

CS 378: Autonomous Intelligent Robotics

Instructor: Jivko Sinapov

<http://www.cs.utexas.edu/~jsinapov/teaching/cs378/>

Machine Learning

Data

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100100011101000000101000110111010110
100100111101110000001111100110100100
100001101101111101010011100001101001
111111010000110111001010111100001011
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011011111010111100010100010100010000
011010011011011010001000101111001101
000101000001100110001100100010010110
100101010100010011100101010101111101
```

Algorithm



Model

$f(\mathbf{x})$

Announcements

**FRI Survey – please take the time to
respond**

Announcements

“According to predicted probabilities in this study, out of every 100 students who enter college, 17 more will complete an undergraduate degree if they complete FRI. For every 100 students who graduate, 23 more will stay in a STEM major if they complete FRI.”

- just accepted paper on the benefits of FRI

Announcements

- An additional half-time (20 hrs/week) summer fellowship is available
- The award is \$1,250
- Lasts 8 weeks, both start and end dates as well as hours are very flexible
- If you'd like it, email me ASAP

Announcements

Final Projects Presentation Date:

Thursday, May 12, 9:00-12:00 noon

Project Deliverables

- Final Report (6+ pages in PDF)
- Code and Documentation (posted on github)
- Presentation including video and/or demo

Project Report Structure / Outline

- Abstract
- Introduction
- Background and/or Related Work
- Technical Approach
- Experiments and/or Evaluation and/or Example Demonstration
- Conclusion and Future Work

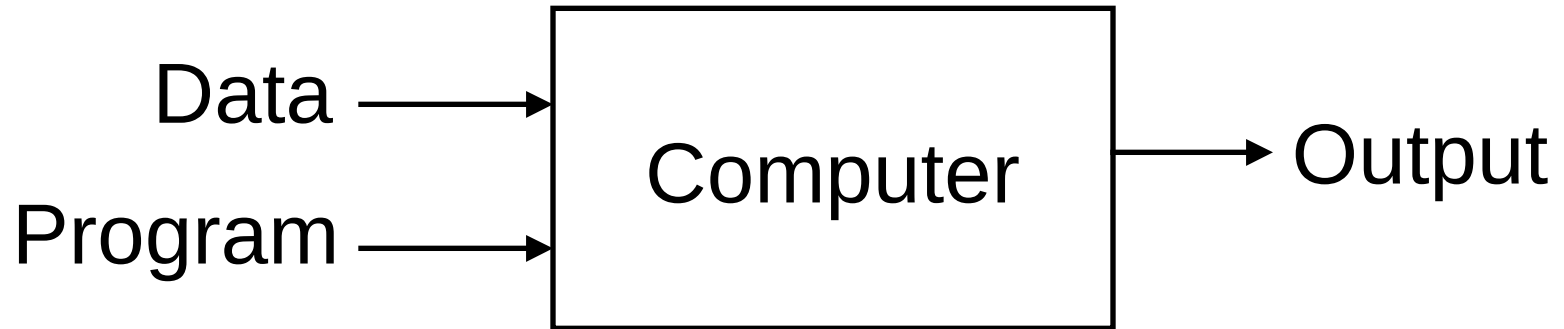
Machine Learning

Main Reference

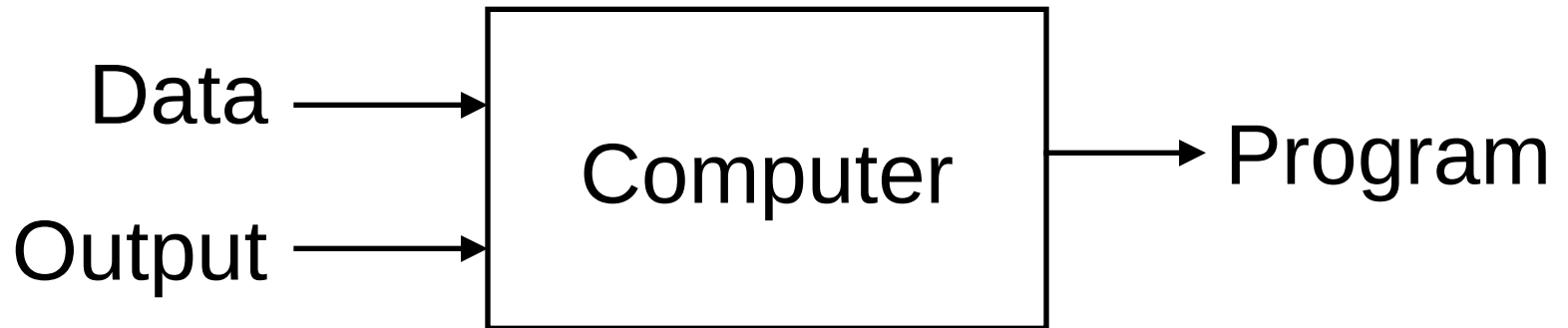
Alex Smola and S.V.N. Vishwanathan,
Introduction to Machine Learning,
Chapter 1, Cambridge University Press, 2008

What is Machine Learning?

Traditional Programming



Machine Learning



What do we mean by program?

What do we mean by program?

- A robot's controller
- A decision function (i.e., classification function)
- A neural network
- A recommendation system
- etc.

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KDnuggets Cartoon



“The machine learning algorithm wants to know if we’d like a dozen wireless mice to feed the Python book we just bought.”

Machine Learning Frameworks

| | supervised | unsupervised |
|------------|----------------------------------|--|
| discrete | classification or categorization | clustering |
| continuous | regression | dimensionality reduction and manifold learning |

Classification

Classification

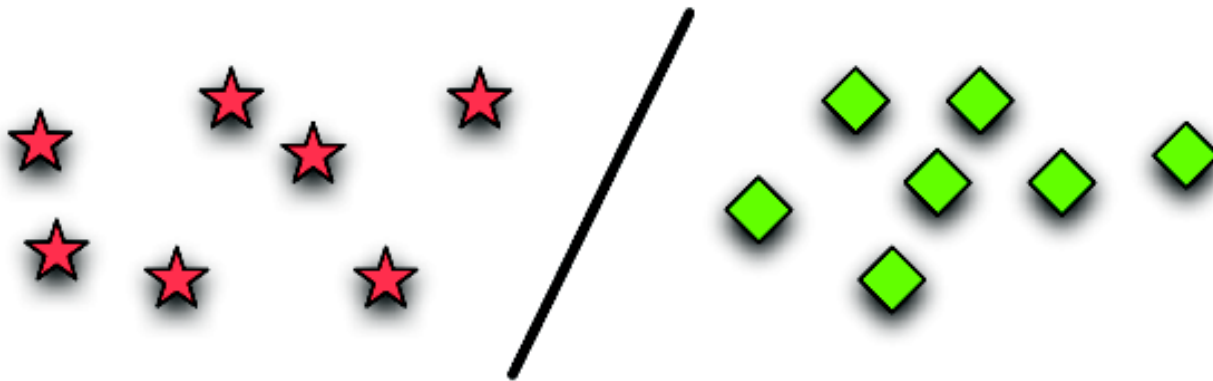


Fig. 1.5. Binary classification; separate stars from diamonds. In this example we are able to do so by drawing a straight line which separates both sets. We will see later that this is an important example of what is called a *linear classifier*.

Classification

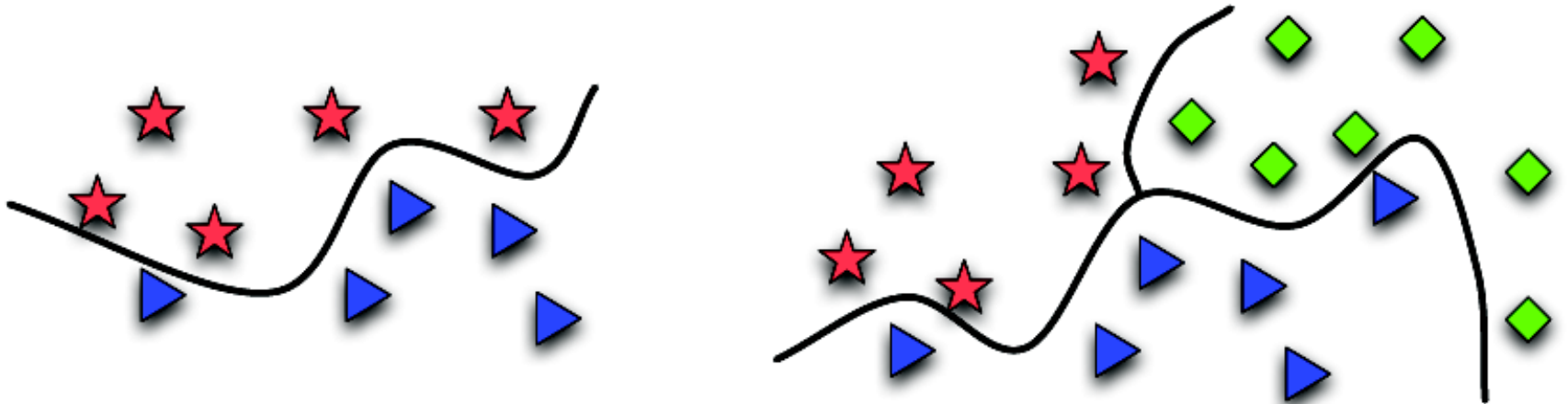


Fig. 1.6. Left: binary classification. Right: 3-class classification. Note that in the latter case we have much more degree for ambiguity. For instance, being able to distinguish stars from diamonds may not suffice to identify either of them correctly, since we also need to distinguish both of them from triangles.

Classification

Inputs:

$$\mathbf{X} := \{x_1, \dots, x_m\}$$

where $x_i \in \mathbb{R}^k$

Outputs:

$$\mathbf{Y} := \{y_1, \dots, y_m\}$$

set of classes:

$$y_i \in \{1, \dots, n\}$$

Machine Learning Framework

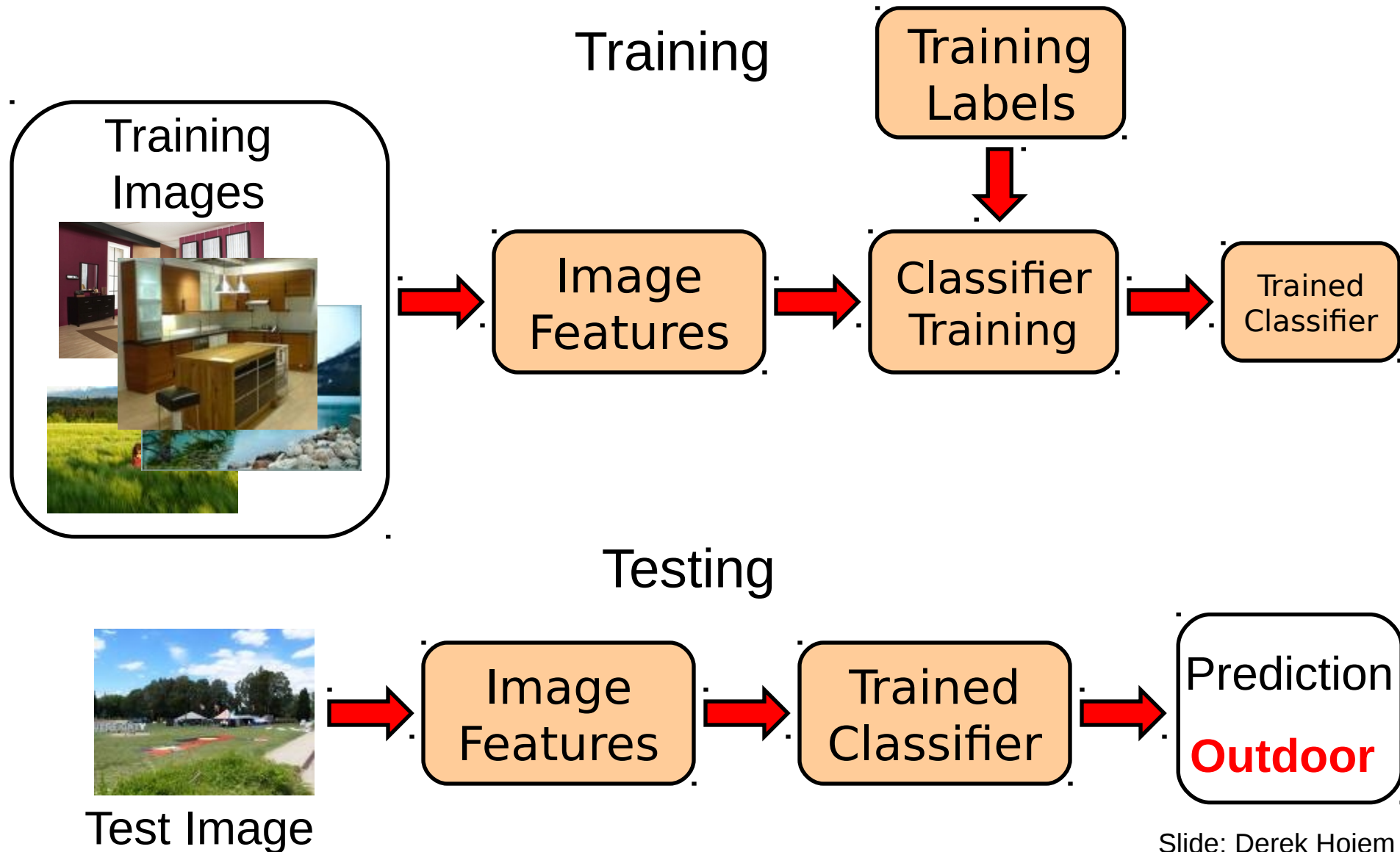
The diagram shows the equation $y = f(x)$ in blue. Below the equation, three labels are positioned: 'output' under 'y', 'classification function' under 'f', and 'data point' under 'x'. Red arrows point from each label to its corresponding variable in the equation: one arrow from 'output' to 'y', one from 'classification function' to 'f', and one from 'data point' to 'x'.

$$y = f(x)$$

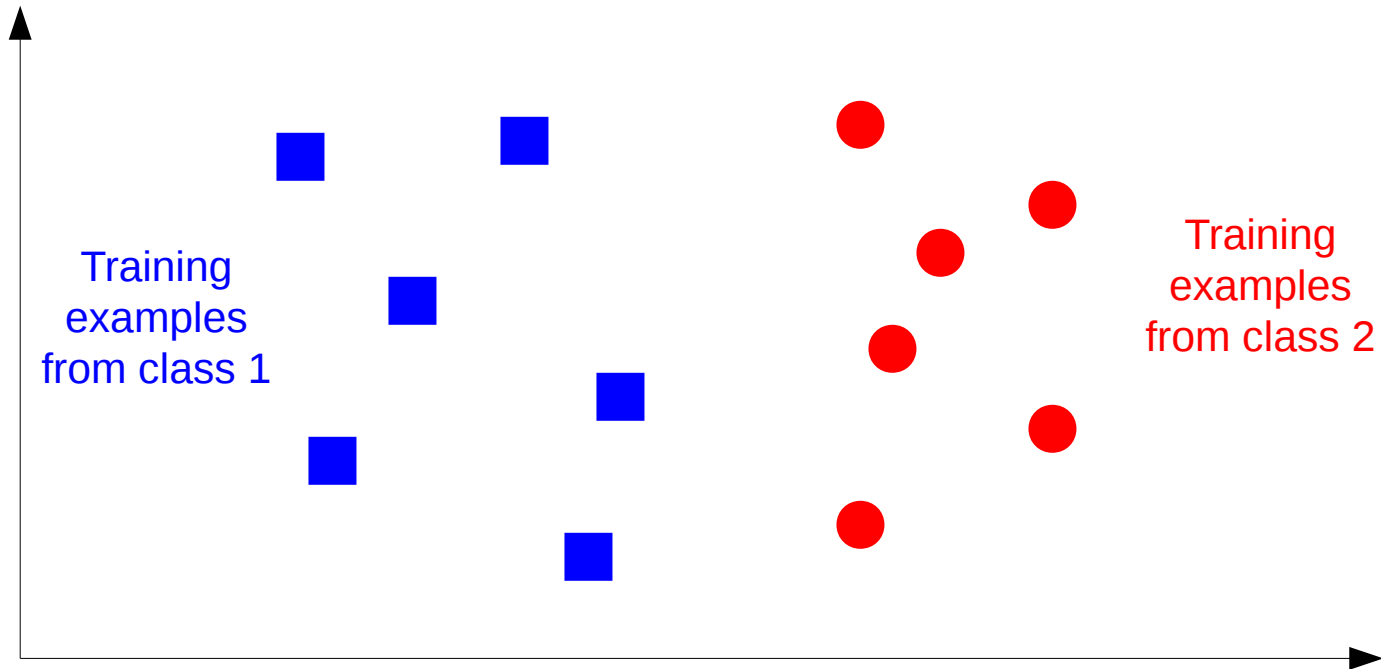
output classification function data point

- **Training:** given a *training set* of labeled examples $\{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_N, y_N)\}$, estimate the function f by minimizing the error on the training set
- **Testing:** apply f to a never before seen *test example* \mathbf{x} and output the predicted value $y = f(\mathbf{x})$

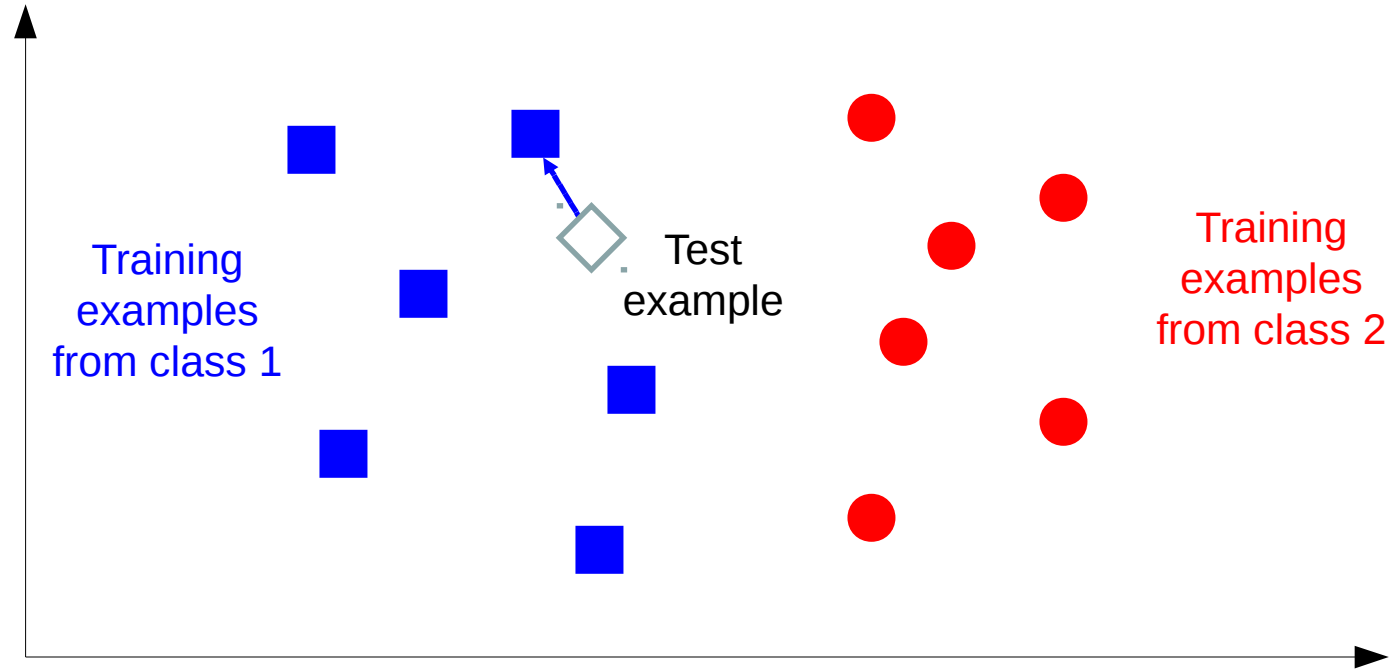
Training and Testing Pipeline



Classification using K-Nearest Neighbors

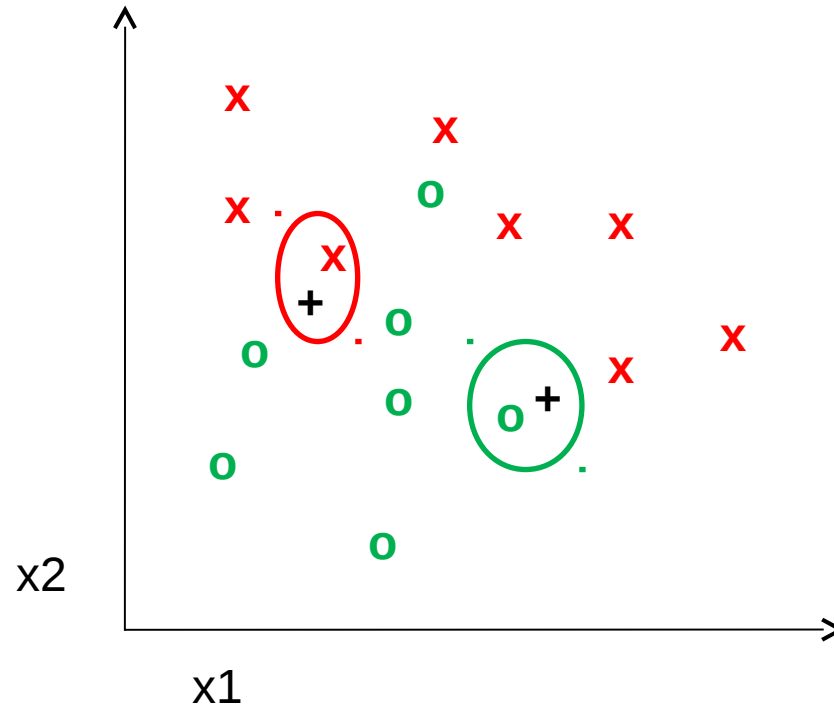


Classification using K-Nearest Neighbors

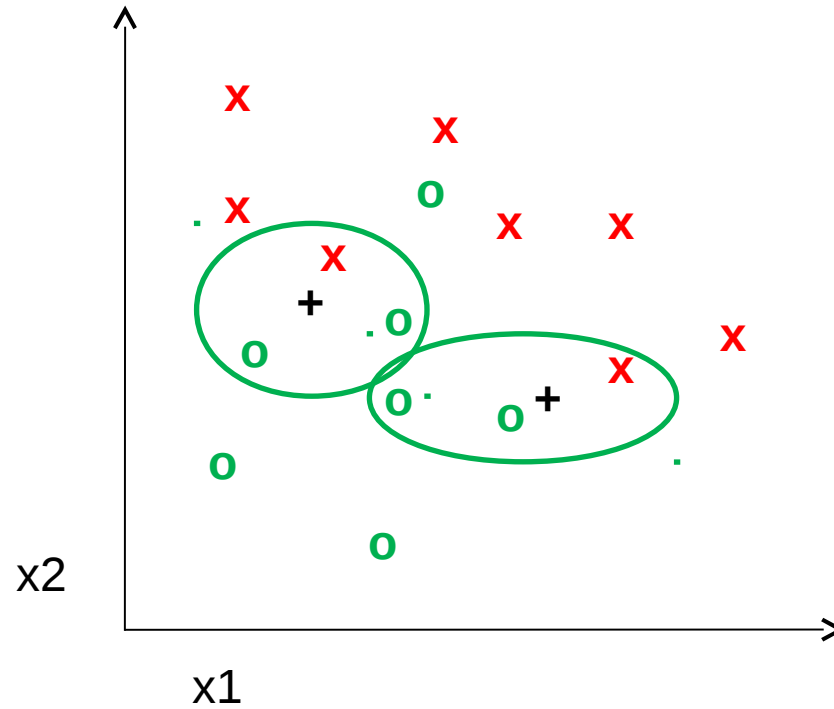


$f(\mathbf{x}) = \text{label of the training example nearest to } \mathbf{x}$

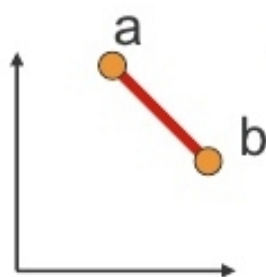
1-Nearest Neighbor



3-Nearest Neighbor

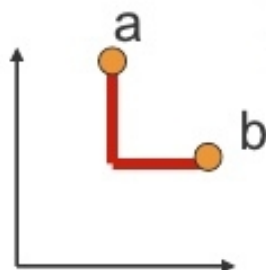


Examples of distances



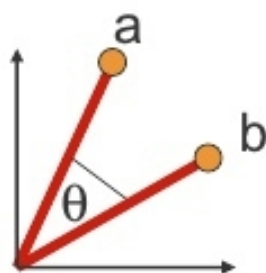
E u c l i d e a n d i s t a n c e

$$\text{dist}(a, b) = \|a - b\|_2 = \sqrt{\sum_i (a_i - b_i)^2}$$



M a n h a t t a n d i s t a n c e

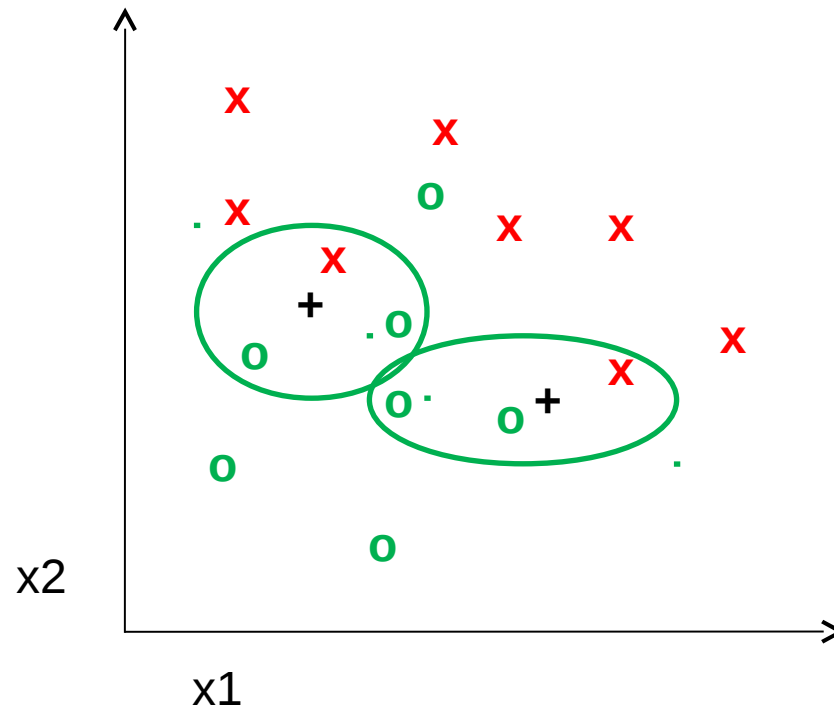
$$\text{dist}(a, b) = \|a - b\|_1 = \sum_i |a_i - b_i|$$



C o s i n e d i s t a n c e

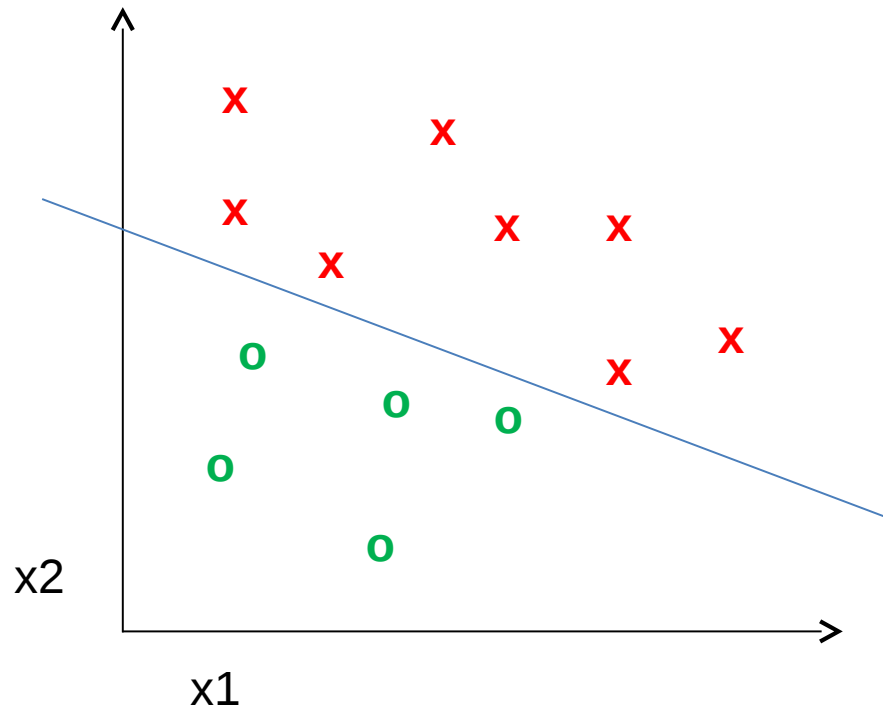
$$\text{dist}(a, b) = \cos^{-1} \frac{\langle a, b \rangle}{\|a\| \|b\|}$$

3-Nearest Neighbor



What are some of the limitations of k-NN?

Linear Classifier



- Finds a *linear function* to separate the classes:

$$f(\mathbf{x}) = \text{sgn}(\mathbf{w} \cdot \mathbf{x} + b)$$

Linear Classifier

Algorithm 1.3 The Perceptron

Perceptron(**X**, **Y**) {reads stream of observations (x_i, y_i) }

Initialize $w = 0$ and $b = 0$

while There exists some (x_i, y_i) with $y_i(\langle w, x_i \rangle + b) \leq 0$ **do**

$w \leftarrow w + y_i x_i$ and $b \leftarrow b + y_i$

end while

Dot product

$$\mathbf{a} = (1, 4, -2)$$

$$\mathbf{b} = (-2, 1, 7)$$

$$\begin{aligned}\mathbf{a} \cdot \mathbf{b} &= 1 \cdot (-2) + 4 \cdot 1 + (-2) \cdot 7 \\ &= -2 + 4 - 14 = -12\end{aligned}$$

Linear Classifier

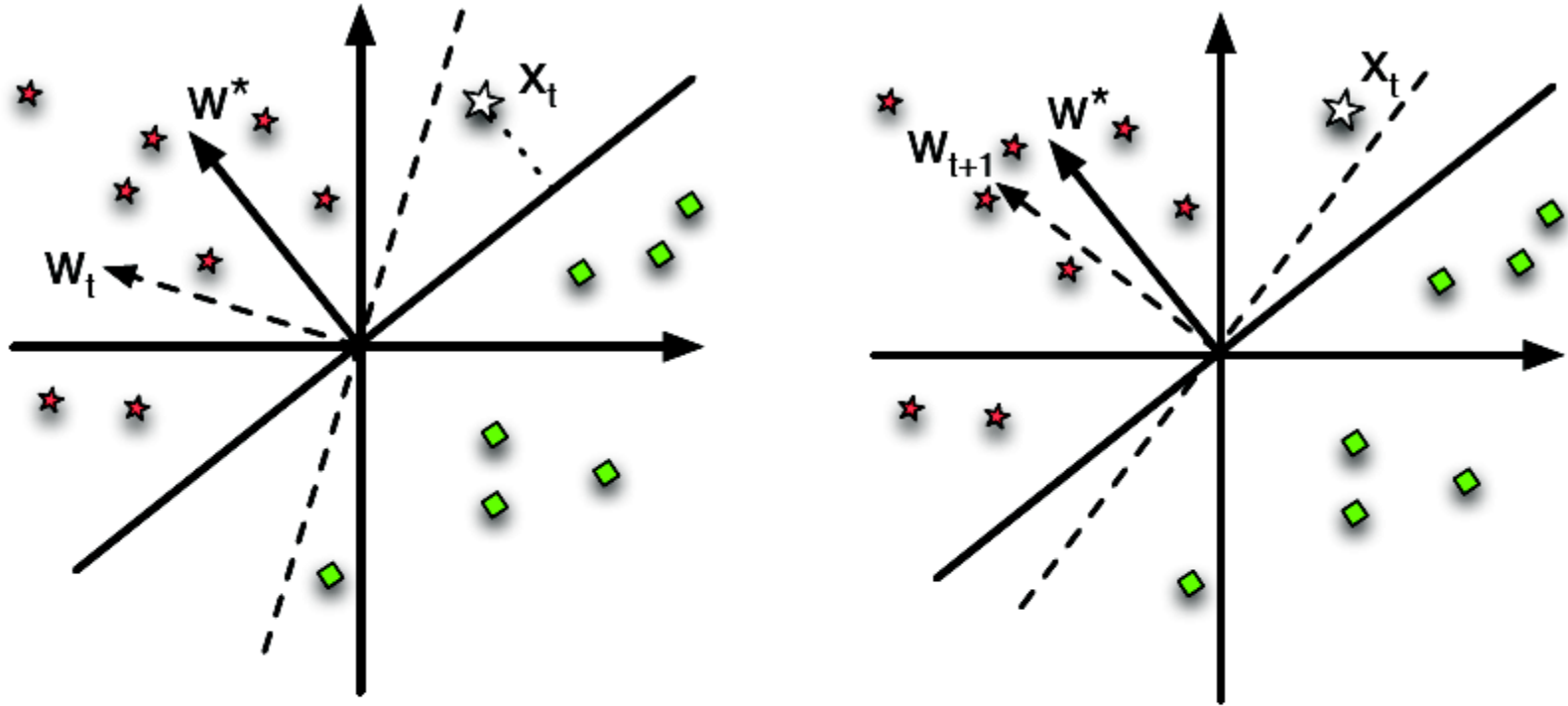
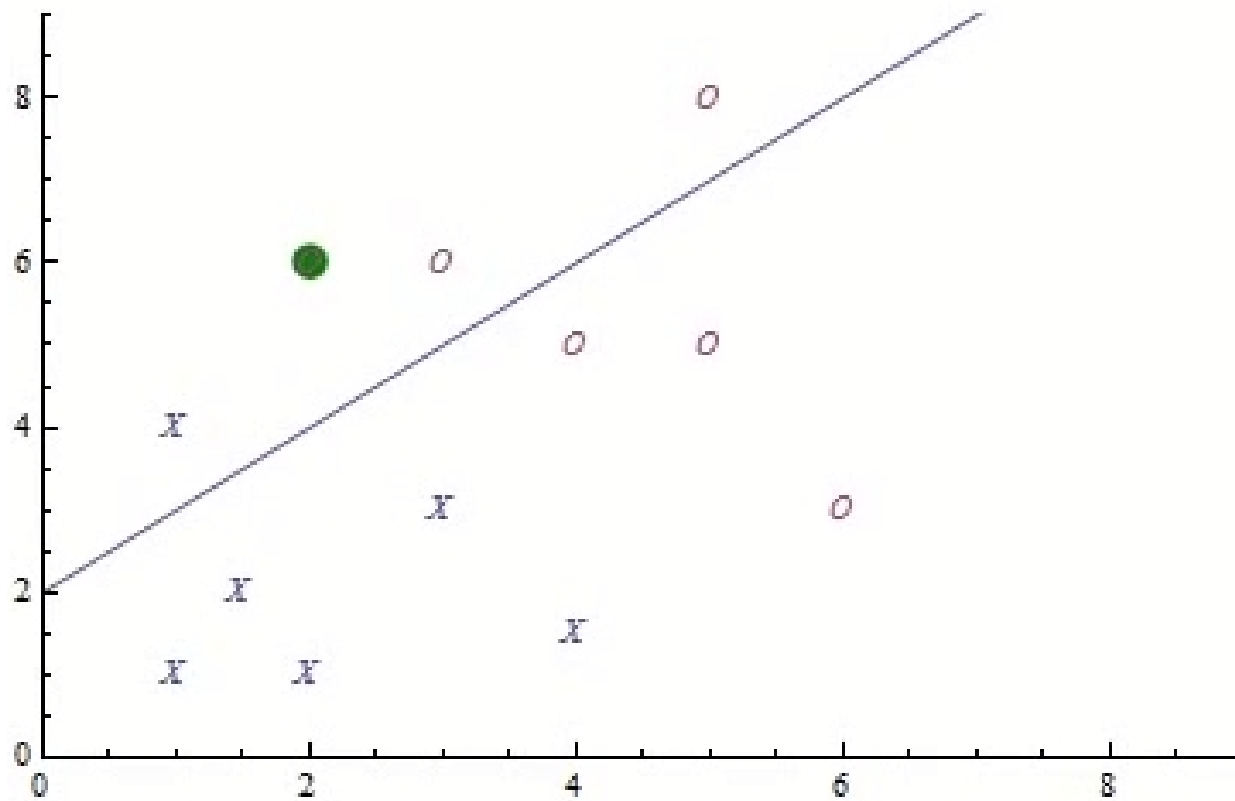
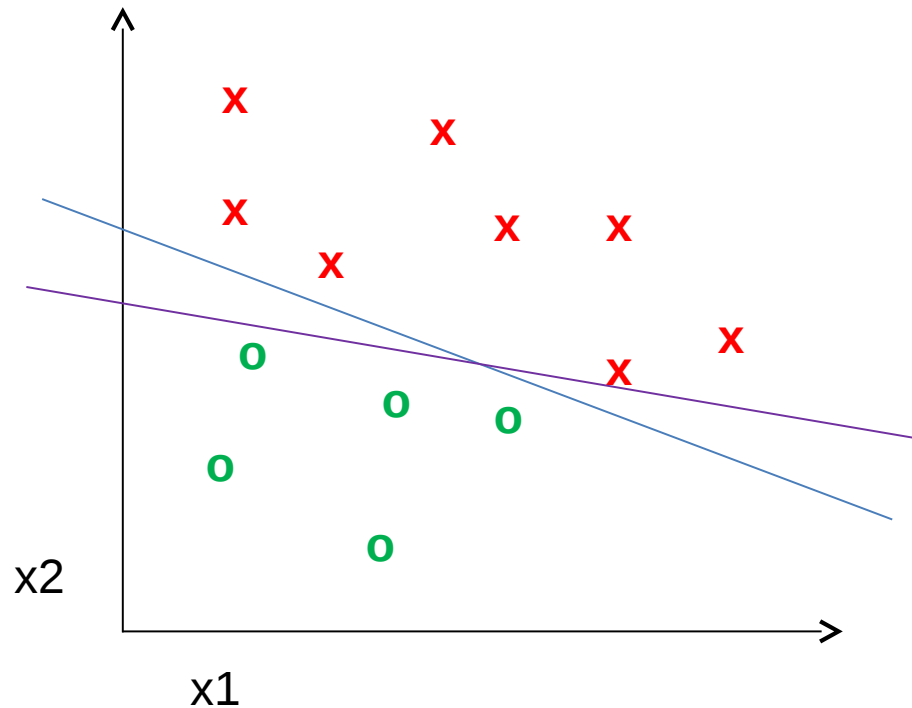


Fig. 1.22. The Perceptron without bias. Left: at time t we have a weight vector w_t denoted by the dashed arrow with corresponding separating plane (also dashed). For reference we include the linear separator w^* and its separating plane (both denoted by a solid line). As a new observation x_t arrives which happens to be mis-classified by the current weight vector w_t we perform an update. Also note the margin between the point x_t and the separating hyperplane defined by w^* . Right: This leads to the weight vector w_{t+1} which is more aligned with w^* .

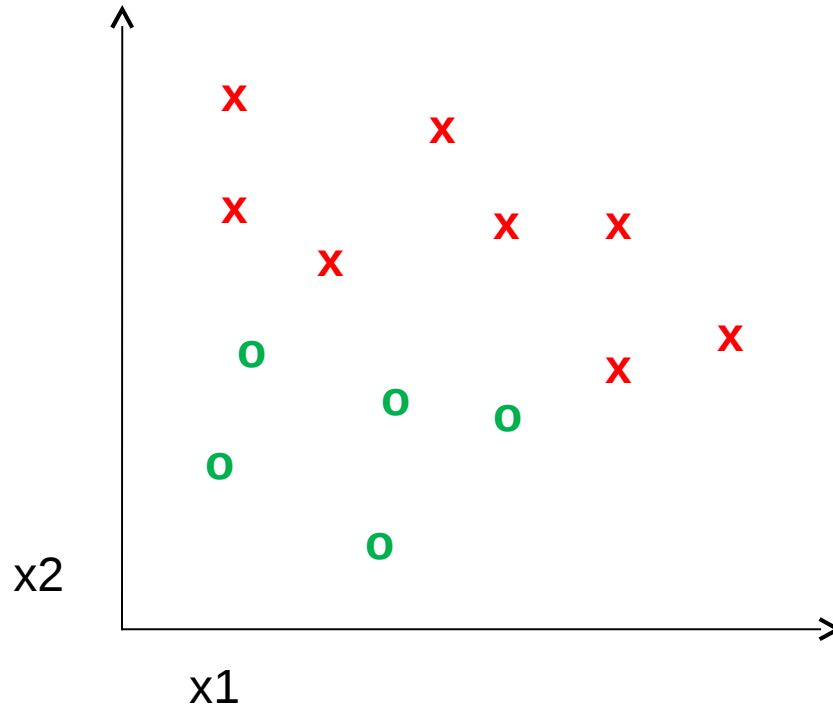


Linear Classifier

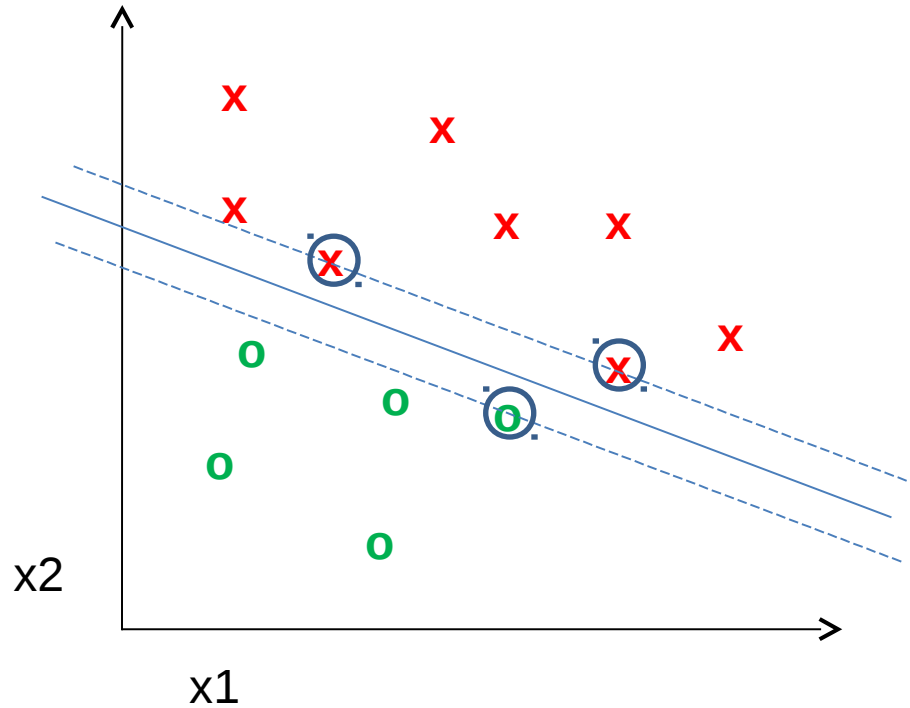


- How do we decide which line is the best?

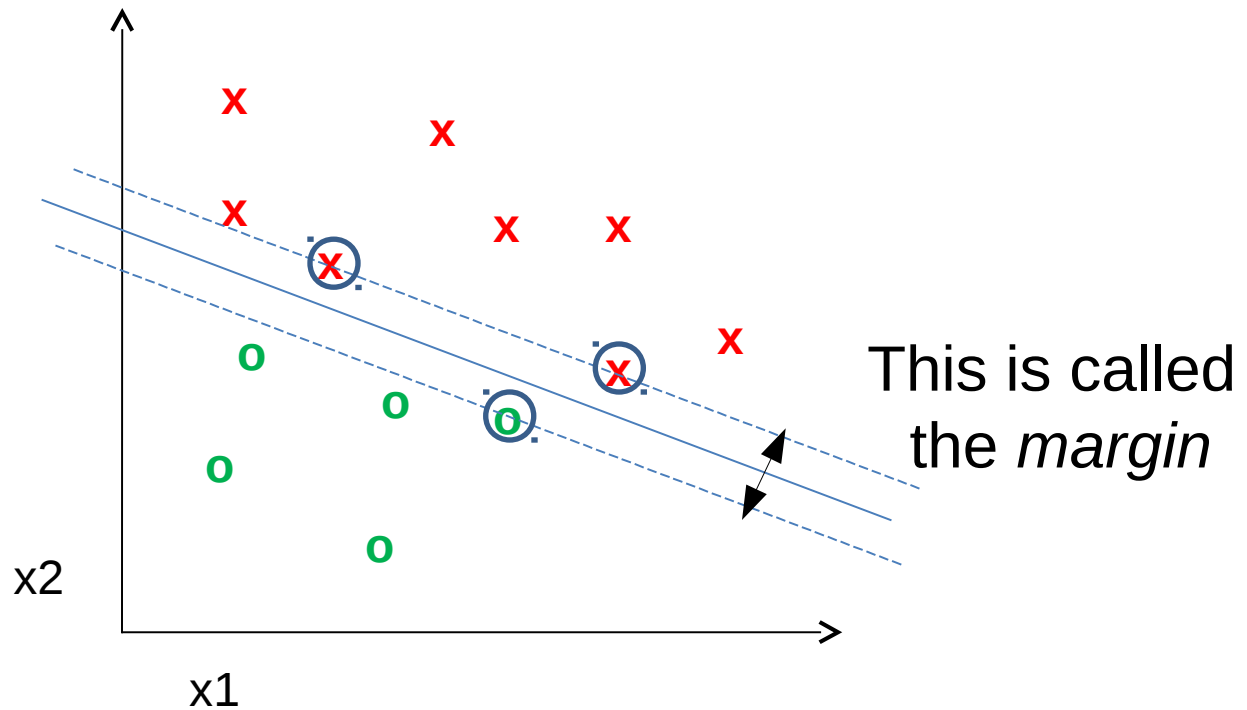
Linear Support Vector Machine



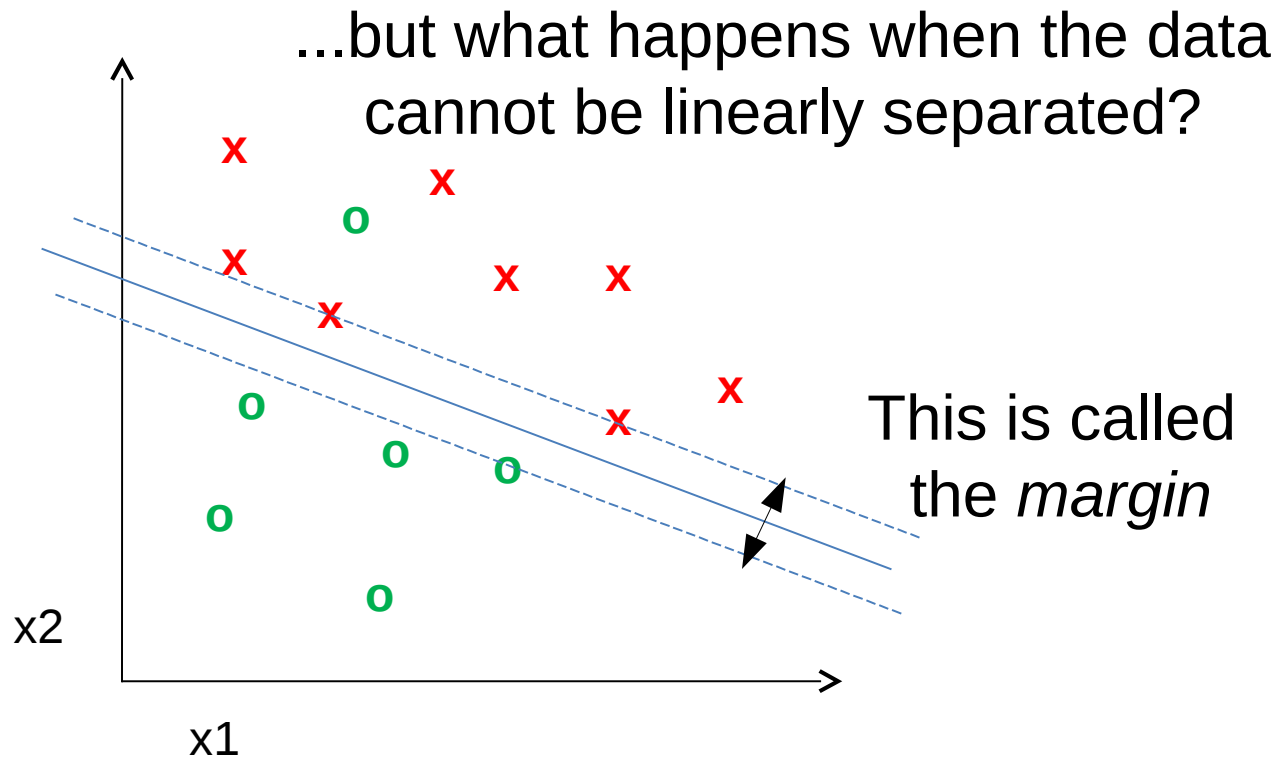
Linear Support Vector Machine



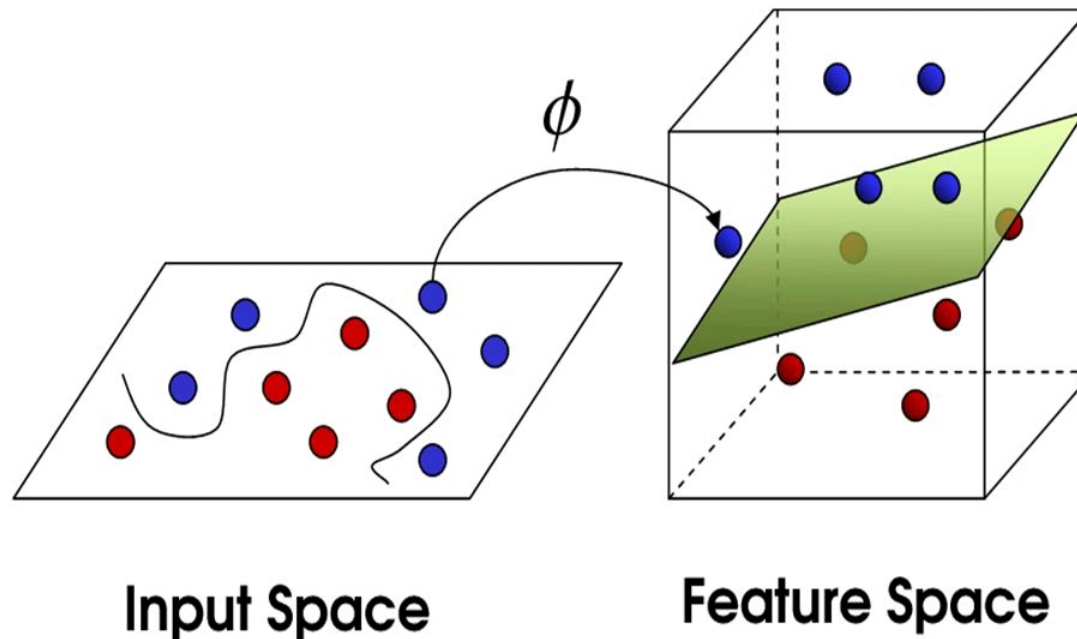
Linear Support Vector Machine



Linear Support Vector Machine



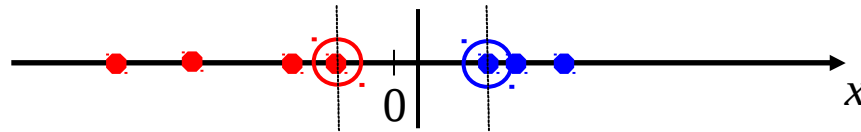
Nonlinear Support Vector Machine



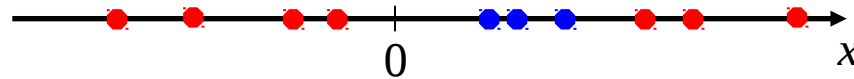
[<http://www.imtech.res.in/raghava/rbpred/svm.jpg>]

Nonlinear Support Vector Machine

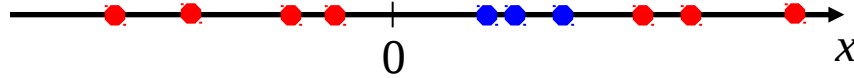
Linearly separable:



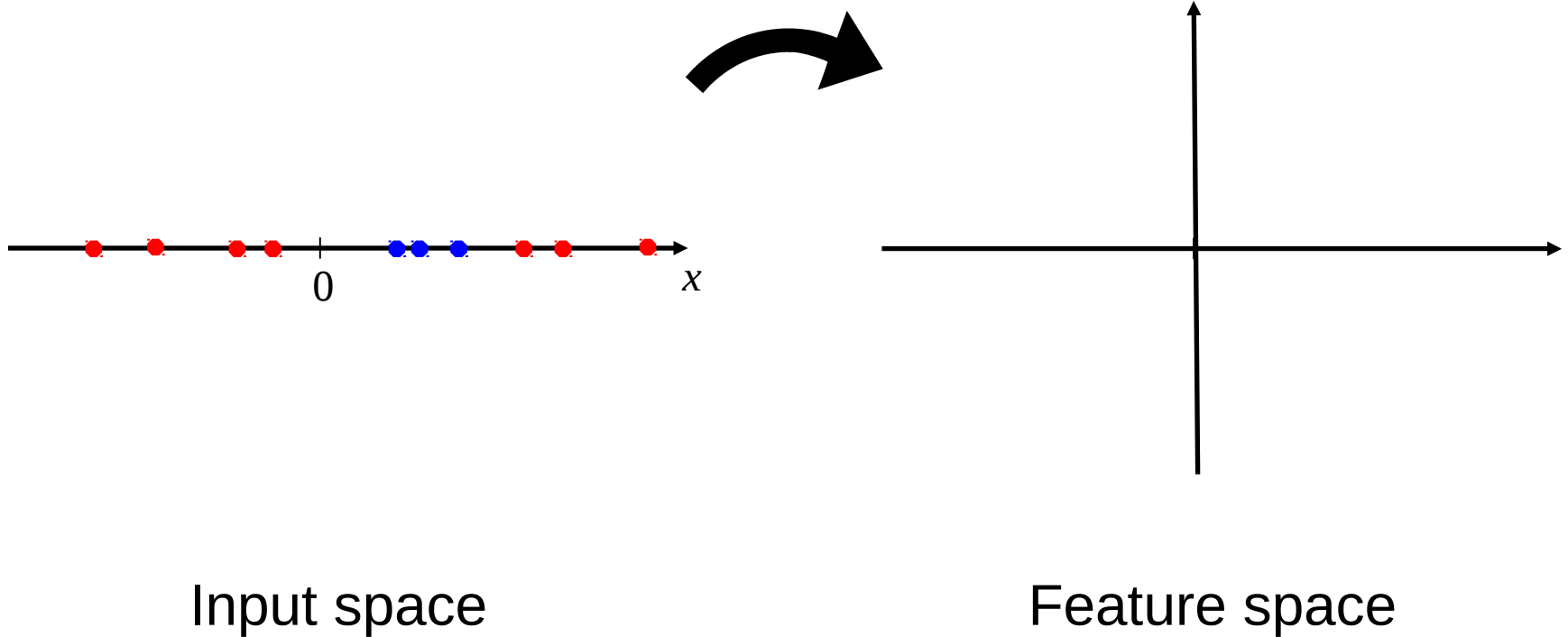
Not linearly separable:



Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

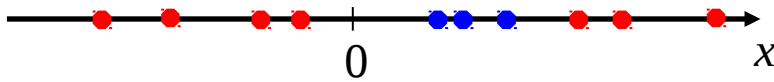


Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

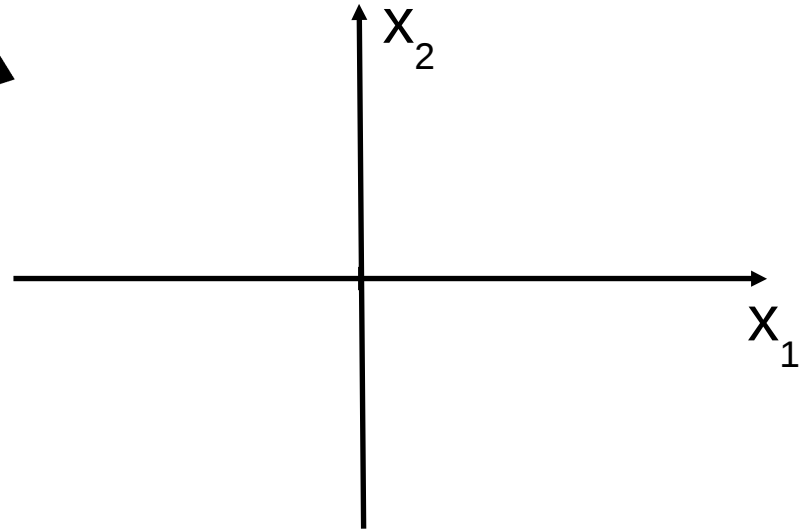


Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

$$\phi(x) \rightarrow \langle x_1, x_2 \rangle$$



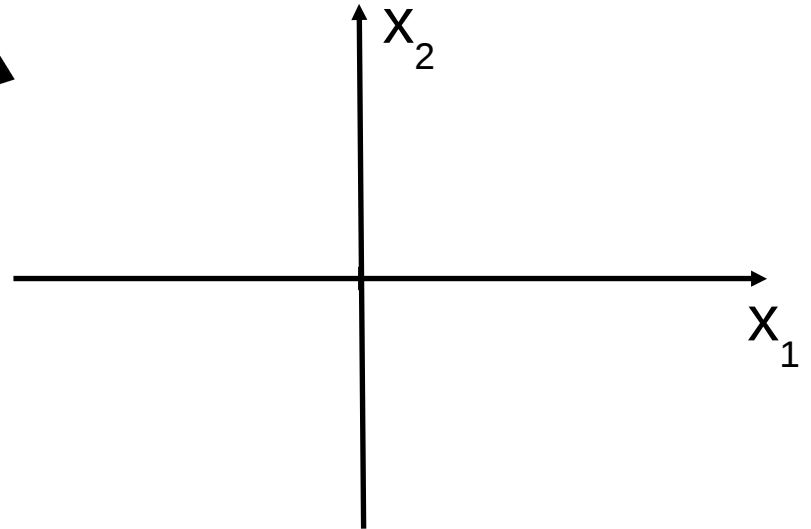
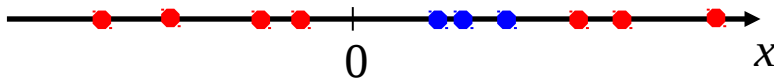
Input space



Feature space

Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

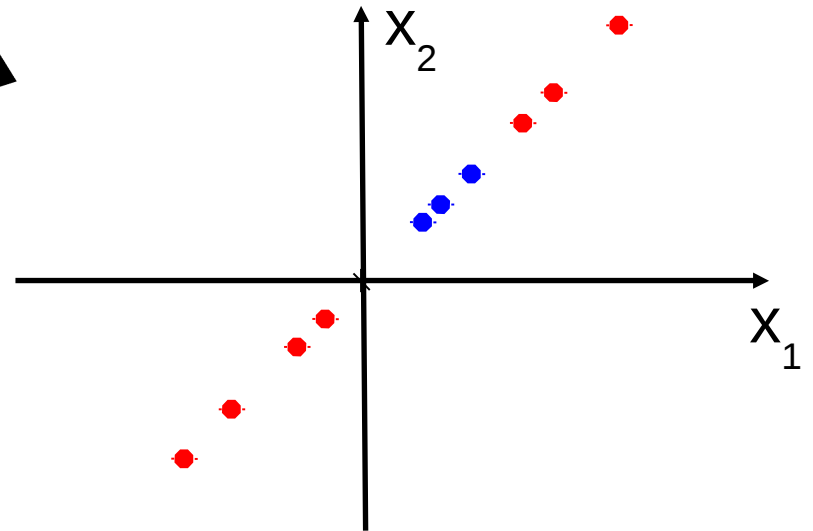
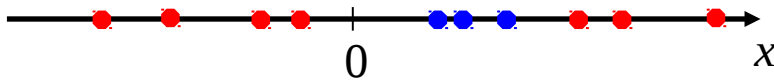
$$\phi(x) \rightarrow \langle x_1, x_2 \rangle$$



In other words, both x_1 and x_2 need to be function of x

Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

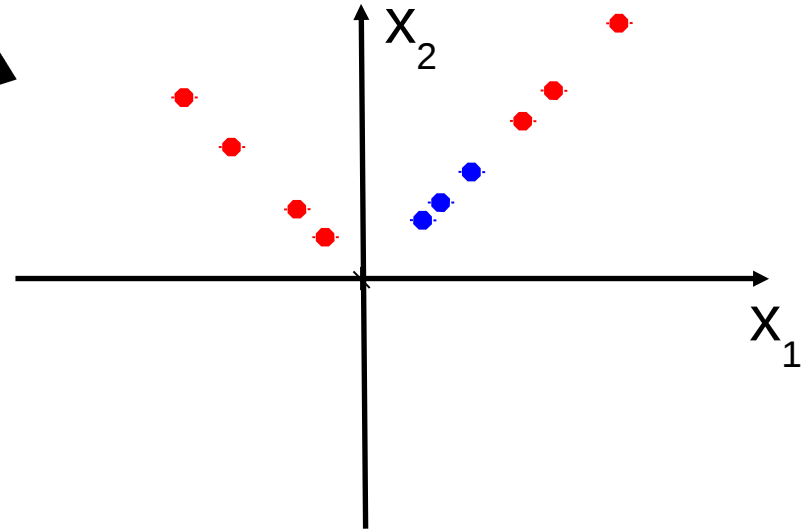
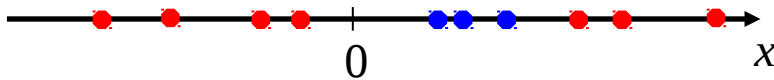
$$\phi(x) \rightarrow \langle x, x \rangle$$



Example: both x_1 and x_2 are set to x

Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

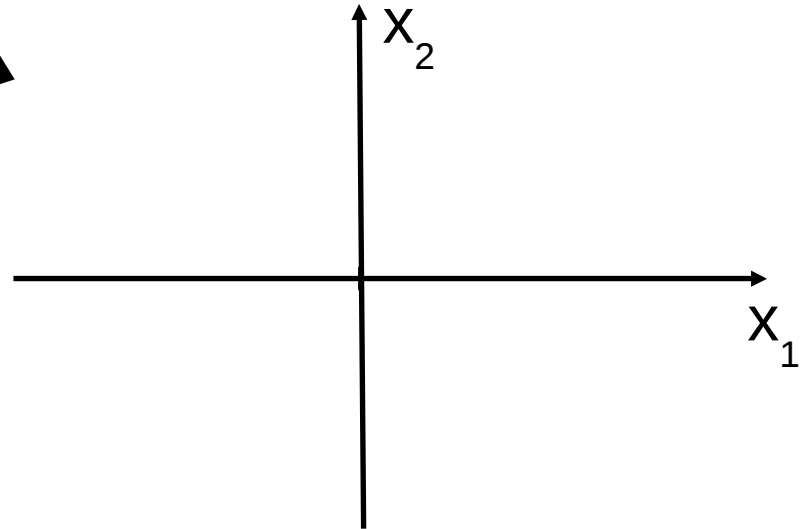
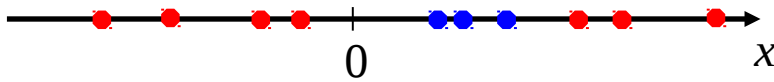
$$\phi(x) \rightarrow \langle x, |x| \rangle$$



Example: $x_1 = x$ and $x_2 = |x|$

Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

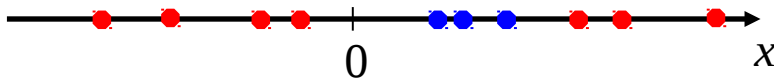
$$\phi(x) \rightarrow \langle x_1, x_2 \rangle$$



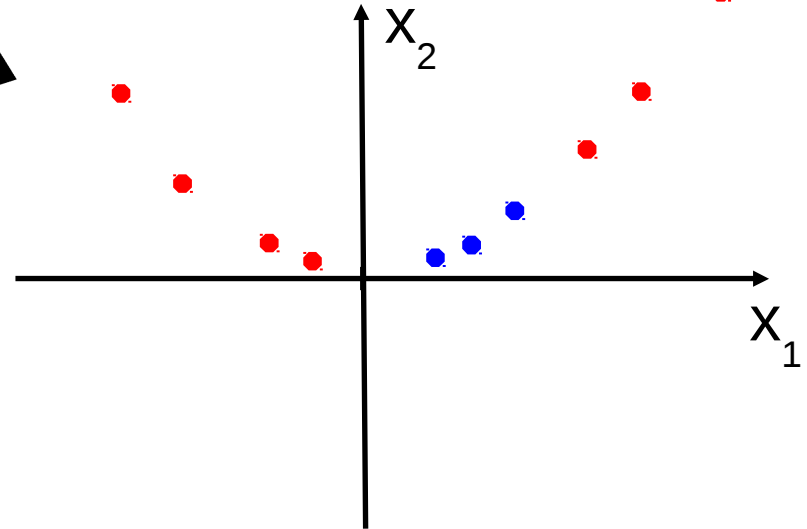
In other words, both x_1 and x_2 need to be function of x

Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

$$\phi(x) \rightarrow \langle x, x^2 \rangle$$



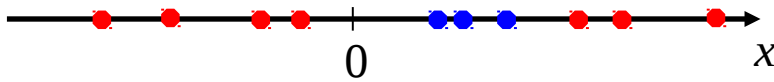
Input space



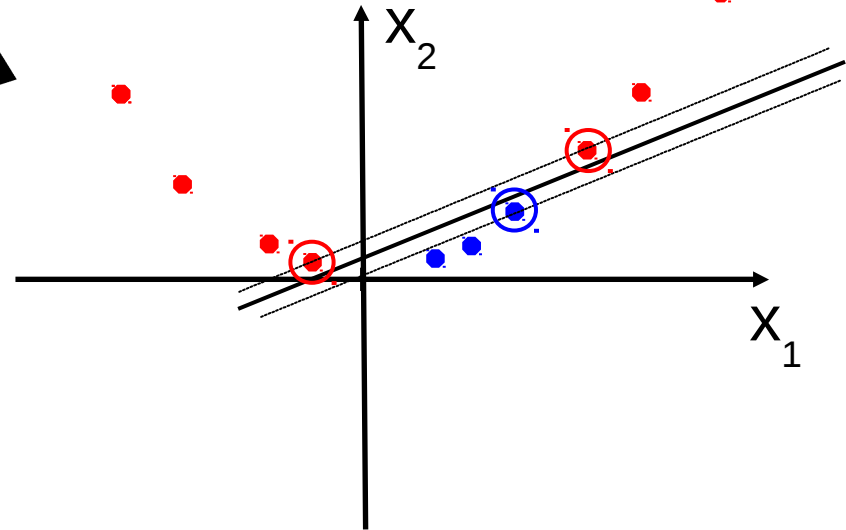
Feature space

Can we construct a mapping function from 1D to 2D such that the data in the 2D space is linearly separable?

$$\phi(x) \rightarrow \langle x, x^2 \rangle$$



Input space



Feature space

Nonlinear Support Vector Machine

- *The kernel trick*: instead of explicitly computing the lifting transformation $\varphi(\mathbf{x})$, define a kernel function K such that

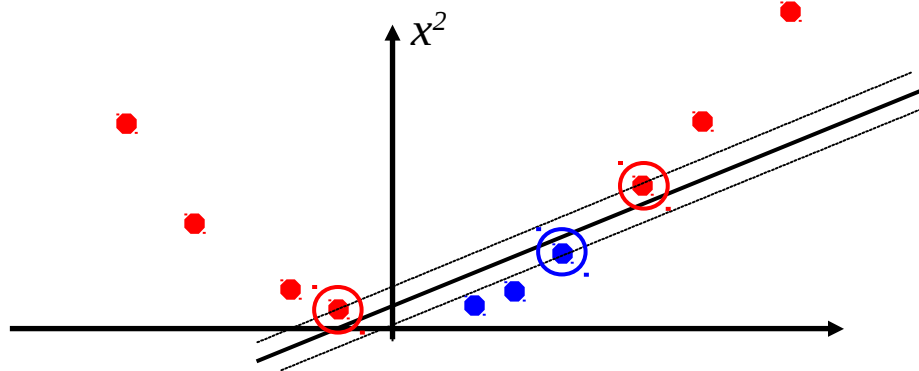
$$K(\mathbf{x}_i, \mathbf{x}_j) = \varphi(\mathbf{x}_i) \cdot \varphi(\mathbf{x}_j)$$

(to be valid, the kernel function must satisfy *Mercer's condition*)

- Intuitively, the kernel function should encode a measure of similarity between \mathbf{x}_i and \mathbf{x}_j

Nonlinear Support Vector Machine

Consider the mapping $\varphi(x) = (x, x^2)$



$$\varphi(x) \cdot \varphi(y) = (x, x^2) \cdot (y, y^2) = xy + x^2 y^2$$

$$K(x, y) = xy + x^2 y^2$$

Nonlinear Support Vector Machine

- Polynomial Kernel:

$$K_{poly}(\mathbf{x}_i, \mathbf{x}_j) = (\mathbf{x}_i^T \mathbf{x}_j + 1.0)^p$$

- Histogram kernel function:

$$K_{hist}(\mathbf{x}_i, \mathbf{x}_j) = e^{-\rho d_{a,b}(\mathbf{x}_i, \mathbf{x}_j)}$$

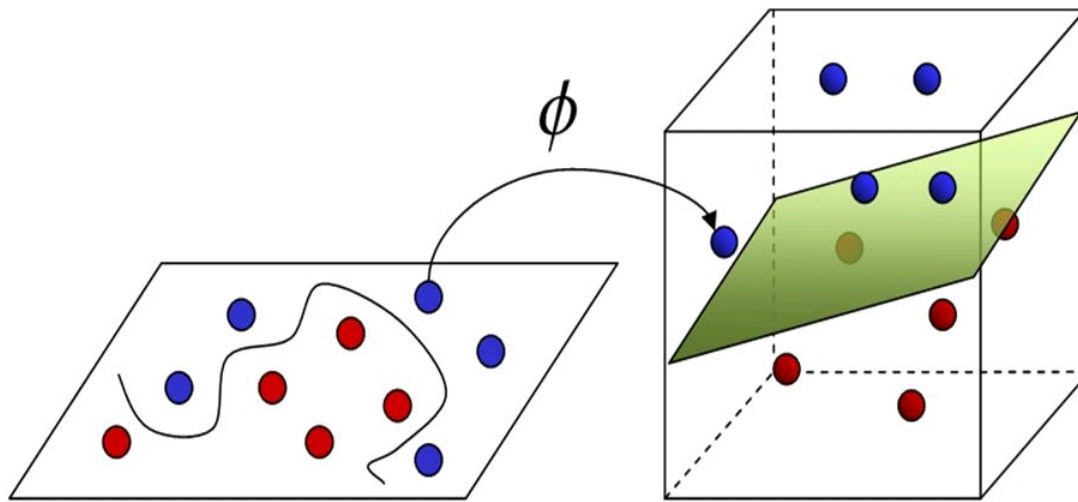
$$d_{a,b}(\mathbf{x}_i, \mathbf{x}_j) = \sum_k |x_{ik}^a - x_{jk}^a|^b$$

Nonlinear Support Vector Machine

- linear: $K(\mathbf{x}_i, \mathbf{x}_j) = \mathbf{x}_i^T \mathbf{x}_j$.
- polynomial: $K(\mathbf{x}_i, \mathbf{x}_j) = (\gamma \mathbf{x}_i^T \mathbf{x}_j + r)^d$, $\gamma > 0$.
- radial basis function (RBF): $K(\mathbf{x}_i, \mathbf{x}_j) = \exp(-\gamma \|\mathbf{x}_i - \mathbf{x}_j\|^2)$, $\gamma > 0$.
- sigmoid: $K(\mathbf{x}_i, \mathbf{x}_j) = \tanh(\gamma \mathbf{x}_i^T \mathbf{x}_j + r)$.

Nonlinear Support Vector Machine

- Support Vector Machine: a discriminative learning algorithm



Input Space

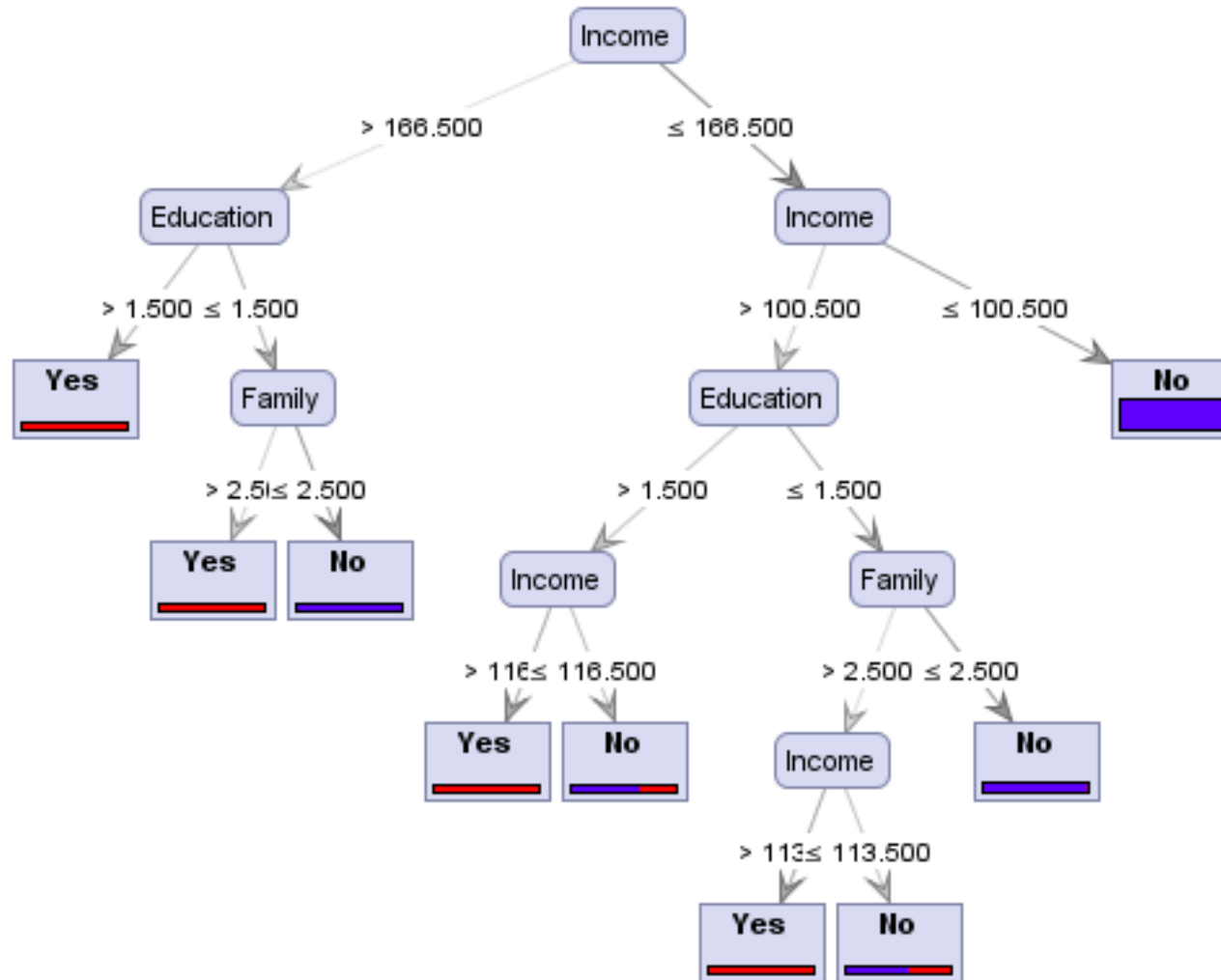
Feature Space

1. Finds maximum margin hyperplane that separates two classes
2. Uses Kernel function to map data points into a feature space in which such a hyperplane exists

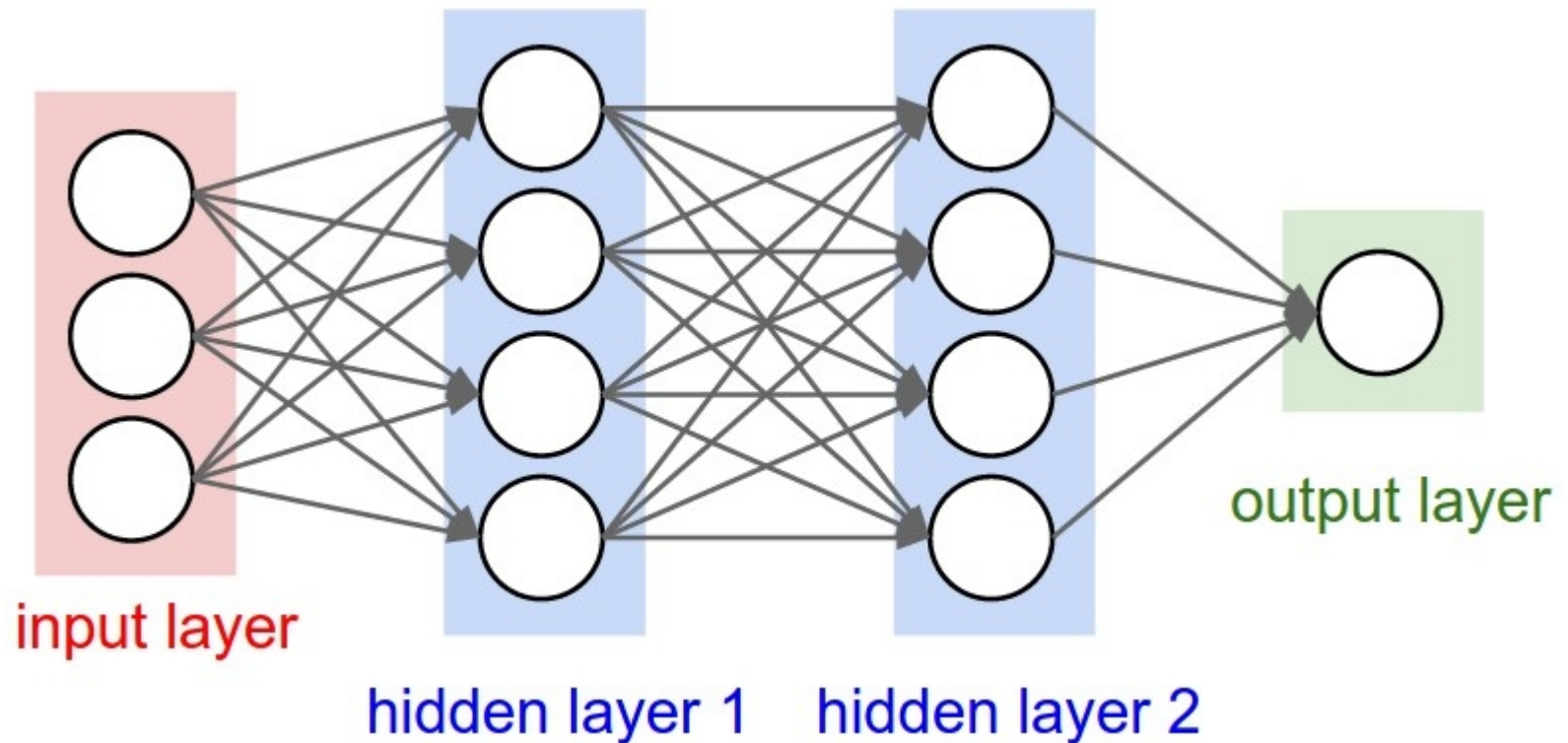
[<http://www.imtech.res.in/raghava/rbpred/svm.jpg>]

There are many other classifiers out there...

Decision Trees

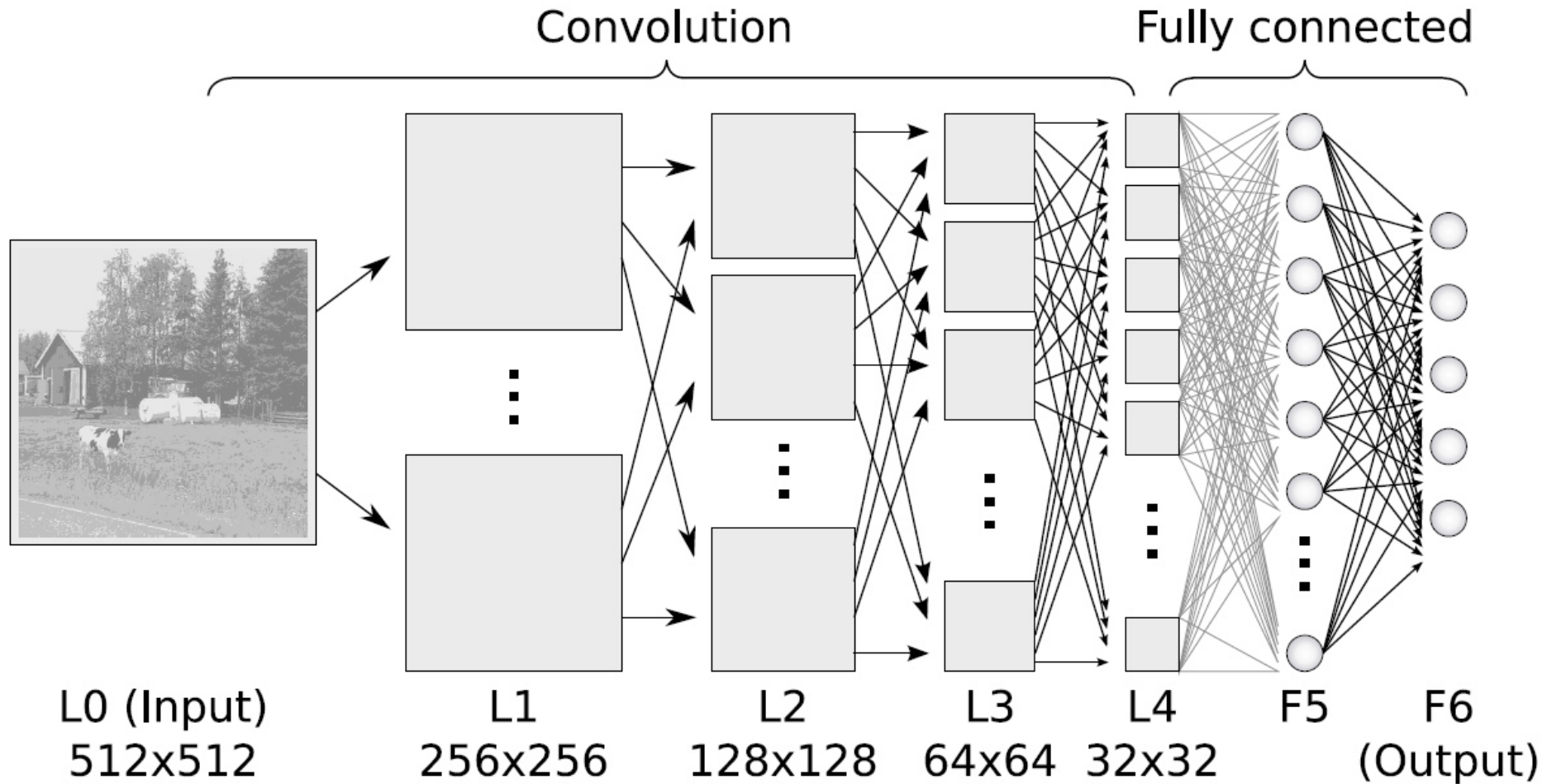


Feed-Forward Neural Networks

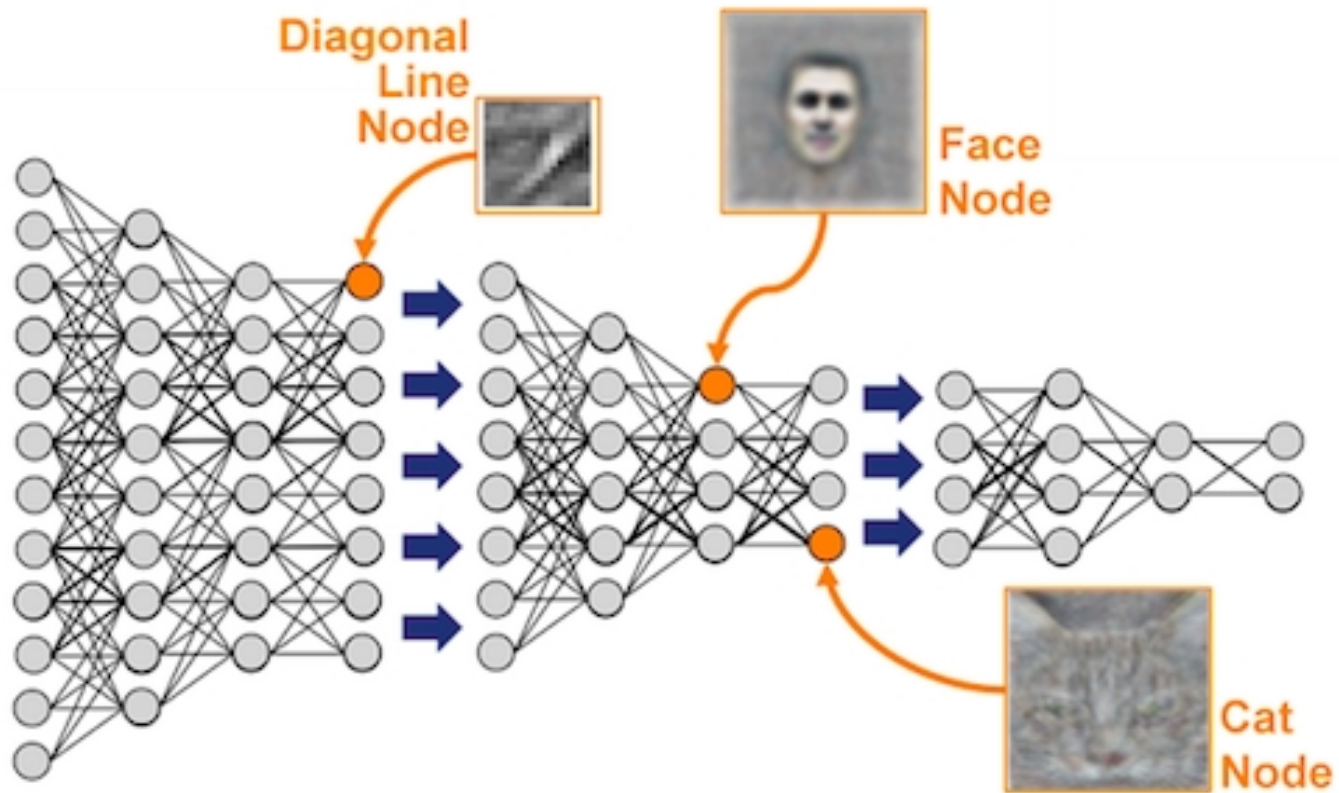


[http://cs231n.github.io/assets/nn1/neural_net2.jpeg]

Deep Learning Methods

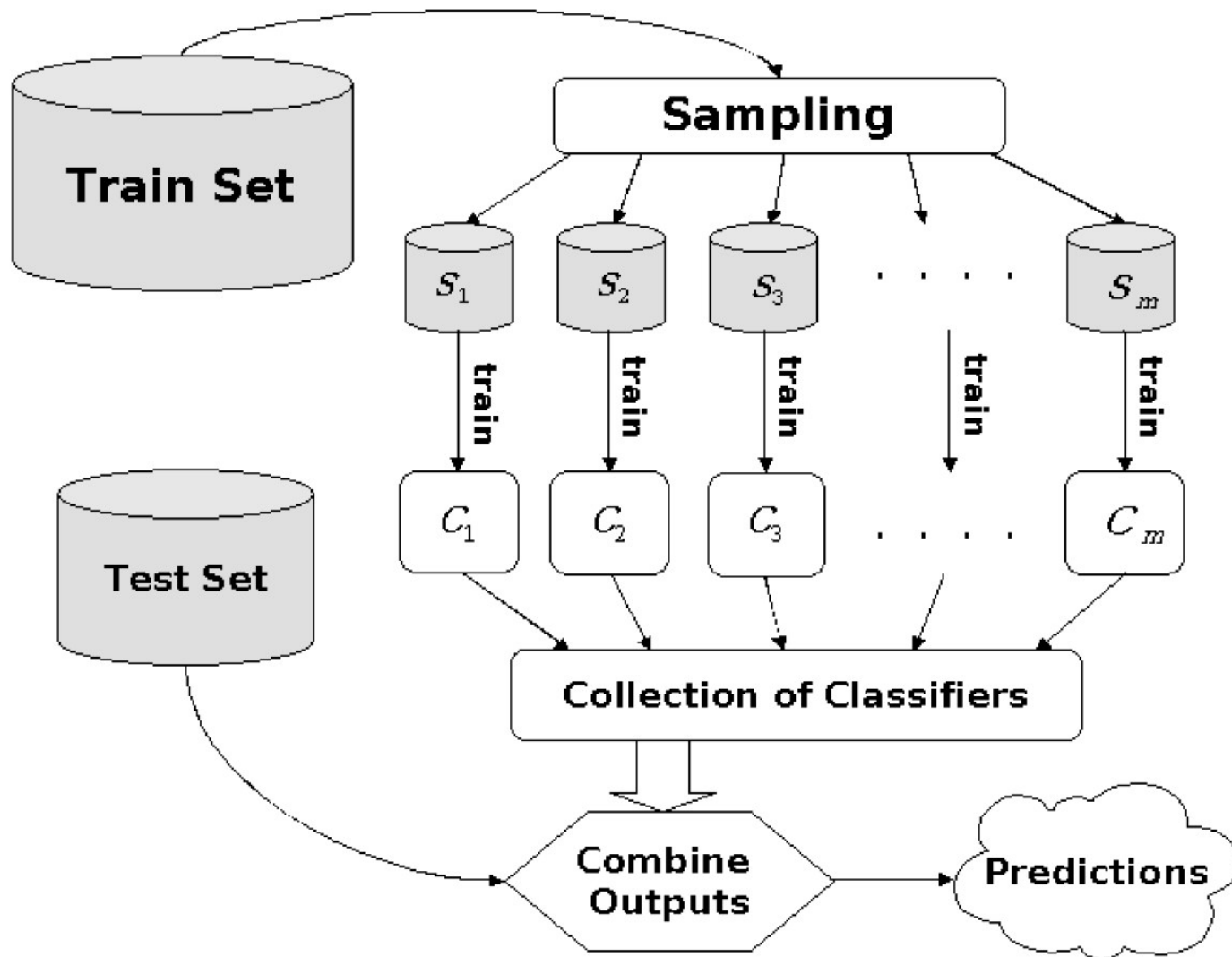


Deep Learning Methods



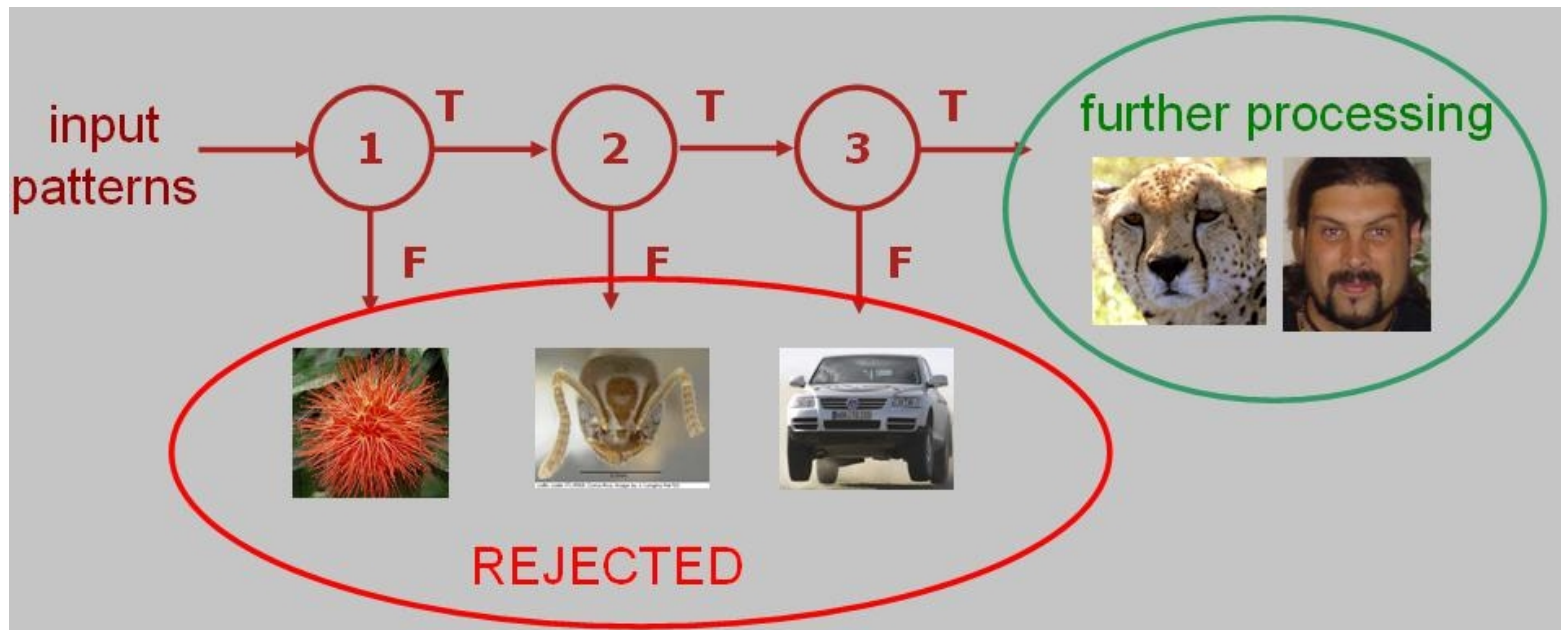
There are many ways to combine
classifiers...

Classifier Ensembles

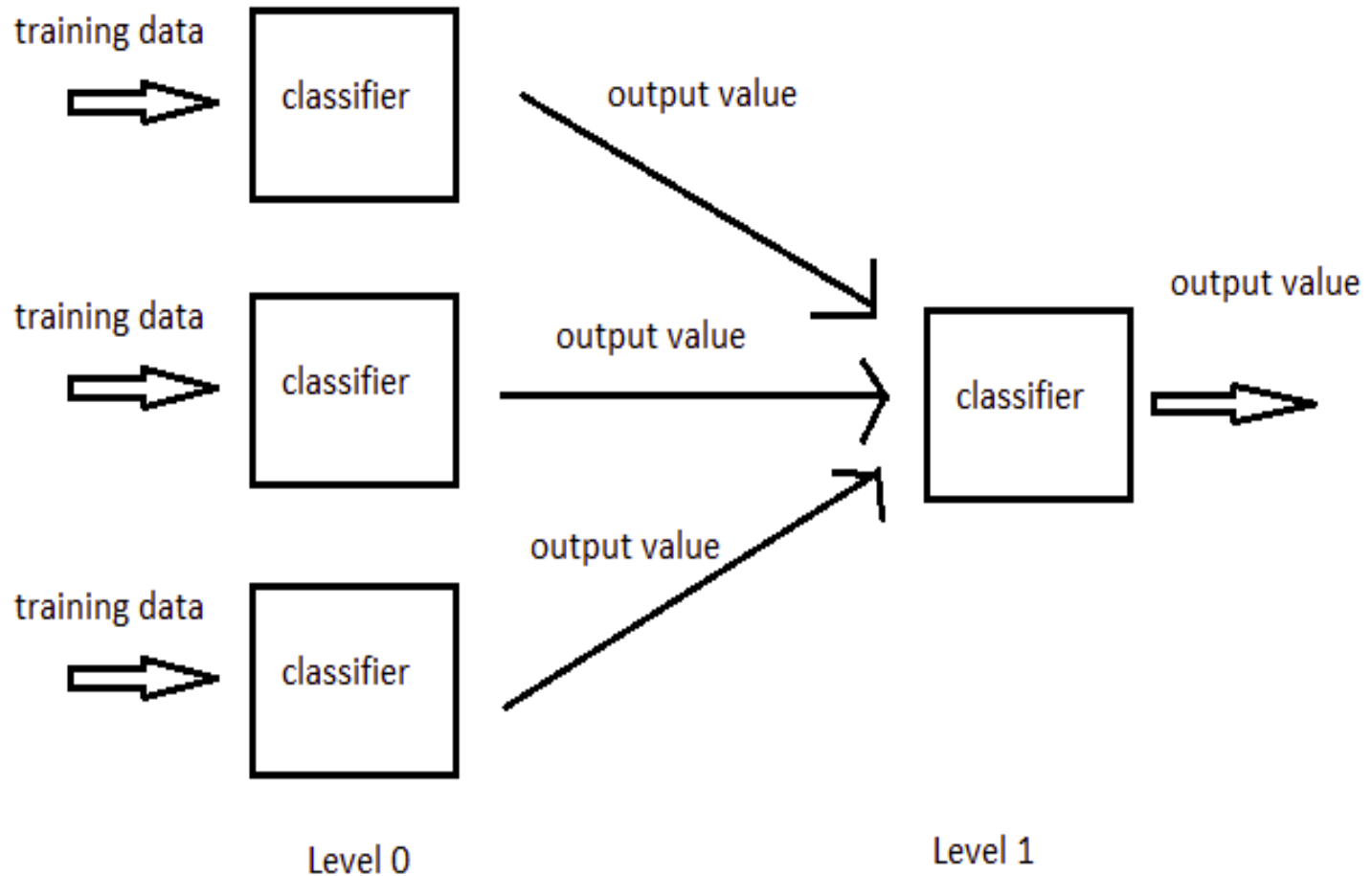


Boosting

Sequences of classifiers that
grows in complexity of classifier



Concept Diagram of Stacking



Discussion

What are some problems faced by our service robots which could benefit from a machine learning solution?

What are some common things in the environment that the robot could learn to classify?

Can a classifier be used for prediction?

Take-home message

“The decision to *use* machine learning is more important than the choice of a *particular* learning method.”

- James Hays, Brown University

Resources

- Introduction to Machine Learning textbook:
<http://alex.smola.org/drafts/thebook.pdf>
- WEKA Machine Learning Library (in Java):
<http://www.cs.waikato.ac.nz/ml/weka/>
- Support Vector Machine example using OpenCV:
http://docs.opencv.org/2.4/doc/tutorials/ml/introduction_to_svm/introduction_to_svm.html

THE END

