# CS344M Autonomous Multiagent Systems Spring 2008

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### **Good Afternoon, Colleagues**

Are there any questions?



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- SDR?
- Open-loop vs. Closed-loop
- Why only 8 agents in TAC?
- Any other TAC? Branch offs?
- Stock trading?





- Progress reports coming back
  - Hand them in with your final reports





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  - Hand them in with your final reports
- Final projects due in 2 1/2 weeks!



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- Clear enough for outsider to understand
  - Exchange papers for proofreading
  - Use undergraduate writing center
- Enough detail so that Doran or I could reimplement





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  - Not "What I did on summer vacation"



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  - How? Why? What alternatives?



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  - How? Why? What alternatives?
- Slides on resources page



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  - Lots of bidders
  - Lots of revenue



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  - New problems always arise
  - Bidders indeed find ways to circumvent mechanisms
- Lessons to be learned via agent-based experiments



# FCC Spectrum Auction #35

- 422 licences in 195 markets (cities)
  - 80 bidders spent \$8 billion
  - ran Dec 12 Jan 26 2001
  - licence is a 10 or 15 mhz spectrum chunk
- Run in rounds
  - bid on each licence you want each round
  - simultaneous; break ties by arrival time
  - current winner and all bids are known
- Allowable bids: 1 to 9 bid increments
  - -1 bid incr is 10% 20% of current price
- Other complex rules



## Model

- Agent goals
  - desire 0, 1, or 2 licences per market
  - desired markets have unique values
  - subject to budget constraint

Assumption: no inter-market value dependencies

- Utility is profit:  $\Sigma_l(value cost)$
- modeled 5 most important bidders
  - others served mainly to raise prices
  - modeled as several small bidders
  - lower valuations (75%  $\rightarrow$  pessimistic)

## **Bidding Strategies**

- Considering self only
  - Knapsack
  - best self-only approach
- Strategic bidding (consider others)
  - threats
  - budget stretching
  - Strategic Demand Reduction (SDR)

### Explicit communication not allowed



# Randomized SDR

### • Figure out allocations dynamically

- round 1: bid for everything you want
- first big bidder winning bid owns licence
- satisfaction = owned value / desired value

#### • Random $\Rightarrow$ uneven allocation

- get small share  $\Rightarrow$  incentive to cheat
- fair: own satisfaction close to average
- if unlucky, take licences until fair
- Small bidders take licences from owners
  - remember licence's owner
  - allocate while small bidders active



## **RSDR vs. Knapsack**

Method	Agent	Profit (\$M)		Ratio	Cost
Knapsack	0	980	<b>(</b> ±170 <b>)</b>	1.00	.82
	1	650	$(\pm 85)$	1.00	.82
	2	830	<b>(</b> ±91 <b>)</b>	1.00	.84
	3	170	<b>(</b> ±20 <b>)</b>	1.00	.84
	4	550	<b>(</b> ±96 <b>)</b>	1.00	.86
RSDR	0	1240	<b>(</b> ±210 <b>)</b>	1.26	.76
	1	820	<b>(</b> ±83 <b>)</b>	1.25	.77
	2	1300	<b>(</b> ±290 <b>)</b>	1.58	.74
	3	300	<b>(</b> ±44 <b>)</b>	1.78	.79
	4	930	<b>(</b> ±240 <b>)</b>	1.68	.76

44% more profit; avg. ratio 1.51



### **Robustness**

- What if someone cheats?
  - cheat: defect back to knapsack
  - others stay out of its way  $\Rightarrow$  big win
- Solution: Punishing RSDR (PRSDR)
  - cheater takes your licence  $\Rightarrow$  take it back
  - take it back first while still have money
  - aggressively punitive: skips optimizers

### Simplification: pointing out cheaters by hand



### **Robustness**

Method	Ratio	Cost
Knapsack	1.00	.84
RSDR	1.51	.76
RSDR Cheater	1.63	.76
RSDR Victim	1.22	.79
PRSDR Cheater	1.02	.83
PRSDR Enforcer	1.17	.81



### **Extensions**

#### Change small bidder valuations

- test robustness
- RSDR is optimal for preserving profit

#### • Multiple cheaters

- current punishment too aggressive
- collapse back to knapsack instead



## **Extentions**

Method	Ratio	Local Ratio	Cost
Multiple Cheater	1.03	1.03	.84
Multiple Enforcer	1.01	1.01	.83
50% Knapsack	1.70	1.00	.74
50% RSDR	3.42	2.02	.51
75% Knapsack	1.00	1.00	.84
75% RSDR	1.51	1.51	.76
85% Knapsack	0.68	1.00	.89
85% RSDR	0.81	1.25	.87



# **Future Work**

- Robustness enhancements
  - better punishment method
- More complex value functions
  - inter-market dependencies
- Automatic cheater detection
  - partial cheating vs. detection arms race
  - smack back into compliance
- Generalization to other auctions
  - more robust to tie-breaking procedure variations



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- Real-world functionality relies on simple assumptions:
  - bidders want more profit
  - bidders familiar with PRSDR and its benefits
  - bidders willing to try it risk-free



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  - **Client:** TACtown  $\leftrightarrow$  Tampa within 5-day period



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  - **Game:** 8 *agents*, 12 min. (why 8?)
  - Agent: simulated travel agent with 8 clients
  - **Client:** TACtown  $\leftrightarrow$  Tampa within 5-day period
- Auctions for flights, hotels, entertainment tickets
  - **Server** maintains markets, sends prices to agents
  - Agent sends bids to server **over network**



## **28 Simultaneous Auctions**

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**Entertainment:** Wrestling/Museum/Park days 1-4 (12)

• Continuous double auction; initial endowments; quote is bid-ask spread; resale allowed

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**Score:** Sum of client utilities – expenditures



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Prices known  $\Rightarrow$   $G^*$  known  $\Rightarrow$  optimal bids known



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Goal: analytically calculate optimal bids



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- Current hotel and flight prices
- Current time in game
- Hotel closing times
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#### New algorithm for conditional density estimation



- Repeat until time bound, for each hotel:
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  - 3. Given these prices compute  $V_0, V_1, \ldots, V_8$ 
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- Value of *i*th copy is avg(  $V_i V_{i-1}$  )



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Flights: Cost/benefit analysis for postponing commitment



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Entertainment: Bid more (ask less) than expected value of having one more (fewer) ticket



# **Finals**

Team	Avg.	Adj.	Institution
ATTac	3622	4154	AT&T
livingagents	3670	4094	Living Systems (Germ.)
whitebear	3513	3931	Cornell
Urlaub01	3421	3909	Penn State
Retsina	3352	3812	CMU
CaiserSose	3074	3766	Essex (UK)
Southampton	3253*	3679	Southampton (UK)
TacsMan	2859	3338	Stanford

- ATTac improves over time
- livingagents is an open-loop strategy

# **Controlled Experiments**

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- *EarlyBidder*: motivated by TAC-01 entry livingagents



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- EarlyBidder: motivated by TAC-01 entry livingagents Immediately bids high for  $G^*$  (with SimpleMean<sub>ns</sub>)
  - Goes to sleep



## **Stability**

#### • 7 EarlyBidder's with 1 ATTac

Agent	Score	Utility
ATTac	$2431 \pm 464$	8909 ± 264
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EarlyBidder gets more utility; ATTac pays less



• *Phase I* : Training from TAC-01 (seeding round, finals)



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- *Phase II* : Training from TAC-01, phases I, II



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Agent	Relative Score	
	Phase I	Phase III
ATTac <sub>ns</sub>	$105.2 \pm 49.5$ (2)	$166.2 \pm 20.8$ (1)
ATTac <sub>s</sub>	$27.8 \pm 42.1$ (3)	$122.3 \pm 19.4$ (2)
EarlyBidder	$140.3 \pm 38.6$ (1)	$117.0 \pm 18.0$ (3)
<i>SimpleMean</i> <sub>ns</sub>	$-28.8 \pm 45.1$ (5)	$-11.5 \pm 21.7$ (4)
SimpleMean <sub>s</sub>	$-72.0 \pm 47.5$ (7)	$-44.1 \pm 18.2$ (5)
$ConditionalMean_{ns}$	$8.6 \pm 41.2$ (4)	$-60.1 \pm 19.7$ (6)
ConditionalMean <sub>s</sub>	$-147.5 \pm 35.6$ (8)	$-91.1 \pm 17.6$ (7)
CurrentPrice	$-33.7 \pm 52.4$ (6)	$-198.8 \pm 26.0$ (8)





- SCM, CAT
- PLAT



# Last-minute bidding (R,O, 2001)

- eBay: first-price, ascending auction
- Amazon: auction extended if bid in last 10 minutes
- eBay: bots exist to incrementally raise your bid to a maximum
- Still people *snipe*. Why?
  - There's a risk that the bid might not make it
  - However, common-value  $\Longrightarrow$  bid conveys info
  - Late-bidding can be seen as implicit collusion
  - Or ..., lazy, unaware, etc. (Amazon and eBay)
- Finding: more late-bidding on eBay,
  - even more on antiques rather than computers

#### Small design-difference matters



# Late Bidding as Best Response

- Good vs. incremental bidders
  - They start bidding low, plan to respond
  - Doesn't give them time to respond
- Good vs. other snipers
  - Implicit collusion
  - Both bid low, chance that one bid doesn't get in
- Good in common-value case
  - protects information

Overall, the analysis of multiple bids supports the hypothesis that last-minute bidding arises at least in part as a response by sophisticated bidders to unsophisticated incremental bidding.