Maintaining the ACL2 Theorem Proving System

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Introduction

Topic of this talk:

What sorts of challenges do we face in making our theorem prover useful in practice?

- Automated reasoning talks often focus on topics such as algorithms, logics, and applications.
- This talk will focus on the pragmatics of maintenance.

For more information:

- See the full paper.
- Try out ACL2 (with assistance of documentation and acl2-help email list): http://www.as.utexas.edu/users/moore/acl

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Imagine that we're going to lunch to have a chat about what we're doing to make automated reasoning useful in practice.

Before We Eat:

Some general background on ACL2

Main Course:

A selection of recent enhancements to ACL2

Dessert:

Discussion

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Before We Eat: Some general background on ACL2

- Introduction to ACL2
- Some milestones
- The user's view of ACL2: A small example
- Summary of some useful ACL2 features

ACL2 (ACL² = ACLACL): A Computational Logic for Applicative Common Lisp

- Programmed primarily in itself: forces attention to sufficient language features and efficiency; functional language facilitates maintenance (vs. Nqthm, e.g.)
- Has evolved with user feedback to see applications, follow "Books and Papers" link from ACL2 home page and then follow "Quick Summary" link
- Source files total 8.4M (Version 3.0.1)
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Some milestones

- 1971-73: Boyer/Moore "Edinburgh Pure Lisp Theorem Prover"
- ▶ 1979: Boyer and Moore, A Computational Logic
- 1986: Kaufmann joins Boyer/Moore project
- ▶ 1988: Boyer and Moore, A Computational Logic Handbook
- 1989: Boyer and Moore begin ACL2 (but continue to maintain Nqthm)
- 1992: Final release of Boyer-Moore "Nqthm" prover
- 1993: Kaufmann formally added as a co-author of ACL2
- 1999: First of six (so far) ACL2 workshops
- > 2000: Computer-Aided Reasoning: An Approach published
- 2006: Boyer, Kaufmann, and Moore win 2005 ACM Software System Award for Boyer-Moore family of provers

The user's view of ACL2: A small example

Example: the length is unchanged when a list is reversed. But first, a summary of ACL2 interaction (thanks, Robert Krug):

- ACL2 is entirely automatic once you start it.
- It has considerable built-in knowledge about predicate logic, linear arithmetic, equality reasoning, etc. — but this is rarely enough.
- Users can examine output of failed proofs to learn what needs to be done to succeed.
- In the example below, we see the typical activity of creating and proving a rewrite rule based on that output.
- Such helper lemmas, when well designed, can be reused automatically.
- There is a large body of proved theorems ("books") distributed with ACL2, containing just such rules.

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The Waterfall



I'll discuss this partial log:

```
ACL2 !>(defthm len-reverse
(equal (len (reverse x)) (len x)))
```

ACL2 Warning [Non-rec] in (DEFTHM LEN-REVERSE ...): A :REWRITE rule generated from LEN-REVERSE will be triggered only by terms containing the non-recursive function symbol REVERSE. Unless this function is disabled, this rule is unlikely ever to be used.

This simplifies, using the :definition REVERSE, to the following two conjectures.

The failed goal:

(IMPLIES (NOT (STRINGP X)) (EQUAL (LEN (REVAPPEND X NIL)) (LEN X)))

With a little thought we submit this rewrite rule, which will complete the proof of len-reverse.

(DEFTHM LEN-REVAPPEND (EQUAL (LEN (REVAPPEND X Y)) (+ (LEN X) (LEN Y))))

```
The failed goal:
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```

```
ACL2 !>(defthm len-revappend
         (equal (len (revappend x v))
                (+ (len x) (len y))))
Name the formula above *1
Perhaps we can prove *1 by induction. Three induction schemes are suggested by
this conjecture. These merge into two derived induction schemes. However, one
of these is flawed and so we are left with one viable candidate.
Time: 0.01 seconds (prove: 0.01, print: 0.00, other: 0.00)
 LEN-REVAPPEND
ACL2 !>(defthm len-reverse
         (equal (len (reverse x)) (len x)))
Summary
Form: ( DEFTHM LEN-REVERSE ...)
Rules: ((:DEFINITION LEN)
        (:REWRITE LEN-REVAPPEND)
        (:TYPE-PRESCRIPTION LEN))
Warnings: Non-rec
Time: 0.00 seconds (prove: 0.00, print: 0.00, other: 0.00)
LEN-REVERSE
ACT.2 1>
```

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```
ACL2 !>:pl len
```

Rune: (:REWRITE LEN-REVERSE) Status: Enabled Lhs: (LEN (REVERSE X)) Rhs: (LEN X) Hyps: T Equiv: EQUAL Backchain-limit-lst: NIL Subclass: ABBREVIATION Rune: (:REWRITE LEN-REVAPPEND) Status: Enabled ACL2 !>:pl (len (reverse (cons a b))) 1. LEN-REVERSE

New term: (LEN (CONS A B)) Hypotheses: <none> Equiv: EQUAL Substitution: ((X CONS A B))

Summary of some useful ACL2 features (1)

Note: This partial list is intended to set the stage for our discussion of maintenance.

- Documentation: over 1000 topics, organized hierarchically with hyperlinks (or 1200+ pages)
- Error messages and warnings
- Macros, and more via make-event
- Top-level read-eval-print loop provides interactive testing
- Efficient evaluation of ground terms in top-level loop and proofs, via guards, compilation, single-threaded objects, and mbe ("must be equal")
- Proof techniques: congruence-based conditional rewriting, many others
- Namespaces via Lisp packages

Summary of some useful ACL2 features (2)

- Books (files) of events (top-level forms): definitions (defun), and theorems (defthm), etc.
 - Certification and subsequent include-book
 - Local events present a logical and maintenance challenge but are very useful for scoping
 - About 1600 books in over 270 directories, contributed by many; useful for regression testing
- Encapsulate scoping mechanism also provides modularity; and it provides partial definitions
- A functional instantiation utility for a kind of "second-order" reasoning

Summary of some useful ACL2 features (3)

- User-installed simplifiers: meta-rules
- Proof control: rule classes, hints (explicit, computed, default), theories
- Database control: undo and undo-the-undo commands
- Interactive proof-checker: a goal manager providing the feel of tactic-based proof assistants but with ACL2 automation available
- Proof debug: proof-checker (above), inspection utility for rewriter loops, break-rewrite rewrite debugger, and proof-tree display for proof log navigation

Main Course: A selection of recent enhancements to ACL2

In the next few slides, we'll discuss a variety of examples that illustrate a range of maintenance tasks, largely in response to user feedback.

I'll keep the slides somewhat terse but provide verbal elaboration. Details may be found in the paper.

Subgoal counting

Ouch - "six constraints generated" yet only five subgoals!

We now augment the goal above by adding the hypothesis indicated by the :USE hint. This produces a propositional tautology. The hypothesis can be derived from AC-FN-LIST-REV via functional instantiation, provided we can establish the six constraints generated.

```
Subgoal 5
(EQUAL (TIMES-LIST X)
(IF (ATOM X)
1
(* (CAR X) (TIMES-LIST (CDR X))))).
```

But simplification reduces this to T, using the :definitions ATOM and TIMES-LIST and primitive type reasoning.

Subgoal 4

. . . .

After a fix:

We now augment provided we can establish the six constraints generated. By the simple :rewrite rules ASSOCIATIVITY-OF-* and UNICITY-OF-1 we reduce the six constraints to five subgoals.

A rough edge in theory control

```
Stack overflow!! The problem: evaluation of
(O<= (fact 65534) 0) in spite of the above disable,
from the following forward-chaining rule:
```

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(IMPLIES (AND (NOT (EQUAL A B))
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Solution: Evaluator that comprehends which rules are enabled.

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These improvements came out of user feedback and were regression tested:

- Avoid certain infinite loops during destructor elimination
- Avoid forward-chaining from a rewritten term
- Avoid certain infinite loops due to interaction of equality reasoning with opening up of recursive functions
- Limit subsumption checks (to 1,000,000 matcher calls)

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A library improvement using MBE (1)

- Many distributed books undergo improvements
- One such set of books is known as the rtl library
- At AMD, we needed more efficient execution

A library improvement using MBE (2)

Old definition of (bits x i j) used floor, mod, and exponentiation:

```
(if (or (not (integerp i)) (not (integerp j)))
     0
   (fl (/ (mod x (expt 2 (1+ i)))
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Now, bits executes using bitwise-and and shift:

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- Set-enforce-redundancy allows user to enforce a style of book management, where proofs are kept in subsidiary books
- Disabledp, like other commands, allows a macro to be an alias for a function
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Portability

We support all major Common Lisp implementations of which we are aware:

- Gnu Common Lisp (GCL)
- OpenMCL
- Allegro Common Lisp
- SBCL
- CMU Common Llsp
- CLISP
- Lispworks

Why support so many platforms?

- Catch bugs
- User choice (e.g., profilers vary)
- Support experimentation (e.g., parallelism in OpenMCL and SBCL (Rager), hash-cons in GCL and OpenMCL (Boyer/Hunt))

Namespace control

Lisp (and ACL2) *packages* provide namespace control: e.g., the same string "ABC" can name a symbol in two different packages. There have been several bugs involving packages:

- Disallow "LISP" package (exists already in some implementations, not others)
- Require uppercase package names at least one Lisp gets this wrong
- Hand-coded function to execute pkg-witness: bug recently found in its default behavior for non-strings

- Improved reporting in rewriter's debugger (break-rewrite) for free variables
- Several bugs related to local presents a serious challenge to implementing logic!
- Double-rewrite utility to override the rewriter's caching of results in the presence of congruences (see recent ACL2 workshop paper)
- Miscellaneous bug fixes, e.g., in timing utility and handling of Lisp type specs (satisfies)
- Recent performance enhancements, especially for theories: Critical for users at Rockwell Collins
- Prover time limits
- Context recovery for failed proofs (redo-flat)

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A final note: Throughout maintenance we make some effort to maintain backward compatibility:

- Support for user community
- Regression suite is critical

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