ACL2 Support for Interactive Proof

Matt Kaufmann The University of Texas at Austin Dept. of Computer Science

Chalmers, August 10, 2015

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Rewriting in ACL2

Demos (II)

Very Brief Survey of ACL2 Features

Conclusion

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But I may skip some material. I hope to leave lots of time for discussion. **Please ask questions** during the talk!

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- ▶ Workshop series: #13 is at UT, Oct. 1-2, 2015.

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► UT Austin: x86 interpreter defined in ACL2, validation by co-simulation, proofs about x86 machine code

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 See M. Kaufmann and J Moore, "Structured Theory Development for a Mechanized Logic." *Journal of Automated Reasoning* 26, no. 2 (2001) 161-203.

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A potential weakness: first-order logic with only basic quantifier support (but recursion helps).

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That talk mentions this link to several demos and their logs:

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Not included above is a larger example (a SASL unification program).

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 - ... but lemmas are usually needed (sometimes from libraries).

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```
[DEMO]: book demo-gl.lisp
(log demo-gl-log.txt)
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The documentation topic for rewrite shows many ways to control the rewriter (needed only occasionally). I'll mention only a few:

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ACL2 !>:pe fold-consts-in-+

(IMPLIES (AND (SYNTAXP (QUOTEP X))

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(EQUAL (+ X (+ Y Z)) (+ (+ X Y) Z))))

ACL2 !>
```

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B. Brock, M. Kaufmann, and J S. Moore. Rewriting with Equivalence Relations in ACL2. *J. Aut. Reasoning* 40 (2008).

M. Kaufmann and J S. Moore. Double Rewriting for Equivalential Reasoning in ACL2. *Proc. ACL2 Workshop* 2006.

M. Kaufmann and J S. Moore. Rough Diamond: An Extension of Equivalence-based Rewriting. *Proc. ITP* 2014.

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Our final demo shows how ACL2 proof development often follows "*the method*":

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- ► The user formulates **conditional rewrite rules** to simplify those checkpoints.
- Repeat.

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- DEMO (excerpted from my TPHOLs 2008 talk) -

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• ... by exploring briefly the ACL2 documentation.

NOTE:

I would be very happy to elaborate on any of these topics!

VERY BRIEF SURVEY OF ACL2 FEATURES (2)

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In particular, we might explore a few debugging features, as time and interest permit.

- accumulatedpersistence
- break-rewrite
- ► cgen
- cw-gstack
- disassemble\$
- ► dmr
- failed-forcing
- ► failure
- find-lemmas
- forward-chainingreports

- guard-debug
- measure-debug
- nil-goal
- ► print-gv
- ► profile-acl2
- ► profile-all
- ▶ proof-checker
- ► proof-tree
- pstack
- quick-and-dirtysubsumptionreplacement-step
- redo-flat

- remove-hyps
- set-debugger-enable
- set-guard-msg
- sneaky
- spacewalk
- ► splitter
- time-tracker
- ► trace
- walkabout
- watch

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