

## Control Flow Graphs

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## Optimizations

- Code transformations to improve program
  - Mainly: improve execution time
  - Also: reduce program size
- Can be done at high level or low level
  - E.g., constant folding
- Optimizations must be safe
  - Execution of transformed code must yield same results as the original code for **all possible executions**

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## Optimization Safety

- Safety of code transformations usually requires certain information that may not be explicit in the code
- Example: dead code elimination
  - (1)  $x = y + 1;$
  - (2)  $y = 2 * z;$
  - (3)  $x = y + z;$
  - (4)  $z = 1;$
  - (5)  $z = x;$
- What statements are dead and can be removed?

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## Optimization Safety

- Safety of code transformations usually requires certain information which may not be explicit in the code
- Example: dead code elimination
  - (1)  $x = y + 1;$
  - (2)  $y = 2 * z;$
  - (3)  $x = y + z;$
  - (4)  $z = 1;$
  - (5)  $z = x;$
- Need to know whether values assigned to  $x$  at (1) is never used later (i.e.,  $x$  is dead at statement (1))
  - Obvious for this simple example (with no control flow)
  - Not obvious for complex flow of control

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## Dead Variable Example

- Add control flow to example:

```
x = y + 1;  
y = 2 * z;  
if (d) x = y+z;  
z = 1;  
z = x;
```

- Is 'x = y+1' dead code? Is 'z = 1' dead code?

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## Dead Variable Example

- Add control flow to example:

```
x = y + 1;  
y = 2 * z;  
if (d) x = y+z;  
z = 1;  
z = x;
```



- Statement x = y+1 is not dead code!
- On **some executions**, value is used later

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## Dead Variable Example

- Add more control flow:

```
while (c) {  
  x = y + 1;  
  y = 2 * z;  
  if (d) x = y+z;  
  z = 1;  
}  
z = x;
```

- Is 'x = y+1' dead code? Is 'z = 1' dead code?

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## Dead Variable Example

- Add more control flow:

```
while (c) {  
  x = y + 1;  
  y = 2 * z;  
  if (d) x = y+z;  
  z = 1;  
}  
z = x;
```



- Statement 'x = y+1' not dead (as before)
- Statement 'z = 1' not dead either!
- On **some executions**, value from 'z=1' is used later

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## Low-level Code

- Harder to eliminate dead code in low-level code:

```
label L1
fjump c L2
x = y + 1;
y = 2 * z;
fjump d L3
x = y+z;
label L3
z = 1;
jump L1
label L2
z = x;
```

Are these statements dead?

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jump L1
label L2
z = x;
```

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## Optimizations and Control Flow

- Application of optimizations requires information
  - Dead code elimination: need to know if variables are dead when assigned values
- Required information:
  - Not explicit in the program
  - Must compute it **statically (at compile-time)**
  - Must characterize **all dynamic (run-time) executions**
- Control flow makes it hard to extract information
  - Branches and loops in the program
  - Different executions = different branches taken, different number of loop iterations executed

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## Control Flow Graphs

- **Control Flow Graph (CFG)** = graph representation of computation and control flow in the program
  - framework for static analysis of program control-flow
- Nodes are **basic blocks** = straight-line, single-entry code, no branching except at end of sequence
- Edges represent possible flow of control from the end of one block to the beginning of the other
  - There may be multiple incoming/outgoing edges for each block

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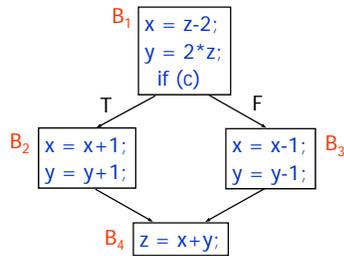
## CFG Example

### Program

```

x = z-2 ;
y = 2*z;
if (c) {
  x = x+1;
  y = y+1;
}
else {
  x = x-1;
  y = y-1;
}
z = x+y;
    
```

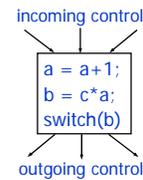
### Control Flow Graph



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## Basic Blocks

- **Basic block** = sequence of consecutive statements such that:
  - Control enters only at beginning of sequence
  - Control leaves only at end of sequence



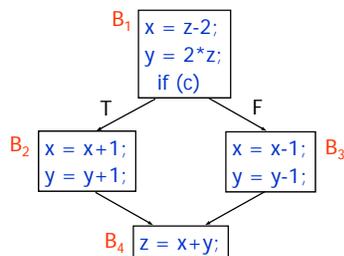
- No branching in or out in the middle of basic blocks

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## Computation and Control Flow

### Control Flow Graph

- Basic Blocks = Nodes in the graph = computation in the program
- Edges in the graph = control flow in the program

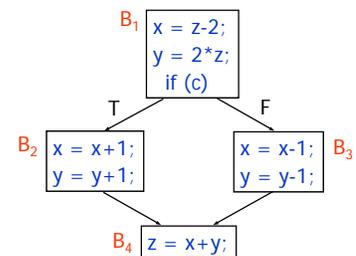


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## Multiple Program Executions

- CFG models all program executions
- Possible execution = path in the graph
- Multiple paths = multiple possible program executions

### Control Flow Graph



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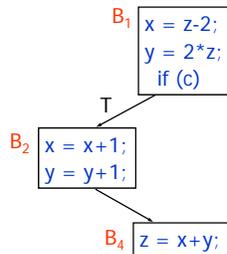
## Execution 1

- CFG models all program executions

- Possible execution = path in the graph

- Execution 1:
  - c is true
  - Program executes basic blocks  $B_1$ ,  $B_2$ ,  $B_4$

### Control Flow Graph



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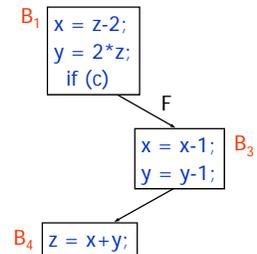
## Execution 2

- CFG models all program executions

- Possible execution = path in the graph

- Execution 2:
  - c is false
  - Program executes basic blocks  $B_1$ ,  $B_3$ ,  $B_4$

### Control Flow Graph



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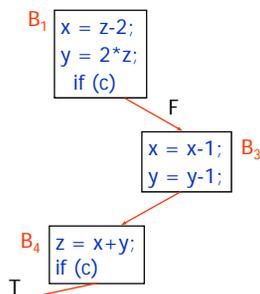
## Infeasible Executions

- CFG models all program executions, and then some

- Possible execution = path in the graph

- Execution 2:
  - c is false and true (!)
  - Program executes basic blocks  $B_1$ ,  $B_3$ ,  $B_4$
  - and the T successor of  $B_4$

### Control Flow Graph

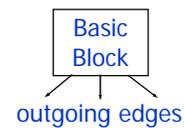


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## Edges Going Out

- Multiple outgoing edges

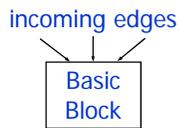
- Basic block executed next may be one of the successor basic blocks
- Each outgoing edge = outgoing flow of control in some execution of the program



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## Edges Coming In

- Multiple incoming edges
- Control **may** come from any of the predecessor basic blocks
- Each incoming edge = incoming flow of control in some execution of the program



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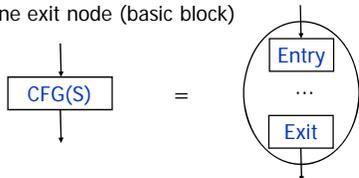
## Building the CFG

- Can construct CFG for either high-level IR or the low-level IR of the program
- Build CFG for high-level IR
  - Construct CFG for each high-level IR node
- Build CFG for low-level IR
  - Analyze jump and label statements

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## CFG for High-level IR

- $CFG(S)$  = flow graph of high-level statement  $S$
- $CFG(S)$  is single-entry, single-exit graph:
  - one entry node (basic block)
  - one exit node (basic block)

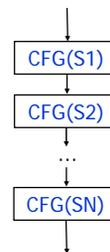


- Recursively define  $CFG(S)$

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## CFG for Block Statement

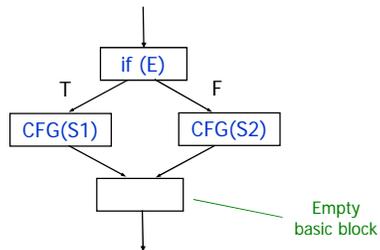
- $CFG(S_1; S_2; \dots; S_N) =$



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## CFG for If-then-else Statement

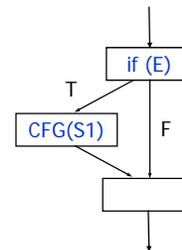
- CFG ( if (E) S1 else S2 )



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## CFG for If-then Statement

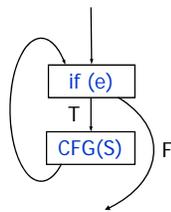
- CFG( if (E) S )



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## CFG for While Statement

- CFG for: while (e) S



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## Recursive CFG Construction

- Nested statements: recursively construct CFG while traversing IR nodes

- Example:

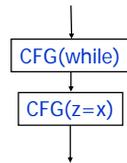
```
while (c) {  
    x = y + 1;  
    y = 2 * z;  
    if (d) x = y+z;  
    z = 1;  
}  
z = x;
```

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## Recursive CFG Construction

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  if (d) x = y+z;
  z = 1;
}
z = x;
```

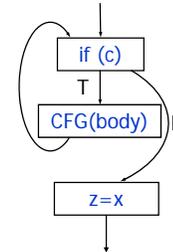


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  z = 1;
}
z = x;
```

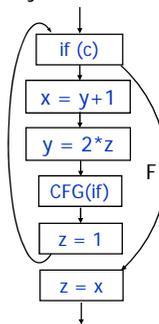


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## Recursive CFG Construction

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while (c) {
  x = y + 1;
  y = 2 * z;
  if (d) x = y+z;
  z = 1;
}
z = x;
```



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## Recursive CFG Construction

- Simple algorithm to build CFG
- Generated CFG
  - Each basic block has a single statement
  - There are empty basic blocks
- Small basic blocks = inefficient
  - Small blocks = many nodes in CFG
  - Compiler uses CFG to perform optimization
  - Many nodes in CFG = compiler optimizations will be time- and space-consuming

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## Efficient CFG Construction

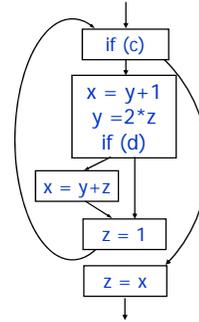
- Basic blocks in CFG:
  - As few as possible
  - As large as possible
- There should be no pair of basic blocks (B1,B2) such that:
  - B2 is a successor of B1
  - B1 has one outgoing edge
  - B2 has one incoming edge
- There should be no empty basic blocks

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## Example

- Efficient CFG:

```
while (c) {
    x = y + 1;
    y = 2 * z;
    if (d) x = y+z;
    z = 1;
}
z = x;
```



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## CFG for Low-level IR

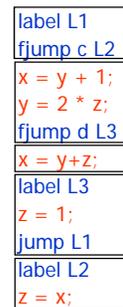
- Identify pre-basic blocks as sequences of:
  - Non-branching instructions
  - Non-label instructions
- No branches (jump) instructions = control doesn't flow out of basic blocks
- No labels instructions = control doesn't flow into blocks

```
label L1
fjump c L2
x = y + 1;
y = 2 * z;
fjump d L3
x = y+z;
label L3
z = 1;
jump L1
label L2
z = x;
```

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## CFG for Low-level IR

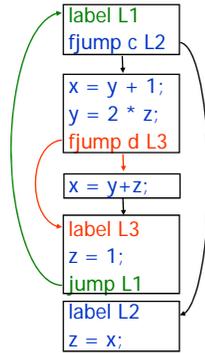
- Basic block start:
  - At label instructions
  - After jump instructions
- Basic blocks end:
  - At jump instructions
  - Before label instructions



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## CFG for Low-level IR

- Conditional jump:  
2 successors
- Unconditional jump:  
1 successor



## CFG for Low-level IR

