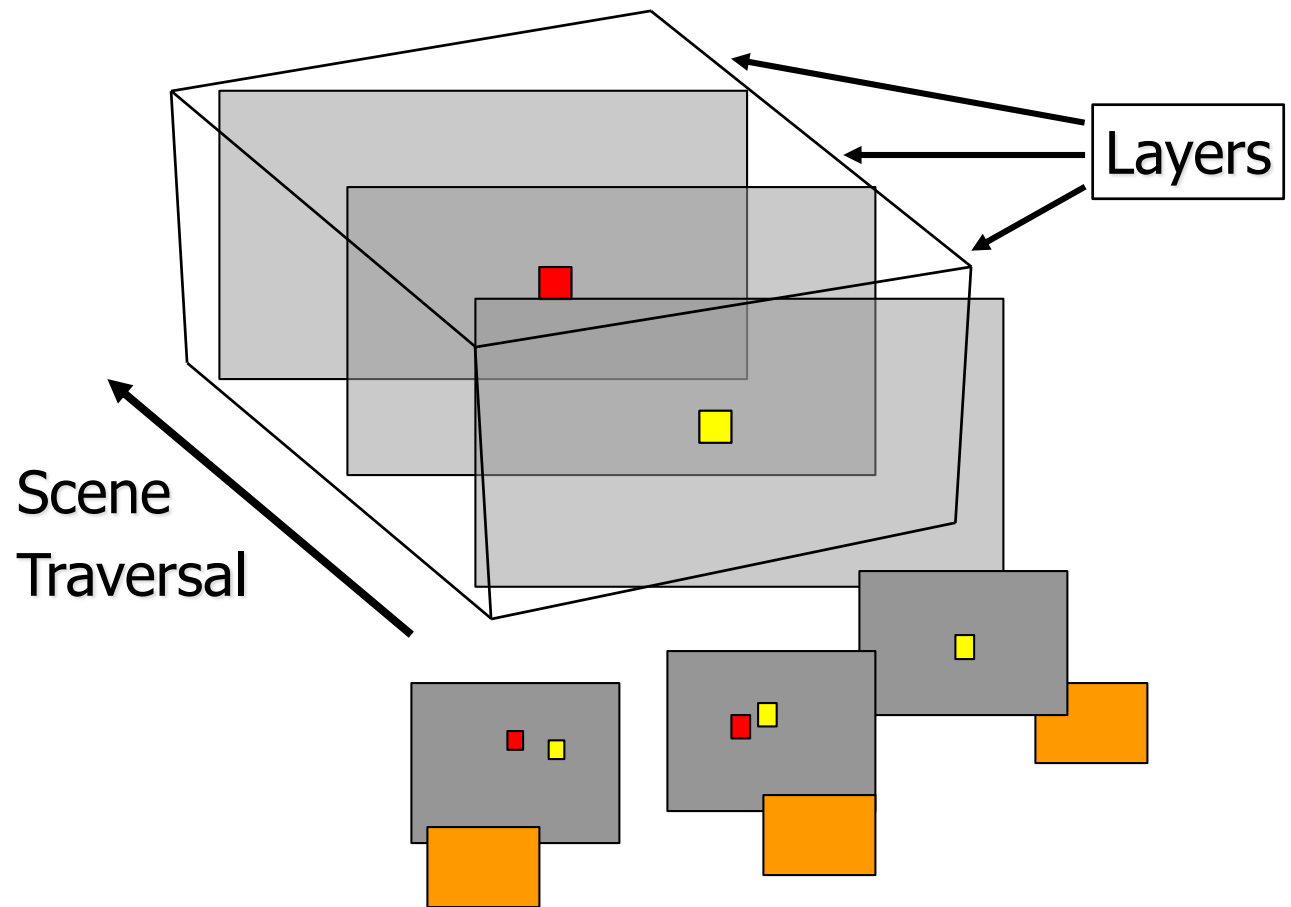
Voxel Coloring Approach

- 1. Choose voxel**
- 2. Project and correlate**
- 3. Color if consistent**
(standard deviation of pixel colors below threshold)



Visibility Problem: in which images is each voxel visible?

Depth Ordering: Visit Occluders First!



Calibrated Image Acquisition



Calibrated Turntable



Selected Dinosaur Images



Selected Flower Images

Voxel Coloring Results



Dinosaur Reconstruction

**72 K voxels colored
7.6 M voxels tested
7 min. to compute
on a 250MHz SGI**



Flower Reconstruction

**70 K voxels colored
7.6 M voxels tested
7 min. to compute
on a 250MHz SGI**

Space Carving Results: African Violet



Input Image (1 of 45)



Reconstruction



Reconstruction



Reconstruction

Improvements

Unconstrained camera viewpoints

- Space carving [\[Kutulakos & Seitz 98\]](#)

Evolving a surface

- Level sets [\[Faugeras & Keriven 98\]](#)
- More recent [work](#) by Pons et al.

Global optimization

- Graph cut approaches
 - > [\[Kolmogoriv & Zabih, ECCV 2002\]](#)
 - > [\[Vogiatzis et al., PAMI 2007\]](#)

Modeling shiny (and other reflective) surfaces

- e.g., [Zickler et al., *Helmholtz Stereopsis*](#)

Binocular Stereo

Binocular Stereo

- Given a calibrated binocular stereo pair, fuse it to produce a depth image

image 1



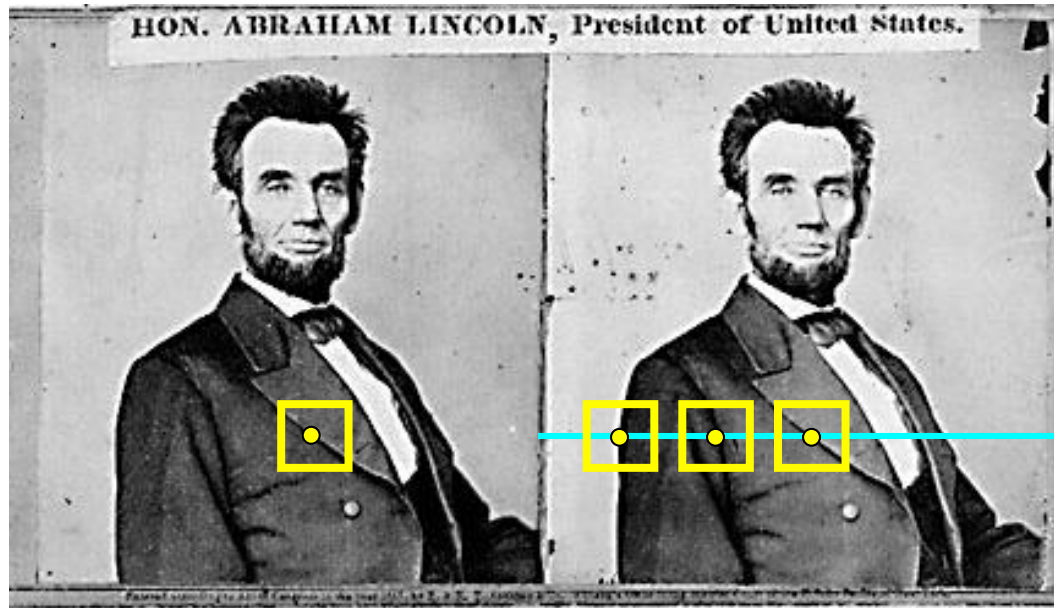
image 2



Dense depth map

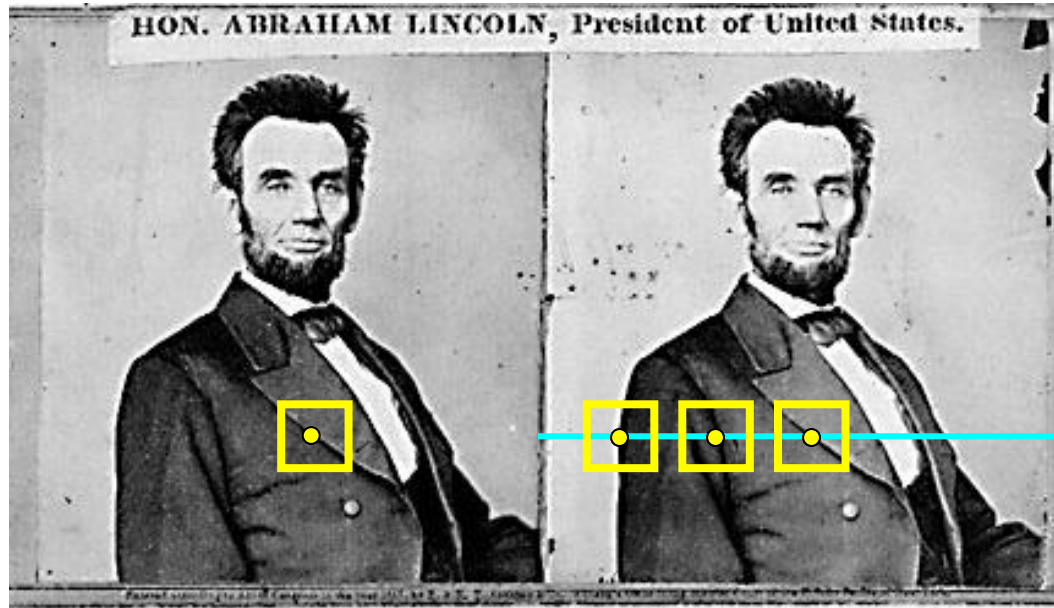


Basic Stereo Matching Algorithm



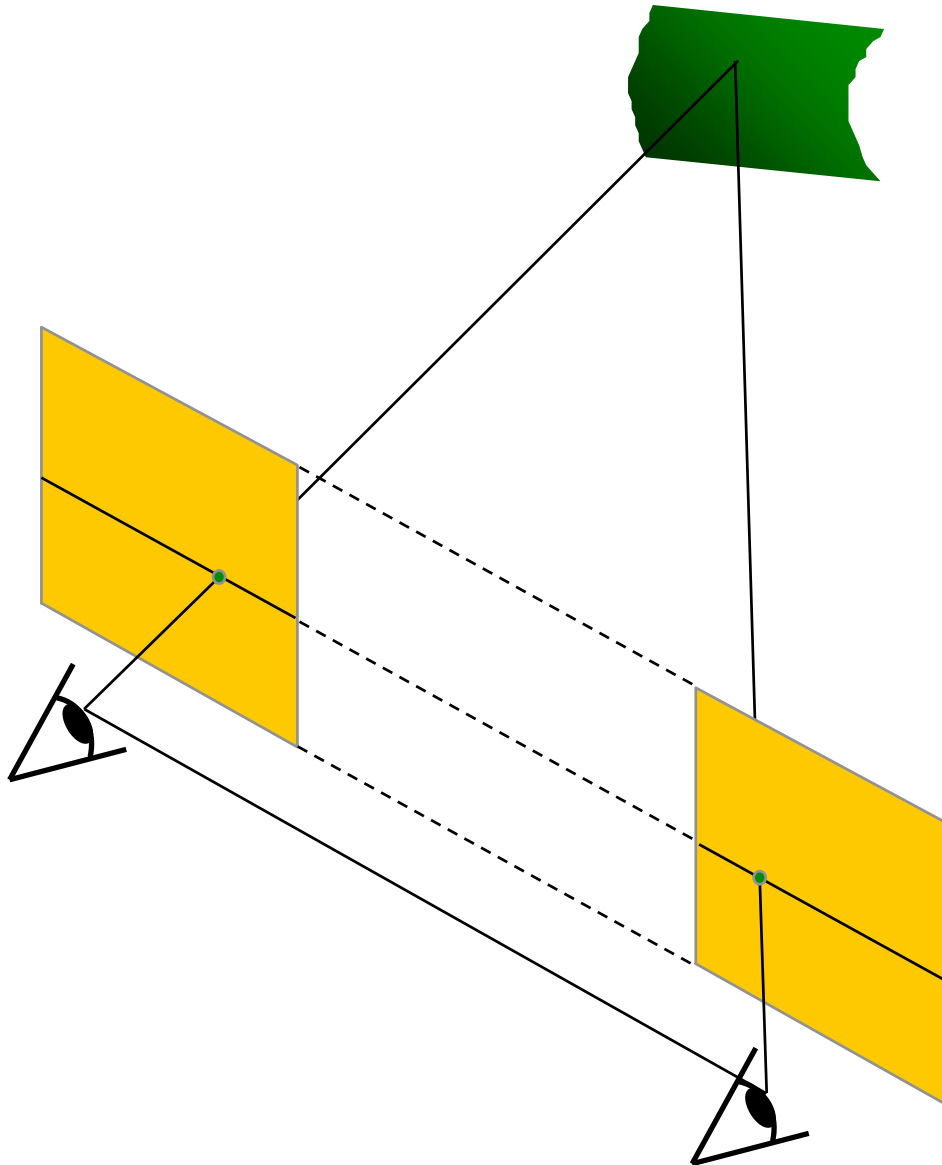
- For each pixel in the first image
 - Find corresponding epipolar line in the right image
 - Examine all pixels on the epipolar line and pick the best match
 - Triangulate the matches to get depth information
- Simplest case: epipolar lines are corresponding scanlines
 - When does this happen?

Basic stereo matching algorithm



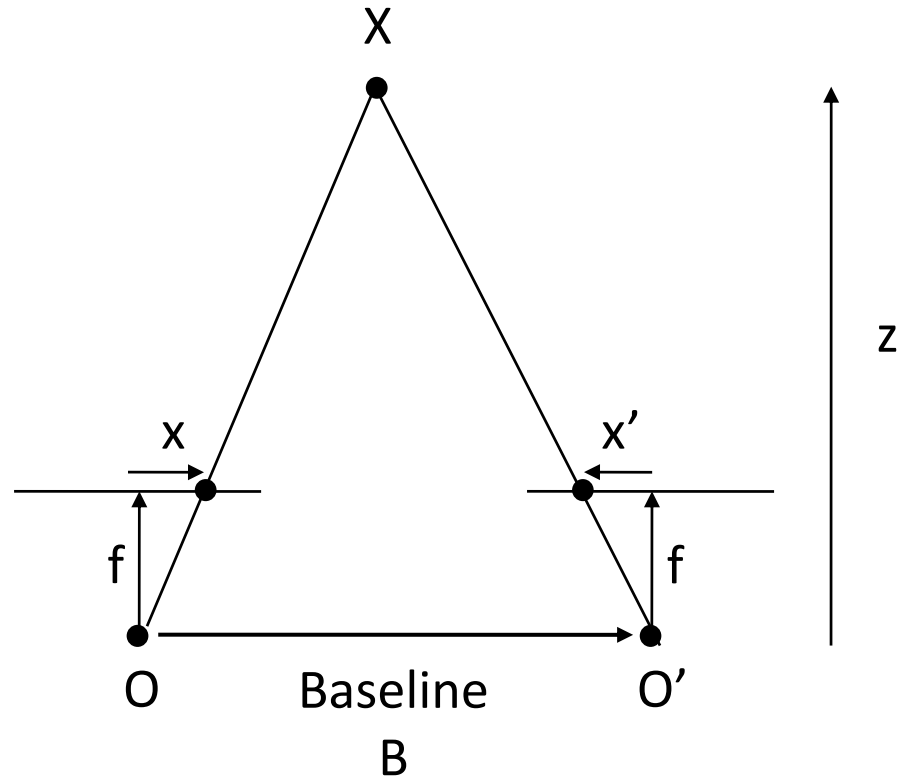
- For each pixel in the first image
 - Find corresponding epipolar line in the right image
 - Examine all pixels on the epipolar line and pick the best match
 - Triangulate the matches to get depth information
- Simplest case: epipolar lines are corresponding scanlines
 - When does this happen?

Simplest Case: Parallel Images



- Image planes of cameras are parallel to each other and to the baseline
- Camera centers are at same height
- Focal lengths are the same
- Then, epipolar lines fall along the horizontal scan lines of the images

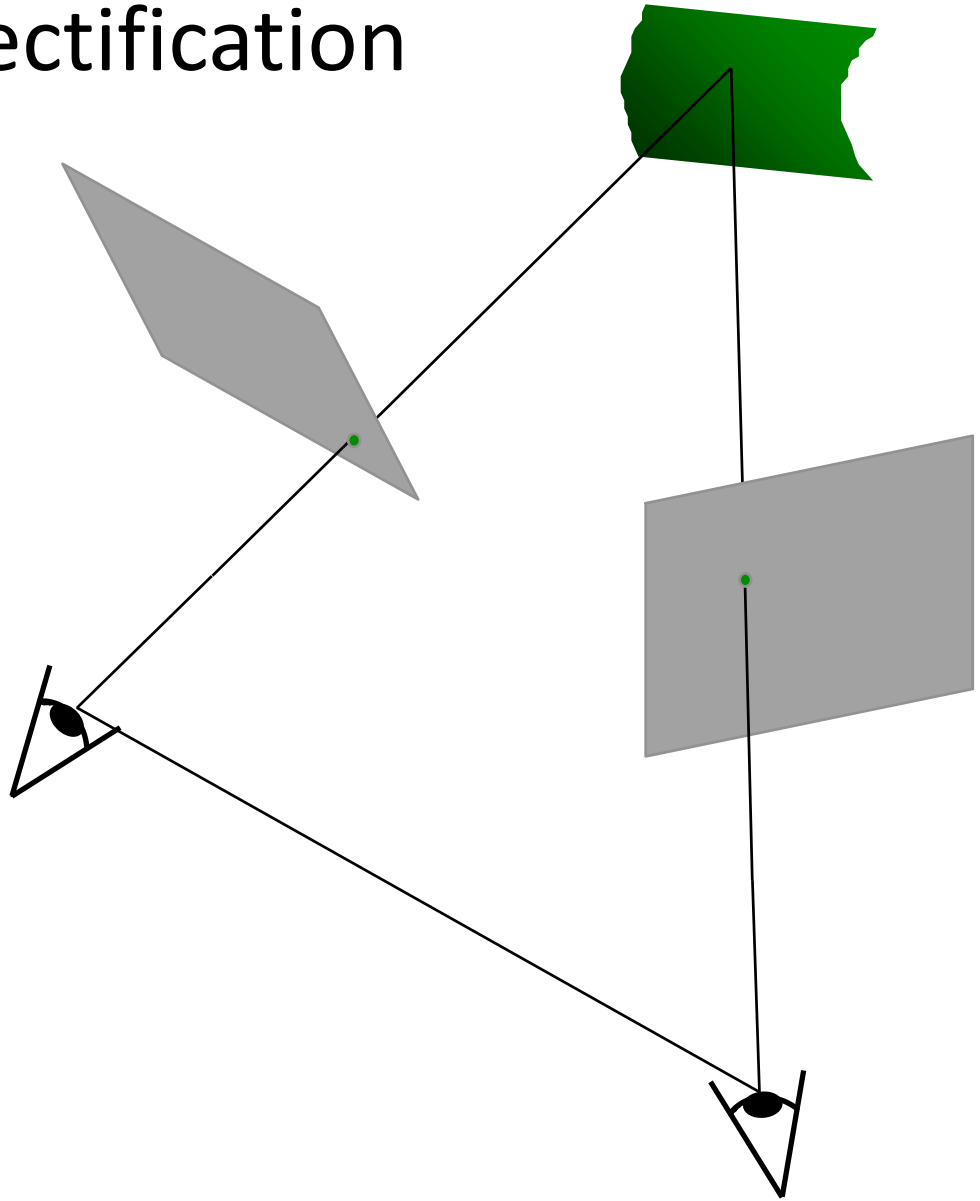
Depth from Disparity



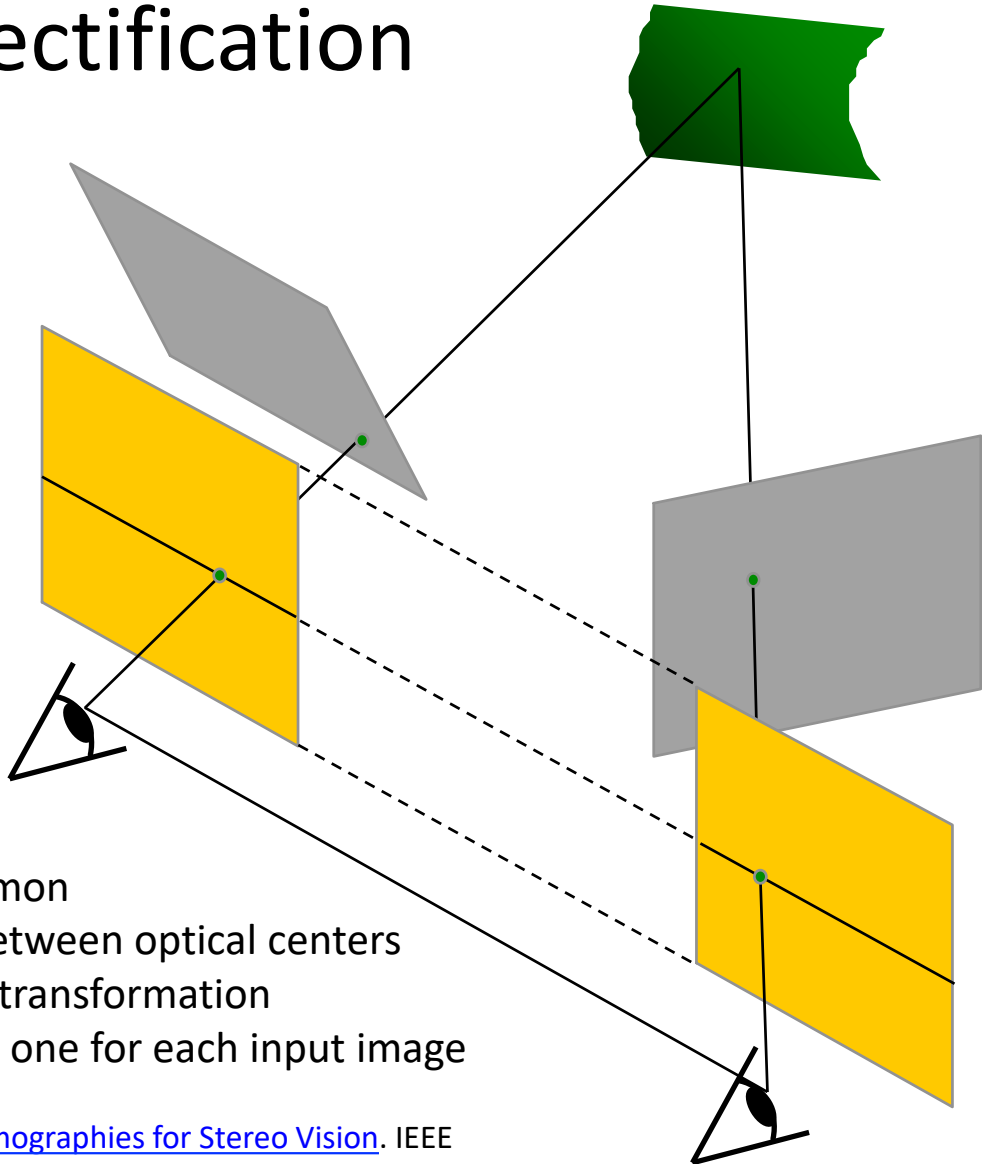
$$\text{disparity} = x - x' = \frac{B \times f}{z}$$

Disparity is inversely proportional to depth!

Stereo Image Rectification



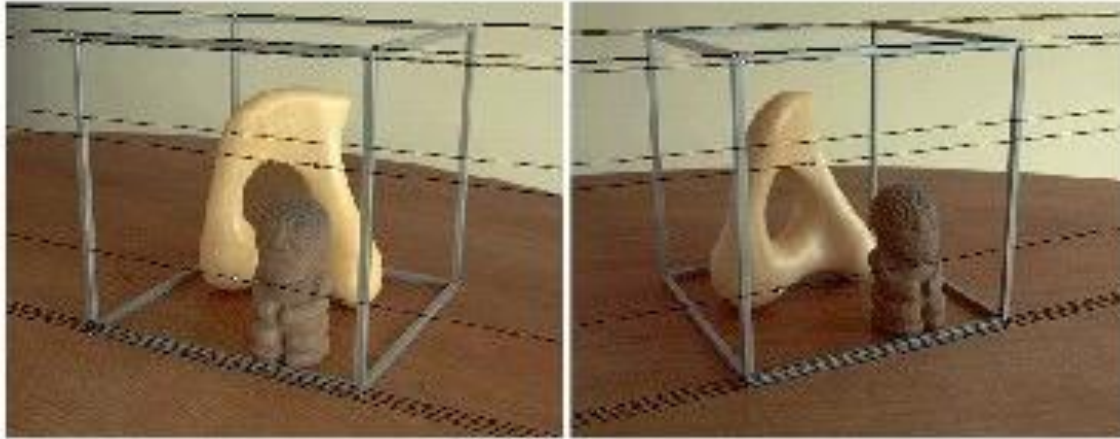
Stereo Image Rectification



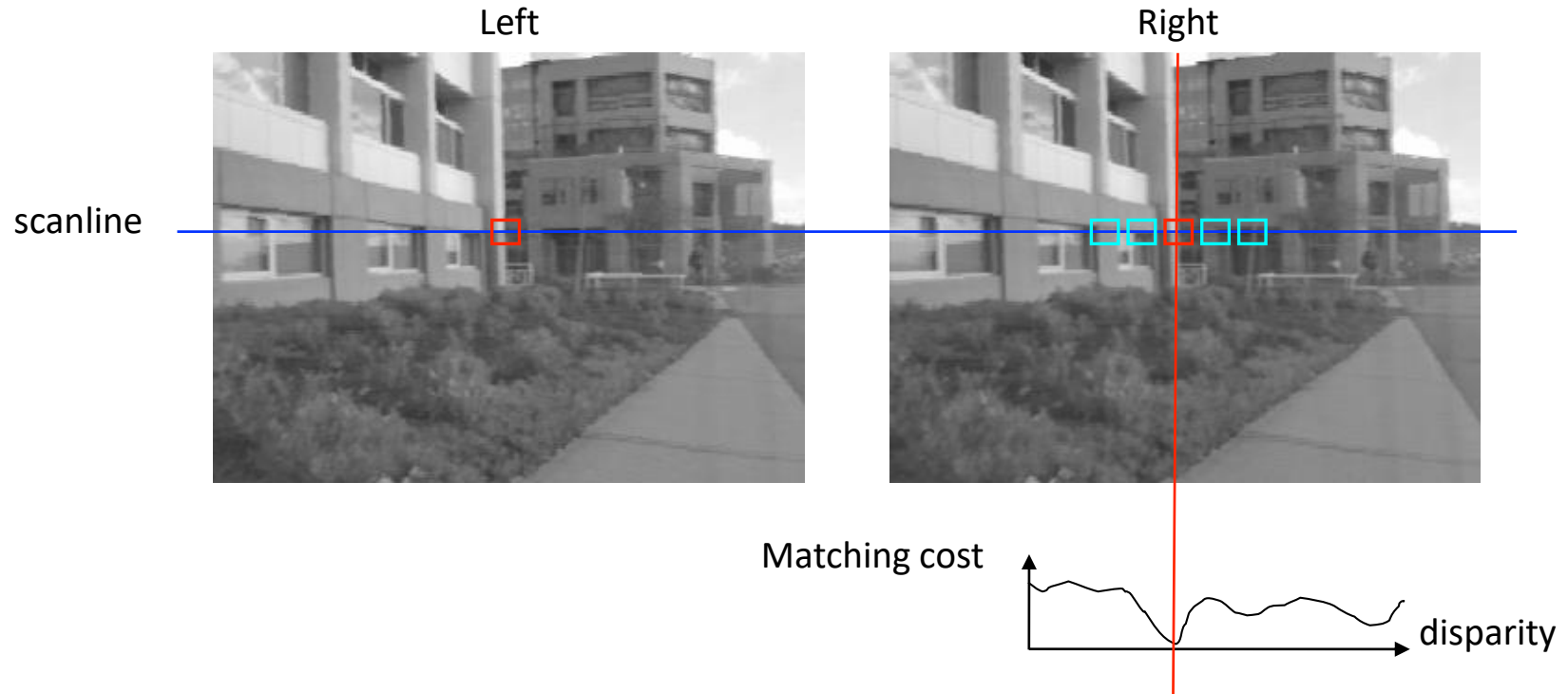
- reproject image planes onto a common
- plane parallel to the line between optical centers
- pixel motion is horizontal after this transformation
- two homographies (3x3 transform), one for each input image reprojection

➤ C. Loop and Z. Zhang. [Computing Rectifying Homographies for Stereo Vision](#). IEEE Conf. Computer Vision and Pattern Recognition, 1999.

Rectification Example

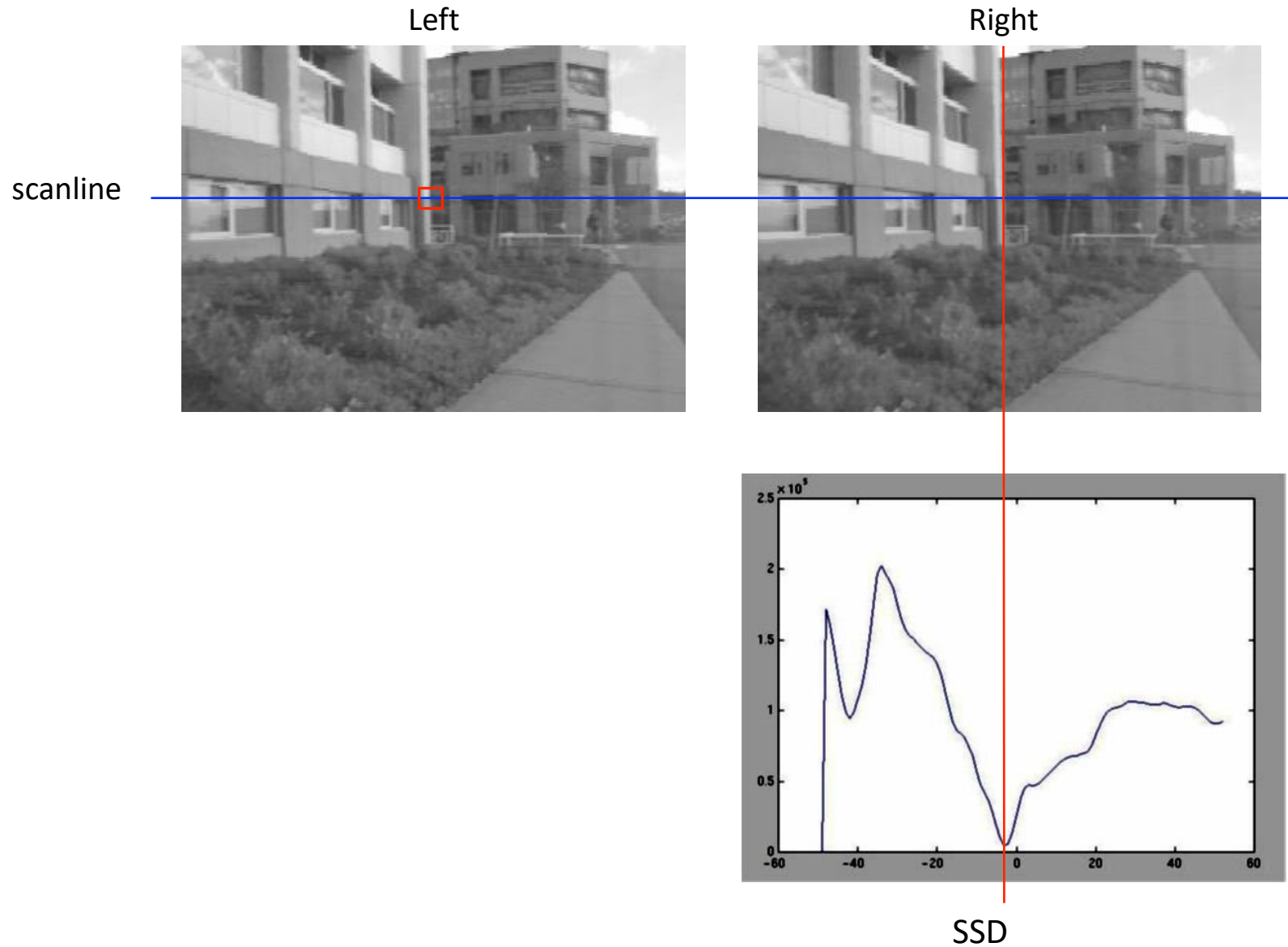


Correspondence search

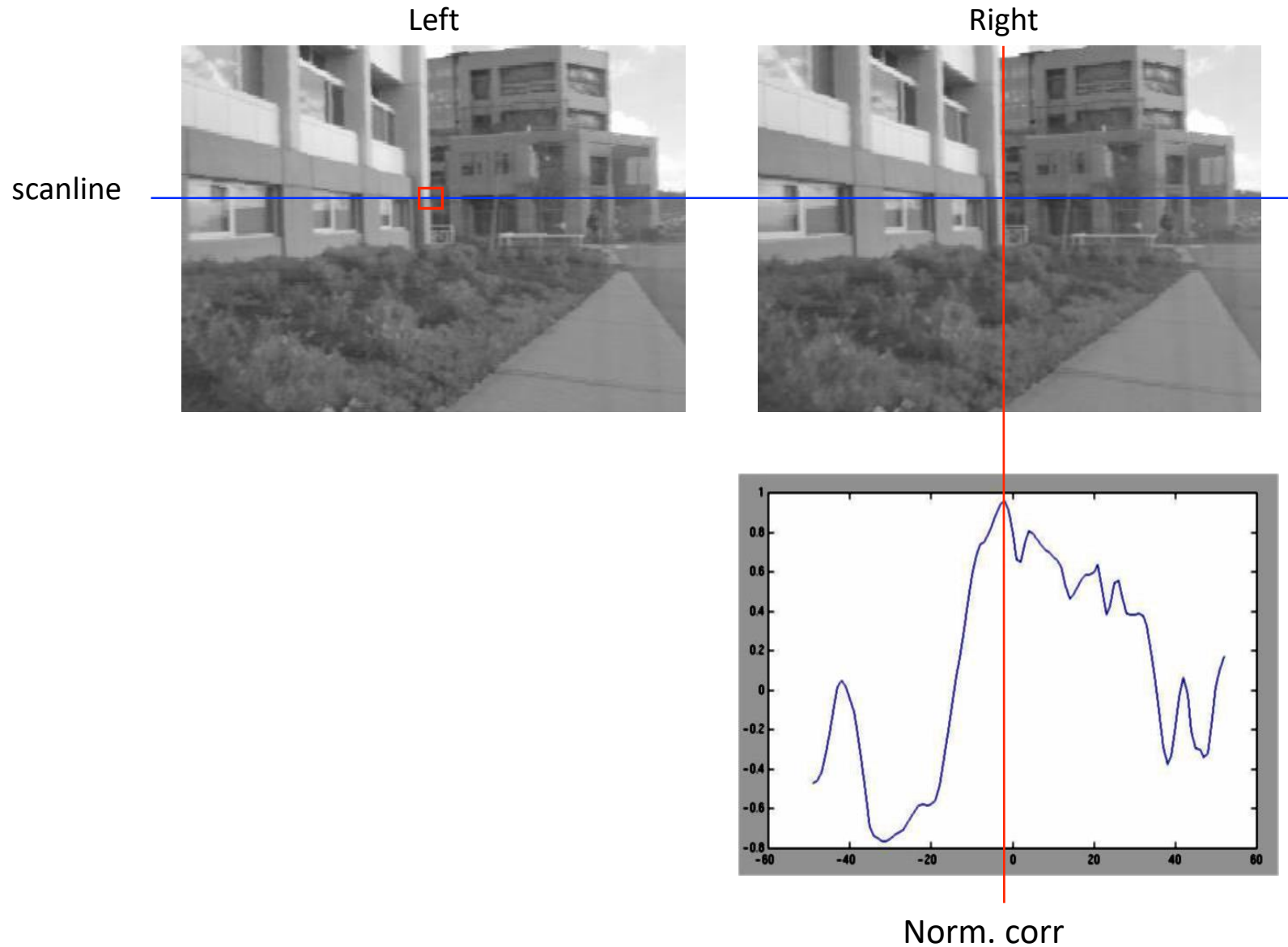


- Slide a window along the right scanline and compare contents of that window with the reference window in the left image
- Matching cost: SSD or normalized correlation

Correspondence search



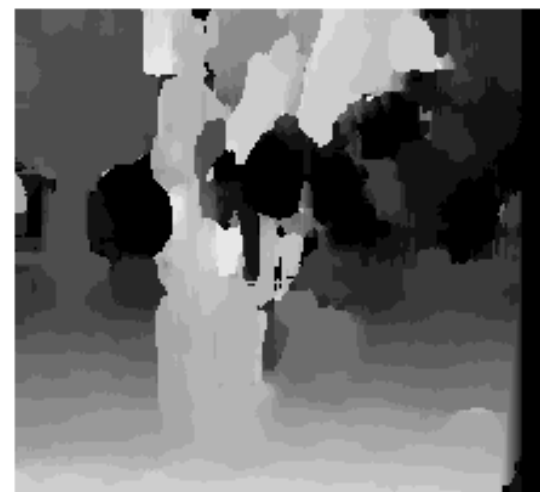
Correspondence search



Effect of window size



$W = 3$



$W = 20$

– Smaller window

+ More detail

– More noise

– Larger window

+ Smoother disparity maps

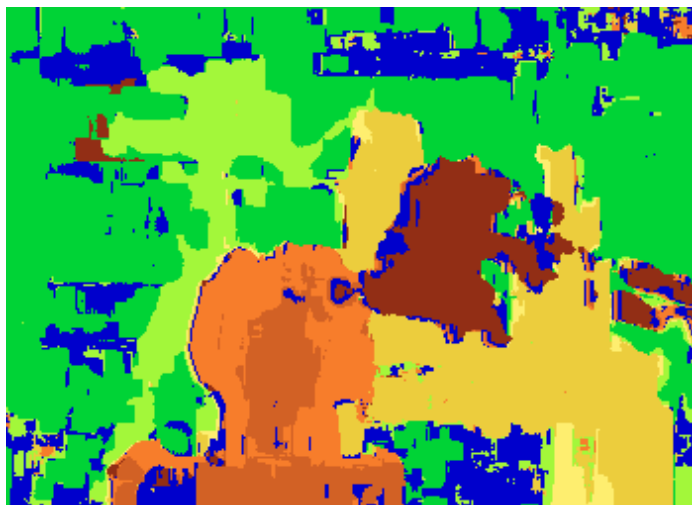
– Less detail

Results with window search

Data



Window-based matching

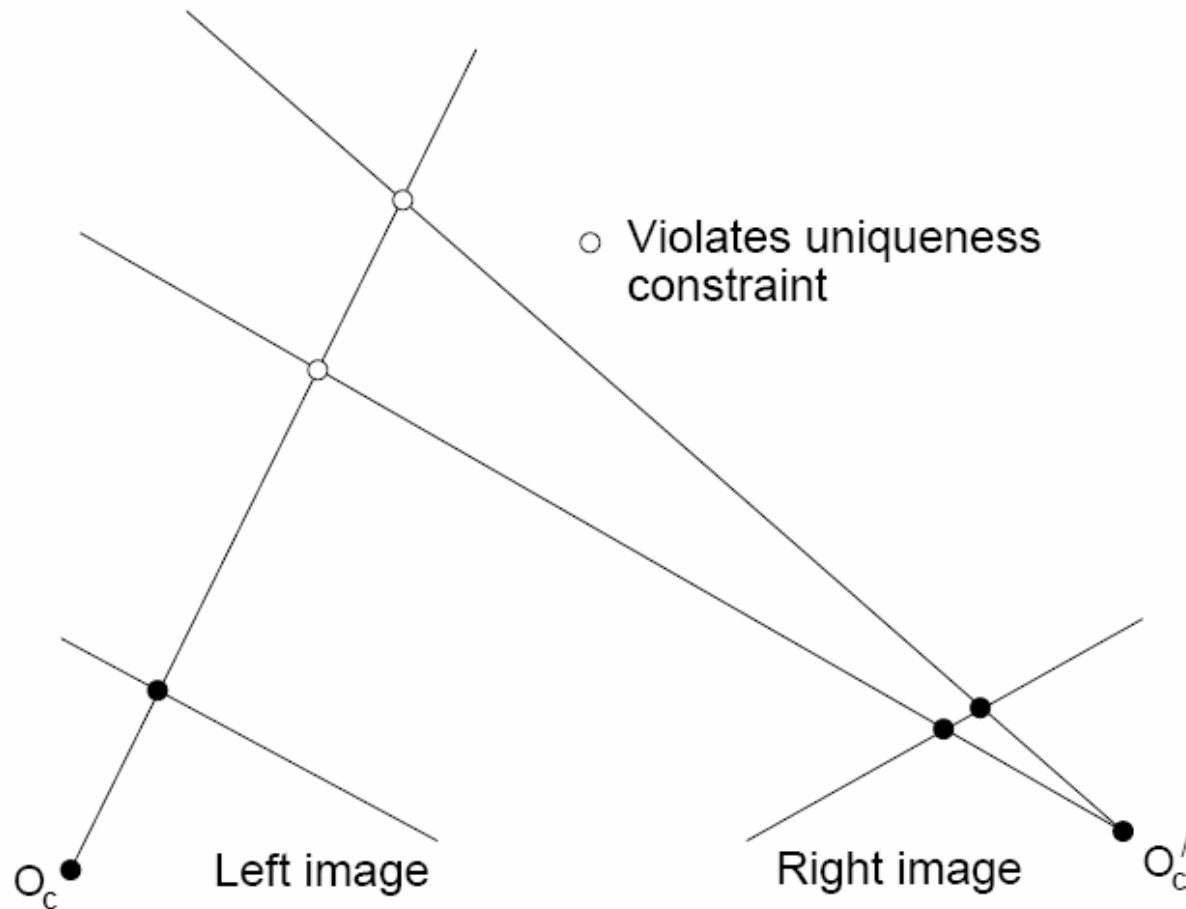


Ground truth



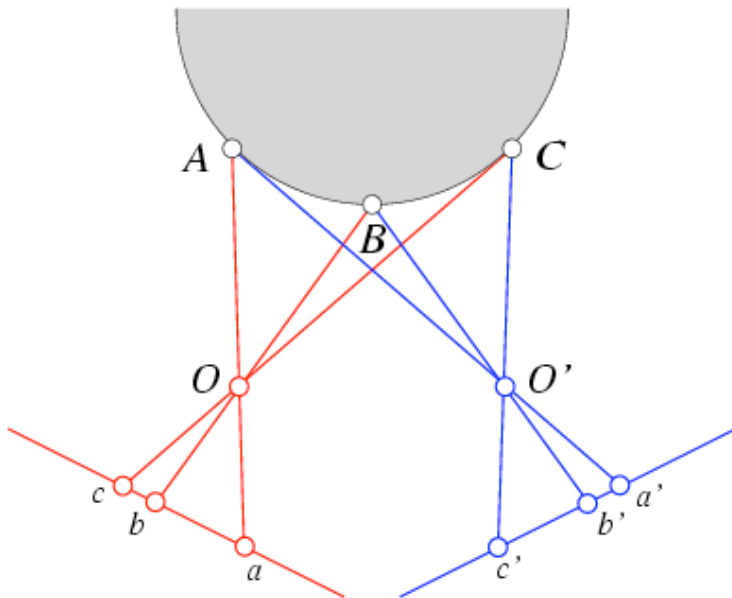
Non-local constraints

- Uniqueness
 - For any point in one image, there should be at most one matching point in the other image



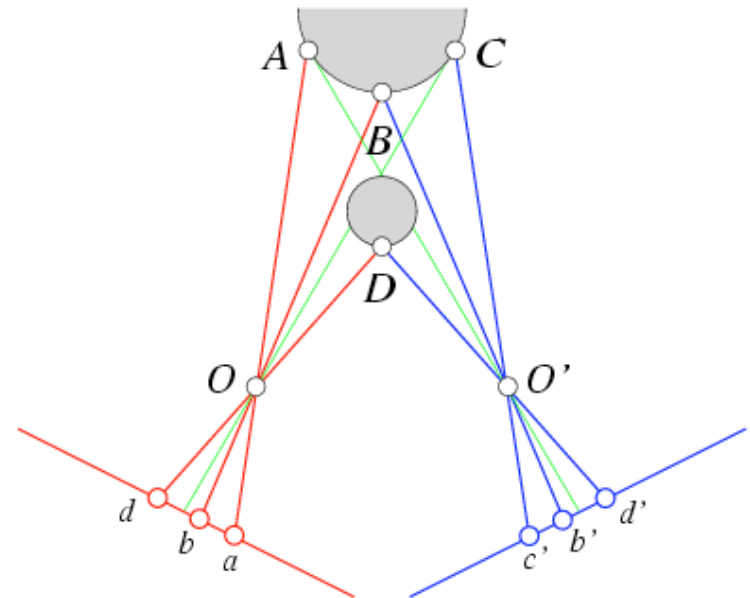
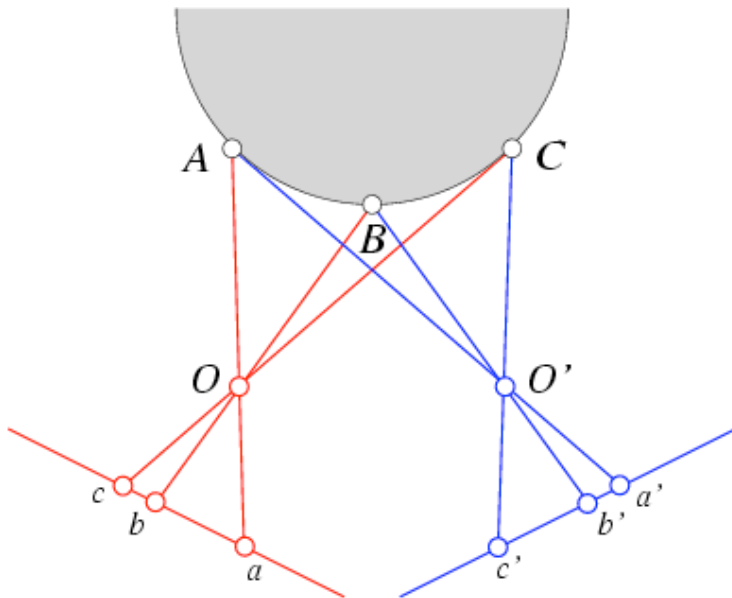
Non-local constraints

- Uniqueness
 - For any point in one image, there should be at most one matching point in the other image
- Ordering
 - Corresponding points should be in the same order in both views



Non-local constraints

- Uniqueness
 - For any point in one image, there should be at most one matching point in the other image
- Ordering
 - Corresponding points should be in the same order in both views



Ordering constraint doesn't hold

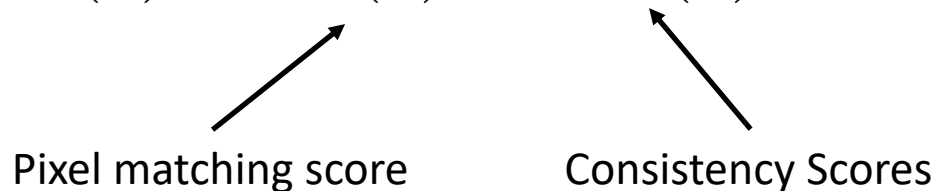
Consistency Constraints

- Uniqueness
 - For any point in one image, there should be at most one matching point in the other image
- Ordering
 - Corresponding points should be in the same order in both views
- Smoothness
 - We expect disparity values to change slowly (for the most part)

MRF Formulation:

$$E(d) = E_d(d) + \lambda E_s(d)$$

Pixel matching score

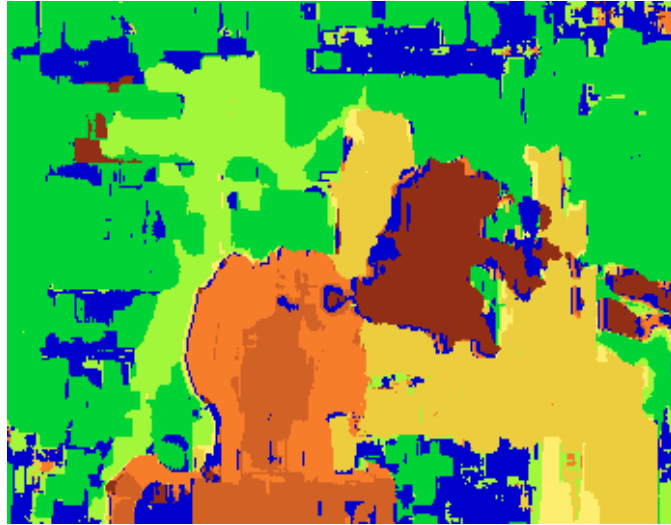


The diagram shows the equation $E(d) = E_d(d) + \lambda E_s(d)$ with two arrows pointing upwards from the labels below to the terms in the equation. One arrow points from 'Pixel matching score' to $E_d(d)$, and the other points from 'Consistency Scores' to $\lambda E_s(d)$.

Consistency Scores

Comparision

Window-Based
Search:

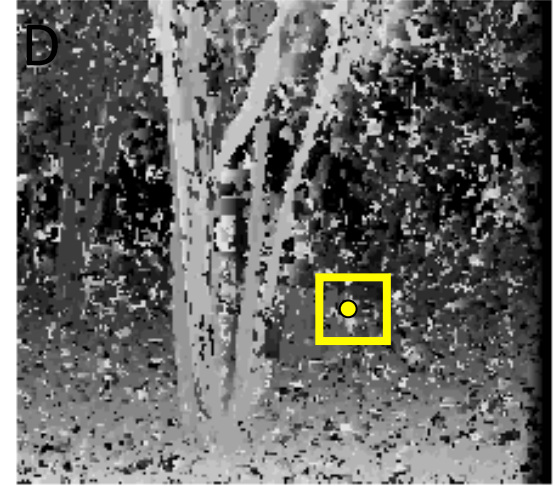
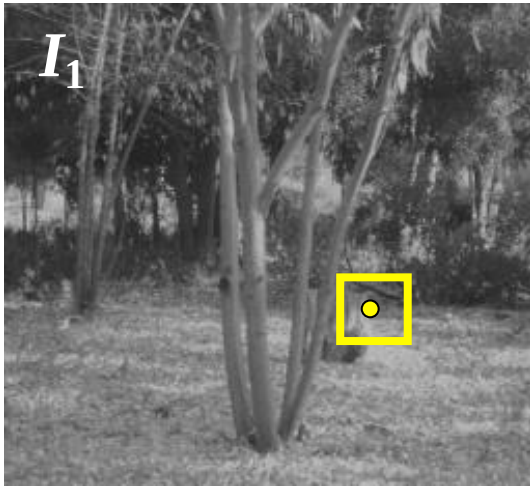


Graph Cut:



Ground Truth

Stereo matching as energy minimization



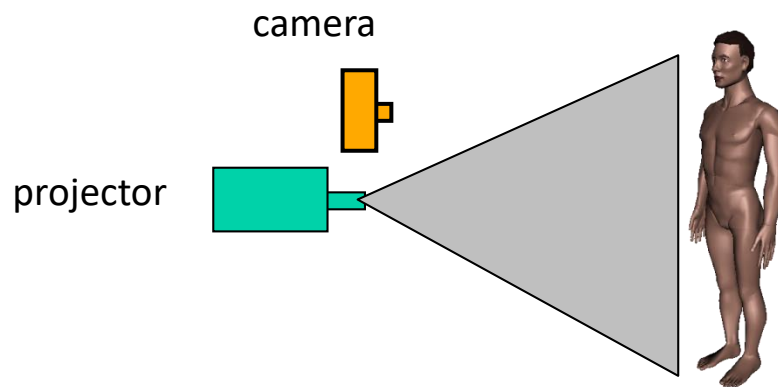
- Graph-cuts can be used to minimize such energy

Y. Boykov, O. Veksler, and R. Zabih, [Fast Approximate Energy Minimization via Graph Cuts](#), PAMI 2001

Active stereo with structured light



- Project “structured” light patterns onto the object
 - Simplifies the correspondence problem
 - Allows us to use only one camera



Kinect: Structured infrared light

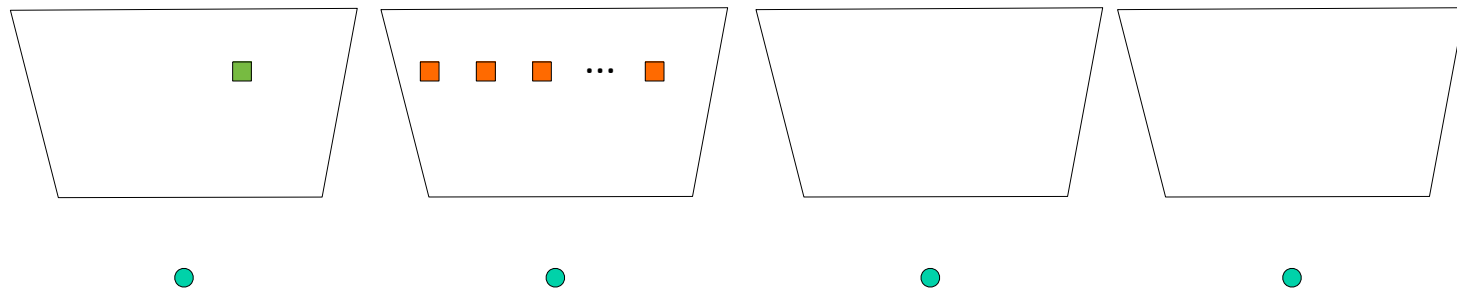


<http://bbzippo.wordpress.com/2010/11/28/kinect-in-infrared/>

Multi-Baseline Stereo

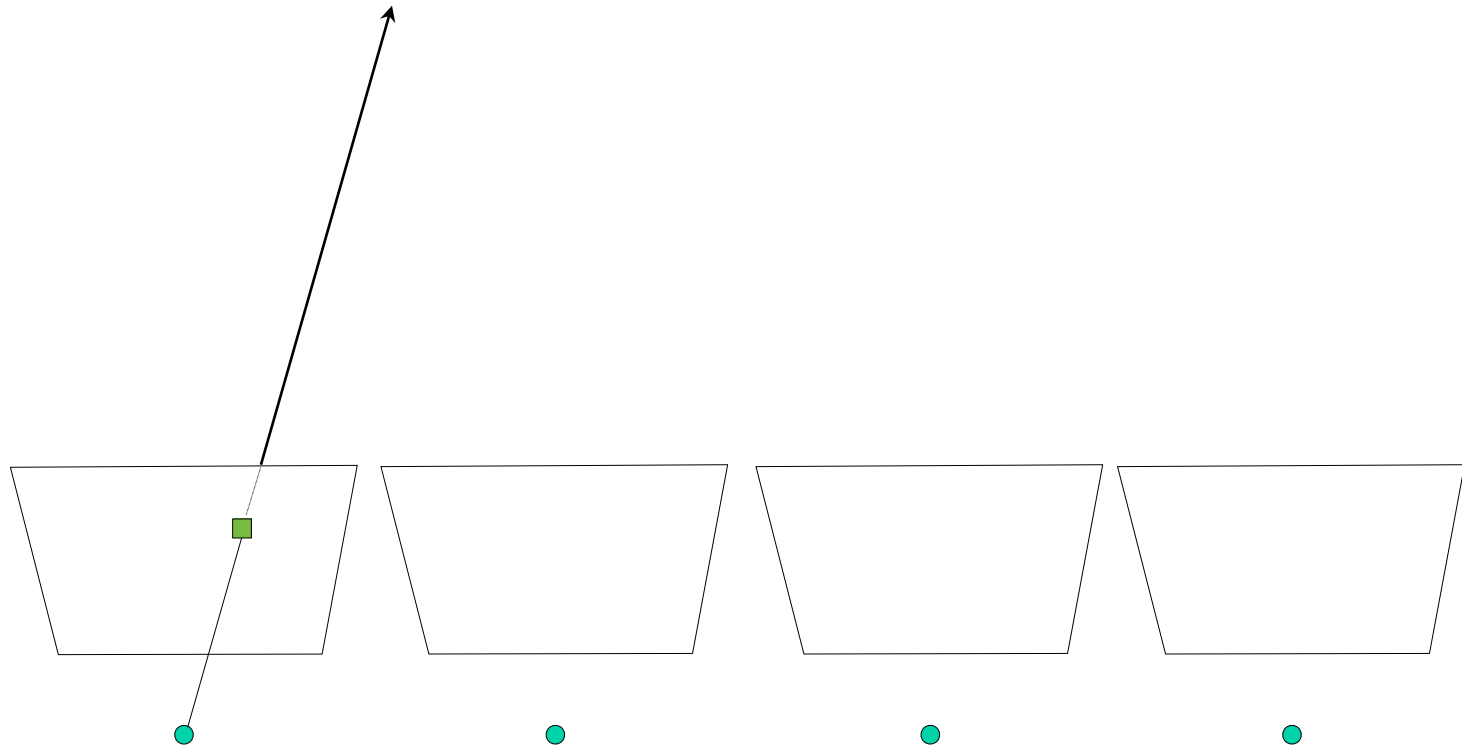
Same formulation with more images

- Change label from disparity to depth
- Change $E_d(d)$ by using more images



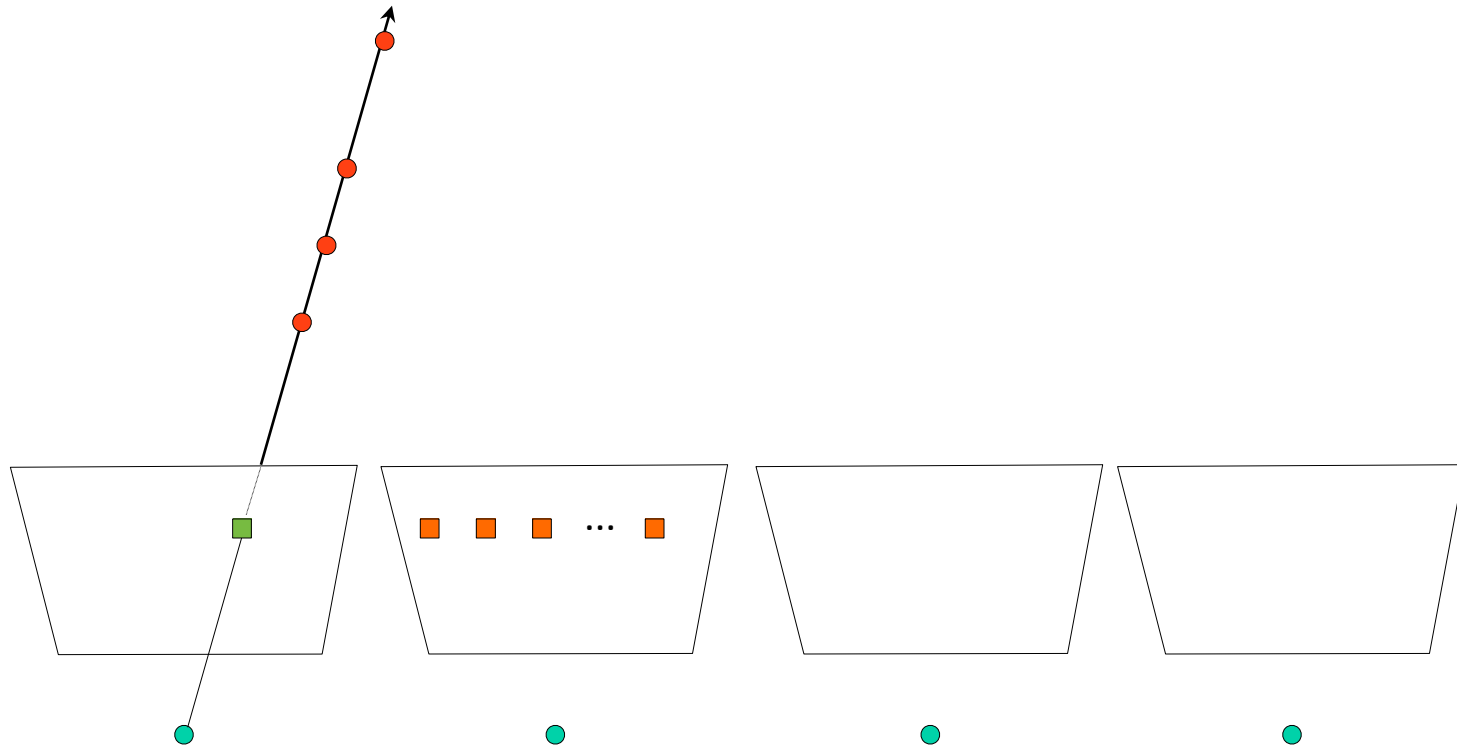
Same formulation with more images

- Change label from disparity to depth
- Change $E_d(d)$ by using more images



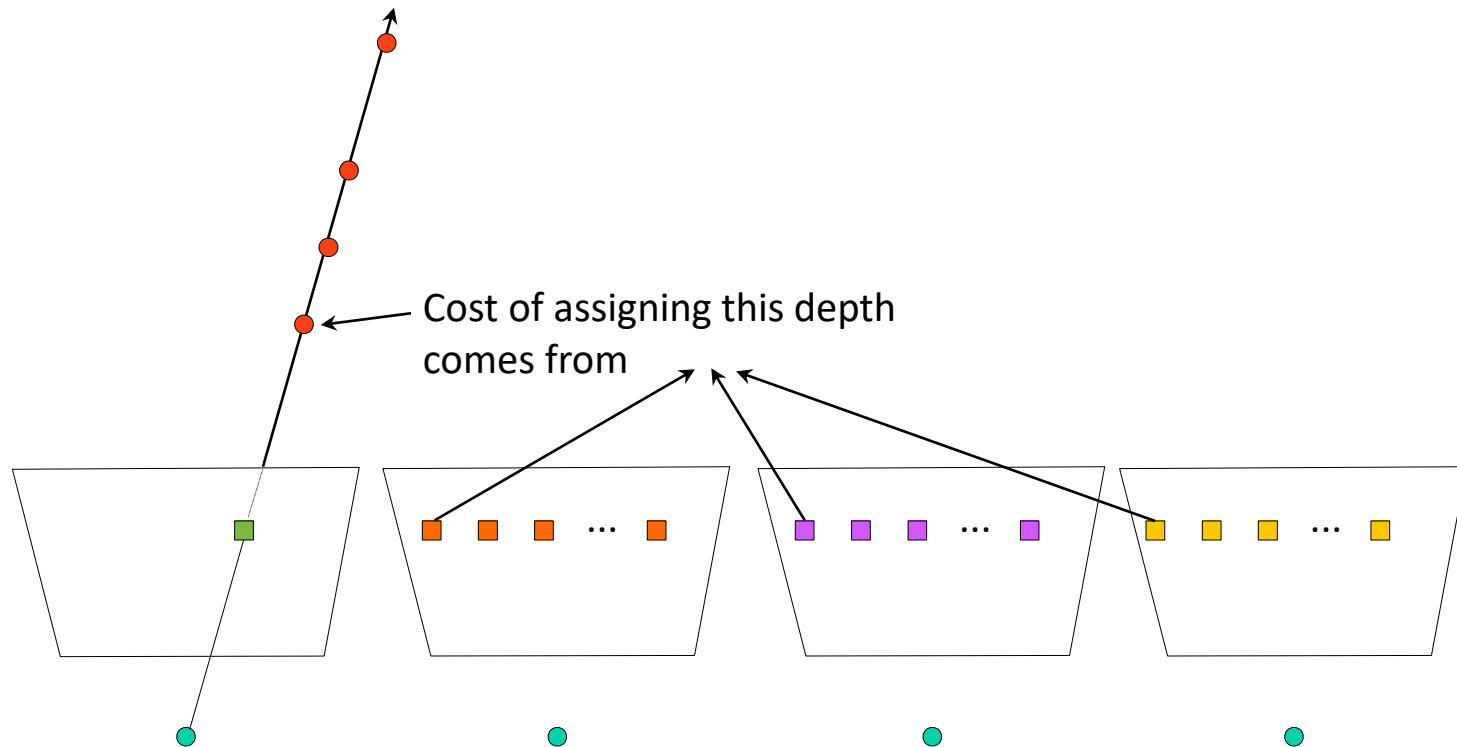
Same formulation with more images

- Change label from disparity to depth
- Change $E_d(d)$ by using more images

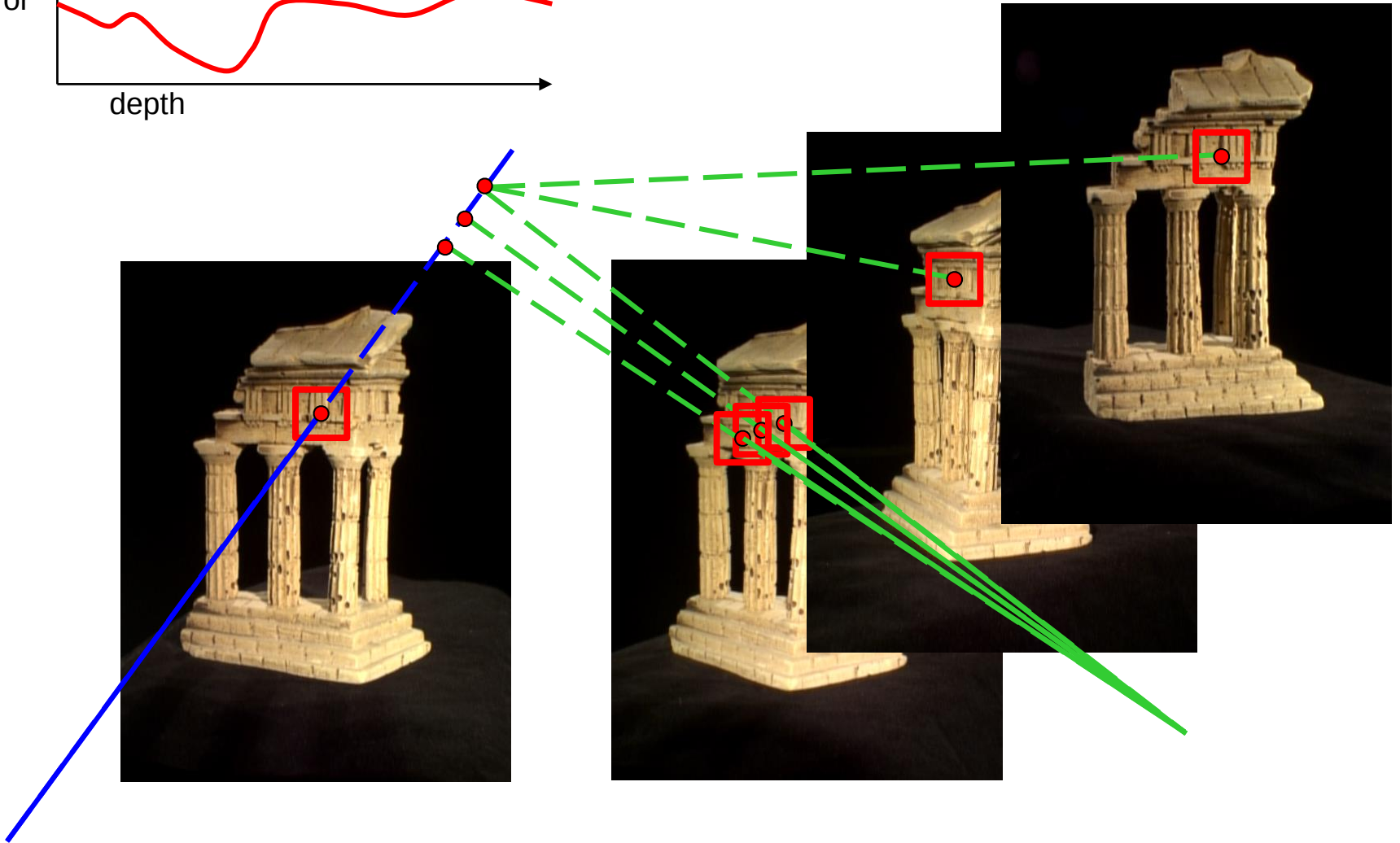
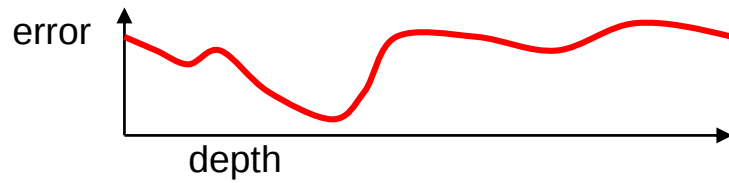


Same formulation with more images

- Change label from disparity to depth
- Change $E_d(d)$ by using more images

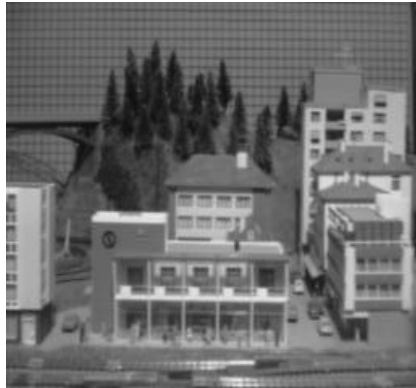


Stereo: Basic Idea



Multiple-Baseline Stereo Results

[Okutomi and Kanade' 93]



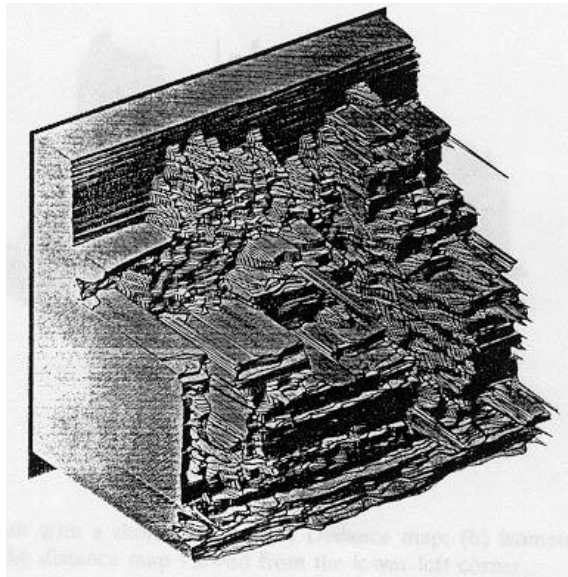
I1



I2



I10



Mesh Reconstruction

Merging Depth Maps

vrip [Curless and Levoy 1996]

- compute weighted average of depth maps

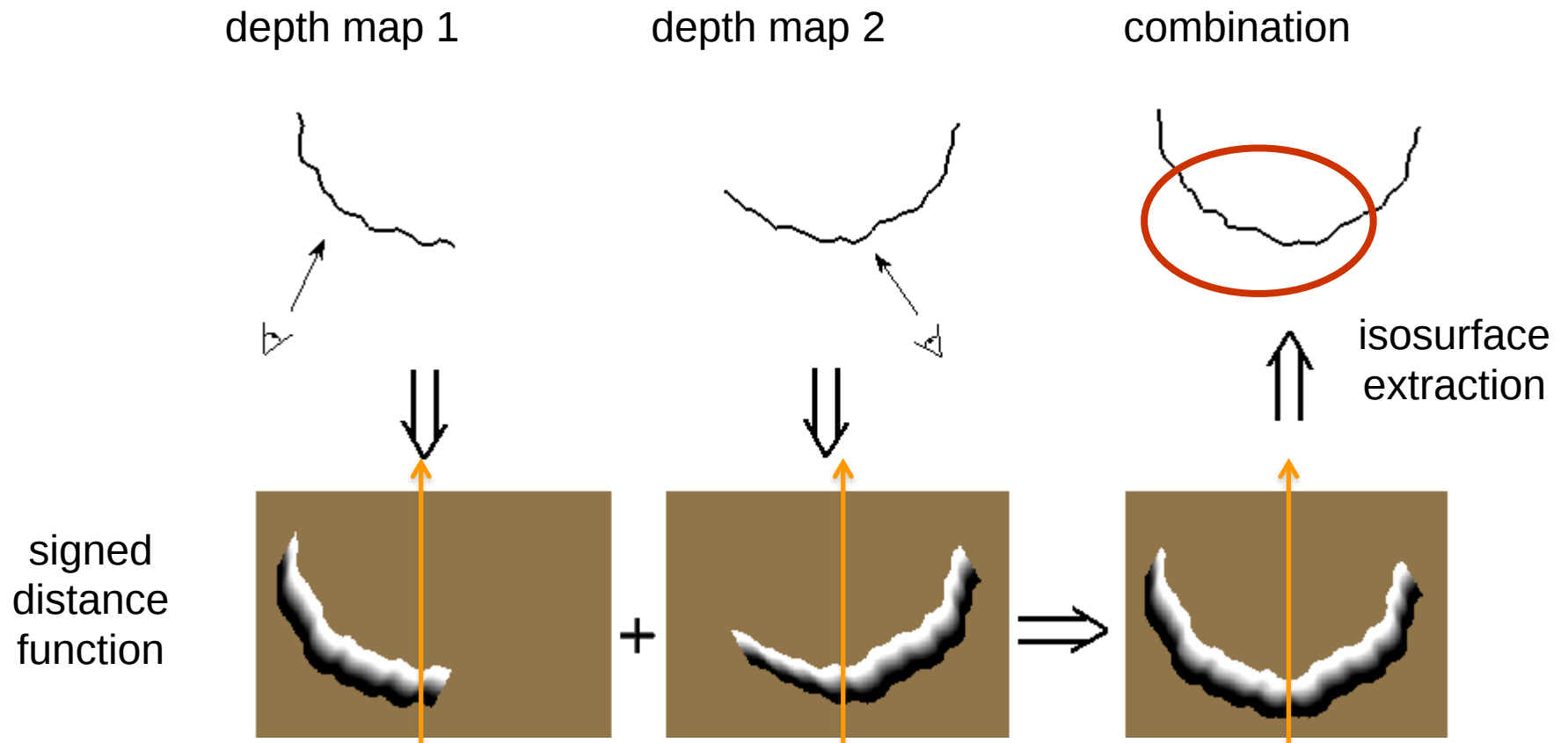


set of depth maps
(one per view)



merged surface
mesh

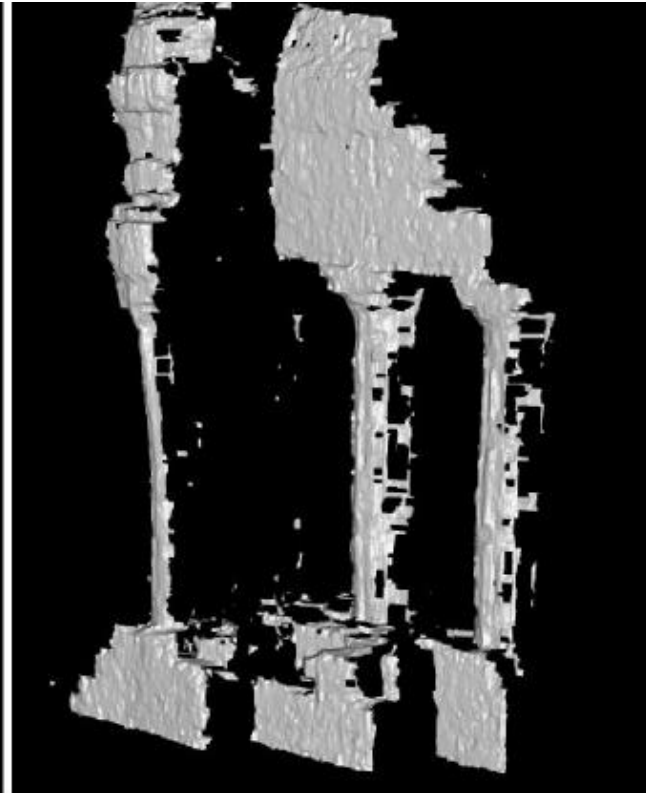
VRIP



Depthmap Merging

Depthmap 1

Depthmap 2



Merging Depth Maps: Temple Model

[Goesele et al. 06]



input image



317 images
(hemisphere)

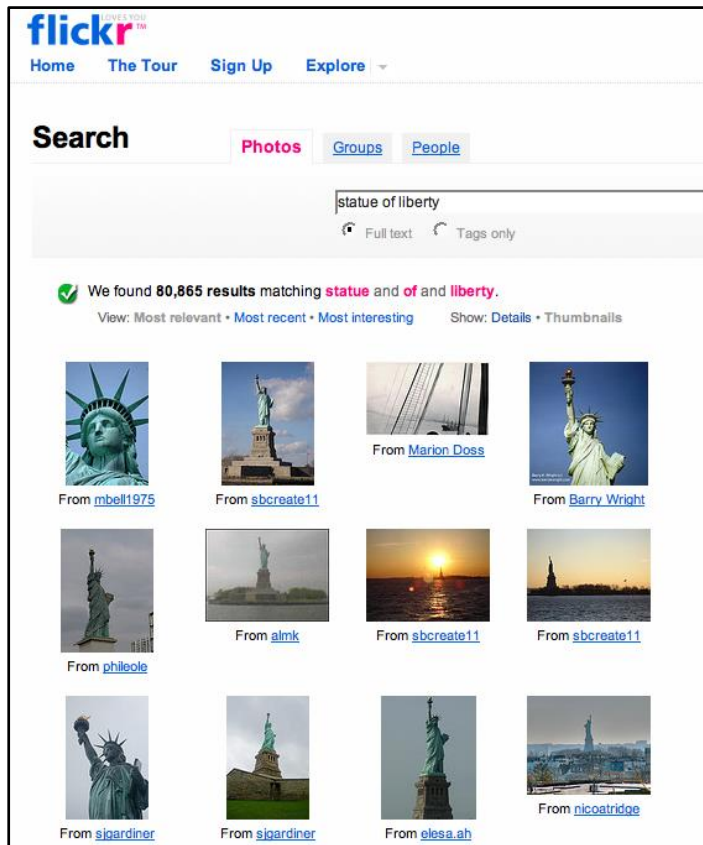


ground truth model

State-of-The-Art

Multi-View Stereo from Internet Collections

[Goesele et al. 07]



Challenges

- Appearance variation



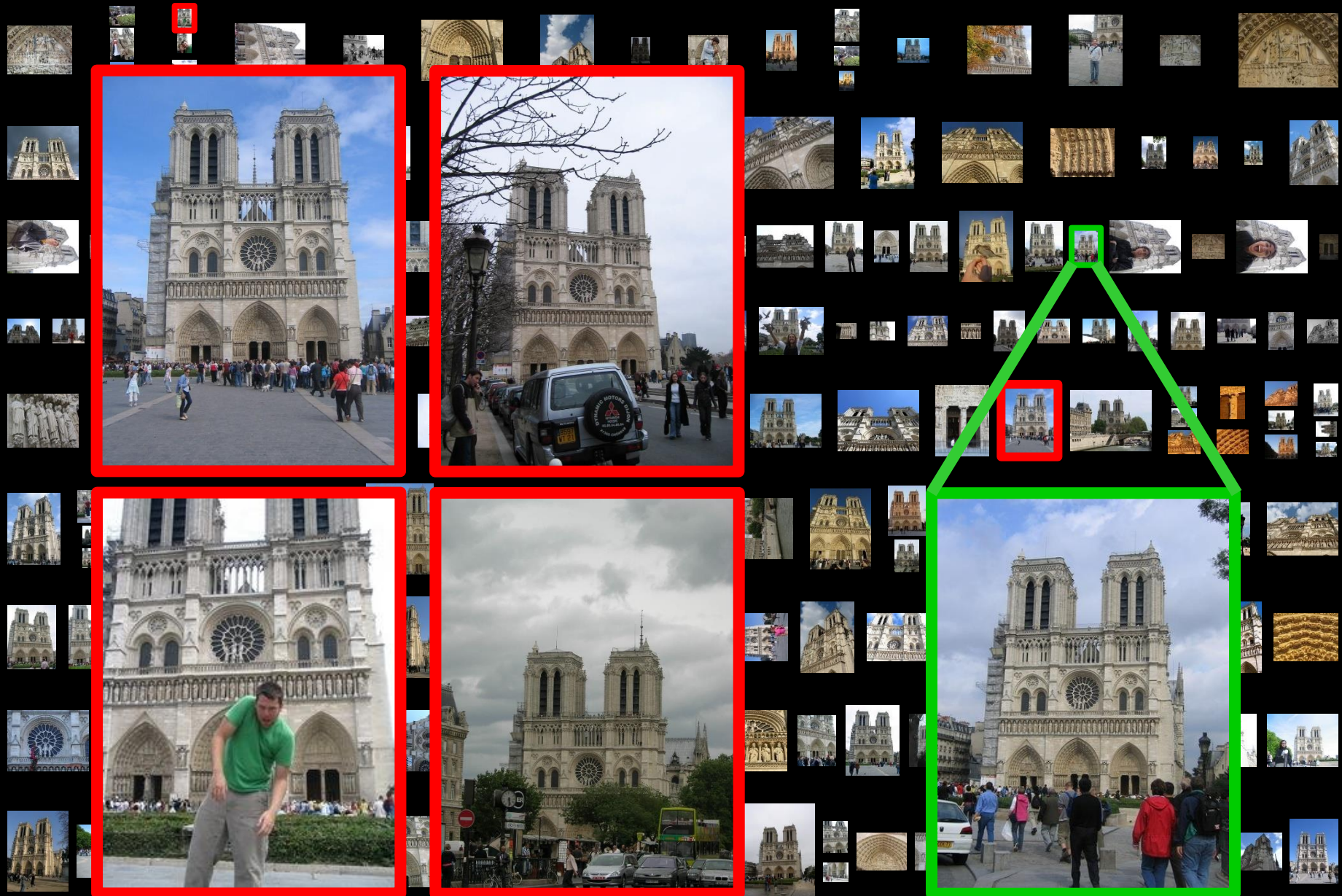
- Resolution



- Massive collections

82754 results for photos matching **notre** and **dame** and **paris**

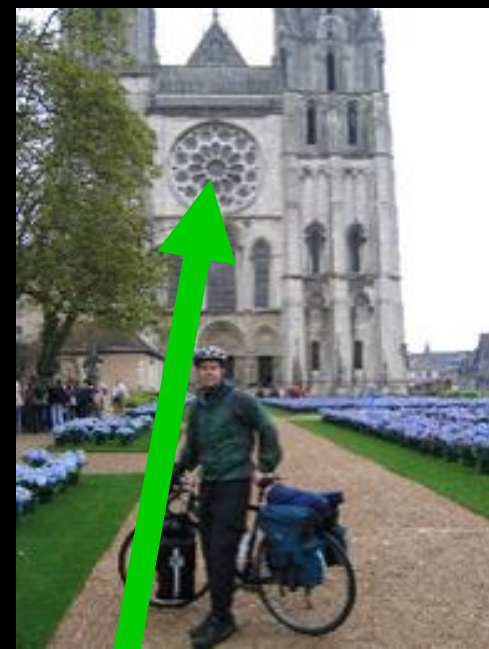
Law of Nearest Neighbors



206 Flickr images taken by 92 photographers



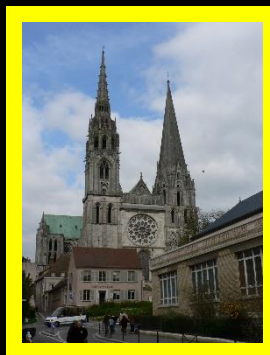
4 best neighboring views



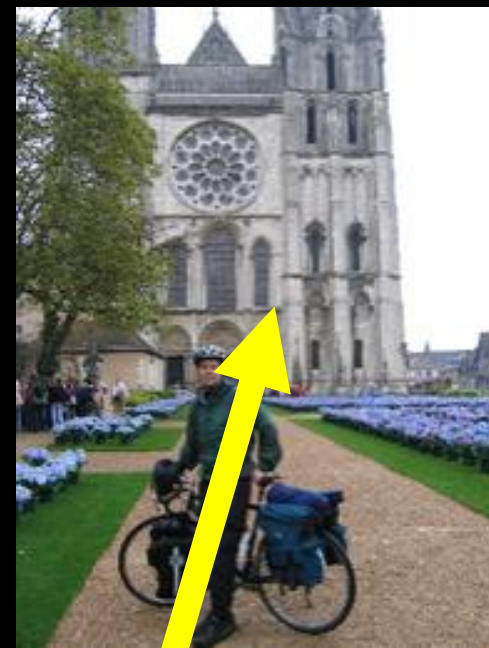
reference view

Local view selection

- Automatically select neighboring views for each **point** in the image
- Desiderata: good matches AND good baselines



4 best neighboring views



reference view

Local view selection

- Automatically select neighboring views for each **point** in the image
- Desiderata: good matches AND good baselines



4 best neighboring views



reference view

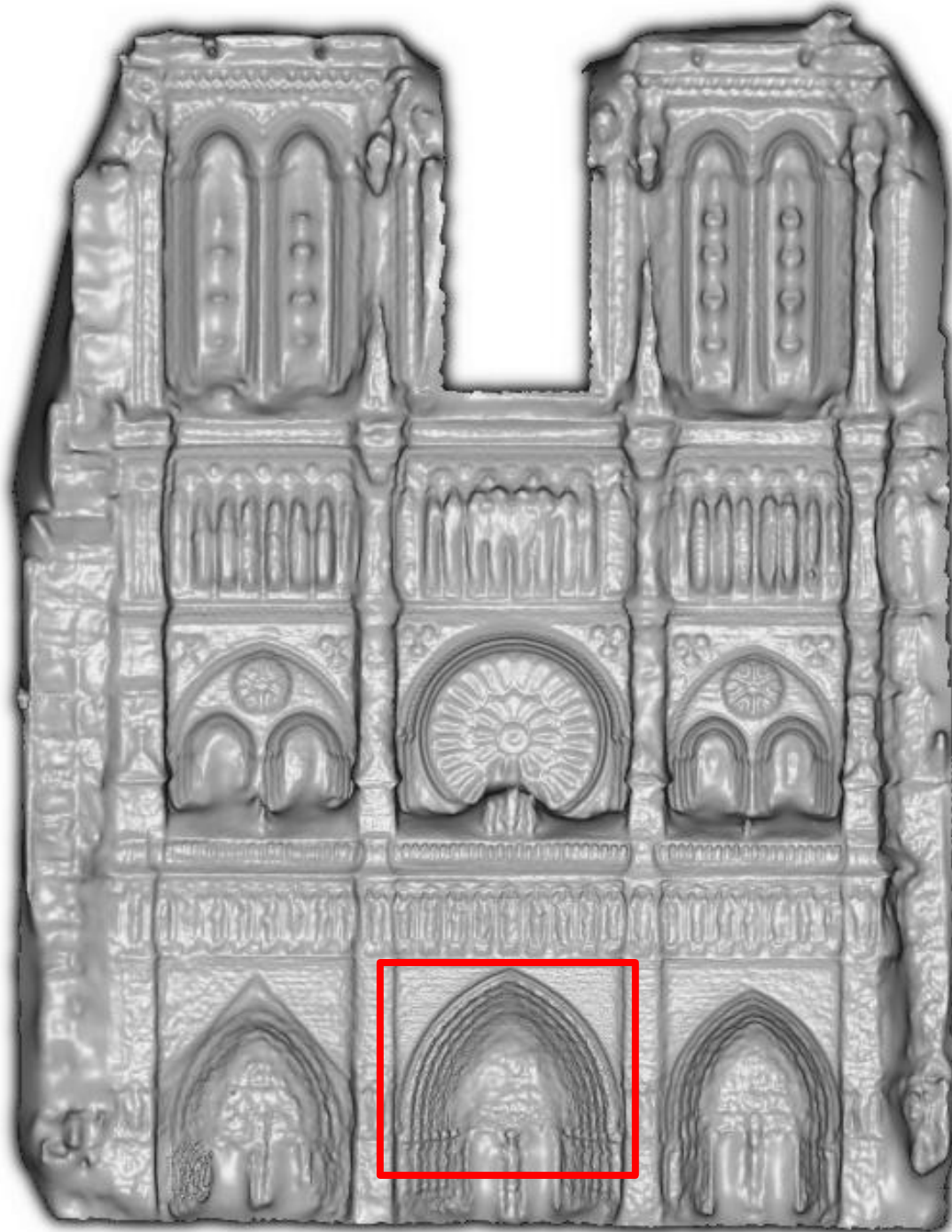
Local view selection

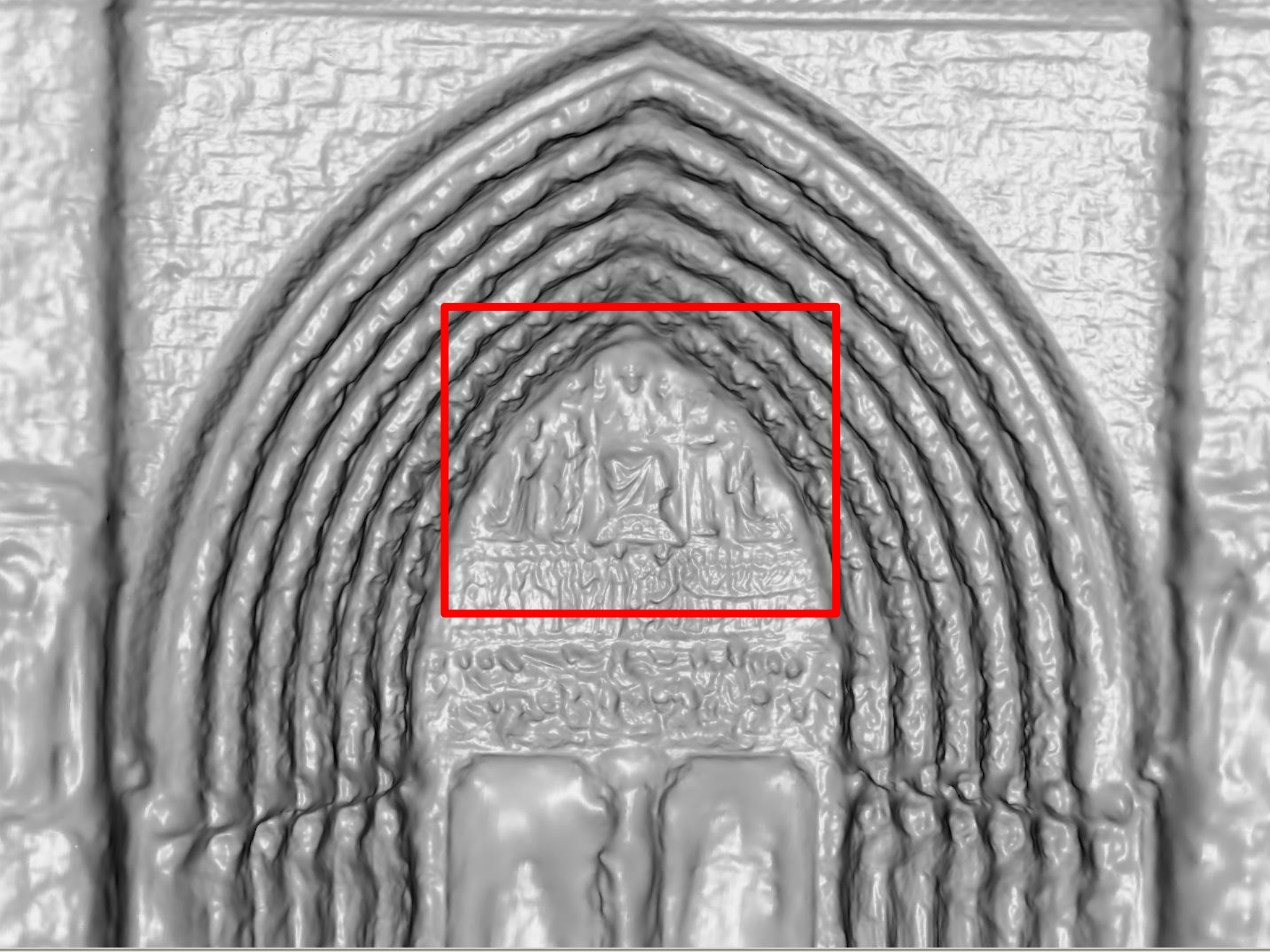
- Automatically select neighboring views for each **point** in the image
- Desiderata: good matches AND good baselines

Notre Dame de Paris

653 images

313 photographers



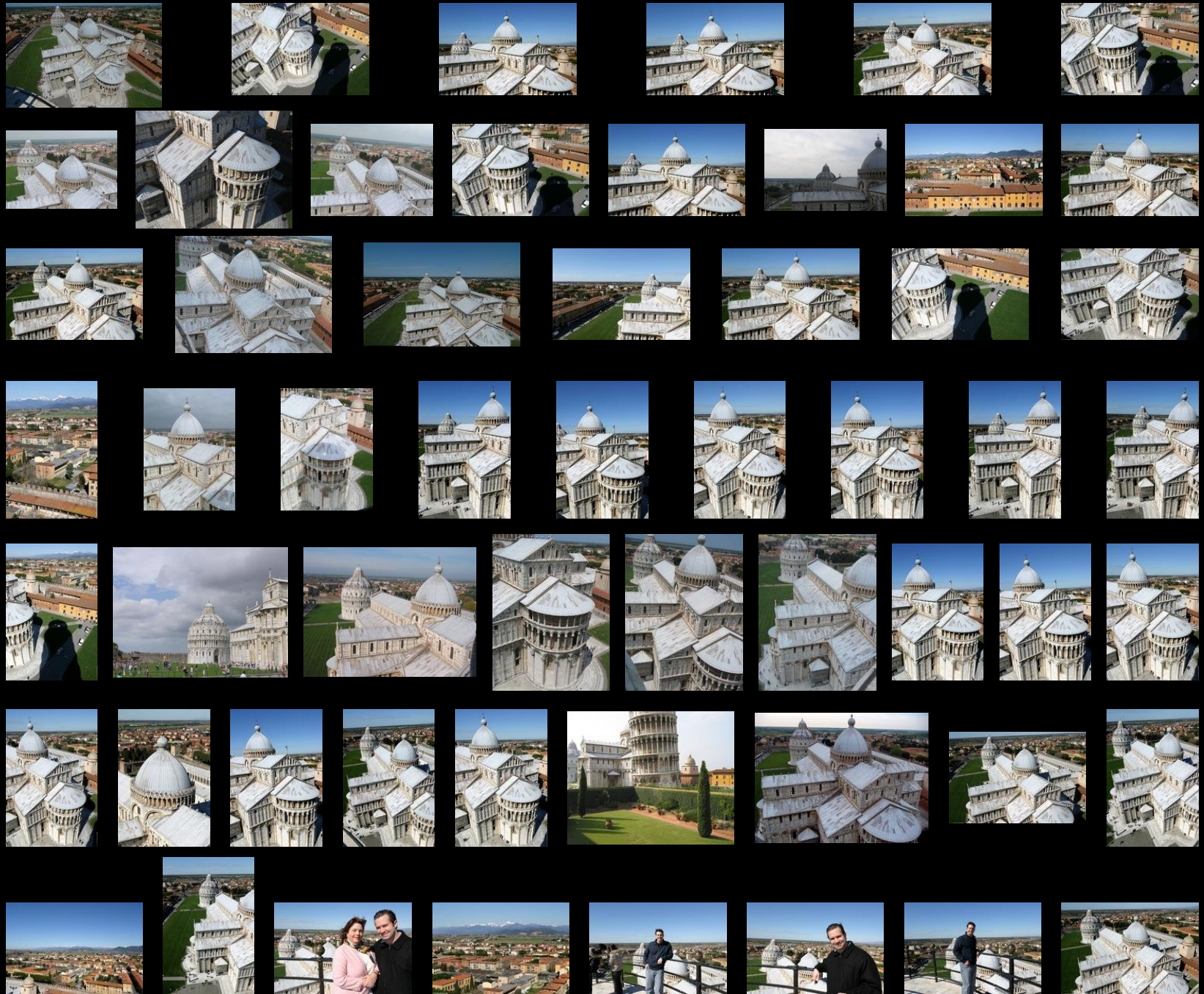




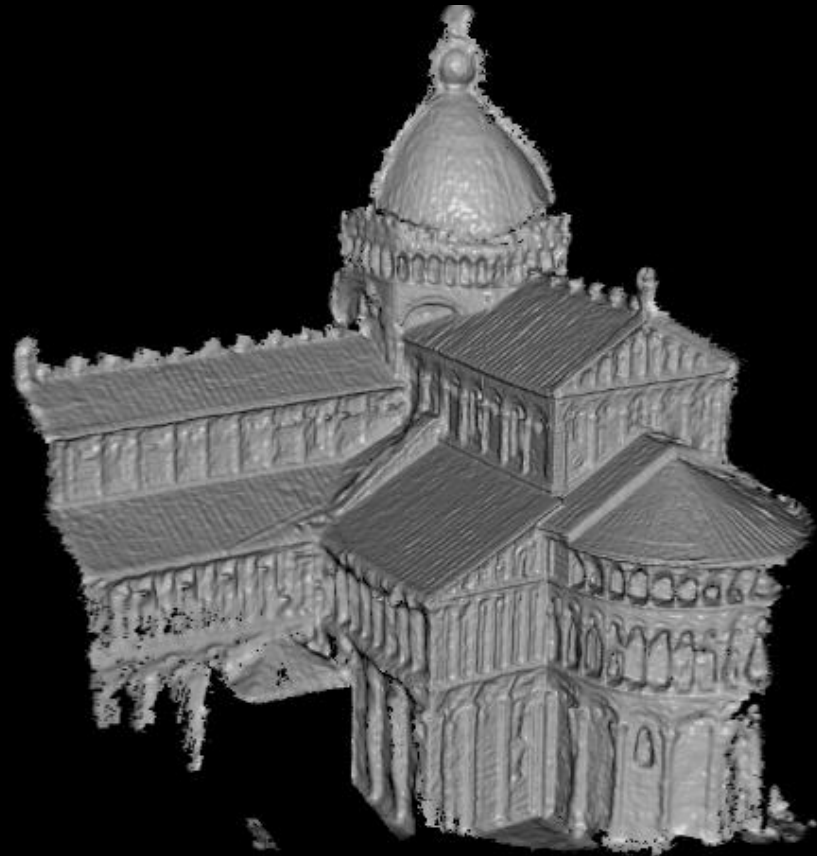
129 *Flickr* images taken by 98 photographers



merged model of Venus de Milo



56 *Flickr* images taken by 8 photographers



merged model of Pisa Cathedral



Accuracy compared to laser scanned model:
90% of points within 0.25% of ground truth

How can Deep Learning Help?