

# Importance Sampling Policy Evaluation with an Estimated Behavior Policy

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The University of Texas at Austin



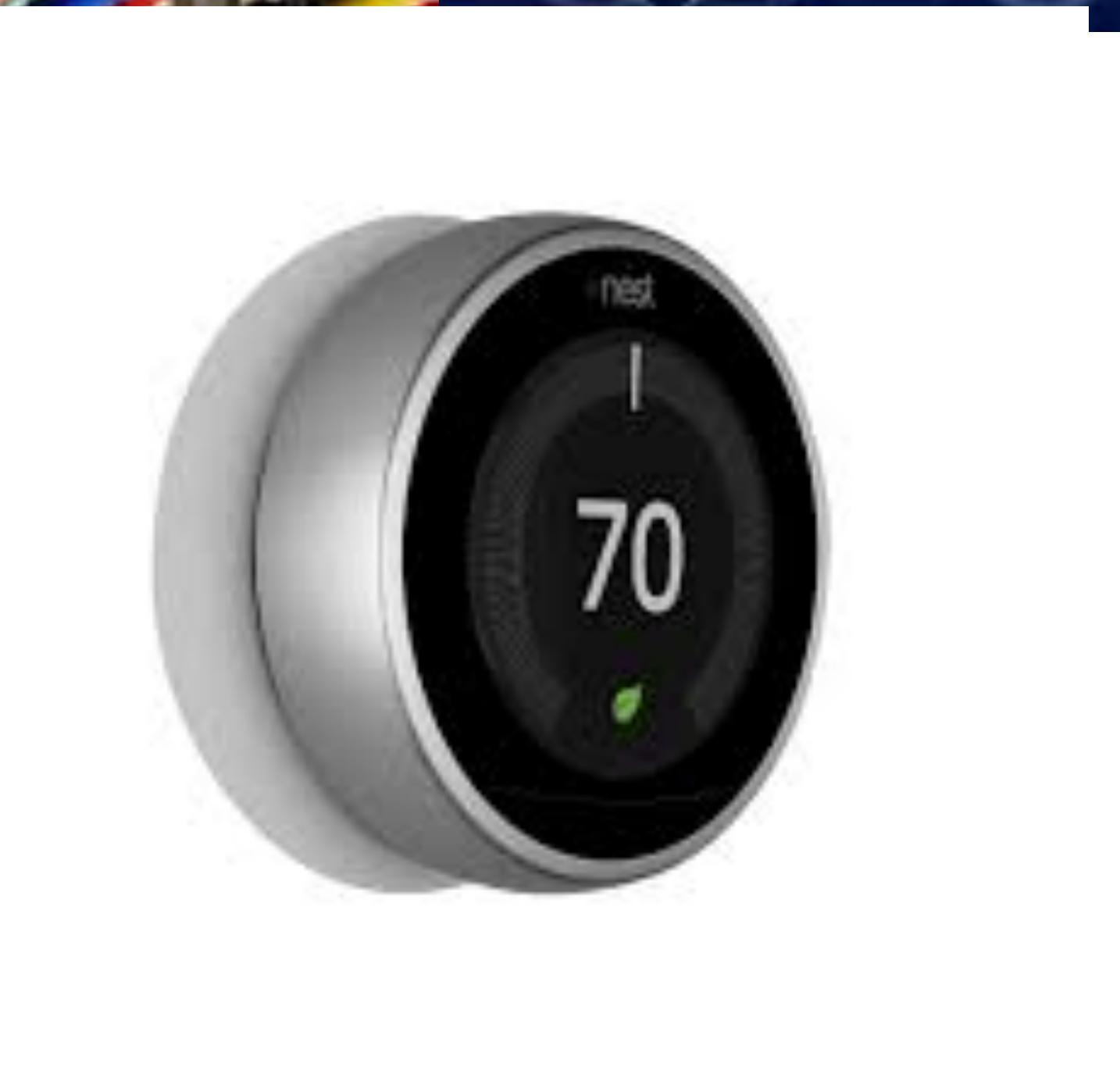
**Personal Autonomous Robotics Lab**





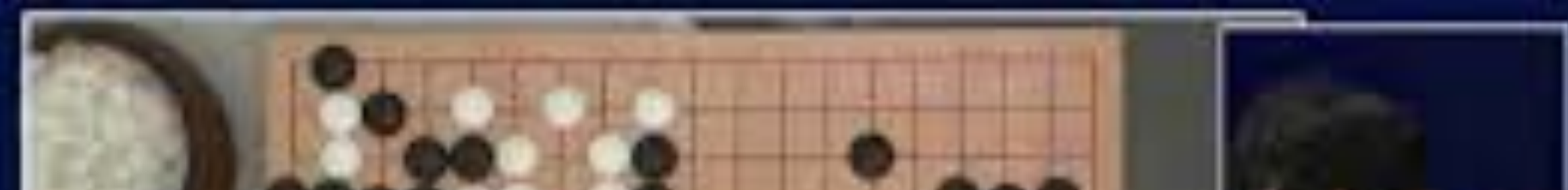








How can RL agents get the most from small amounts of experience?



**MARKETING**  
SALES SEARCH





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Study importance sampling for the RL sub-problem of policy evaluation.





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← Policy of interest

← Data collection policy (behavior policy)

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Provide empirical and theoretical support that **estimating the behavior policy improves importance sampling** for policy evaluation.

# Batch Policy Evaluation



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Given batch of trajectory data:

$$\{(S_0^i, A_0^i, R_0^i, \dots, S_L^i, A_L^i, R_L^i)\}_{i=1}^m$$

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Given a target policy:

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Estimate:

$$v(\pi) := \mathbf{E} \left[ \sum_{t=0}^L \gamma^t R_t \right]$$

# Ordinary Importance Sampling in RL



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$$\text{OIS}(\pi, \mathcal{D}) = \frac{1}{m} \sum_{i=1}^m \prod_{t=0}^L \frac{\pi(a_t | s_t)}{\pi_b(a_t | s_t)} \sum_{t=0}^L \gamma^t R_t$$

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Discounted sum of  
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Correction from  
behavior policy to  
target policy

Discounted sum of  
rewards



# Regression Importance Sampling

$$\text{RIS}(n)(\pi, \mathcal{D}) = \frac{1}{m} \sum_{i=1}^m \prod_{t=0}^L \frac{\pi(a_t | s_t)}{\pi_{\mathcal{D}}(a_t | s_{t-n}, a_{t-n}, \dots, s_t)} \sum_{t=0}^L \gamma^t R_t$$

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Maximum likelihood  
behavior policy estimate.

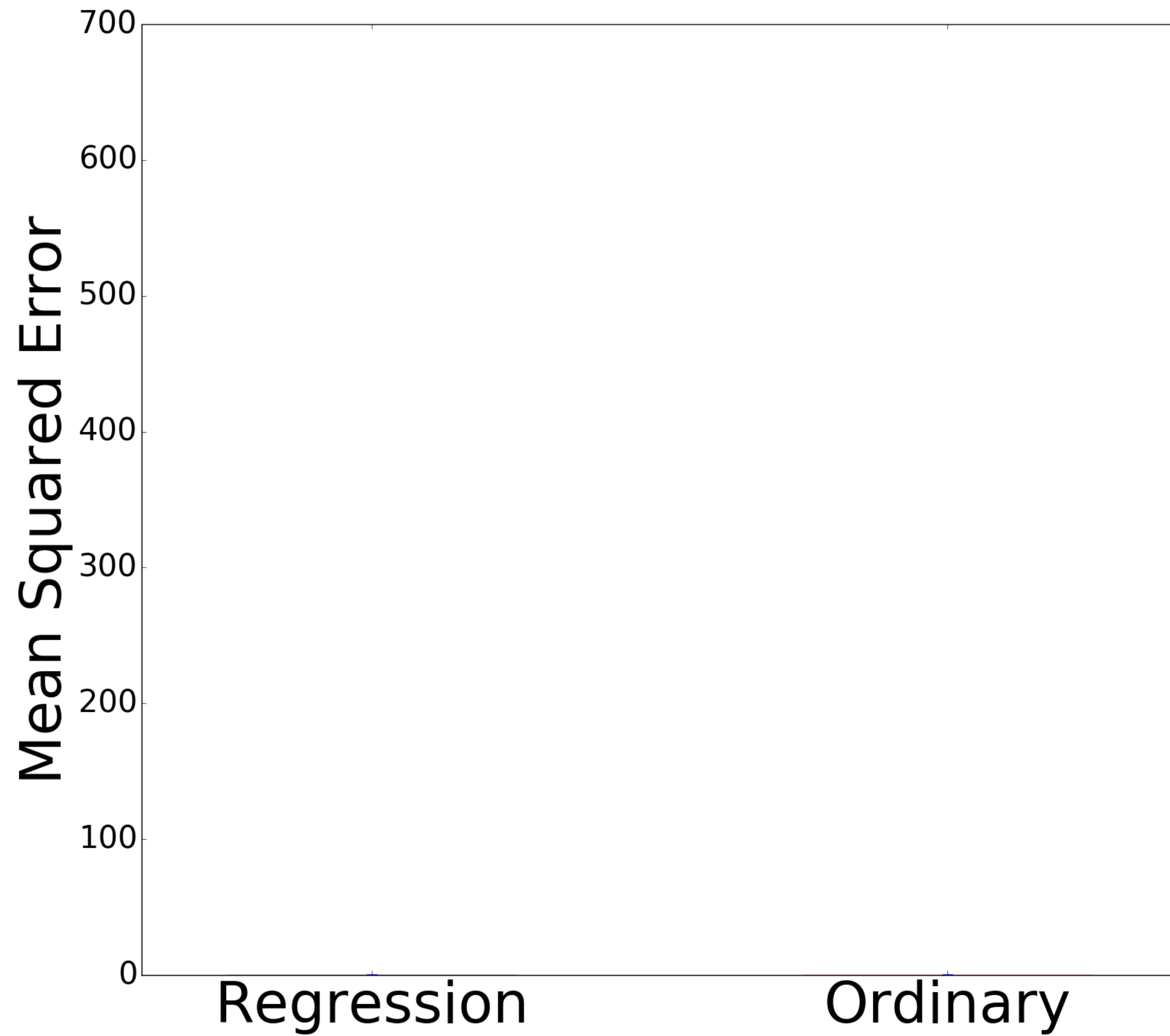
# Regression Importance Sampling

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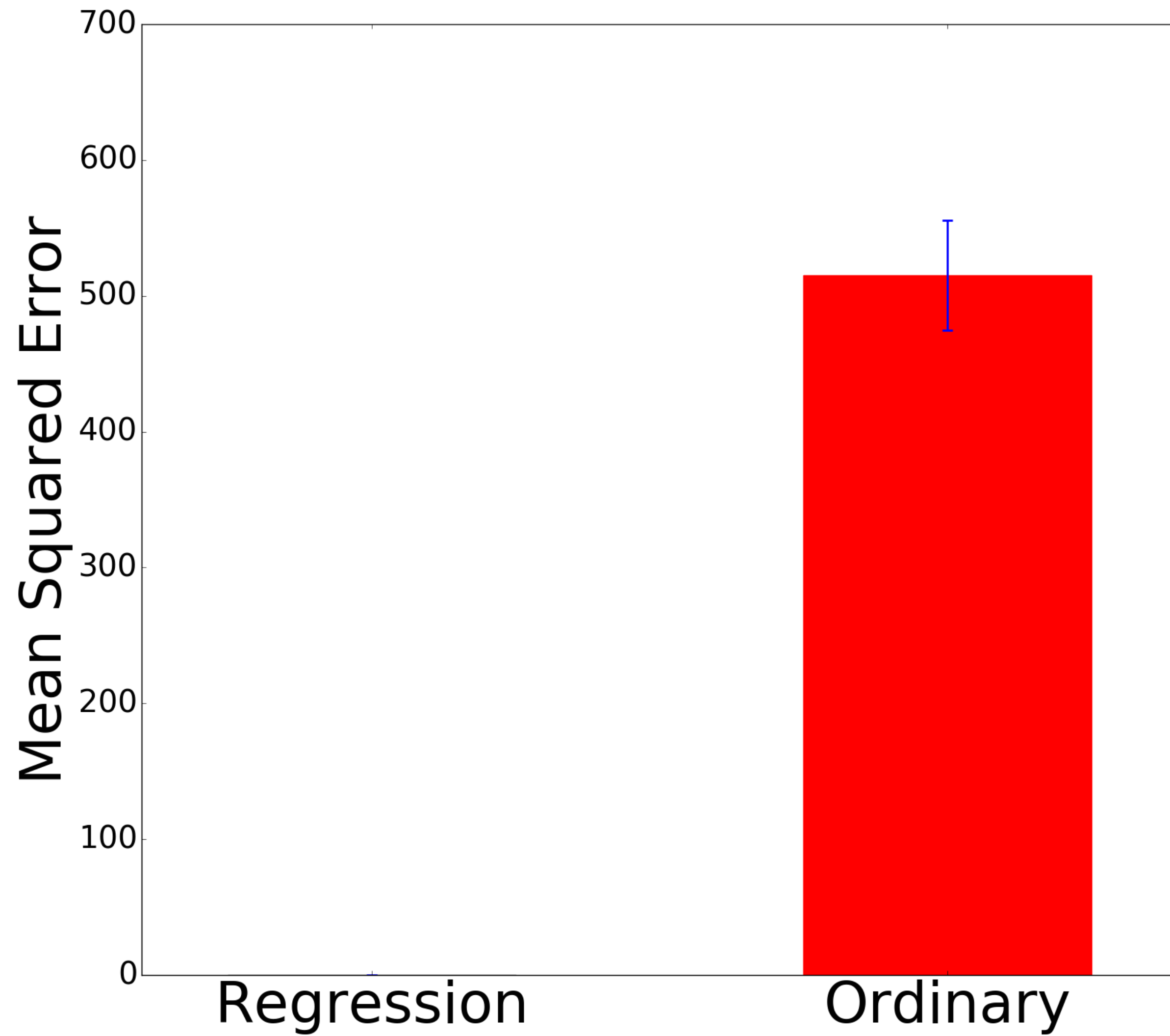
Correction from  
empirical distribution  
to target policy.



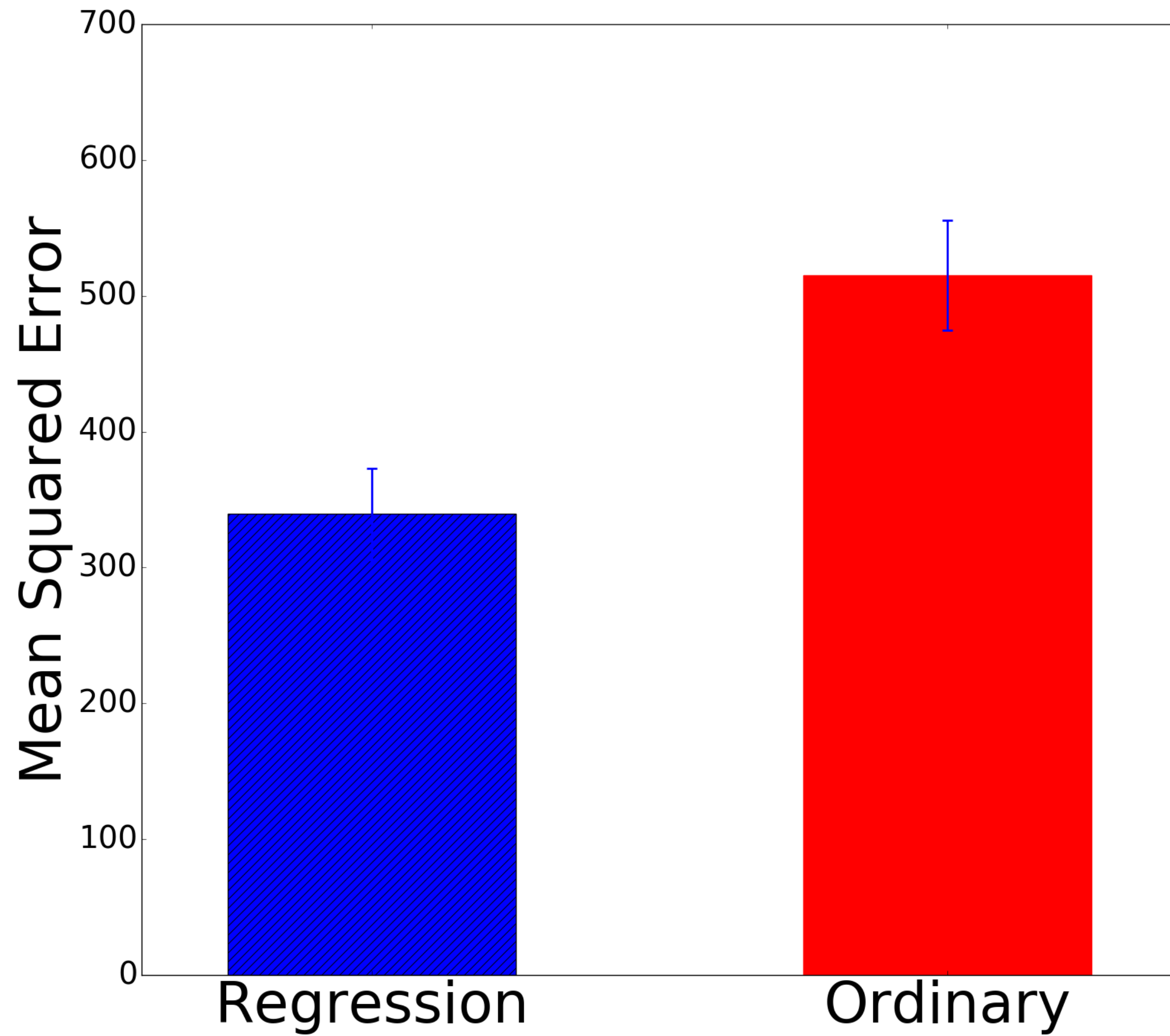




OpenAI's RoboschoolHopper-v1



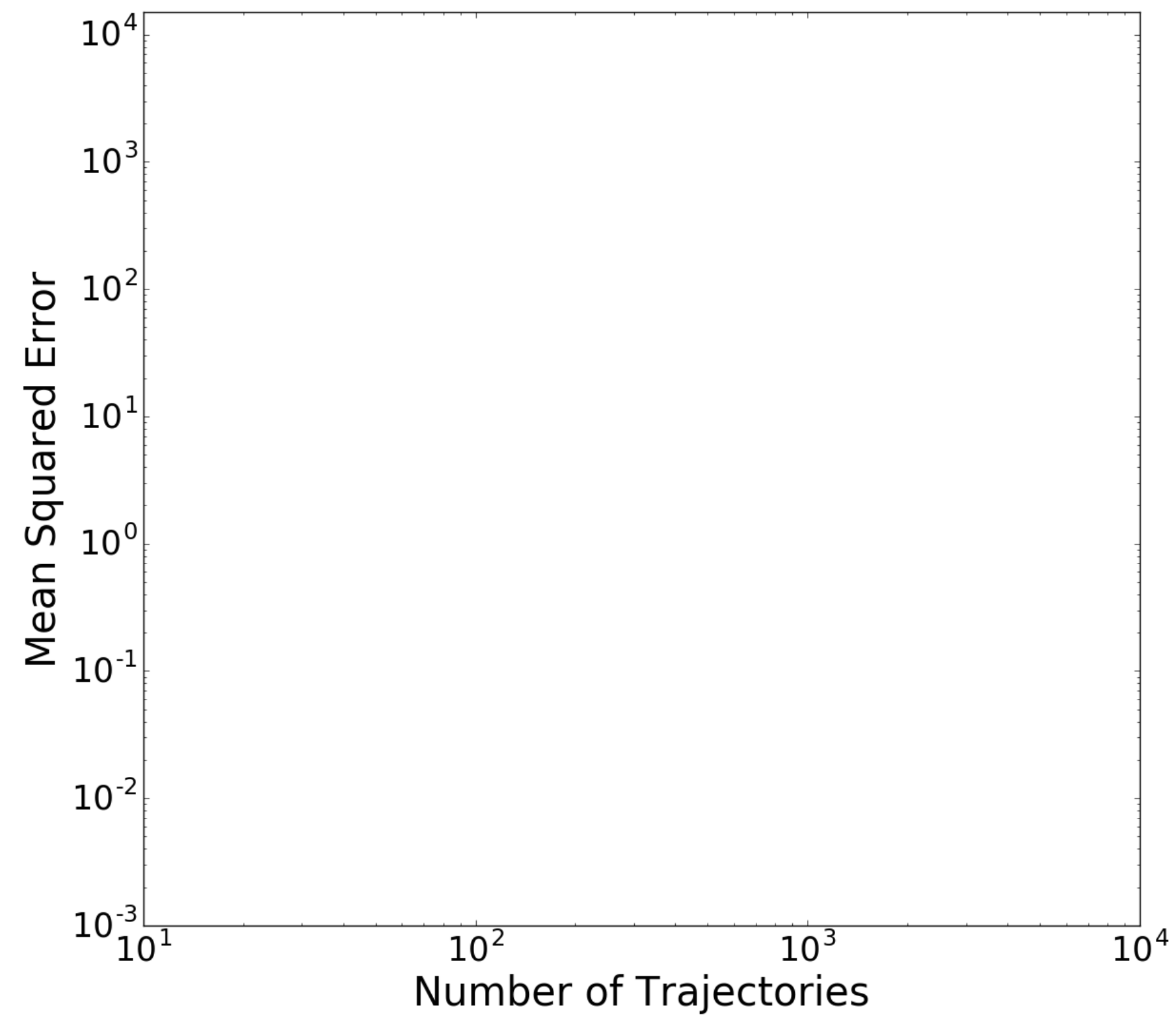
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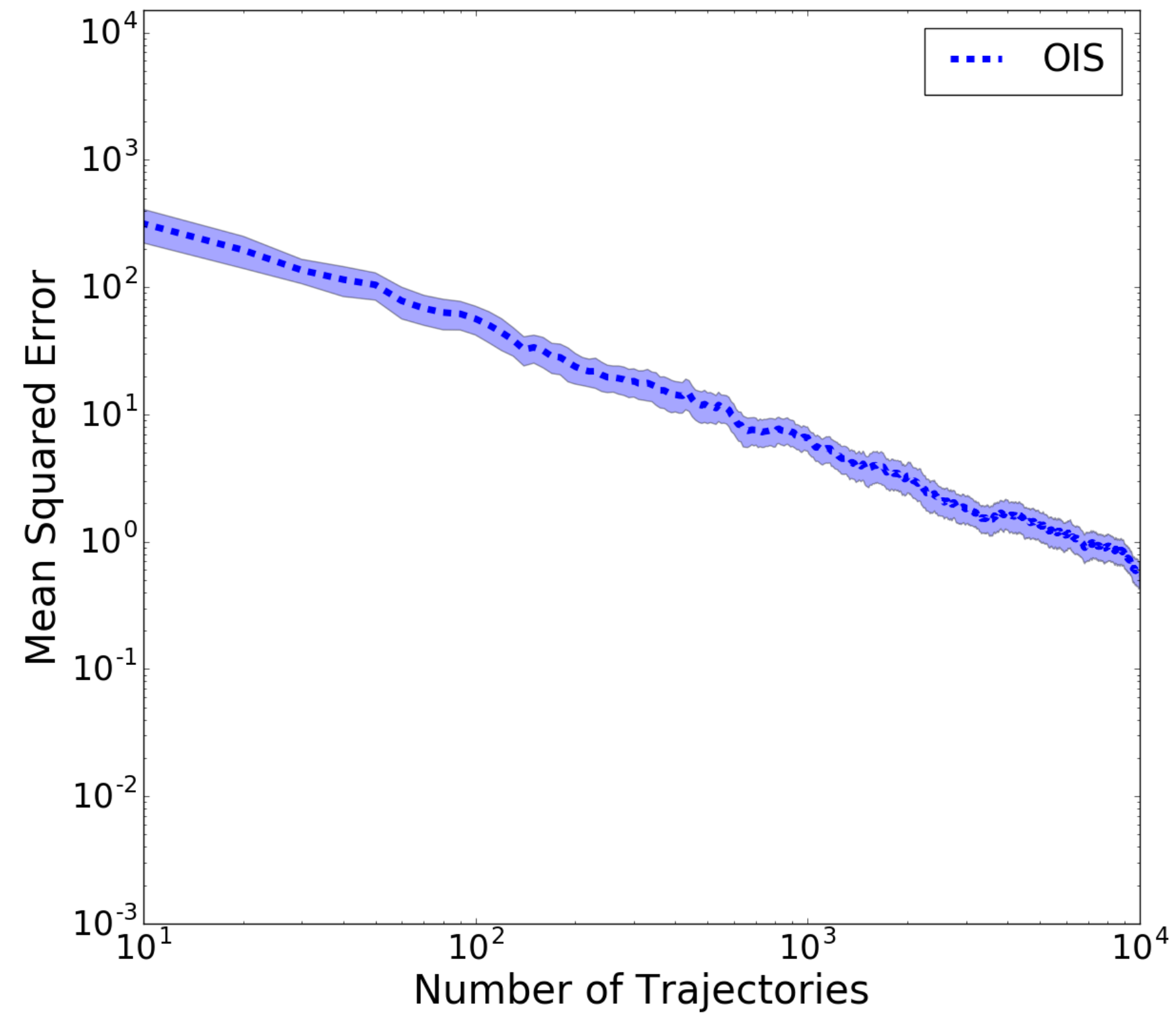


# Empirical Results



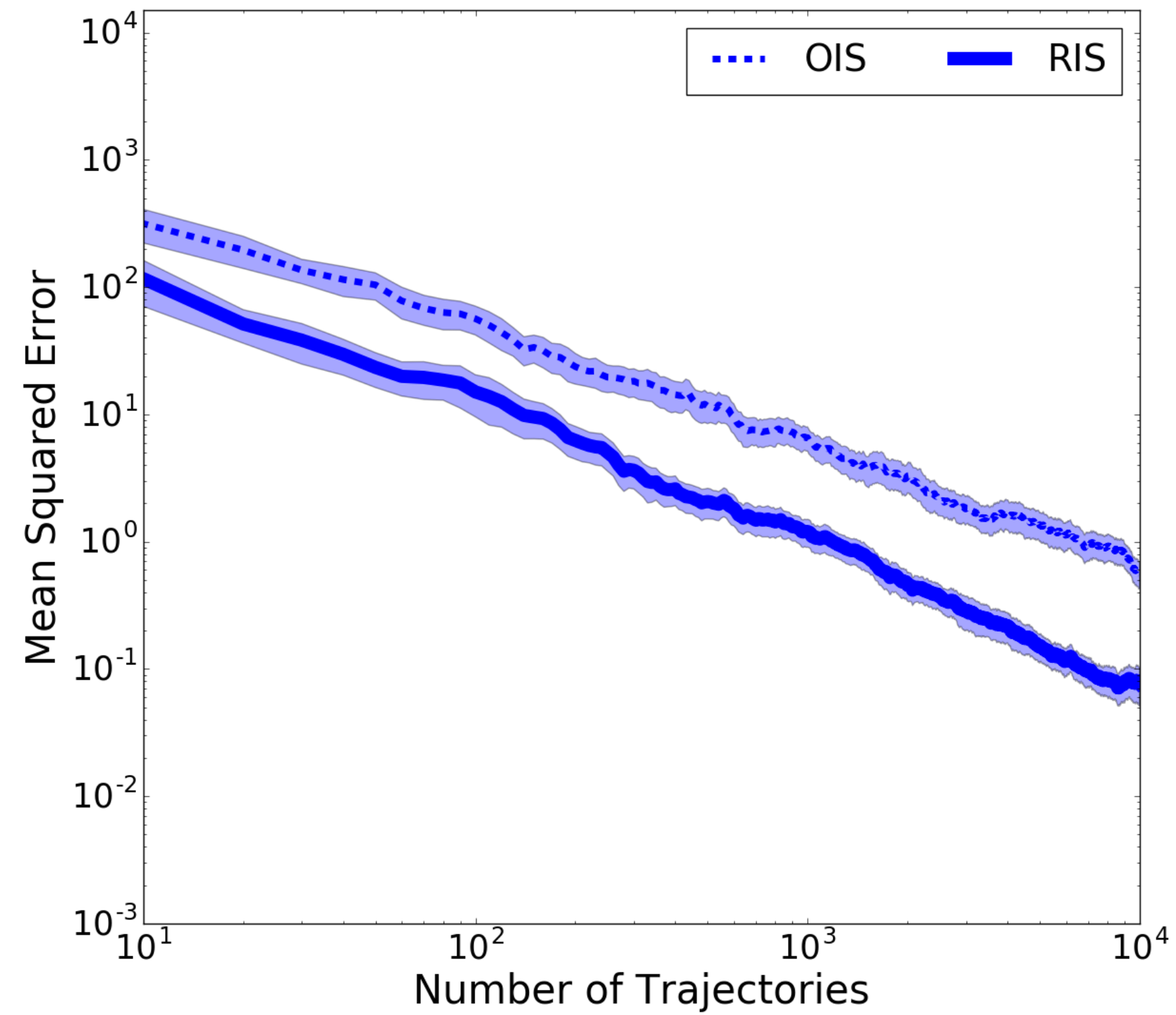
Gridworld

# Empirical Results



Gridworld

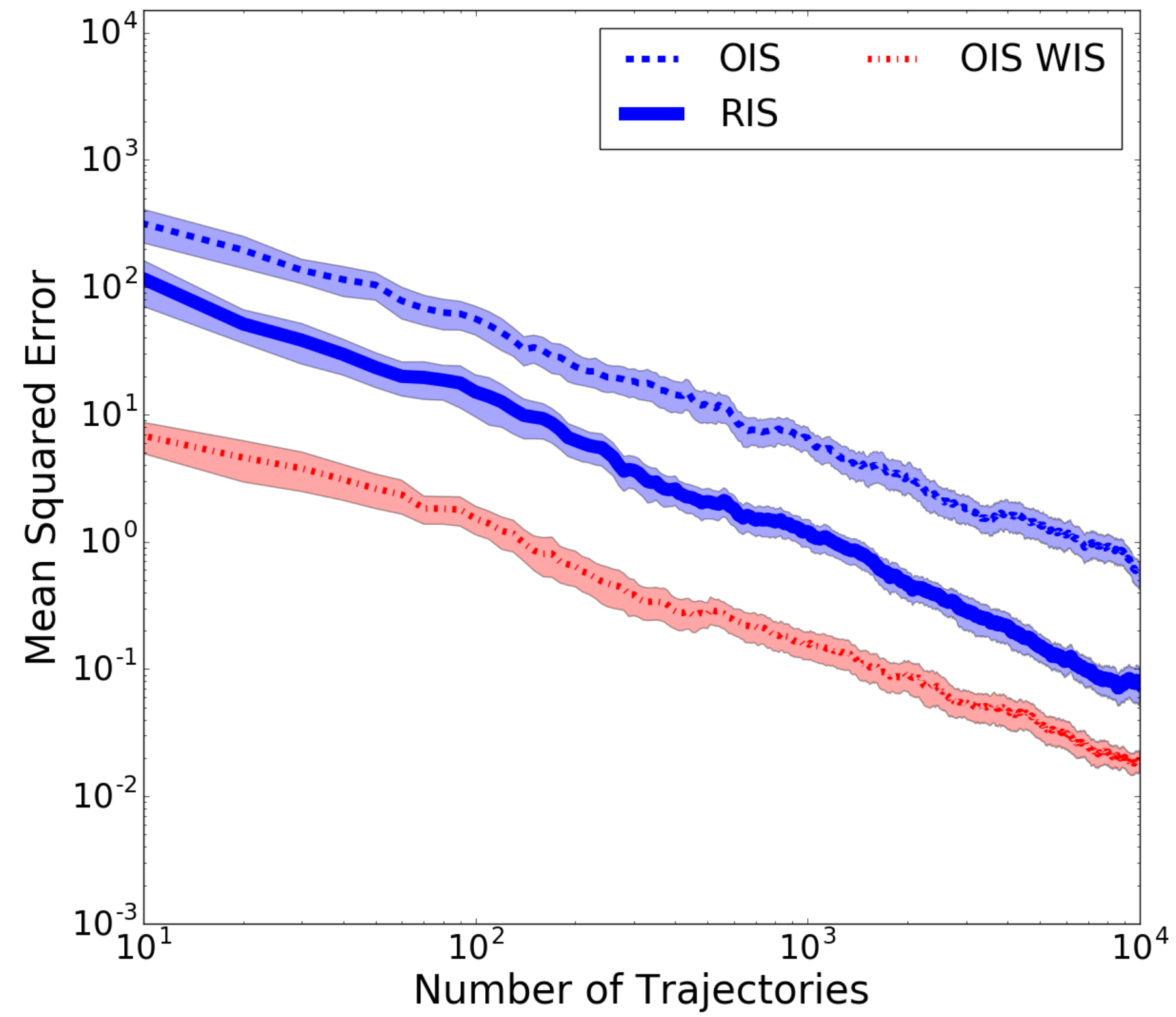
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Gridworld

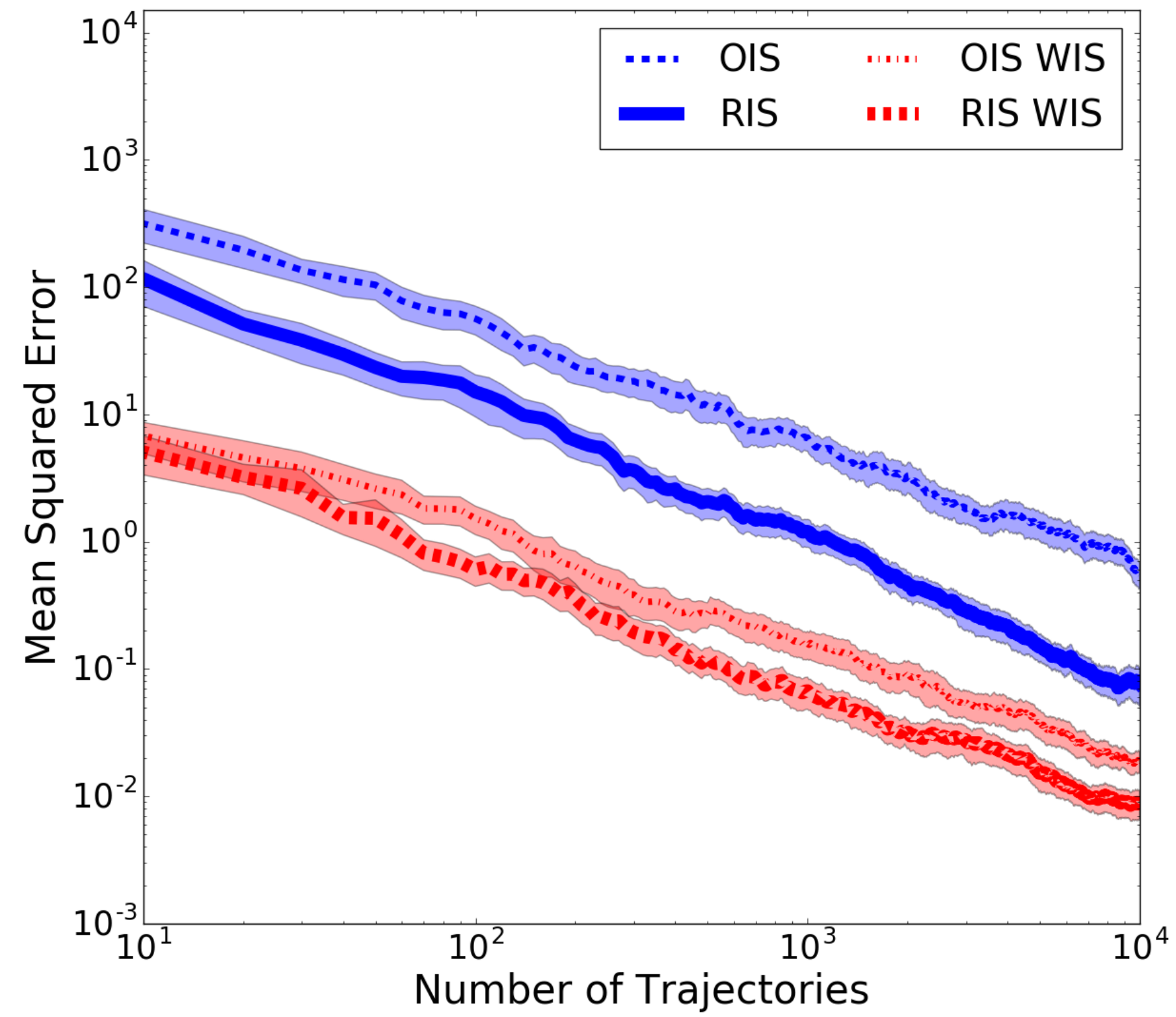


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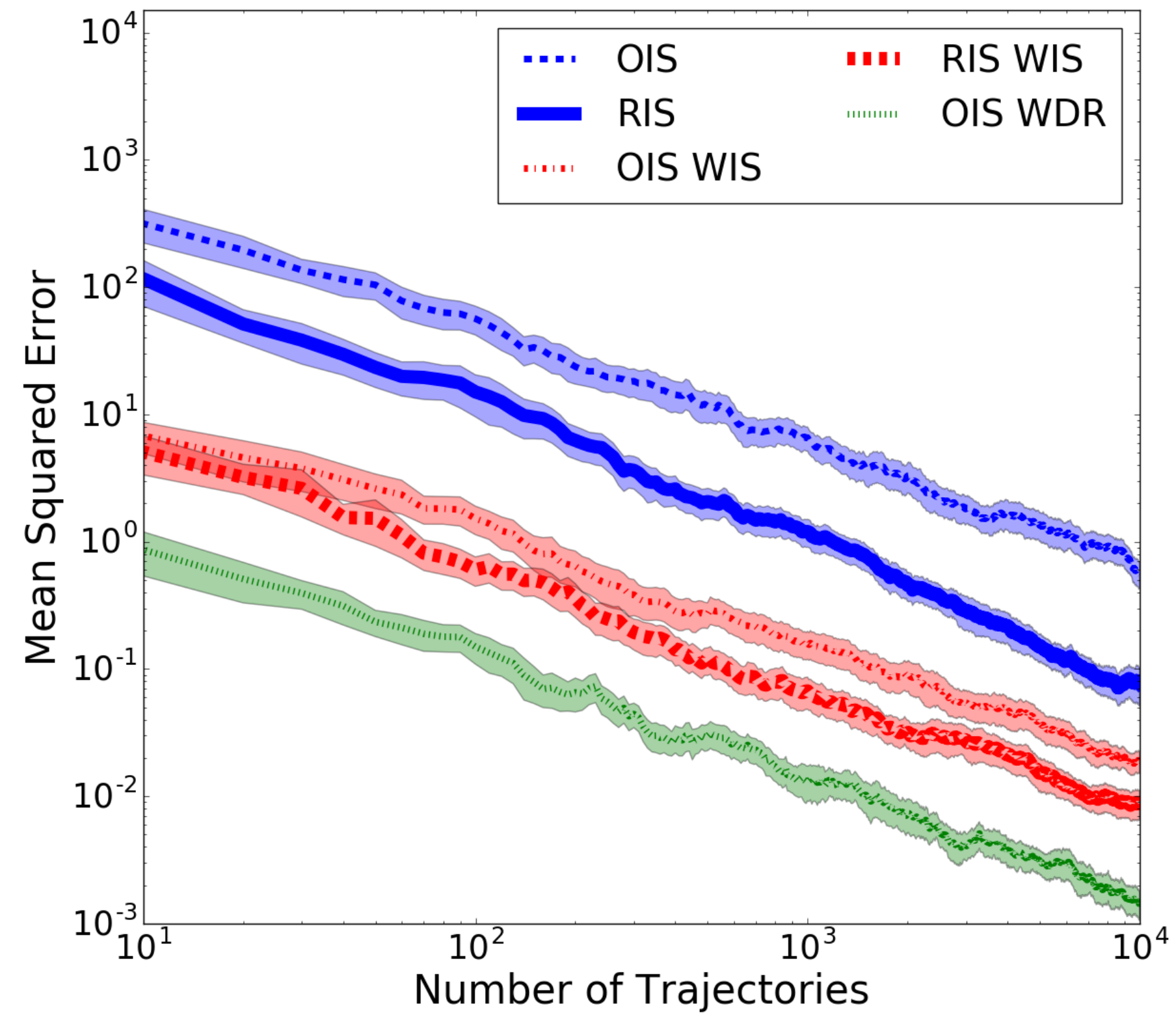
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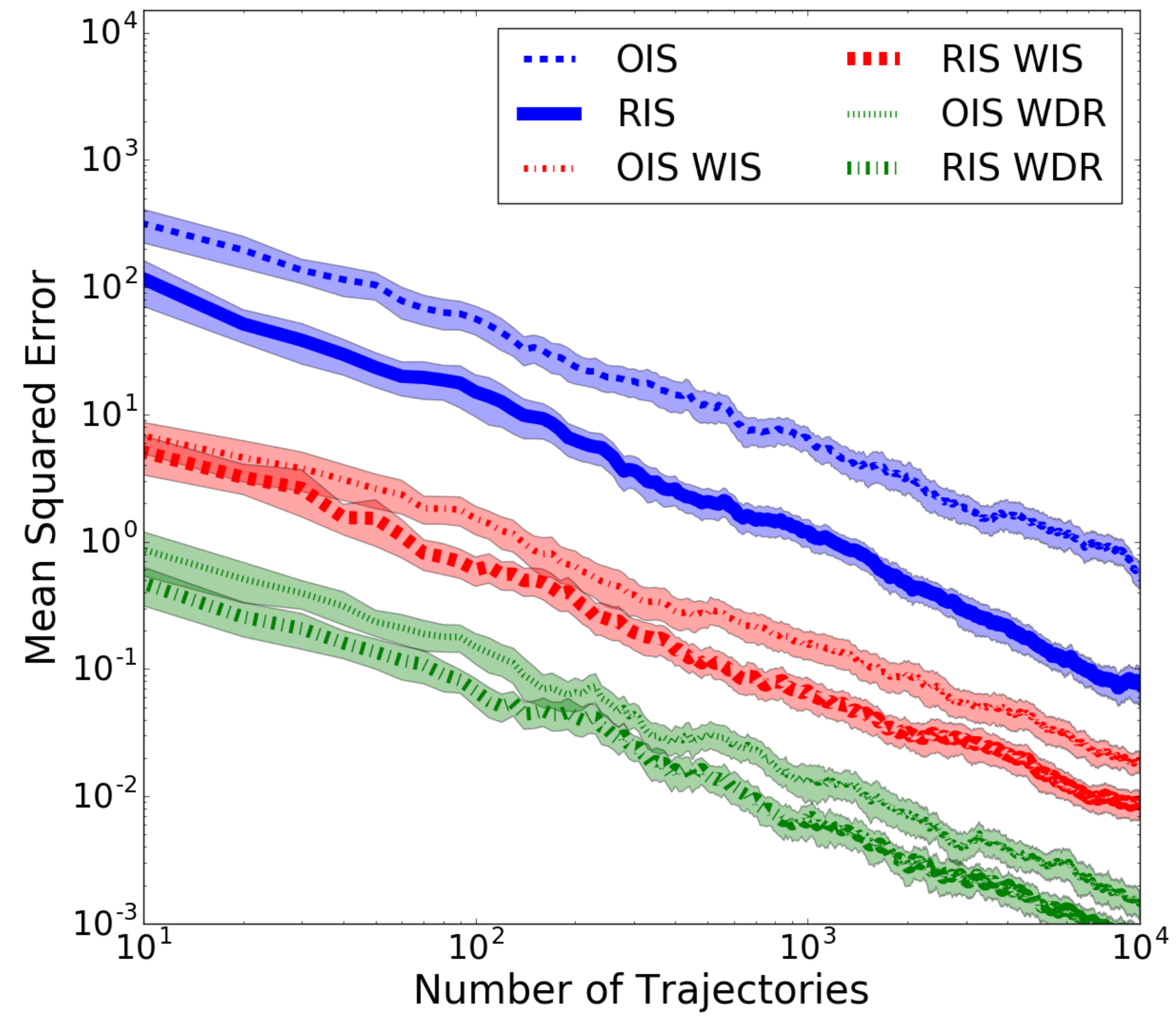
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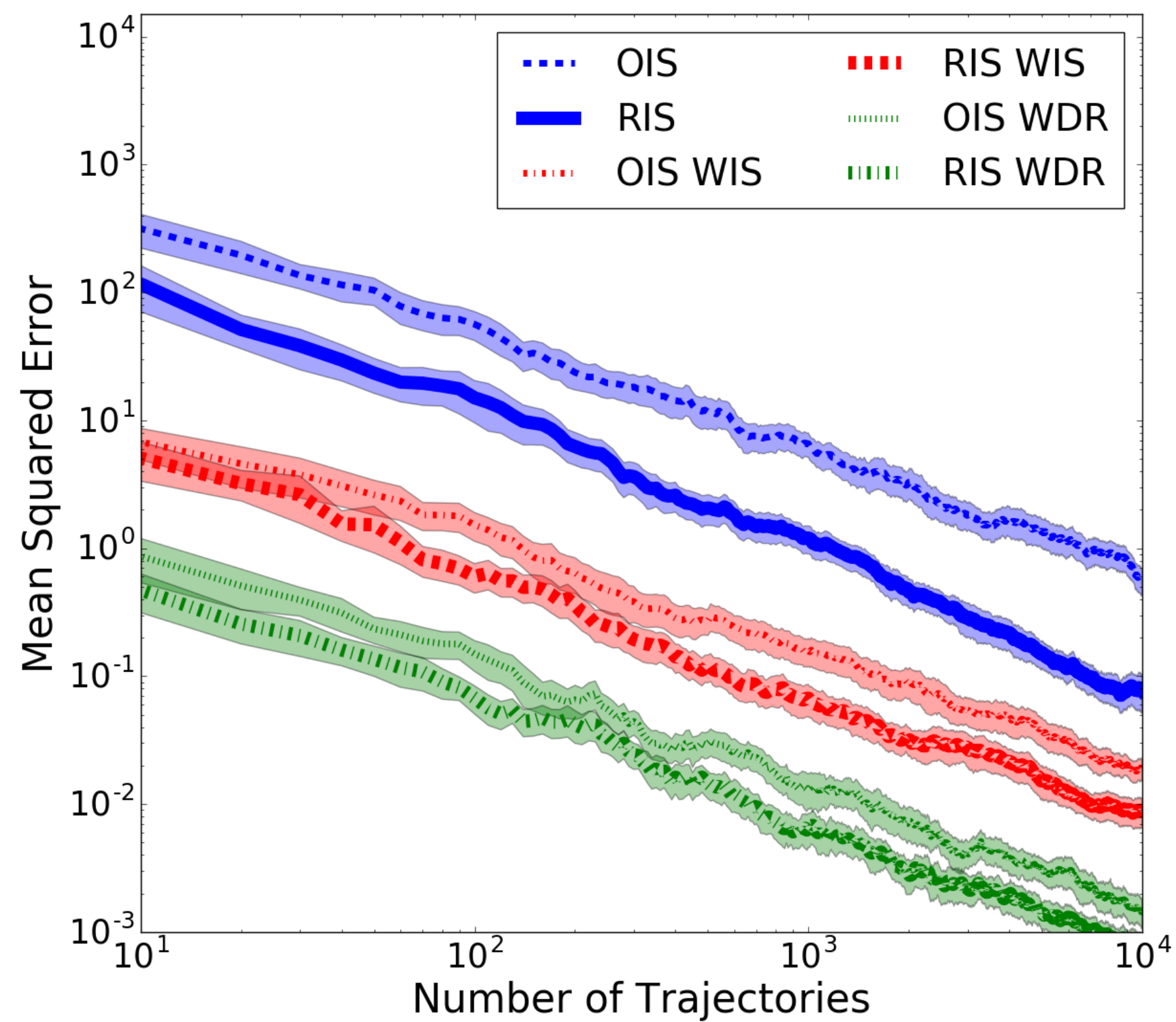


# Empirical Results

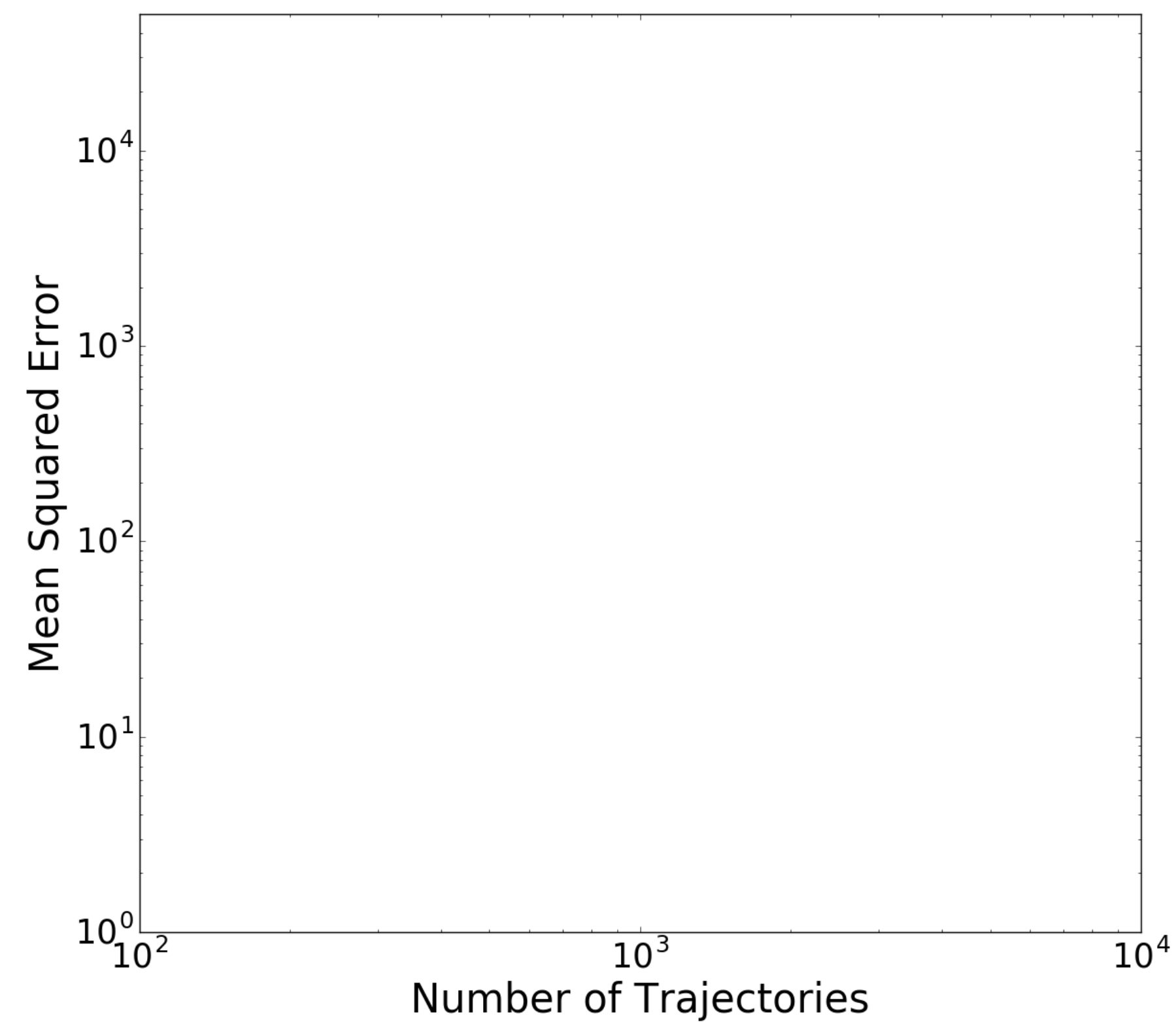


Gridworld

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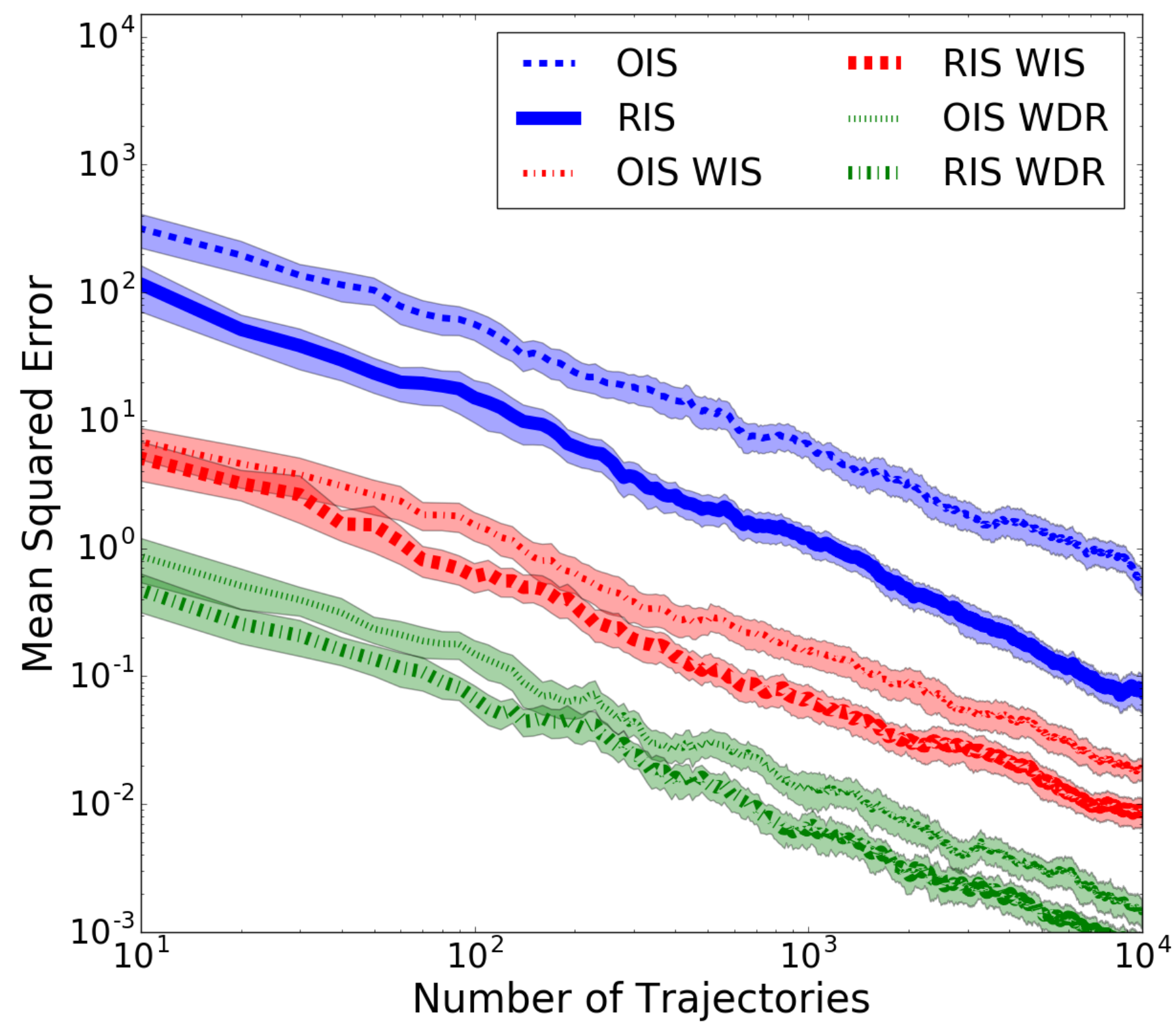


Gridworld

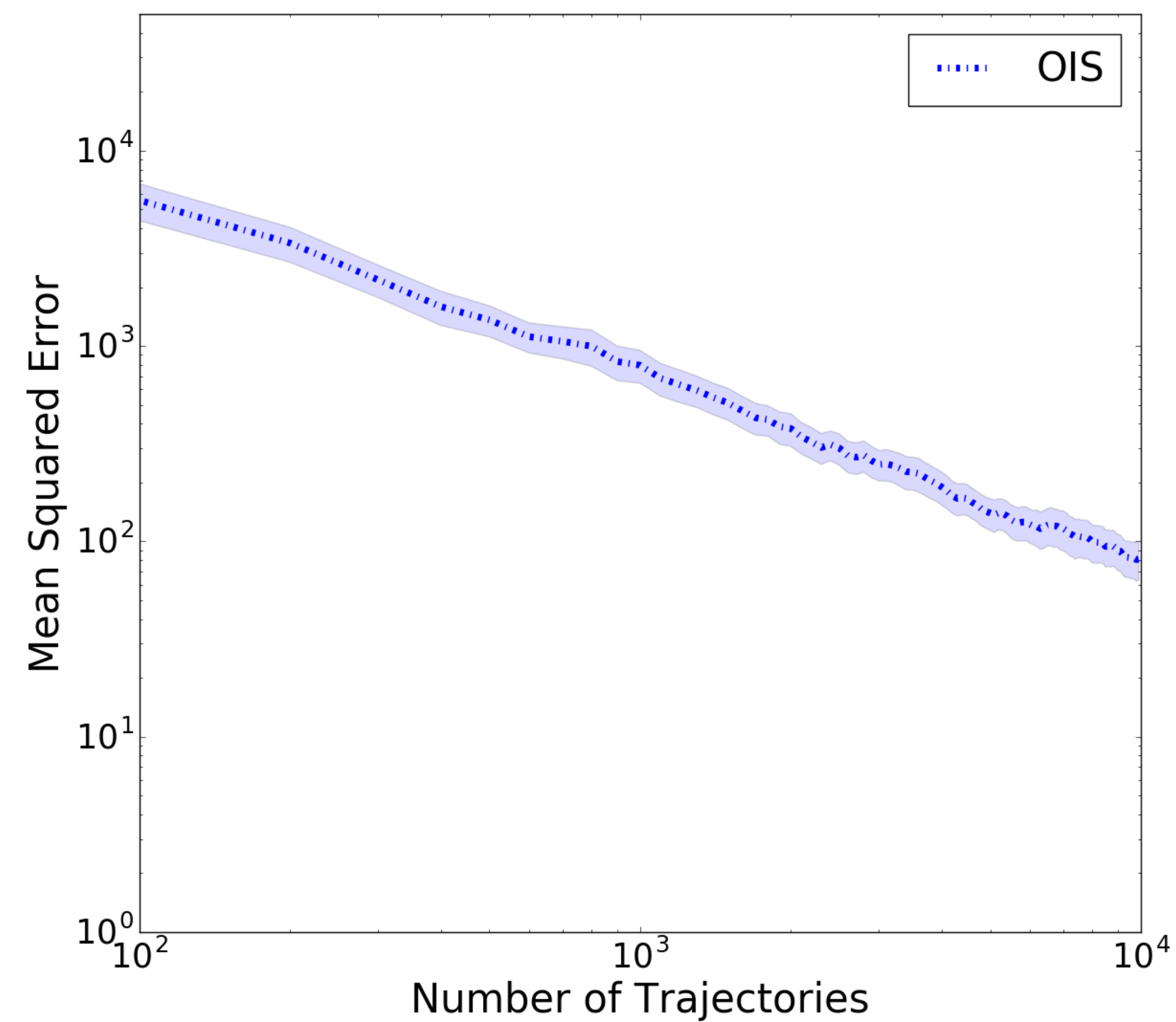


Linear Dynamical System

# Empirical Results



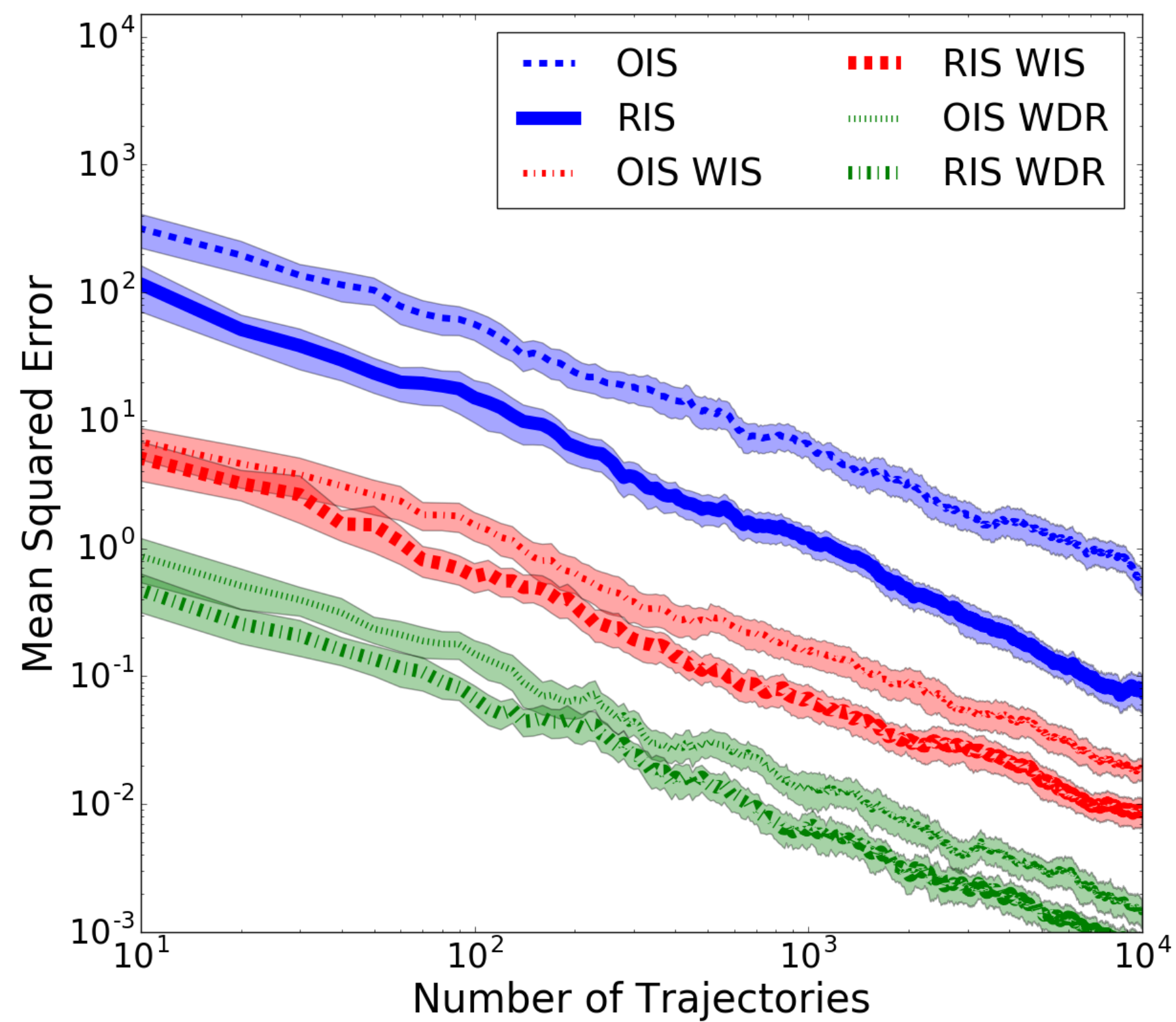
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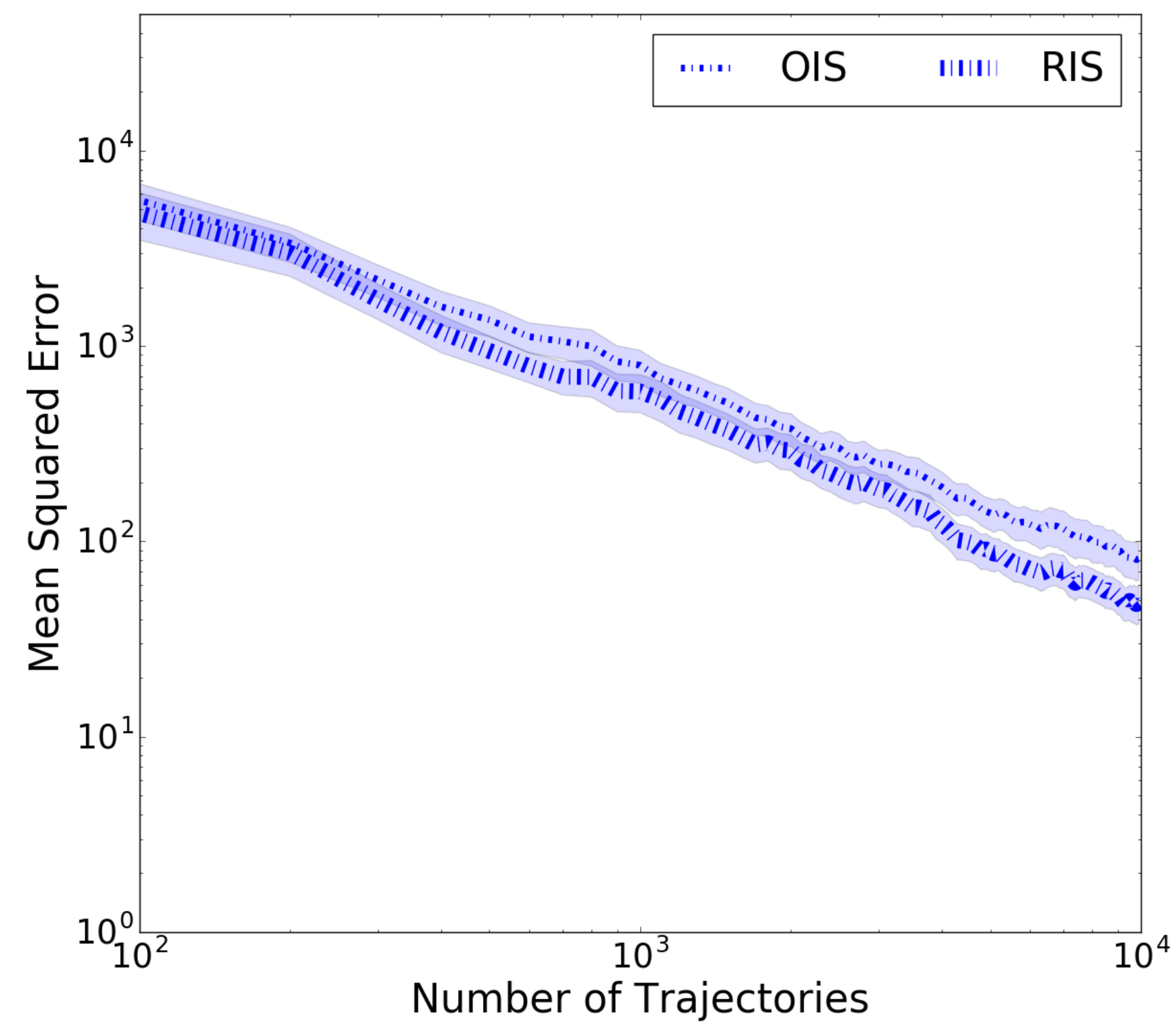
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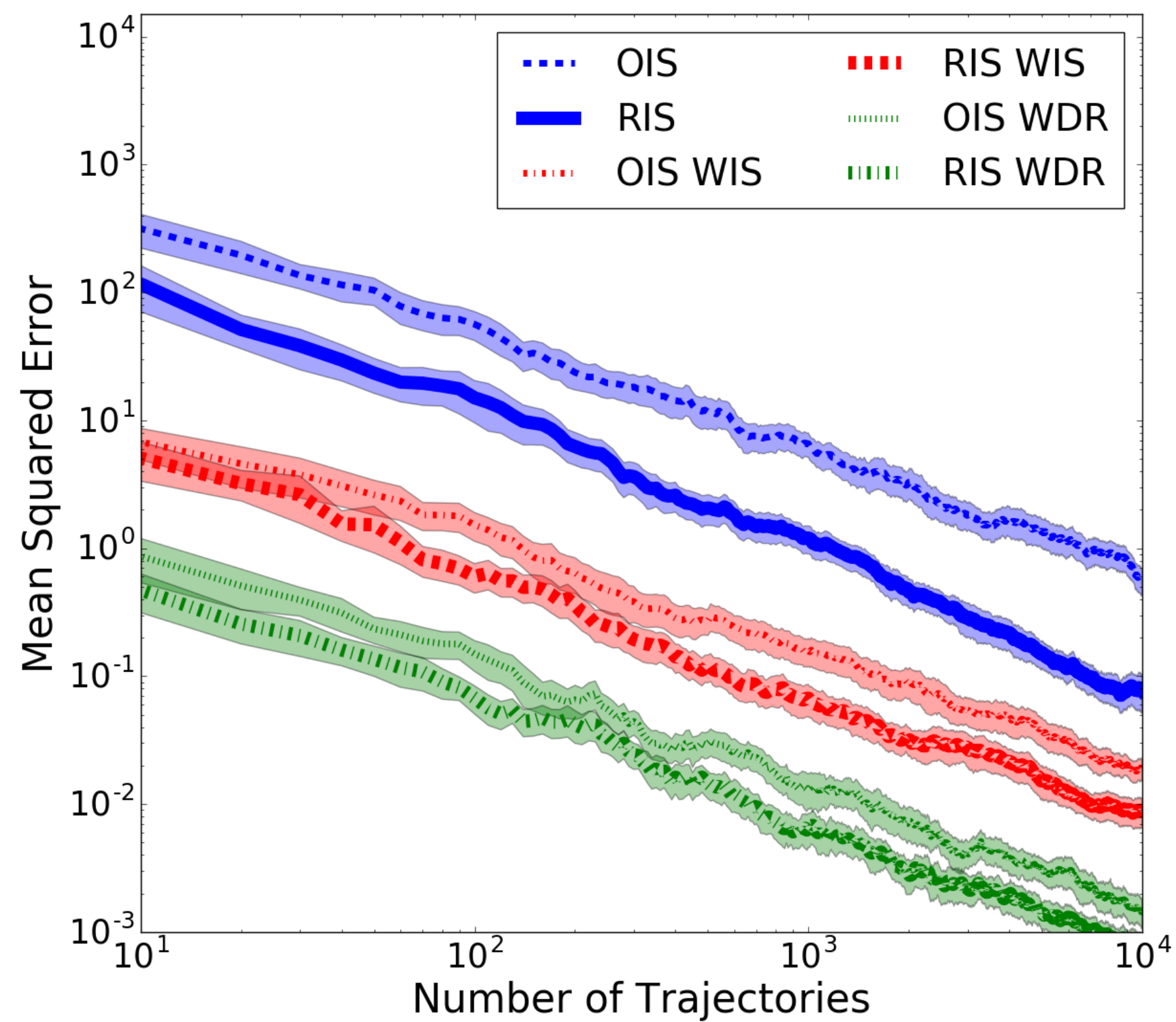


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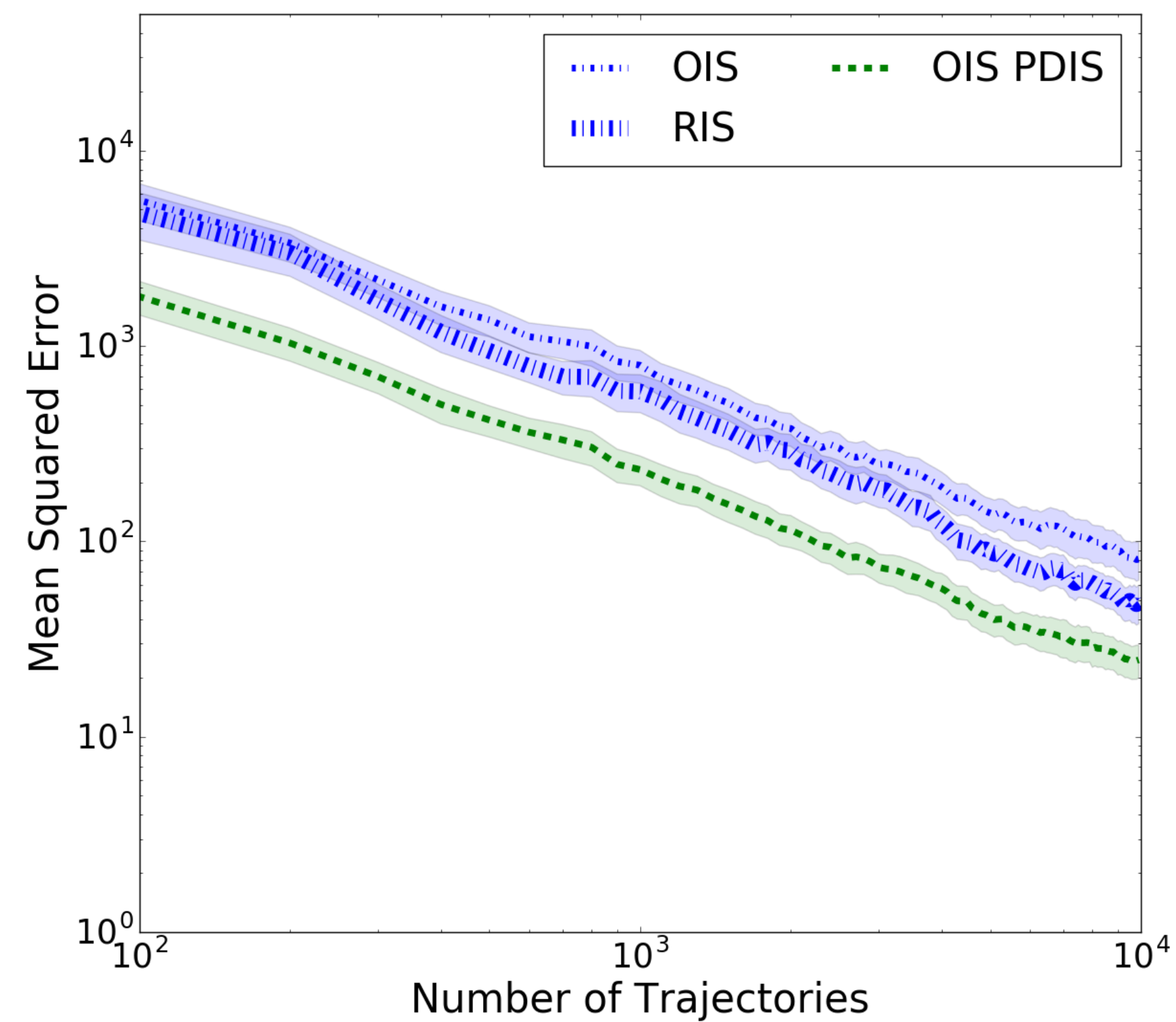


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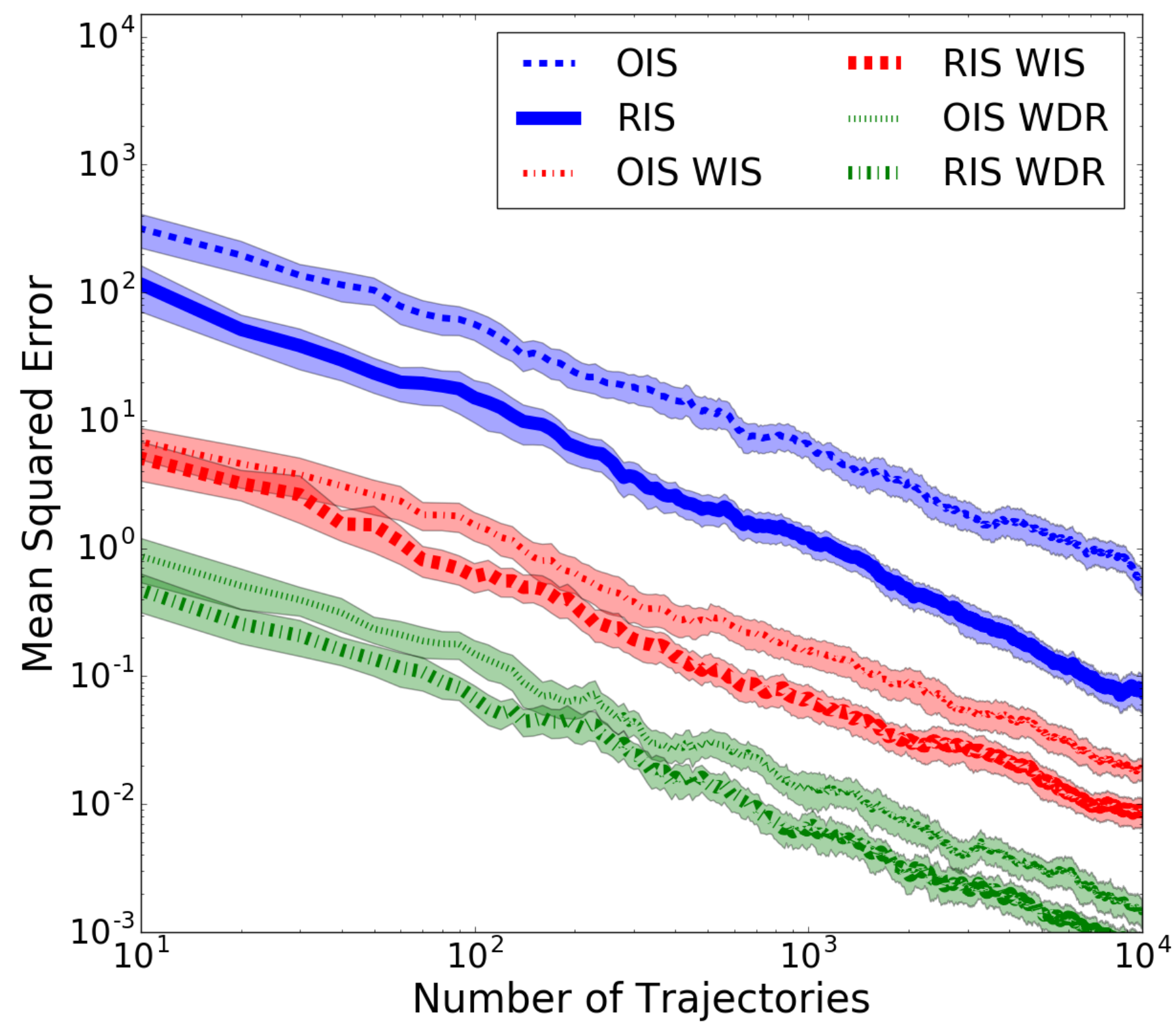


Gridworld

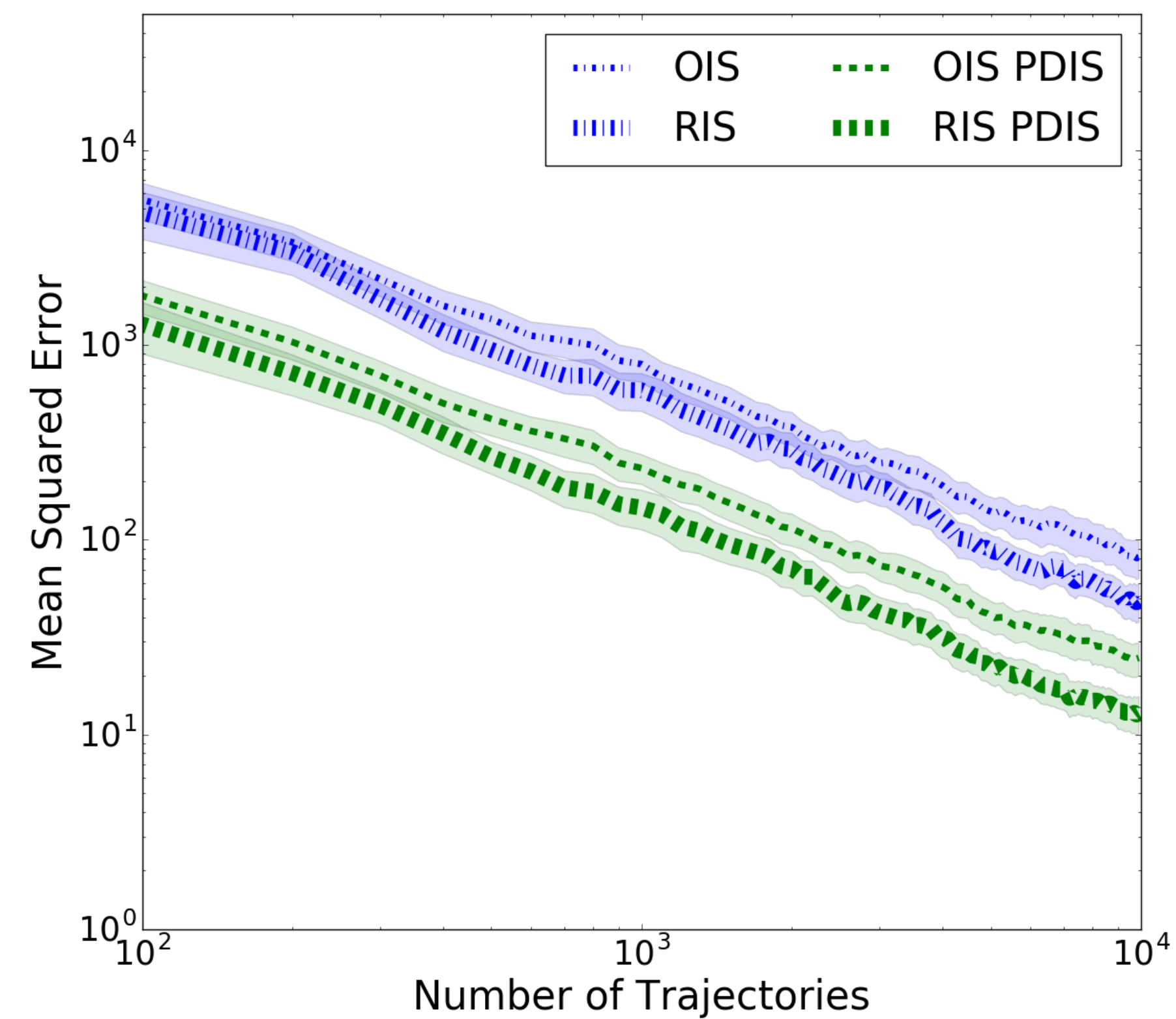


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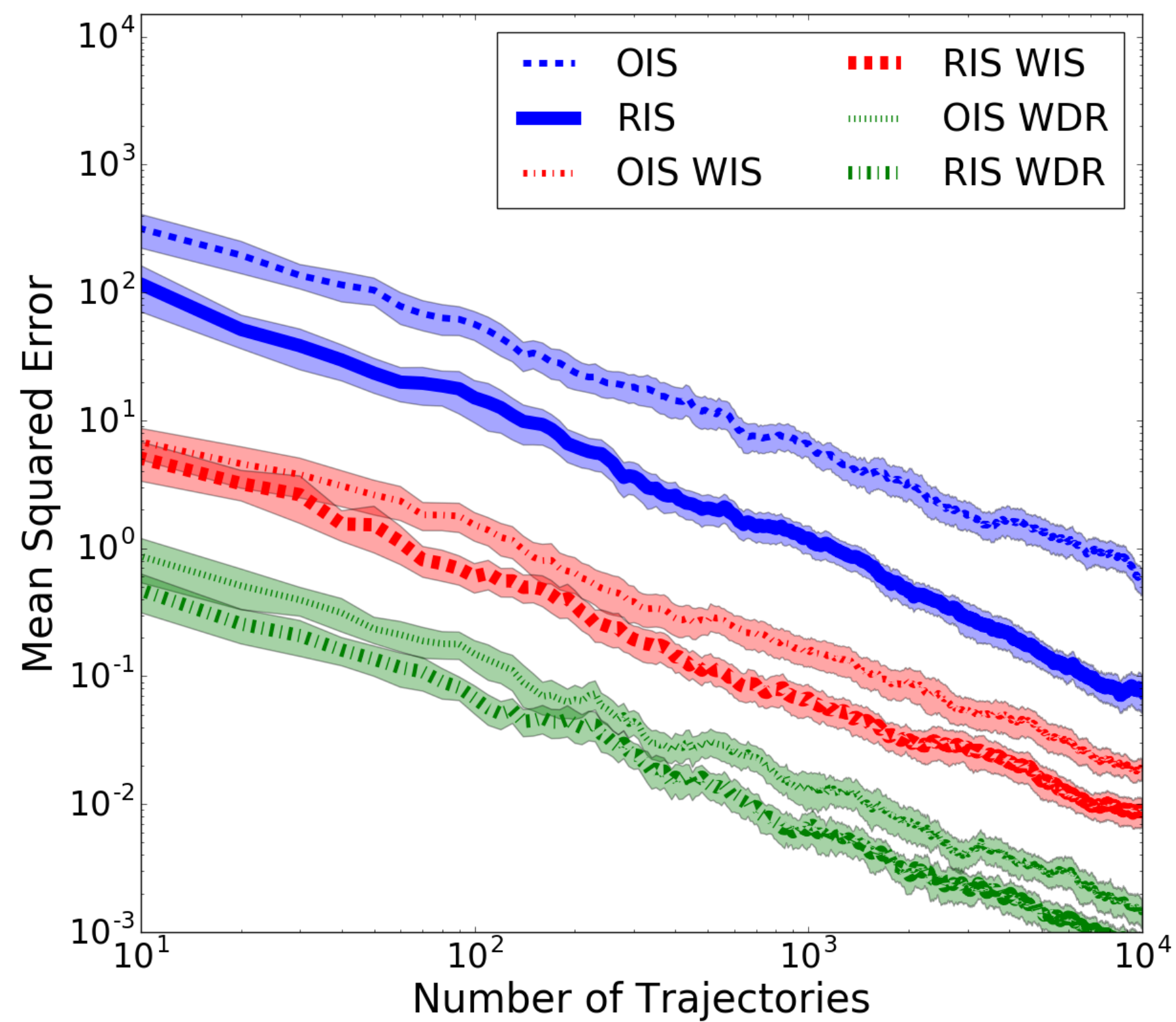
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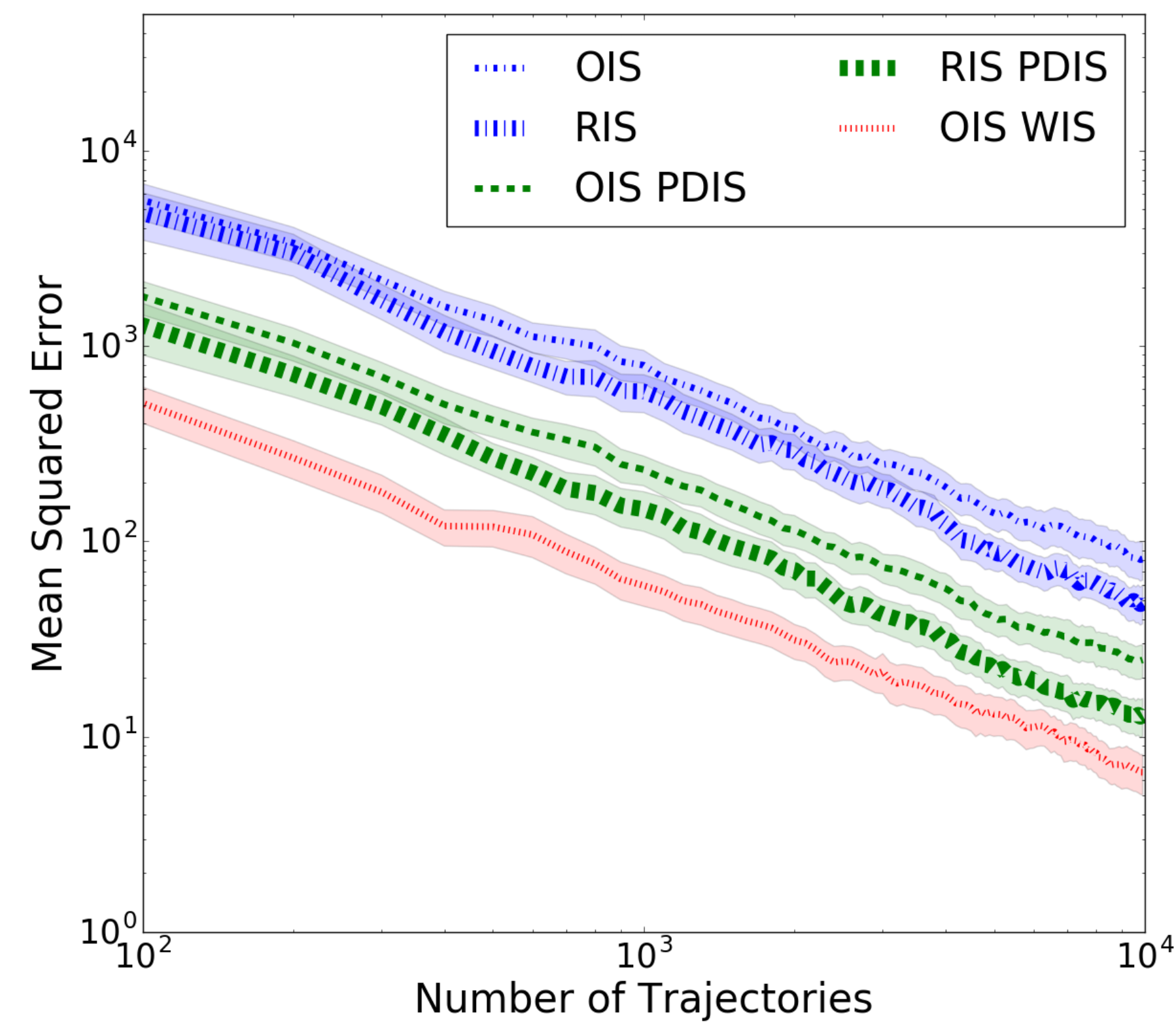
Linear Dynamical System



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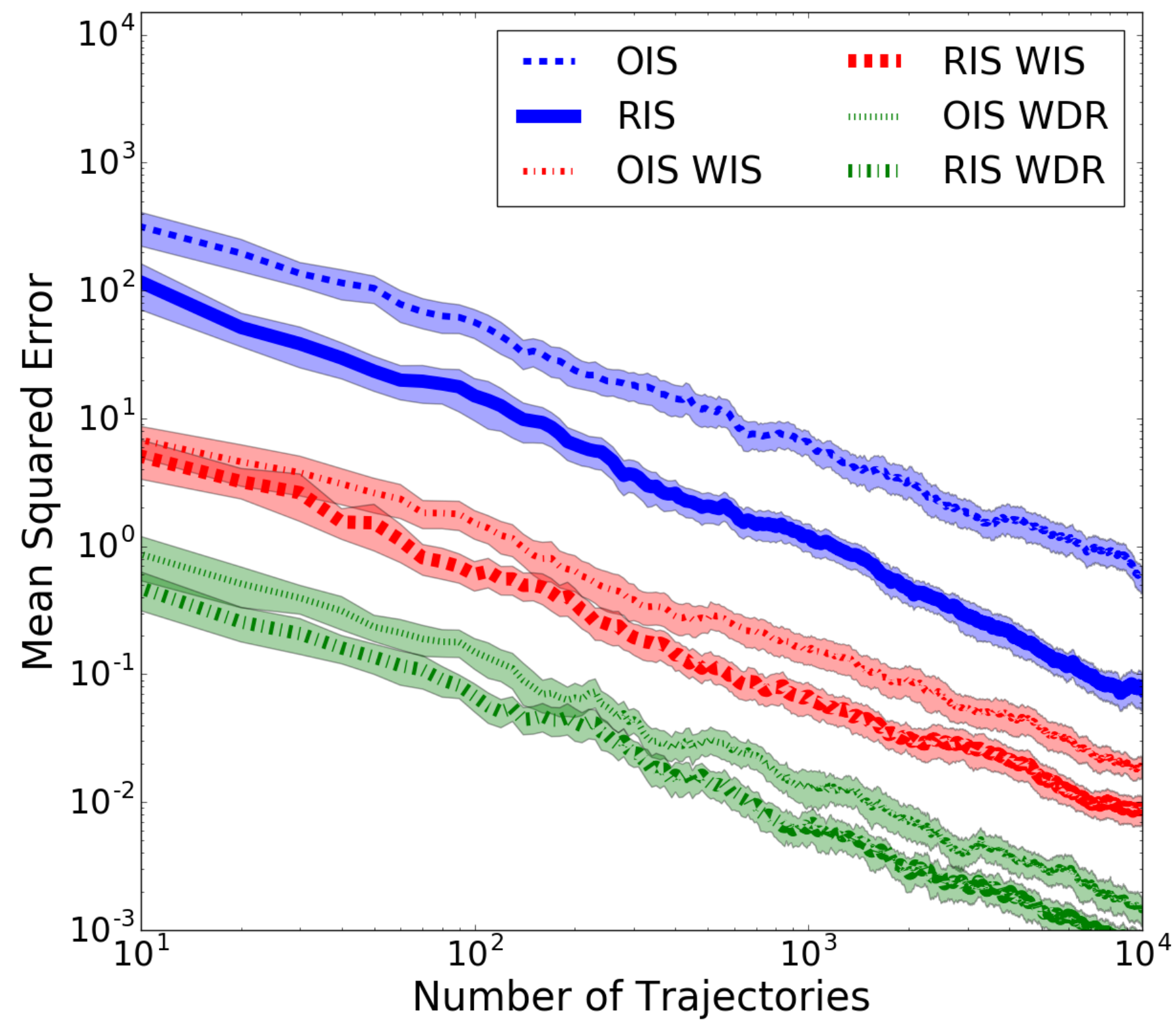
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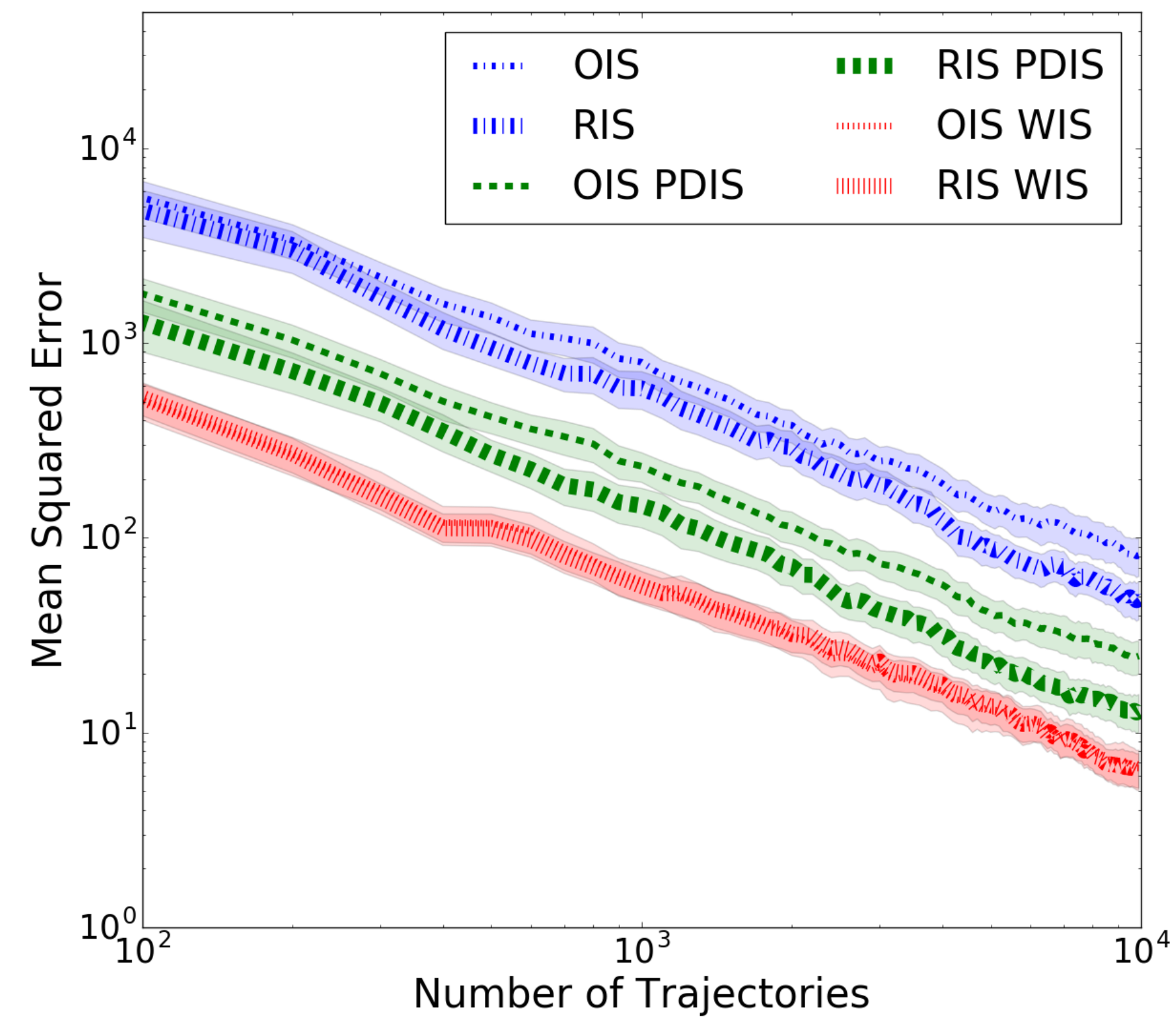
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# Empirical Results



Gridworld



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# Related Work

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1. Estimated Propensity Scores (Hirano et al. 2003, Li et al. 2015).

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We are the first to show using an **estimated behavior policy** improves importance sampling in **multi-step environments**.

Tuesday 6:30-9, Pacific Ballroom #109

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1. Off-policy importance sampling methods typically use the known behavior policy action probabilities.

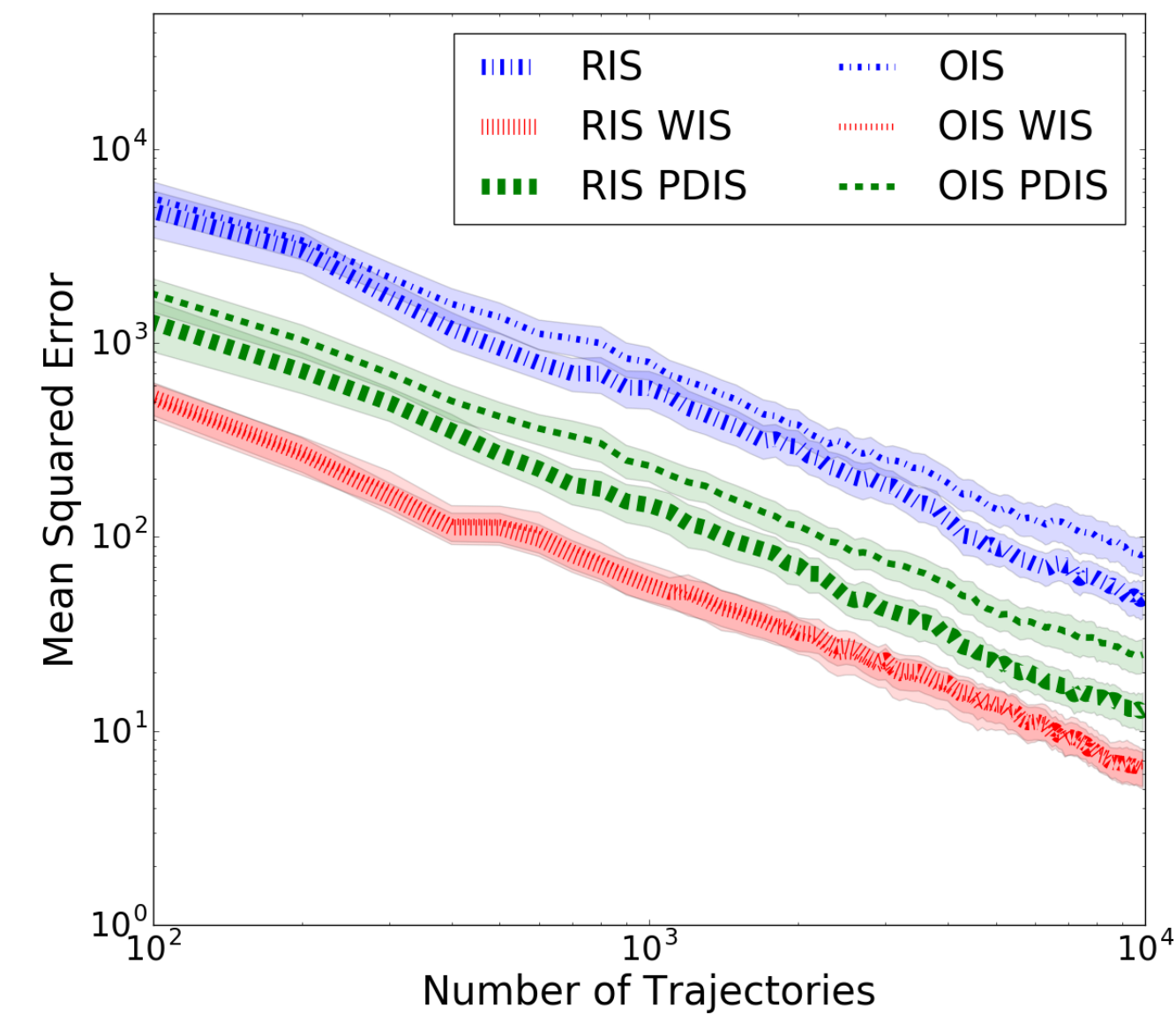
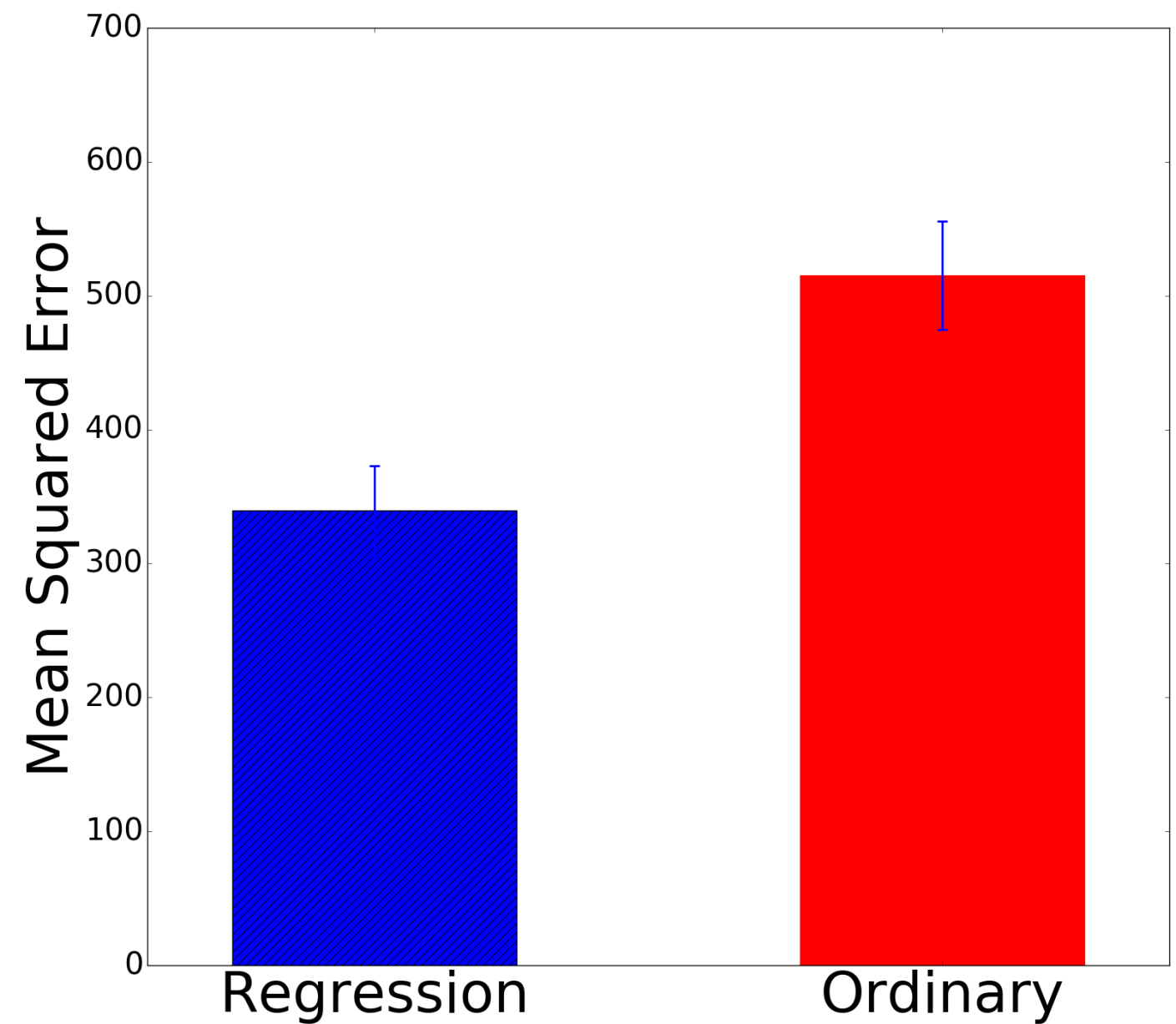
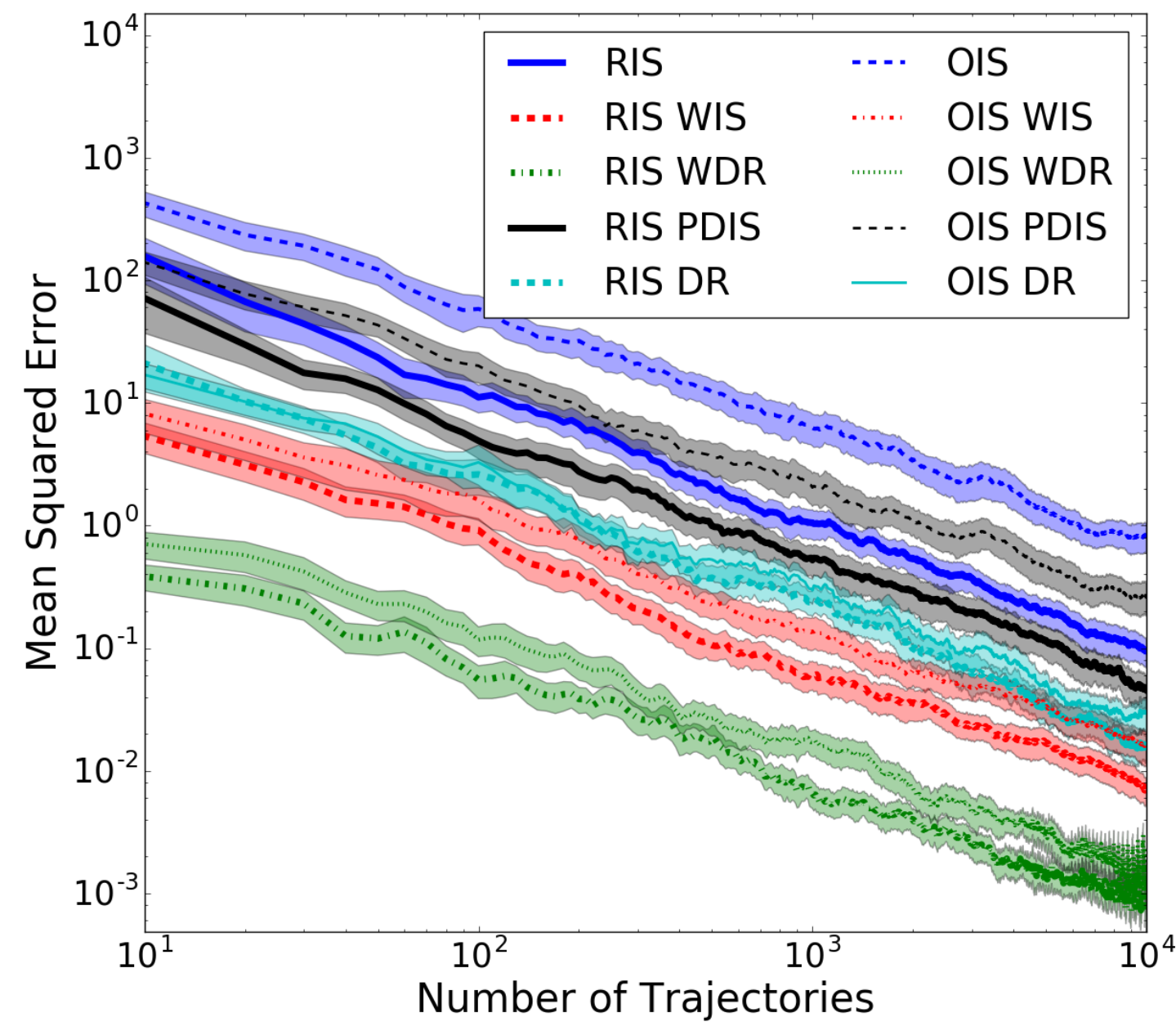
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2. Replacing the true behavior policy action probabilities with their empirical estimate **increases the effectiveness** of importance sampling.



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1. Off-policy importance sampling methods typically use the known behavior policy action probabilities.
2. Replacing the true behavior policy action probabilities with their empirical estimate **increases the effectiveness** of importance sampling.
3. We introduced the **regression importance sampling** and show it improves batch policy evaluation in a wide range of RL tasks.



Tuesday 6:30-9,  
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