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## Motivation



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- If answer is yes, program is error-free
- If answer is no, there are two possibilities:



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- If answer is yes, program is error-free
- If answer is no, there are two possibilities:
  - Either the program is indeed buggy
  - Or report is a false alarm

• When verifier fails to prove property, user must decide whether report is real bug or false alarm.



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- When verifier fails to prove property, user must decide whether report is real bug or false alarm.
- But manually classifying error reports is time-consuming and error-prone.
- Furthermore, user must redo all the reasoning the tool performed just to discover where it became stuck.
- Very painful process for most users of static analysis tools!



A new technique for semi-automating error report classification when automated program verification fails

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- Queries capture only the information verifier is missing ⇒ user contributes facts verifier could not decide on its own

A new technique for semi-automating error report classification when automated program verification fails



- Allows verifier to interact with user by asking small, relevant queries until report is classified as real bug or false positive
- Queries capture only the information verifier is missing ⇒ user contributes facts verifier could not decide on its own
- Answering queries much easier than classifying error report

Key Idea #1: Analysis makes explicit not only facts it knows, but also facts it does not know



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Key Idea #1: Analysis makes explicit not only facts it knows, but also facts it does not know

- Sources of imprecision/incompleteness in static analysis represented using abstraction variables
- For example, if value of variable is unknown after a loop, represent this unknown value using abstraction variable
- This representation allows analysis to be "introspective" and reason about what facts it could be missing





• Given known facts F and desired outcome O, abductive inference finds simple explanatory hypothesis E such that

 $F \wedge E \models O$  and  $SAT(F \wedge E)$ 



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- We use abductive inference to generate simple explanations that either guarantee that program is error-free or definitely buggy
- These abductive explanations are presented as queries to user

• Input: invariants computed by verifier and assertion to discharge



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- Technique computes formulas I and  $\phi$  describing invariant and assertion in terms of abstraction variables
- Use abduction to compute simple and general explanation Γ s.t.:

 $\Gamma \wedge I \models \phi$  and  $SAT(\Gamma \wedge I)$ 



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 Abductive explanation Γ is presented to user as proof obligation query



- Input: invariants computed by verifier and assertion to discharge
- Technique computes formulas *I* and φ describing invariant and assertion in terms of abstraction variables
- Use abduction to compute simple and general explanation  $\Gamma$  s.t.:

 $\Gamma \wedge I \models \phi \text{ and } \operatorname{SAT}(\Gamma \wedge I)$ 

- Abductive explanation  $\Gamma$  is presented to user as proof obligation query
- If  $\Gamma$  is invariant, report is false alarm



• Proof obligation query used to show report is false alarm



- Proof obligation query used to show report is false alarm
- We generate another query, called failure witness query, to show report is a real bug



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- We generate another query, called failure witness query, to show report is a real bug
- To generate failure witness query, solve a dual abductive inference problem:

 $\Delta \wedge I \models \neg \phi$  and  $SAT(\Delta \wedge I)$ 

• If  $\Delta$  can hold in some program execution, then report is real bug!



• Our technique helps user classify error reports by generating simple queries



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- If user answers "no" or "I don't know", technique computes new abductive explanation distinct from previous ones



- Our technique helps user classify error reports by generating simple queries
- If query is a proof obligation and user answers yes, report classified as false alarm
- If query is a failure witness and user answers yes, report classified as real bug
- If user answers "no" or "I don't know", technique computes new abductive explanation distinct from previous ones
- Interaction continues until report is classified as real bug or false alarm


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void foo(int flag,
          unsigned int n)
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  int k = 1;
  int x = havoc();
  if(flaq) k = x;
  int i=0, j=0;
  while(i<=n)</pre>
    i++;
    j+=i;
  int z = k+i+j;
  assert(z>2*n);
```

• Suppose a verification tool reports potential error for this example

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- Want to classify report as false alarm or real bug using our technique

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- Since precise values of i and j are unknown after loop, represent their values using α<sub>i</sub> and α<sub>j</sub>

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- Want to classify report as false alarm or real bug using our technique
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- Since precise values of i and j are unknown after loop, represent their values using  $\alpha_i$  and  $\alpha_j$
- Similarly, represent unknown value of x as abstraction variable  $\alpha_x$

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void foo(int flag,
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  int k = 1;
  int x = havoc();
  if(flaq) k = x;
  int i=0, j=0;
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 Perform symbolic value propagation to represent z's value in terms of α's and function inputs



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- If flag is zero,  $z = 1 + \alpha_i + \alpha_j$

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void foo(int flag,
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  int k = 1;
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- Perform symbolic value propagation to represent z's value in terms of α's and function inputs
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- Perform symbolic value propagation to represent z's value in terms of α's and function inputs
- If flag is zero,  $z = 1 + \alpha_i + \alpha_j$
- If flag is non-zero,  $\mathbf{z} = \alpha_x + \alpha_i + \alpha_j$
- Thus, condition under which assertion succeeds is:

 $\phi = \begin{array}{l} (1 + \alpha_i + \alpha_j > 2 * n \land \neg flag) \lor \\ (\alpha_x + \alpha_i + \alpha_j > 2 * n \land flag) \end{array}$ 

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• Now, we want to utilize invariants inferred by verification tool

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- And that i is greater than n after loop: α<sub>i</sub> > n
- Finally, since **n** is unsigned,  $n \ge 0$
- Putting this all together, we know the invariants:

 $\mathcal{I} = \alpha_x \ge 0 \land \alpha_i > 0 \land n \ge 0$ 

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• To classify error report, we solve two abductive inference problems.

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- First, find proof obligation  $\Gamma$  s.t:

 $\Gamma \wedge \mathcal{I} \models \phi$ 

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• Solution computed by our technique is:

 $\Gamma = \alpha_j \ge n$ 

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#### $\mathcal{I} = \alpha_x \ge 0 \land \alpha_i > 0 \land n \ge 0$

 Next, solve another abductive inf. problem to compute failure witness Δ:

 $\Delta \wedge \mathcal{I} \models \neg \phi$ 

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• Next, we compare  $\Gamma$  and  $\Delta$  to decide which one is more promising:

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 Query: Is j>=n invariant?
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- Thus, we classify report as false alarm

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- In this case, easy to show j >= n is invariant
- Thus, we classify report as false alarm
- Easier to answer this query than to manually classify error report

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Use minimum satisfying assignments and quantifier elimination to compute simple and general explanations

• Performed user study to evaluate new technique









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- Our technique: Given code and series of queries, asked to answer "Yes", "No", or "Don't know"
- Based on answers to queries, report classified automatically









### Results of User Study

• With manual classification, programmers classified 51.1% of reports incorrectly

### Manual Classification


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- With assisted classification, programmers classified only 7.3% of reports incorrectly

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#### Assisted Classification



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- With manual classification, programmers classified 51.1% of reports incorrectly
- With assisted classification, programmers classified only 7.3% of reports incorrectly
- Our technique dramatically improves classification accuracy
- Also dramatically reduces time needed to classify report
- Using manual classification, programmers need 293 seconds on average
- Using new technique, programmers take 55 seconds on average

#### Manual Classification







• New technique to help programmers classify error reports as real bugs or false alarms



- New technique to help programmers classify error reports as real bugs or false alarms
- Uses abductive inference to compute simple queries that capture what analysis is missing



- New technique to help programmers classify error reports as real bugs or false alarms
- Uses abductive inference to compute simple queries that capture what analysis is missing
- Interacts with user until report is classified as bug/false alarm



- New technique to help programmers classify error reports as real bugs or false alarms
- Uses abductive inference to compute simple queries that capture what analysis is missing
- Interacts with user until report is classified as bug/false alarm
- User study shows technique dramatically improves classification speed and accuracy

#### Related Work:

- Ball, T., Naik, M., Rajamani, S.: From Symptom to Cause: Localizing Errors in Counterexample Traces. POPL 2003
- Jose, M., Majumdar, R.: Cause Clue Clauses: Error Localization using Maximum Satisfiability. PLDI 2011
- Groce, A.: Error Explanation with Distance Metrics. TACAS 2004
- Dillig, I., Dillig, T., McMillan, K., Aiken, A.: Minimum Satisfying Assignments for SMT. CAV 2012.

