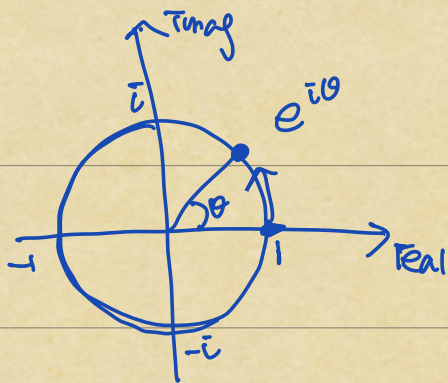
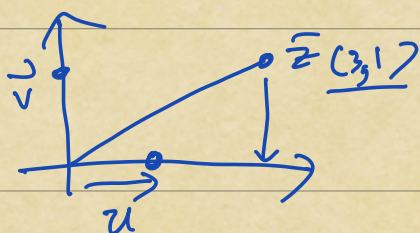
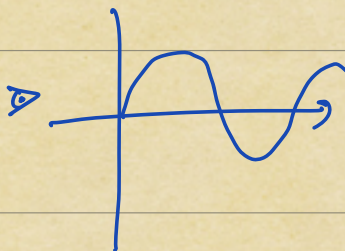




$$e^{i\theta} = \cos \theta + i \sin \theta$$

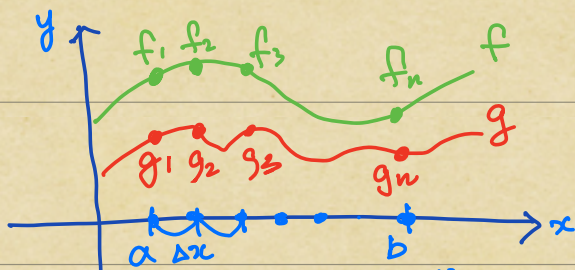


$$\vec{z} = \underbrace{\langle \vec{z}, \vec{u} \rangle}_3 \vec{u} + \underbrace{\langle \vec{z}, \vec{v} \rangle}_1 \vec{v}$$

$$\vec{v} = [v_1 \ v_2 \ v_3 \ \dots] \quad \vec{w} = [w_1 \ w_2 \ w_3 \ \dots]$$

$$\langle \vec{v}, \vec{w} \rangle = [v_1 \ v_2 \ v_3 \ \dots] \begin{bmatrix} w_1 \\ w_2 \\ \vdots \end{bmatrix}$$

$$= v_1 w_1 + v_2 w_2 + \dots$$



* inner product of ^{two} functions f, g

$$f = [f_1 \ f_2 \ \dots \ f_n]$$

$$g = [g_1 \ g_2 \ \dots \ g_n]$$

$$\langle f, g \rangle = \frac{(f_1 g_1 + f_2 g_2 + \dots + f_n g_n) \Delta x}{\Delta x = \frac{b-a}{n-1}}$$

$$f(x) = 1$$

$$g(x) = 2$$



$$n=4$$

$$n=8$$

$$\langle f, g \rangle = 1 \times 2 + 1 \times 2 = 8$$

$$= 1 \times 2 + 1 \times 2 = 16$$

$$\langle \underline{f(x)} \cdot \underline{g(x)} \rangle = \int_a^b f(x) \cdot \overline{g(x)} dx$$

represents how "similar" $f(x) \cdot g(x)$ / $f(x) \cdot g(x)$ involve complex #

$$C = a + ib$$

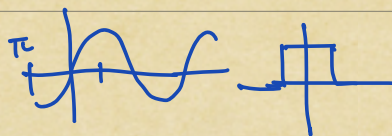
$$\bar{C} = a - ib \quad (\text{conjugate})$$

* Fourier series

suppose $f(x)$ be a periodic function $T = 2\pi$ $[-\pi, \pi]$

Fourier series shows that

f is an infinite sum of $\sin/\cos$ waves



$$f(x) = \sum_{k=-\infty}^{\infty} \langle \underline{f(x)} \cdot \underline{e^{ikx}} \rangle \underline{e^{ikx}}$$

$$= \frac{A_0}{2} + \sum_{n=1}^{\infty} (\underline{A_n} \cdot \cos(nx) + \underline{B_n} \cdot \sin(nx))$$

$$A_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \cdot \cos(nx) dx \quad B_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \cdot \sin(nx) dx$$

$$n=0 \quad \boxed{A_0 = \frac{1}{\pi} \int_{-\pi}^{\pi} f(x) dx} \quad B_0 = 0$$