

# **The Y86 – A Technology Driver**

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# Outline

- 1 Technology Driver: The Y86
- 2 Y86 Processor Modeling
- 3 Y86 Processor Modeling – NOP
- 4 Y86 Processor Modeling – Ra + Rb
- 5 Y86 Processor Modeling – POP
- 6 Popcount Specification
- 7 Popcount Program
- 8 Popcount Program Proof Request
- 9 Fibonacci Specification
- 10 Fibonacci Program
- 11 Main Y86 Program, Used to Call FIB
- 12 Fibonacci Program Step Count
- 13 Fibonacci Initial State
- 14 Y86 Poised to Execute FIB
- 15 Minimum Requirement to Execute FIB
- 16 Fibonacci Proof Statement
- 17 Conclusion

# Introduction

Attempting to develop a machine-code verification environment.

- We are developing ISA models suitable for code analysis.
- We are developing a proof environment for ISA code.
- Our work is based on commercial-sized problems.

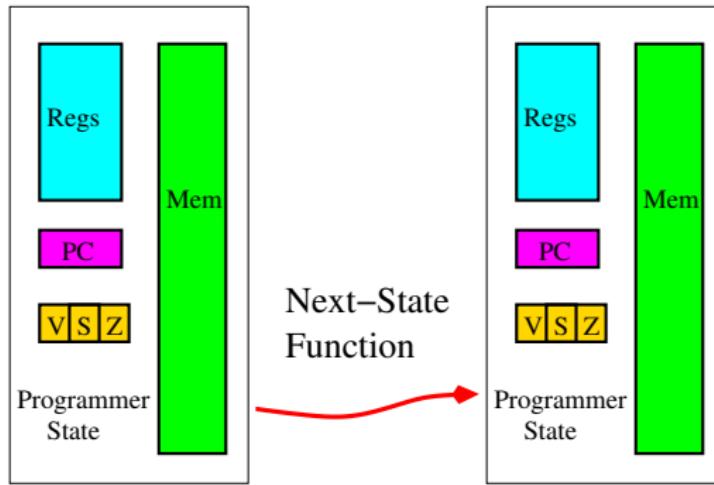
Overall goals:

- Accurate simulation environment for binary code investigation.
- First stage: ability to run FreeBSD/Linux binaries.
- Second stage: ability to boot and run FreeBSD/Linux.
- Provide code analysis capabilities for X86-based systems.

# Technology Driver: The Y86

We use our Y86 model as a technology driver.

- Our Y86 model is used by 100+ students in my architecture class
- We are using it as a basis for our hypervisor study project
- We are using it to develop various microprocessor memory models



# Y86 Processor Modeling

```
(defund y86 (x86-32 n)
  (declare (xargs :guard (and (natp n)
                               (x86-32p x86-32)))
           :measure (acl2-count n)))
  (if (mbe :logic (zp n) :exec (= n 0))
      x86-32
      (if (ms x86-32)
          x86-32
          (let ((x86-32 (y86-step x86-32)))
            (y86 x86-32 (1- n))))))
```

# Y86 Processor Modeling – NOP

```
(defund y86-nop (x86-32)
  (b* ((pc (eip x86-32))

    ;; Memory Probe
    ((if (< *2^32-2* pc))
     (update-ms (list :at-location pc
                      :instruction 'nop
                      :memory-probe nil)
                x86-32))

    ;; Update PC
    (x86-32 (update-eip (+ pc 1) x86-32)))
  x86-32))
```

# Y86 Processor Modeling – Ra + Rb

```
(defund y86-rA-+-rB-to-rB (x86-32)
  (b*
    (;; Get program counter
     (pc (eip x86-32))
     ;; Memory Probe
     ((if (< *2^32-3* pc))
      (update-ms
       (list :at-location pc
             :instruction 'addl
             :memory-probe nil) x86-32)))
    ;; Decode registers
    (rA-rB (rm08 (+ pc 1) x86-32))
    (rB (n03 rA-rB))
    (rA (n03 (ash rA-rB -4)))
    (b3 (n01 (ash rA-rB -3)))
    (b7 (n01 (ash rA-rB -7)))
    ;; Register decoding problem?
    ((if (= (logior b3 b7) 1))
     (update-ms
      (list :at-location pc
            :instruction 'addl
            :b7 b7 :b3 b3
            :ra rA :rb rB) x86-32)))
    ;; Get register values
    (rA-val (rgfi rA x86-32))
    (rB-val (rgfi rB x86-32))
    ;; Calculate result
    (result (n32+ rA-val rB-val))
    ;; Calculate flags
    (zf (if (= result 0) 1 0))
    (sfr (< result (expt 2 31)))
    (sf (if sfr 0 1))
    (sfa (< rA-val (expt 2 31)))
    (sfb (< rB-val (expt 2 31)))
    (of (if (eq sfa sfb)
           (if (eq sfr sfa) 0 1)
           0))
    ;; Store results
    (x86-32 (update-rgfi rB result x86-32))
    (x86-32 (y86-ALU-results-store-flgs
              zf sf of x86-32))
    ;; Update PC
    (x86-32 (update-eip (+ pc 2) x86-32)))
    x86-32))
```

# Y86 Processor Modeling – POP

```
(defund y86-popl (x86-32)
  (b* ;; Memory probe and decoding check removed!!!
    ((pc (eip x86-32))

     ;; Decode registers
     (rA-rB (rm08 (+ pc 1) x86-32))
     (rA (n03 (ash rA-rB -4)))
     (b3-b0 (n04 rA-rB))
     (b7 (n01 (ash rA-rB -7)))

     ;; Ordering is critical when :esp is
     ;; target, if POPL needs to overwrite
     ;; the contents of the :esp register.
     (esp (rgfi *mr-esp* x86-32))
     (esp+4 (n32+ esp 4))
     (MemAtStackPt (rm32 esp x86-32))
     (x86-32 (update-rgfi *mr-esp* esp+4 x86-32))
     (x86-32 (update-rgfi rA MemAtStackPt x86-32))

     ;; Update PC
     (x86-32 (update-eip (+ pc 2) x86-32)))
     x86-32))
```

# Popcount Specification

Lisp has a built-in population count function: LOGCOUNT.

In C, it might look like:

```
int popcount ( int v ) {  
    return (( v == 0 ) ? 0 : (v & 1) + popcount( v / 2 )); }
```

Thus, we would like to verify a similar program.

# Popcount Program

Here is a population count program in Y86 assembler.

```
(defconst *popcount-source*  
  
  ; Register Usage:  
  ;   %eax -- evolving count  
  ;   %ebx -- input argument, which is erased as it is counted  
  ;   %ecx -- tmp  
  ;   %edx -- mask, starts as 1 and is shifted left each iteration  
  ;   %esi -- constant 1  
  
  '(popcount  
  
    ; Subroutine setup  
    (pushl %ebp)           ; 0: Save superior frame pointer  
    (rrmovl %esp %ebp)     ; 2: Set frame pointer  
    (pushl %ebx)           ; 4: Save callee-save register  
    (pushl %esi)           ; 6: Save callee-save register  
  
    (mrmlvl 8(%ebp) %ebx)  ; 8: Get <v>  
    (xordl %eax %eax)      ; 14: %eax <- 0  
    (irmovl 1 %esi)         ; 16: %edx <- 1  
    (rrmovl %esi %edx)      ; 22: %esi <- 1
```

# Popcount Program

loop

```
(rrmovl %ebx %ecx)      ; 24: Evolving <v>
(andl  %edx %ecx)       ; 26: Bit a 1?
(je    move_mask)        ; 28  Jump if bit is zero

(xorl  %edx %ebx)       ; 33: Erase bit just counted
(addl  %esi %eax)        ; 35: Add 1 to the count
```

move\_mask

```
(addl  %edx %edx)        ; 37: Shift mask left
(andl  %ebx %ebx)        ; 39: Anything left to count?
(jne   loop)              ; 41: If so, keep counting
```

popcount\_leave

```
(popl  %esi)              ; 46: Restore callee-save register
(popl  %ebx)              ; 48: Restore callee-save register
(rrmovl %ebp %esp)         ; 50: Restore stack pointer
(popl  %ebp)               ; 52: Restore previous frame pointer
(ret)                      ; 54: Subroutine return
```

# Popcount Program Proof Request

```
(def-gl-thm y86-popcount-correct-reduced-symsim
  :hyp (n32p n)
  :concl (let* ((start-eip (cdr (assoc-eq 'call-popcount
                                             *popcount-symbol-table*)))
                 (halt-eip (cdr (assoc-eq 'halt-of-main
                                             *popcount-symbol-table*))))
                 (esp 8192)
                 (x86-32 (popcount-init-x86-32 n esp start-eip))
                 (count 300)
                 (x86-32 (y86 x86-32 count)))
            (and (equal (rgfi *mr-eax* x86-32)
                        (logcount n))
                 (equal (eip x86-32)
                        halt-eip)))
  :g-bindings
  '((n  (:g-number ,(gl-int 0 1 33)))
    (esp (:g-number ,(gl-int 33 1 33))))
  :rule-classes nil)
```

# Fibonacci Specification

```
(defun fib (x)
  (declare (xargs :guard (natp x)))
  (mbe :logic
        (if (zp x)
            0
            (if (= x 1)
                1
                (+ (fib (- x 2)) (fib (- x 1))))))
        :exec
        (if (< x 2)
            x
            (+ (fib (- x 2)) (fib (- x 1)))))))
```

Aside: ACL2 functions can be memoized.

```
(memoize 'fib :condition '(< 40 x))
```

# Equivalent Function Proof Statement

```
(defun f1 (fx-1 fx n-more)
  (declare (xargs :guard (and (natp fx-1)
                               (natp fx) (natp n-more)))))
  (if (zp n-more)
      fx
      (f1 fx (+ fx-1 fx) (1- n-more)))))

(defun fib2 (x)
  (declare (xargs :guard (natp x)))
  (if (zp x)
      x
      (f1 0 1 (1- x)))))

(defthm fib2-is-fib
  (implies (natp x)
            (equal (fib2 x) (fib x))))
```

# Fibonacci Program

```
(defconst *fib-source*
  '(fib
    ;; Subroutine setup
    (pushl %ebp)           ; 0: Save superior frame pointer
    (rrmovl %esp %ebp)     ; 2: Set frame pointer
    (pushl %ebx)           ; 4: Save callee-save registers on stack
    (pushl %esi)           ; 6:
    (mrmlvl 8(%ebp) %ebx) ; 8: Get <N>

    ;; Zero test
    (xorl %eax %eax)      ; 14: %eax := 0
    (andl %ebx %ebx)       ; 16: Set flags
    (jle fib_leave)        ; 18: Return 0, if <N> <= 0

    ;; One test
    (irmovl 1 %eax)        ; 23: %eax := 1
    (rrmovl %ebx %ecx)     ; 29: %ecx := <N>
    (subl %eax %ecx)       ; 31: %ecx := <N> - 1
    (je fib_leave)         ; 33: Return 1, if <N> == 0
```

# Fibonacci Program

```
; ; Push (- N 1) on stack for recursive FIB call

(pushl %ecx)          ; 38: Push (<N> - 1)
fib-1
(call fib)            ; 40: Recursively call fib(<N> - 1)
(popl %ecx)           ; 45: Restore stack pointer
(rrmovl %eax %esi)   ; 47: Save fib(<N> - 1)

(irmovl 2 %ecx)       ; 49:
(subl %ecx %ebx)     ; 55: <N> - 2

; ; Push (- N 2) on stack for recursive FIB call

(pushl %ebx)          ; 57: Push (<N> - 2)
fib-2
(call fib)            ; 59: Recursively call fib(<N> - 2)
(popl %ecx)           ; 64: Restore stack pointer

(addl %esi %eax)      ; 66: fib(<N> - 2) + fib(<N> - 1)
```

# Fibonacci Program

```
; ; Subroutine leave  
  
fib_leave  
  
(popl    %esi)      ; 68: Restore callee-save register  
(popl    %ebx)      ; 70: Restore callee-save register  
(rrmovl %ebp %esp) ; 72: Restore stack pointer  
(popl    %ebp)      ; 74: Restore previous frame pointer  
(ret)               ; 76: Subroutine return  
  
end-of-code
```

# Main Y86 Program, Used to Call FIB

```
;; Main program

(align 16)          ; 80: Align to 16-byte address
main               ; 80: "main" program
(irmovl stack %esp) ; 80: Initialize stack pointer (%esp)
(rrmovl %esp %ebp) ; 86: Initialize frame pointer (%ebp)
(irmovl 6 %eax)    ; 88: <N>: fibonacci( <N> )

(pushl %eax)        ; 94: Push argument on stack
call-fib
(call fib)          ; 96: Call Fibonacci subroutine
return-from-fib

(popl %ebx)          ; 101: Restore local stack position
(halt)              ; 103: Halt

;; Stack

(pos 8192)          ; 8192: Assemble position
stack               ; 8192: Thus, "stack" has value 8192
))
```

# Fibonacci Program Step Count

```
(defun fib-count (n)
  ; Return the number of steps taken by y86,
  ; starting at a call of FIB and ending just
  ; after corresponding (ret) in the FIB routine.

  (declare (xargs :guard (natp n)
                  :ruler-extenders :all))
  (1+           ; (for the call instr)
  (cond ((zp n) 13)    ; 8 (prelude) + 5 (postlude, to fib_leave)
        ((eql n 1) 17) ; 8 + 4 (extra prelude when N = 1) + 5
        (t (+ 13         ; 8 (prelude)
              (fib-count (- n 1))
              5
              (fib-count (- n 2))
              7)))))
```

# Fibonacci Initial State

```
(defun fib-init-x86-32 (n esp eip)
  ; N is our formal, esp is the stack pointer
  ; just before (call fib), and eip position of
  ; the (call fib) instruction. It's important
  ; that addresses from *fib-binary* don't include
  ; esp, and in fact there's sufficient separation
  ; to let the stack grow as fib is executed
  ; without smashing the fib code.

  (declare (xargs :guard (and (n32p n)
                               (n32p esp)
                               (n32p eip))))
  (init-y86-state nil
    eip
    `(((:esp . ,esp))
      nil
      *fib-binary*
      (wm32 esp n (create-x86-32)) ; n is on the top of the stack
      ))
```

# Y86 Poised to Execute FIB

```
(defun poised-at-fib-n (n x86-32)
  (declare (xargs :guard (and (n32p n) (x86-32p x86-32))))
  (let ((esp (rgfi *mr-esp* x86-32)))
    (and (n32p (+ 3 esp))
         ;; Call has not yet taken place (next step is the call)
         (equal n (rm32 esp x86-32))
         ;; We check that the stack necessary won't overwrite the
         ;; code.  The nesting of calls is at most n, and for each
         ;; stack frame we push four doublewords.
         (<= (cdr (assoc-eq 'end-of-code ; just past the return
                           *fib-symbol-table*))
              (- esp ; subtract max number of bytes to be pushed
                  (fib-stack-max-bytes n)))))

(defun poised-at-fib-base (eip x86-32)
  (declare (xargs :guard (and (x86-32p x86-32) (n32p eip))))
  (and (mem-segment-p *fib-binary* x86-32)
       (equal (eip x86-32) eip)))

(defun poised-at-fib (n eip x86-32)
  (declare (xargs :guard (and (n32p n) (n32p eip) (x86-32p x86-32))))
  (and (poised-at-fib-base eip x86-32)
       (poised-at-fib-n n x86-32)))
```

# Minimum Requirement to Execute FIB

```
(defun reduce-fib (x86-32)
  (declare (xargs :guard (x86-32p x86-32)))
  (let ((esp (rgfi *mr-esp* x86-32)))
    (fib-init-x86-32 (rm32 esp x86-32)
                      esp
                      (cdr (assoc-eq 'call-fib
                                    *fib-symbol-table))))))
```

# Fibonacci Proof Statement

```
(defthm y86-fib-correct-up-to-3-reduced
  (let ((eip (cdr (assoc-eq 'call-fib *fib-symbol-table*)))
        (esp (rgfi *mr-esp* x86-32)))
    (implies (and (natp n)
                  (< n 3)
                  (n32p esp)
                  (n32p (+ esp 3))
                  (f-stack-okp n esp)
                  (x86-32p x86-32)
                  (poised-at-fib n eip x86-32))

                (let* ((x86-32 (reduce-fib x86-32))
                      (x86-32 (y86 x86-32 (fib-count n)))))

                (and (equal (rgfi *mr-eax* x86-32)
                            (fib n))

                      (equal (eip x86-32)
                             (cdr (assoc-eq 'return-from-fib
                                           *fib-symbol-table*)))))))
```

# Conclusion

We continue to expand our modeling and analysis capabilities.

- We are attempting to use our symbolic-simulation capability to verify programs.
- We want to specify a executable subset a commercial ISA that is suitable for analyzing programs.
  - We are building memory models
  - We are developing a co-simulation mechanism for model validation
  - Such a model can be used as a built-to and a compile-to specification
  - Such a model can symbolically execute code
  - Such a model can be used to safely explore all manner of malware
- We wish to take advantage of asynchronous computation where appropriate.

We perform all of our work in an environment where we can prove or disprove theorems about our models.