

# Practical Vision-Based Monte Carlo Localization on a Legged Robot

Mohan Sridharan    Gregory Kuhlmann    Peter Stone

Learning Agents Research Group  
Department of Computer Sciences  
The University of Texas at Austin

IEEE International Conference on Robotics and Automation,  
2005

# The Problem

## Mobile Robot Localization

Maintain **estimate** of global **position** and **orientation** over time

- Given **map** of fixed landmark locations
- **Not SLAM**

# The Problem

## Mobile Robot Localization

Maintain **estimate** of global **position** and **orientation** over time

- Given **map** of fixed landmark locations
- **Not SLAM**

# Challenging Platform

## Typical Platform

- Wheeled robot
- Range-finding sensors

## Sony Aibo ERS-7

- Color **CMOS Camera** in nose
  - Narrow field-of-view ( $56^\circ$ )
  - 30 YCrCb frames per second
- **Quadruped**
- 576MHz processor
  - All **on-board processing**

# Challenging Platform

## Our Platform

- Legged robot
- Vision-based sensors

### Sony Aibo ERS-7

- Color **CMOS Camera** in nose
  - Narrow field-of-view ( $56^\circ$ )
  - 30 YCrCb frames per second
- **Quadruped**
- 576MHz processor
  - All **on-board processing**



# Goal

## Desiderata

- Navigate to **specific point** quickly
- Remain localized while **colliding**
- Recover quickly from **kidnappings**

## Approach

- Begin with **baseline** MCL algorithm
- Add set of practical **enhancements**

Large improvement over baseline

# Goal

## Desiderata

- Navigate to **specific point** quickly
- Remain localized while **colliding**
- Recover quickly from **kidnappings**

## Approach

- Begin with **baseline** MCL algorithm
- Add set of practical **enhancements**

Large improvement over baseline

# Goal

## Desiderata

- Navigate to **specific point** quickly
- Remain localized while **colliding**
- Recover quickly from **kidnappings**

## Approach

- Begin with **baseline** MCL algorithm
- Add set of practical **enhancements**

**Large improvement over baseline**

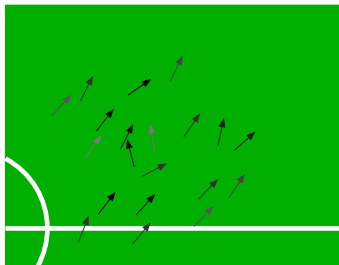


# Method: Particle Filtering

- Estimate  $p(h_T | o_T, a_{T-1}, o_{T-1}, a_{T-2}, \dots, a_0)$ :  
Distribution of **poses** given observations and actions
- Represented by finite set of samples: particles
  - Each is a hypothesis:  $\langle \langle x, y, \theta \rangle, p \rangle$
- Average to get single estimate of pose and confidence

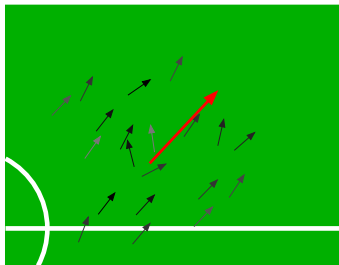
# Method: Particle Filtering

- Estimate  $p(h_T | o_T, a_{T-1}, o_{T-1}, a_{T-2}, \dots, a_0)$ :  
Distribution of poses given observations and actions
- Represented by finite set of samples: **particles**
  - Each is a hypothesis:  $\langle \langle x, y, \theta \rangle, p \rangle$
- Average to get single estimate of pose and confidence



# Method: Particle Filtering

- Estimate  $p(h_T | o_T, a_{T-1}, o_{T-1}, a_{T-2}, \dots, a_0)$ :  
 Distribution of poses given observations and actions
- Represented by finite set of samples: particles
  - Each is a hypothesis:  $\langle \langle x, y, \theta \rangle, p \rangle$
- Average to get **single estimate** of pose and confidence



# Outline

- 1 **Practical Enhancements**
  - Distance-Based Updates
  - Landmark Histories
  - Extended Motion Model
  
- 2 **Empirical Results**
  - Physical Robot Experiments
  - Simulation Experiments

# Outline

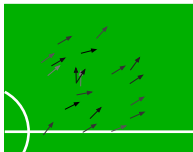
- 1 Practical Enhancements
  - Distance-Based Updates
  - Landmark Histories
  - Extended Motion Model
- 2 Empirical Results
  - Physical Robot Experiments
  - Simulation Experiments

# Baseline: Observation Update

- Need **sensor model**:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- Update each particle when robot sees something
  - Compute similarity for each observed landmark in frame
    - Use angles only [Rofer and Jungel, 2003]
    - Measured and expected angle difference
  - Compute product of similarities
  - Adjust probability closer to new value

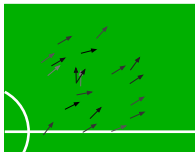
# Baseline: Observation Update

- Need sensor model:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- **Update** each particle **when robot sees something**
  - Compute similarity for each observed landmark in frame
    - Use angles only [Rofer and Jungel, 2003]
    - Measured and expected angle difference
  - Compute product of similarities
  - Adjust probability closer to new value



# Baseline: Observation Update

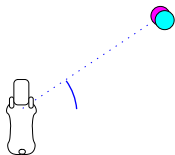
- Need sensor model:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- Update each particle when robot sees something
  - Compute **similarity** for each observed landmark in frame
    - Use **angles only** [Rofer and Jungel, 2003]
    - Measured and expected angle difference
  - Compute product of similarities
  - Adjust probability closer to new value





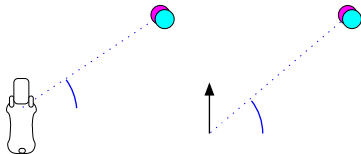
# Baseline: Observation Update

- Need sensor model:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- Update each particle when robot sees something
  - Compute similarity for each observed landmark in frame
    - Use angles only [Rofer and Jungel, 2003]
    - **Measured** and expected angle difference
  - Compute product of similarities
  - Adjust probability closer to new value



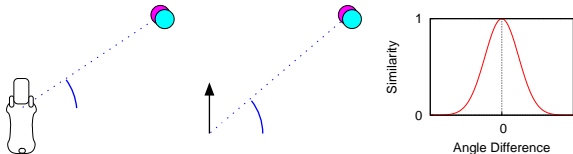
# Baseline: Observation Update

- Need sensor model:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- Update each particle when robot sees something
  - Compute similarity for each observed landmark in frame
    - Use angles only [Rofer and Jungel, 2003]
    - Measured and **expected** angle difference
  - Compute product of similarities
  - Adjust probability closer to new value



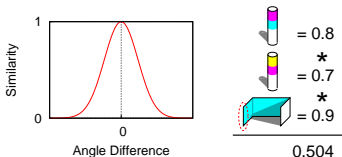
# Baseline: Observation Update

- Need sensor model:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- Update each particle when robot sees something
  - Compute similarity for each observed landmark in frame
    - Use angles only [Rofer and Jungel, 2003]
    - Measured and expected angle **difference**
  - Compute product of similarities
  - Adjust probability closer to new value



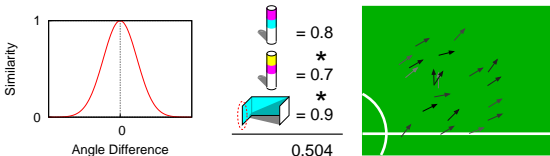
# Baseline: Observation Update

- Need sensor model:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- Update each particle when robot sees something
  - Compute similarity for each observed landmark in frame
    - Use angles only [Rofer and Jungel, 2003]
    - Measured and expected angle difference
  - Compute **product of similarities**
  - Adjust probability closer to new value



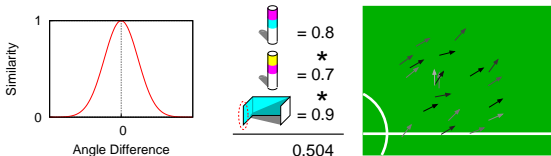
# Baseline: Observation Update

- Need sensor model:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- Update each particle when robot sees something
  - Compute similarity for each observed landmark in frame
    - Use angles only [Rofer and Jungel, 2003]
    - Measured and expected angle difference
  - Compute product of similarities
  - **Adjust probability** closer to new value



# Baseline: Observation Update

- Need sensor model:  $p(o|h)$ 
  - Predicts observations given pose hypothesis using map
- Update each particle when robot sees something
  - Compute similarity for each observed landmark in frame
    - Use angles only [Rofer and Jungel, 2003]
    - Measured and expected angle difference
  - Compute product of similarities
  - Adjust probability **closer to new value**

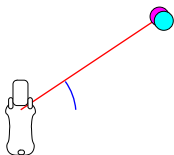


# Enhancement: Distance-Based Updates

- Enhancement to **observation update**
  - Use **distance** in addition to **angle**
- Update each particle
  - Difference between measured and expected distance
  - Use average of distance and angle similarities
- **Distances must be very accurate**

# Enhancement: Distance-Based Updates

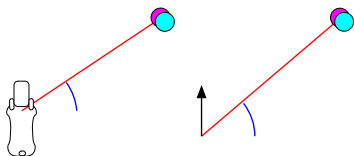
- Enhancement to observation update
  - Use **distance** in addition to **angle**
- Update each particle
  - Difference between **measured** and expected distance
  - Use average of distance and angle similarities
- Distances must be very accurate





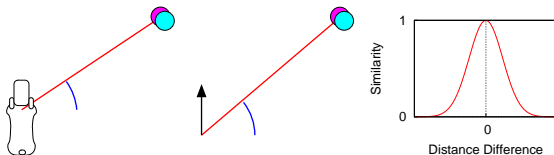
# Enhancement: Distance-Based Updates

- Enhancement to observation update
  - Use **distance** in addition to **angle**
- Update each particle
  - Difference between **measured** and **expected** distance
  - Use average of distance and angle similarities
- Distances must be very accurate



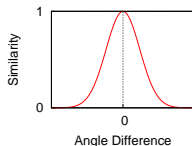
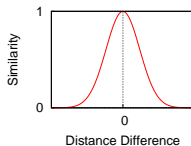
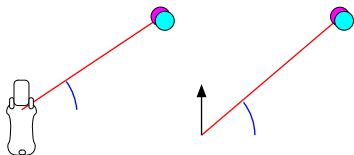
# Enhancement: Distance-Based Updates

- Enhancement to observation update
  - Use **distance** in addition to **angle**
- Update each particle
  - Difference between measured and expected distance
  - Use average of **distance** and angle similarities
- Distances must be very accurate



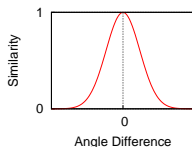
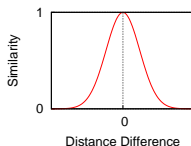
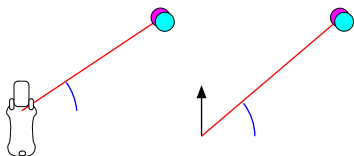
# Enhancement: Distance-Based Updates

- Enhancement to observation update
  - Use **distance** in addition to **angle**
- Update each particle
  - Difference between measured and expected distance
  - Use average of **distance** and **angle** similarities
- Distances must be very accurate



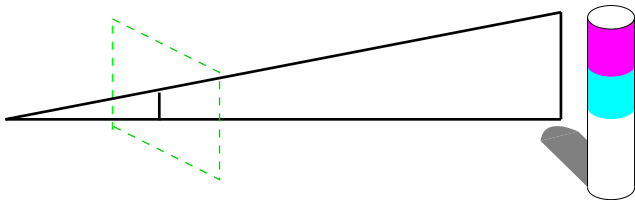
# Enhancement: Distance-Based Updates

- Enhancement to observation update
  - Use **distance** in addition to **angle**
- Update each particle
  - Difference between measured and expected distance
  - Use average of distance and angle similarities
- **Distances must be very accurate**



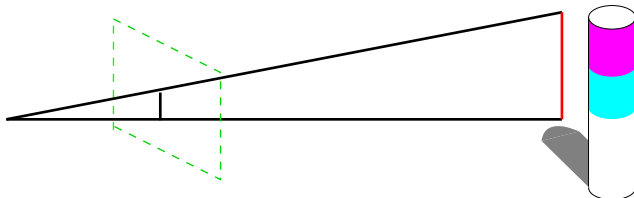
# Estimating Landmark Distances

- Know actual height of beacon and focal length of camera
- Measure height of beacon in image
- Use similar triangles to find distance
- **Error** due to pixelized segmentation, distortion, etc.



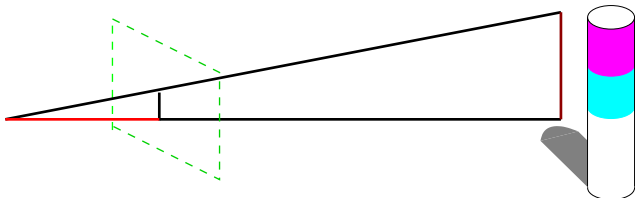
# Estimating Landmark Distances

- Know **actual height of beacon** and focal length of camera
- Measure height of beacon in image
- Use similar triangles to find distance
- **Error** due to pixelized segmentation, distortion, etc.



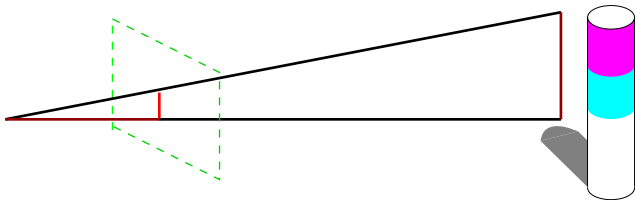
# Estimating Landmark Distances

- Know actual height of beacon and **focal length of camera**
- Measure height of beacon in image
- Use similar triangles to find distance
- **Error** due to pixelized segmentation, distortion, etc.



# Estimating Landmark Distances

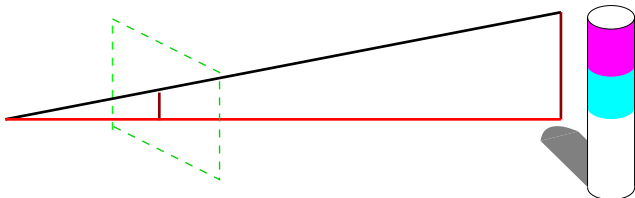
- Know actual height of beacon and focal length of camera
- Measure **height of beacon in image**
- Use similar triangles to find distance
- **Error** due to pixelized segmentation, distortion, etc.





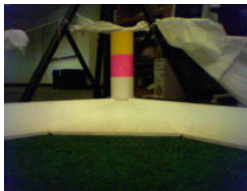
# Estimating Landmark Distances

- Know actual height of beacon and focal length of camera
- Measure height of beacon in image
- Use similar triangles to find **distance**
- **Error** due to pixelized segmentation, distortion, etc.



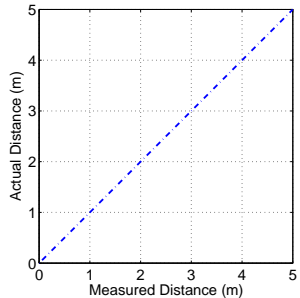
# Estimating Landmark Distances

- Know actual height of beacon and focal length of camera
- Measure height of beacon in image
- Use similar triangles to find distance
- **Error** due to pixelized segmentation, distortion, etc.



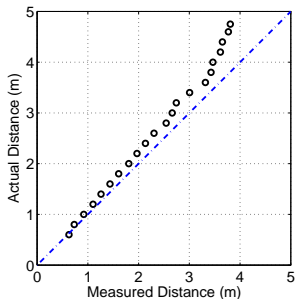
# Function Approximation

- Place robot at **known distances**
- Actual and Measured don't match (Nonlinear relationship)
- Approximate function using cubic regression for each landmark
- Maximum error reduced to 5%



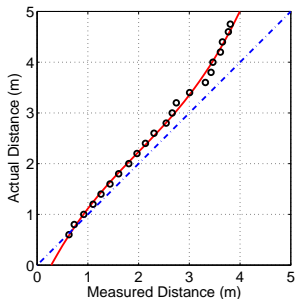
# Function Approximation

- Place robot at known distances
- Actual and Measured **don't match**  
 (Nonlinear relationship)
- Approximate function using cubic regression for each landmark
- Maximum error reduced to 5%



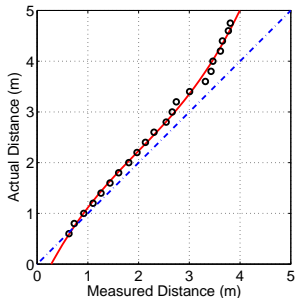
# Function Approximation

- Place robot at known distances
- Actual and Measured don't match (Nonlinear relationship)
- **Approximate function** using cubic regression **for each landmark**
- Maximum error reduced to 5%



# Function Approximation

- Place robot at known distances
- Actual and Measured don't match (Nonlinear relationship)
- **Approximate function** using cubic regression **for each landmark**
- Maximum error reduced to **5%**

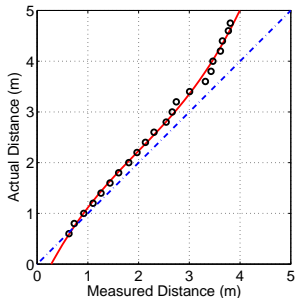


# Function Approximation

- Place robot at known distances
- Actual and Measured don't match (Nonlinear relationship)
- **Approximate function** using cubic regression **for each landmark**
- Maximum error reduced to **5%**

## Result

**Distances safe to use.**



# Outline

- 1 **Practical Enhancements**
  - Distance-Based Updates
  - **Landmark Histories**
  - Extended Motion Model
- 2 Empirical Results
  - Physical Robot Experiments
  - Simulation Experiments

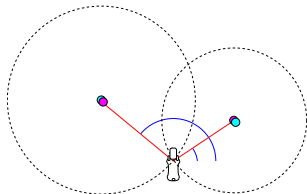
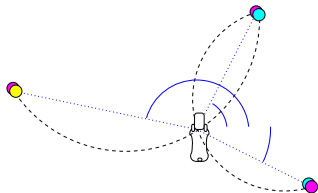


## Baseline: Reseeding

- Based on **Sensor Resetting MCL** [Lenser et al., 2000]
  - Helps **recovery when lost**
- Triangulate position using multiple landmarks
  - Three landmarks using just **angles**
  - Two landmarks using **distances** and **angles**
- Add new hypotheses before resampling step

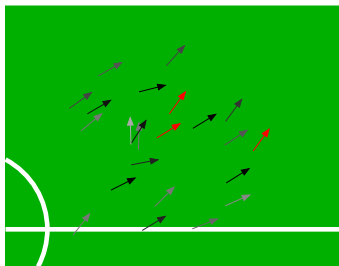
## Baseline: Reseeding

- Based on Sensor Resetting MCL [Lenser et al., 2000]
  - Helps recovery when lost
- **Triangulate** position using multiple landmarks
  - Three landmarks using just **angles**
  - Two landmarks using **distances** and **angles**
- Add new hypotheses before resampling step



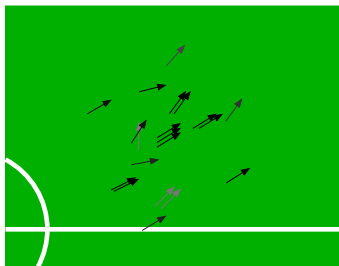
## Baseline: Reseeding

- Based on Sensor Resetting MCL [Lenser et al., 2000]
  - Helps recovery when lost
- Triangulate position using multiple landmarks
  - Three landmarks using just **angles**
  - Two landmarks using **distances** and **angles**
- **Add new hypotheses** before resampling step



## Baseline: Reseeding

- Based on Sensor Resetting MCL [Lenser et al., 2000]
  - Helps recovery when lost
- Triangulate position using multiple landmarks
  - Three landmarks using just **angles**
  - Two landmarks using **distances** and **angles**
- Add new hypotheses before **resampling step**



## Baseline: Reseeding

- Based on Sensor Resetting MCL [Lenser et al., 2000]
  - Helps recovery when lost
- Triangulate position using multiple landmarks
  - Three landmarks using just **angles**
  - Two landmarks using **distances** and **angles**
- Add new hypotheses before resampling step

### Shortcoming

- Robot must see multiple landmarks **in the same frame**
  - Infrequent with **narrow field-of-view** camera

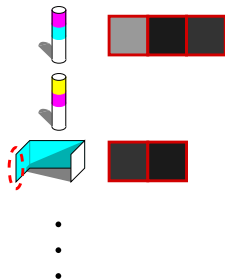
# Enhancement: Landmark Histories

- Want **more reseeding values**
  - Maintain **“history”** of recent observations
- Observation list for each landmark
  - Record: Dist, Ang, Conf, Timestamp, Odometer
- Motion update
- Confidence decay
- Remove old
- Weighted average
- Combine for reseed

# Enhancement: Landmark Histories

- Want more reseeding values
  - Maintain “history” of recent observations
- **Observation list** for each landmark
  - Record: Dist, Ang, Conf, Timestamp, Odometer

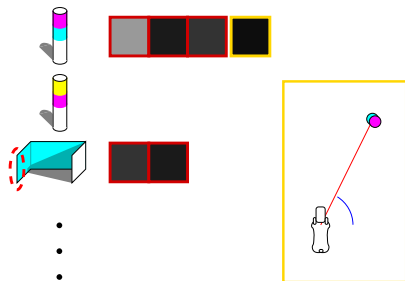
- Motion update
- Confidence decay
- Remove old
- Weighted average
- Combine for reseed



# Enhancement: Landmark Histories

- Want more reseeding values
  - Maintain “history” of recent observations
- Observation list for each landmark
  - Record:** Dist, Ang, Conf, Timestamp, Odometer

- Motion update
- Confidence decay
- Remove old
- Weighted average
- Combine for reseed

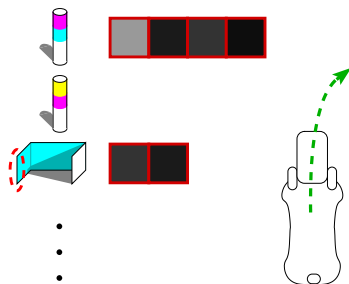




# Enhancement: Landmark Histories

- Want more reseeding values
  - Maintain “history” of recent observations
- Observation list for each landmark
  - Record: Dist, Ang, Conf, Timestamp, Odometer

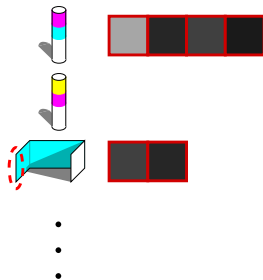
- Motion update**
- Confidence decay
- Remove old
- Weighted average
- Combine for reseed



# Enhancement: Landmark Histories

- Want more reseeding values
  - Maintain “history” of recent observations
- Observation list for each landmark
  - Record: Dist, Ang, Conf, Timestamp, Odometer

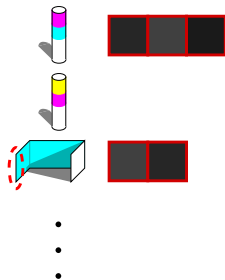
- Motion update
- Confidence decay**
- Remove old
- Weighted average
- Combine for reseed



# Enhancement: Landmark Histories

- Want more reseeding values
  - Maintain “history” of recent observations
- Observation list for each landmark
  - Record: Dist, Ang, Conf, Timestamp, Odometer

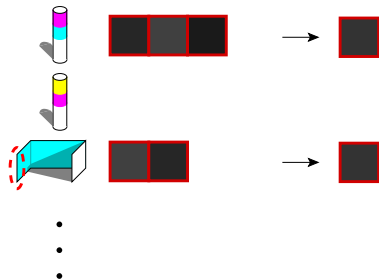
- Motion update
- Confidence decay
- **Remove old**
- Weighted average
- Combine for reseed



# Enhancement: Landmark Histories

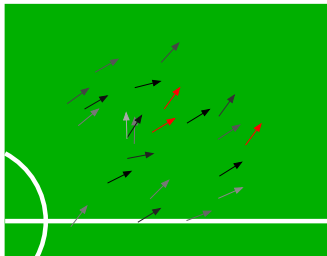
- Want more reseeding values
  - Maintain “history” of recent observations
- Observation list for each landmark
  - Record: Dist, Ang, Conf, Timestamp, Odometer

- Motion update
- Confidence decay
- Remove old
- Weighted average**
- Combine for reseed



# Enhancement: Landmark Histories

- Want more reseeding values
  - Maintain “history” of recent observations
- Observation list for each landmark
  - Record: Dist, Ang, Conf, Timestamp, Odometer
- Motion update
- Confidence decay
- Remove old
- Weighted average
- **Combine for reseed**

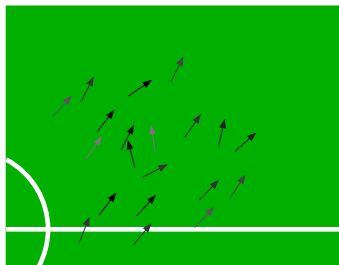
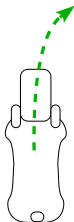


# Outline

- 1 Practical Enhancements
  - Distance-Based Updates
  - Landmark Histories
  - **Extended Motion Model**
- 2 Empirical Results
  - Physical Robot Experiments
  - Simulation Experiments

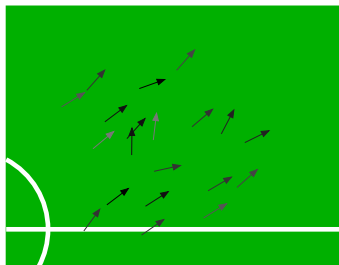
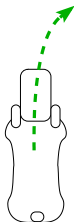
# Baseline: Motion Update

- Need **motion model**:  $p(h'|h, a)$ 
  - Predict new pose given previous hypothesis and action
- **Update** each particle **when robot moves**
  - Use **odometry** velocities to translate particles



# Baseline: Motion Update

- Need **motion model**:  $p(h'|h, a)$ 
  - Predict new pose given previous hypothesis and action
- **Update** each particle **when robot moves**
  - Use **odometry** velocities to **translate particles**





# Enhancement: Extended Motion Model

## Problem

- Tradeoff between **speed** and **motion model accuracy**
  - Large steps over small distances inaccurate
  - Unable to navigate to specific point

## Solution: Change Behavior

- Use accurate but slower walk near target

# Enhancement: Extended Motion Model

## Problem

- Tradeoff between speed and motion model accuracy
  - Large steps over small distances inaccurate
  - Unable to navigate to specific point

## Solution: Change Behavior

- Use accurate but slower walk near target

# Enhancement: Extended Motion Model

## Problem

- Tradeoff between speed and motion model accuracy
  - Large steps over small distances inaccurate
  - Unable to navigate to **specific point**

## Solution: Change Behavior

- Use accurate but slower walk near target

# Enhancement: Extended Motion Model

## Problem

- Tradeoff between speed and motion model accuracy
  - Large steps over small distances inaccurate
  - Unable to navigate to specific point

## Solution: Change Behavior

- Use **accurate but slower** walk near target
  - Step size reduced to 10% within 300mm of target

# Enhancement: Extended Motion Model

## Problem

- Tradeoff between speed and motion model accuracy
  - Large steps over small distances inaccurate
  - Unable to navigate to specific point

## Solution: Change Behavior

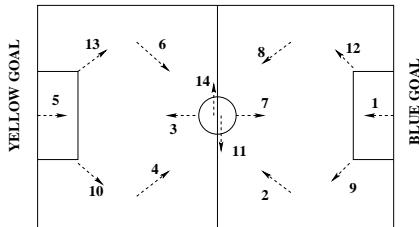
- Use accurate but slower walk near target
  - **Step size reduced** to 10% within 300mm of target

# Outline

- 1 Practical Enhancements
  - Distance-Based Updates
  - Landmark Histories
  - Extended Motion Model
- 2 Empirical Results
  - Physical Robot Experiments
  - Simulation Experiments

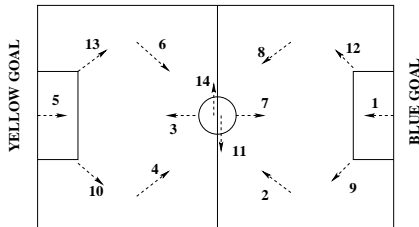
# Test for Accuracy and Time

- **Environment:** RoboCup Legged League field
  - Size: roughly  $3m \times 5m$
  - Landmarks: **4 beacons**, **4 goal edges**
- Visit sequence of **14 points and headings**
- After stabilizing at a point, measure
  - **Time** taken
  - Position and orientation **error**



# Test for Accuracy and Time

- **Environment:** RoboCup Legged League field
  - Size: roughly  $3m \times 5m$
  - Landmarks: **4 beacons**, **4 goal edges**
- Visit sequence of **14 points and headings**
- After stabilizing at a point, measure
  - **Time** taken
  - Position and orientation **error**





# Test for Accuracy and Time

## Six Localization Conditions

- 1 Baseline (**None**)
- 2 Landmark Histories (**HST**)
- 3 Distance-based probability updates (**DST**)
- 4 Function approximation of distances (**FA**)
- 5 Function approx. + distance-based updates (**FA+DST**)
- 6 All enhancements (**All**)

- Extended Motion Model **present in all**
- Average across **10 runs** for each

# Test for Accuracy and Time

## Six Localization Conditions

- 1 Baseline (**None**)
- 2 Landmark Histories (**HST**)
- 3 Distance-based probability updates (**DST**)
- 4 Function approximation of distances (**FA**)
- 5 Function approx. + distance-based updates (**FA+DST**)
- 6 All enhancements (**All**)

- Extended Motion Model **present in all**
- Average across **10 runs** for each

# Results

Enhan.	Dist Err (cm)	Ang Err (deg)	Total Time (s)
None	19.75±12.0	17.75±11.48	161.25±3.43
HST	17.92±9.88	10.68±5.97	161.26±5.96
DST	25.07±13.73	9.14±5.46	196.18±12.18
FA	15.19±8.59	10.21±6.11	171.85±15.19
DST+FA	13.72±8.07	9.5±5.27	151.28±48.06
All	9.65±7.69	3.43±4.49	162.54±4.38

- With all enhancements
  - 50% reduction in position error
  - 80% reduction in orientation error
  - No significant change in time

# Results

Enhan.	Dist Err (cm)	Ang Err (deg)	Total Time (s)
None	19.75±12.0	17.75±11.48	161.25±3.43
HST	17.92±9.88	10.68±5.97	161.26±5.96
DST	25.07±13.73	9.14±5.46	196.18±12.18
FA	15.19±8.59	10.21±6.11	171.85±15.19
DST+FA	13.72±8.07	9.5±5.27	151.28±48.06
All	9.65±7.69	3.43±4.49	162.54±4.38

- With all enhancements
  - 50% reduction in position error
  - 80% reduction in orientation error
  - No significant change in time

# Results

Enhan.	Dist Err (cm)	Ang Err (deg)	Total Time (s)
None	$19.75 \pm 12.0$	$17.75 \pm 11.48$	$161.25 \pm 3.43$
HST	$17.92 \pm 9.88$	$10.68 \pm 5.97$	$161.26 \pm 5.96$
DST	$25.07 \pm 13.73$	$9.14 \pm 5.46$	$196.18 \pm 12.18$
FA	$15.19 \pm 8.59$	$10.21 \pm 6.11$	$171.85 \pm 15.19$
DST+FA	$13.72 \pm 8.07$	$9.5 \pm 5.27$	$151.28 \pm 48.06$
All	$9.65 \pm 7.69$	$3.43 \pm 4.49$	$162.54 \pm 4.38$

- With all enhancements
  - 50% reduction in position error
  - 80% reduction in orientation error
  - **No significant change in time**

# Results

Enhan.	Dist Err (cm)	Ang Err (deg)	Total Time (s)
None	19.75±12.0	17.75±11.48	161.25±3.43
HST	17.92±9.88	10.68±5.97	161.26±5.96
DST	25.07±13.73	9.14±5.46	196.18±12.18
FA	15.19±8.59	10.21±6.11	171.85±15.19
DST+FA	13.72±8.07	9.5±5.27	151.28±48.06
All	9.65±7.69	3.43±4.49	162.54±4.38

- Additional findings
  - Bad distance updates hurt (25% increase in error)
  - Func. Approx. largest contributor
  - Combined better than in isolation

# Results

Enhan.	Dist Err (cm)	Ang Err (deg)	Total Time (s)
None	19.75±12.0	17.75±11.48	161.25±3.43
HST	17.92±9.88	10.68±5.97	161.26±5.96
DST	25.07±13.73	9.14±5.46	196.18±12.18
FA	15.19±8.59	10.21±6.11	171.85±15.19
DST+FA	13.72±8.07	9.5±5.27	151.28±48.06
All	9.65±7.69	3.43±4.49	162.54±4.38

- Additional findings
  - Bad distance updates hurt (25% increase in error)
  - **Func. Approx. largest contributor**
  - Combined better than in isolation

# Results

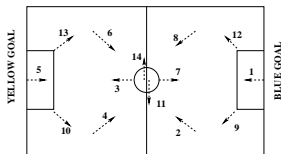
Enhan.	Dist Err (cm)	Ang Err (deg)	Total Time (s)
None	19.75±12.0	17.75±11.48	161.25±3.43
HST	17.92±9.88	10.68±5.97	161.26±5.96
DST	25.07±13.73	9.14±5.46	196.18±12.18
FA	15.19±8.59	10.21±6.11	171.85±15.19
DST+FA	13.72±8.07	9.5±5.27	151.28±48.06
All	9.65±7.69	3.43±4.49	162.54±4.38

- Additional findings
  - Bad distance updates hurt (25% increase in error)
  - Func. Approx. largest contributor
  - **Combined better than in isolation**



# Test for Stability

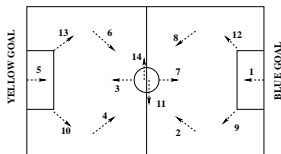
- Test ability to **stay localized** once at target
- Robot **stationary** at each of **14 points**



- 1 Attempt to localize for 10 seconds
- 2 Record deviation of pose estimate for 20 seconds

# Test for Stability

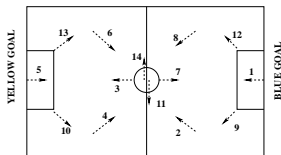
- Test ability to **stay localized** once at target
- Robot **stationary** at each of **14 points**



- 1 Attempt to **localize** for 10 seconds
- 2 Record deviation of pose estimate for 20 seconds

# Test for Stability

- Test ability to **stay localized** once at target
- Robot **stationary** at each of **14 points**



- 1 Attempt to localize for 10 seconds
- 2 **Record deviation** of pose estimate for 20 seconds

# Results

Enhanc.	Dist Dev (cm)	Ang Dev (deg)
None	2.63	0.678
HST	1.97	0.345
DST	9.26	3.05
FA	1.46	0.338
DST+FA	4.07	1.30
All	1.32	0.332

- Significant improvement in stability
- Bad distance updates again perform worst
- Func. Approx. alone does as well as All
  - Distance information useful in reseed estimates

# Results

Enhanc.	Dist Dev (cm)	Ang Dev (deg)
None	2.63	0.678
HST	1.97	0.345
DST	9.26	3.05
FA	1.46	0.338
DST+FA	4.07	1.30
All	1.32	0.332

- Significant improvement in stability
- **Bad distance updates again perform worst**
- Func. Approx. alone does as well as All
  - Distance information useful in reseed estimates

# Results

Enhan.	Dist Dev (cm)	Ang Dev (deg)
None	2.63	0.678
HST	1.97	0.345
DST	9.26	3.05
FA	1.46	0.338
DST+FA	4.07	1.30
All	1.32	0.332

- Significant improvement in stability
- Bad distance updates again perform worst
- **Func. Approx. alone does as well as All**
  - Distance information useful in reseed estimates

# Evaluating Extended Motion Model

- Test impact of extended MM **in isolation**
- Evaluate ability to **navigate to a point**
  - Used **“keeper”** home position
  - **Displace** robot by hand a fixed distance
  - Allow to **return** to home position
  - **Measure** position and orientation error and time
- Average of ten runs

# Results

Enhan.	Dist Err (cm)	Ang Err (deg)	Time (s)
None	12.89	15.0	17.21
Extended MM	7.50	5.5	18.14

- 40% reduction in position error
- 60% reduction in orientation error
- Only a small increase in time



# Results

Enhan.	Dist Err (cm)	Ang Err (deg)	Time (s)
None	12.89	15.0	17.21
Extended MM	7.50	5.5	18.14

- 40% reduction in position error
- 60% reduction in orientation error
- Only a small increase in time

# Results

Enhan.	Dist Err (cm)	Ang Err (deg)	Time (s)
None	12.89	15.0	17.21
Extended MM	7.50	5.5	18.14

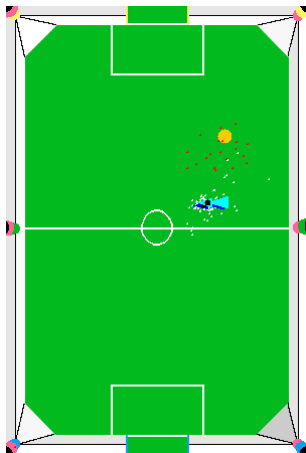
- 40% reduction in position error
- 60% reduction in orientation error
- **Only a small increase in time**

# Outline

- 1 Practical Enhancements
  - Distance-Based Updates
  - Landmark Histories
  - Extended Motion Model
- 2 Empirical Results
  - Physical Robot Experiments
  - Simulation Experiments

# Simulator

- Abstract noisy observations and movements
- Always know **ground truth**
- Perturbations **repeatable**



# Test for Recovery

- Robot follows **figure 8** path
  - **Perturbed** once every 30 seconds
- Two types of interference
  - **Collisions** (stop for 5s)
  - **Kidnappings** (teleported 1.2m)
- **Measure** position and angle error on subset of conditions
  - Averaged over 2 hours (about 50 laps)

# Test for Recovery

- Robot follows **figure 8** path
  - **Perturbed** once every 30 seconds
- Two types of interference
  - **Collisions** (stop for 5s)
  - **Kidnappings** (teleported 1.2m)
- **Measure** position and angle error on subset of conditions
  - Averaged over 2 hours (about 50 laps)

# Test for Recovery

- Robot follows **figure 8** path
  - **Perturbed** once every 30 seconds
- Two types of interference
  - **Collisions** (stop for 5s)
  - **Kidnappings** (teleported 1.2m)
- **Measure** position and angle error on subset of conditions
  - Averaged over 2 hours (about 50 laps)

# Results

Enhan.	Distance Error (cm)		
	Undisturbed	Colliding	Kidnapped
None	8.03	27.7	74.3
HST	17.6	25.3	27.3
DST+FA	7.83	16.2	31.5
All	8.67	14.4	13.5

- As expected, performance worse in presence of perturbations
- Enhancements mitigate performance degradation
  - Over 900% error increase for kidnappings without enhancements
  - Reduced to 56% increase with all enhancements
- Orientation error results similar



# Results

Enhan.	Distance Error (cm)		
	Undisturbed	Colliding	Kidnapped
None	8.03	27.7	74.3
HST	17.6	25.3	27.3
DST+FA	7.83	16.2	31.5
All	8.67	14.4	13.5

- As expected, performance worse in presence of perturbations
- **Enhancements mitigate performance degradation**
  - Over 900% error increase for kidnappings without enhancements
  - Reduced to 56% increase with all enhancements
- **Orientation** error results similar

# Results

Enhan.	Distance Error (cm)		
	Undisturbed	Colliding	Kidnapped
None	8.03	27.7	74.3
HST	17.6	25.3	27.3
DST+FA	7.83	16.2	31.5
All	8.67	14.4	13.5

- As expected, performance worse in presence of perturbations
- Enhancements mitigate performance degradation
  - Over 900% error increase for kidnappings without enhancements
  - Reduced to 56% increase with all enhancements
- Orientation error results similar

# Results

Enhan.	Distance Error (cm)		
	Undisturbed	Colliding	Kidnapped
None	8.03	27.7	74.3
HST	17.6	25.3	27.3
DST+FA	7.83	16.2	31.5
All	<b>8.67</b>	14.4	<b>13.5</b>

- As expected, performance worse in presence of perturbations
- Enhancements mitigate performance degradation
  - Over 900% error increase for kidnappings without enhancements
  - **Reduced to 56% increase with all enhancements**
- **Orientation** error results similar

# Results

Enhan.	Distance Error (cm)		
	Undisturbed	Colliding	Kidnapped
None	8.03	27.7	74.3
HST	17.6	25.3	27.3
DST+FA	7.83	16.2	31.5
All	8.67	14.4	13.5

- As expected, performance worse in presence of perturbations
- Enhancements mitigate performance degradation
  - Over 900% error increase for kidnappings without enhancements
  - Reduced to 56% increase with all enhancements
- **Orientation** error results similar

# Summary

- Monte Carlo Localization works well **in theory**
- Practical implementation **issues**
  - Especially using **vision-based legged** robots
- Three Enhancements
  - Significant **improvement** over baseline
  - More dramatic for **unmodeled movements**
- Help others avoid potential **pitfalls**