



Recap

- Motion planning: finding a collision-free path from A to B
- Two families:
 - (Graph) Search Based Motion Planning
 - Sampling Based Motion Planning
- Ideally, instead of finding <u>a path</u>, we find the <u>shortest path</u>

R.O.B.O.T. Comics

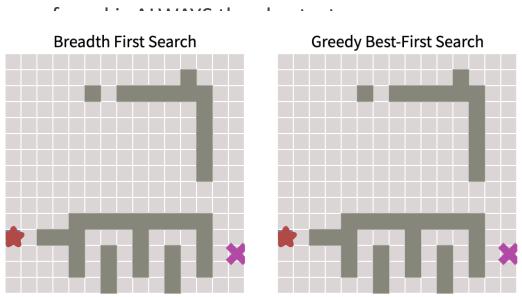


"HIS PATH-PLANNING MAY BE SUB-OPTIMAL, BUT IT'S GOT FLAIR."

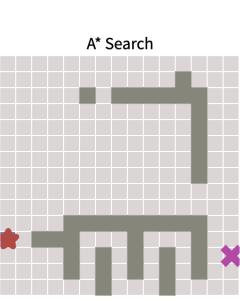


Exercise – Optimality

- Optimal algorithm:
 - If the algorithm finds a path, the path









Play with them!

- https://cs.stanford.edu/people/abisee/tutorial/bfs.html
- https://cs.stanford.edu/people/abisee/tutorial/dfs.html
- https://cs.stanford.edu/people/abisee/tutorial/greedy.html
- https://cs.stanford.edu/people/abisee/tutorial/astar.html



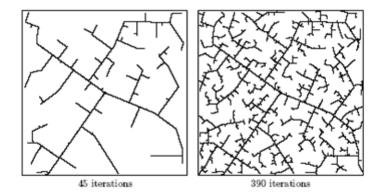
Summary of Graph Search Algorithms

- Breadth First Search: First in first out, optimal but slow
- Depth First Search: Last in first out, not optimal and meandering
- Greedy Best First: Goes for the target, fast but easily tricked
- A* Search: "Best of both worlds": optimal and fast
- Dijkstra: Explores in increasing order of cost, optimal but slow



What will you learn today?

- Sampling based motion planning
 - Why do we need them? Curse of dimensionality
 - PRM
 - RRT





General Insights from Motion Planning

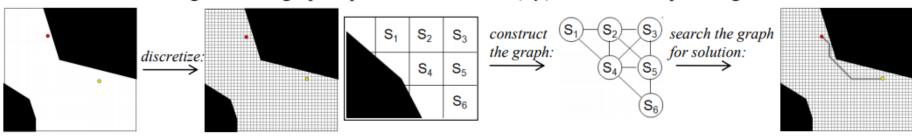
In the real world, the computational time for motion planning for robots is key and depends on two factors:

- Obstacle checking: This is significant if
 - Your robot is complex (e.g. a manipulator arm with many joints),
 - If your environment representation is complex (e.g. detailed meshes to perform collision checking with)
 - If you have a very large number of samples to check
- Priority queue operations: This is significant if
 - Planning in high-dimensional space, hence large state spaces
 - Many alternatives, with no clear inferior / superior choices



What is the problem with search-based motion planners?

2D grid-based graph representation for 2D (x,y) search-based planning:



- Constructing the graph (check all cells to see if they are in collision or not) becomes the real bottleneck!
- Curse of dimensionality!
 - The complexity of the algorithm increases exponentially with the dimensions of the problem

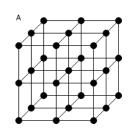


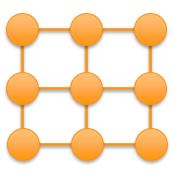
What is the problem with search-based motion planners?

- Curse of dimensionality!
 - The complexity of the search algorithm increases exponentially with the dimensions of the problem
- How many iterations until I find a path with BFS? How many nodes/edges are there if...
 - the problem is 1D
 - the problem is 2D
 - the problem is 3D

...





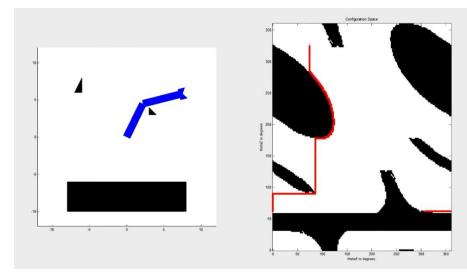




That is really bad for robot arms

- Dimensionality of the space = number of joints
- 7 DoF robot → 7 dimensions!

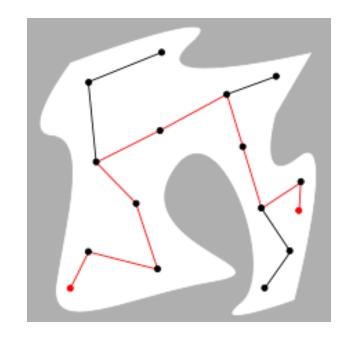
- Imagine we discretize each joint by 5 (0, 45, 90, 135, 180 degrees)
 - Number of cells: 16807



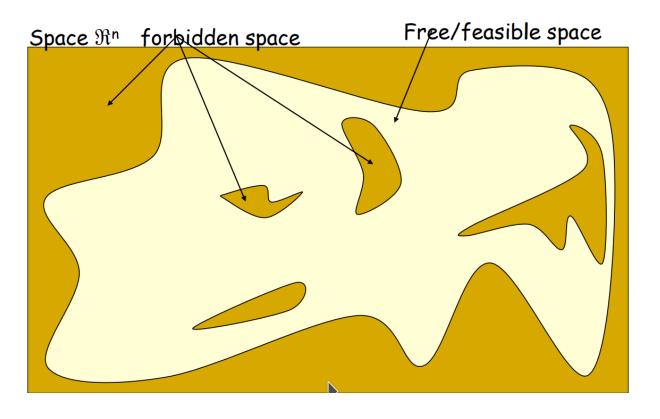


Alternative: Sampling

- We "control" the number of collision checks through a sampling process on the configuration space
- Most significant algorithms:
 - Probabilistic roadmaps (PRM)
 - Rapidly-exploring random trees (RRT)

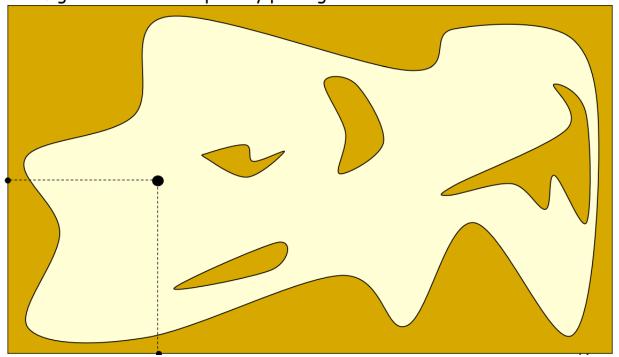






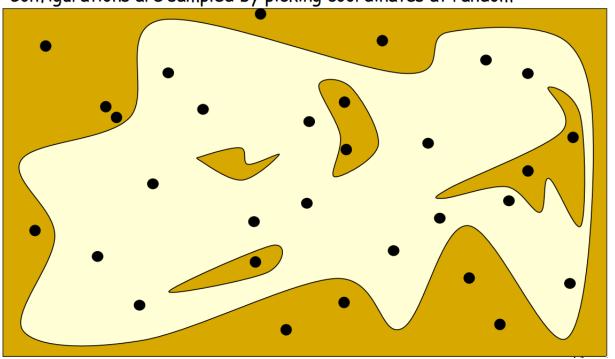


Configurations are sampled by picking coordinates at random



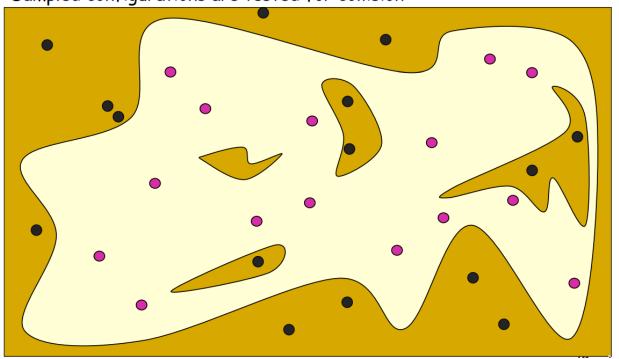


Configurations are sampled by picking coordinates at random



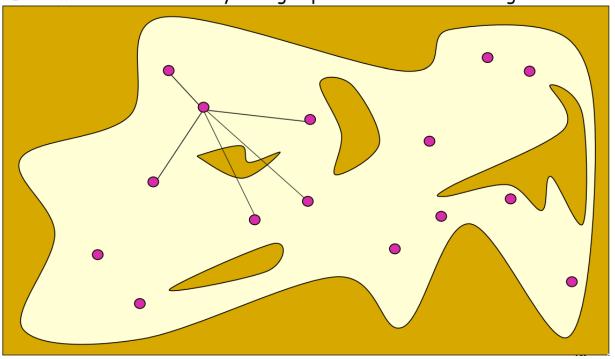


Sampled configurations are tested for collision



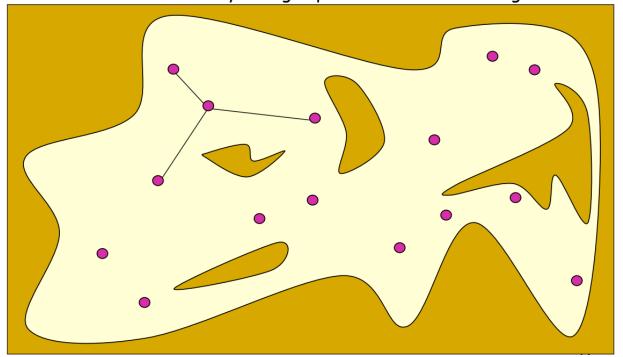


Each milestone is linked by straight paths to its nearest neighbors



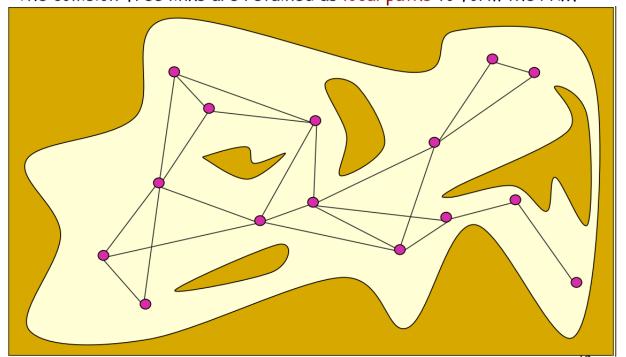


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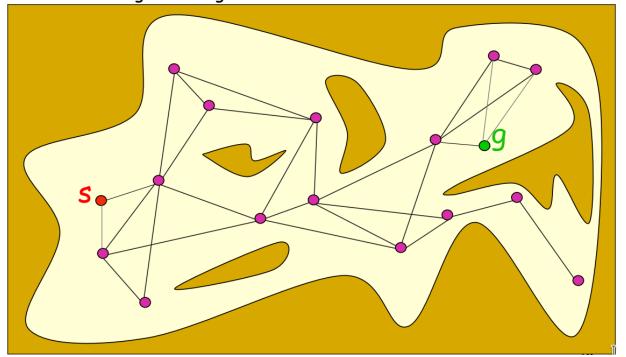


The collision-free links are retained as local paths to form the PRM



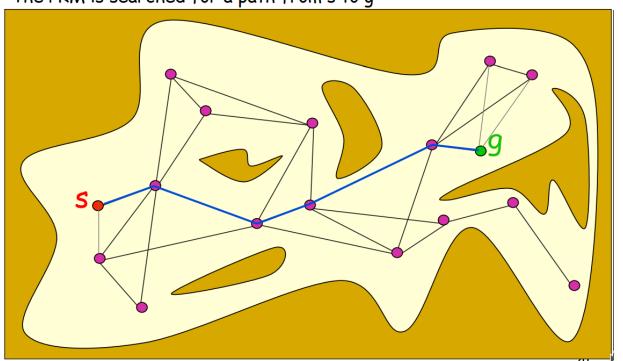


The start and goal configurations are included as milestones





The PRM is searched for a path from s to g





- Build Phase:
 - Randomly sample points in configuration-space. Reject the ones in collision
 - Connect points:
 - We can limit length of the connections: within a ball D
 - We can limit the number of connections per point: at most K connections
 - But we only connect them if the direct line is collision-free
 - Done!
- Query Phase:
 - Add start and goal nodes
 - Run graph search (A* / Dijkstra / ...)

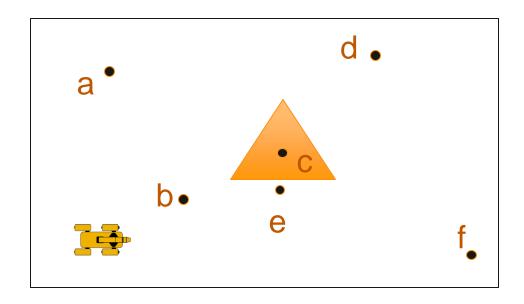


https://pollev.com/robertomartinmartin739

Exercise – PRM

 Given the problem of the map (no limit in connection length or number of connections)

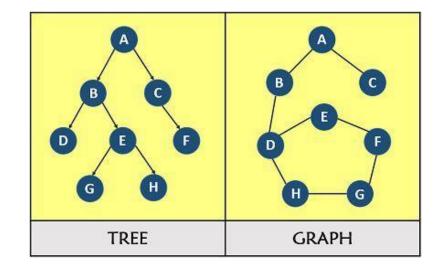






Rapidly-Exploring Random Trees (RRT)

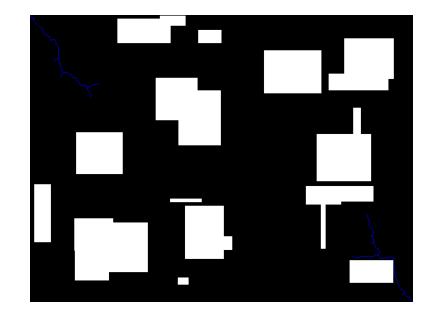
- What is a tree?
 - A type of graph that:
 - it is connected
 - doesn't have cycles
 - has a single node that is the root (has no parents)





Rapidly-Exploring Random Trees (RRT)

- Sample a random point in the space
- Create a new node in the tree going from the closest node to the random point towards the point
- Check if the new node is in collision
 - Yes: go to the next iteration
 - No: add to the tree (connected to the closest node) and go to next iteration

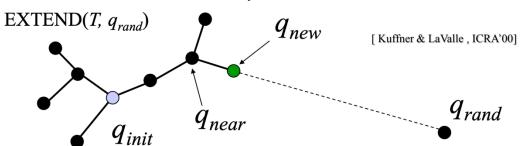




Rapidly-Exploring Random Trees (RRT)

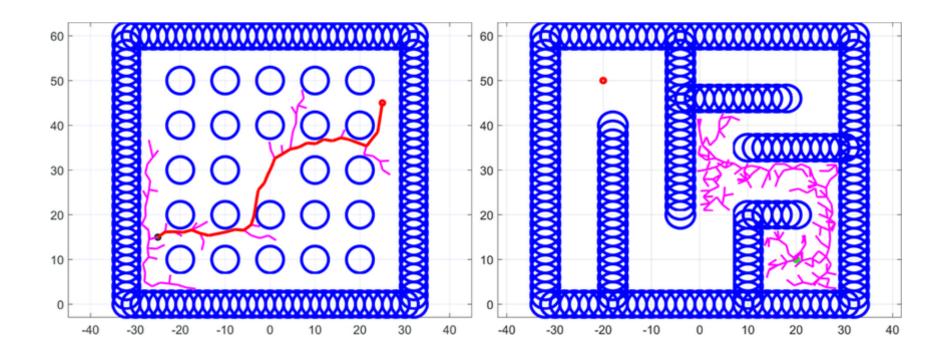
- Sample a random point in the space
- Create a new node in the tree going from the closest node (qnear) to the random point towards the point a distance of "step size" (ε)
- Check if the new node is in collision
 - Yes: go to the next iteration
 - No: add to the tree (connected to the closest node) and go to next iteration

```
BUILD_RRT (q<sub>init</sub>) {
    T.init(q<sub>init</sub>);
    for k = 1 to K do
        q<sub>rand</sub> = RANDOM_CONFIG();
        EXTEND(T, q<sub>rand</sub>)
}
```



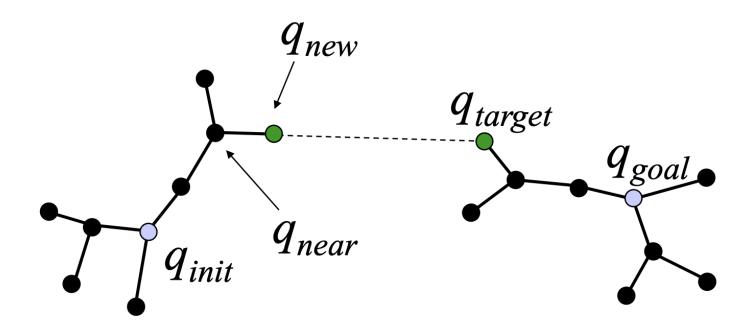


Variant 1: Goal-Biased RRT





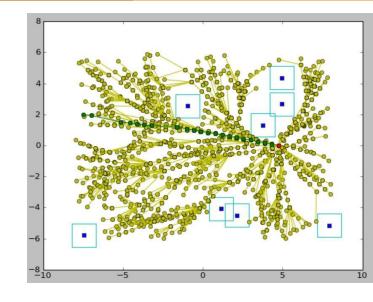
Variant 2: Bidirectional RRT / RRT-Connect

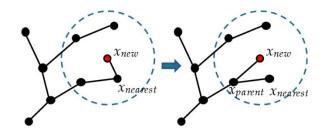


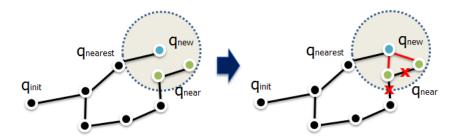


Variant 3: RRT*

- Computes and stores the distance from each node to the parent node
- RRT* algorithm rewires the tree when it finds new connections
- Finds optimal paths (after infinite time...)!





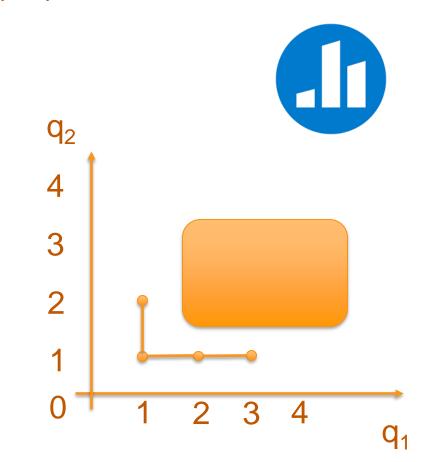




Exercise - RRT

Given the problem of the map

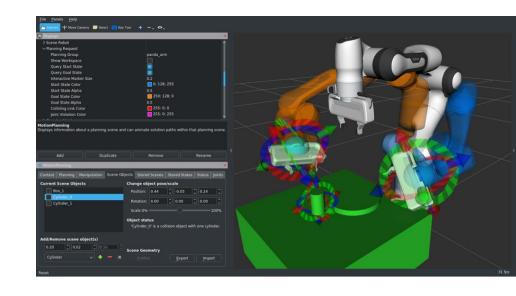
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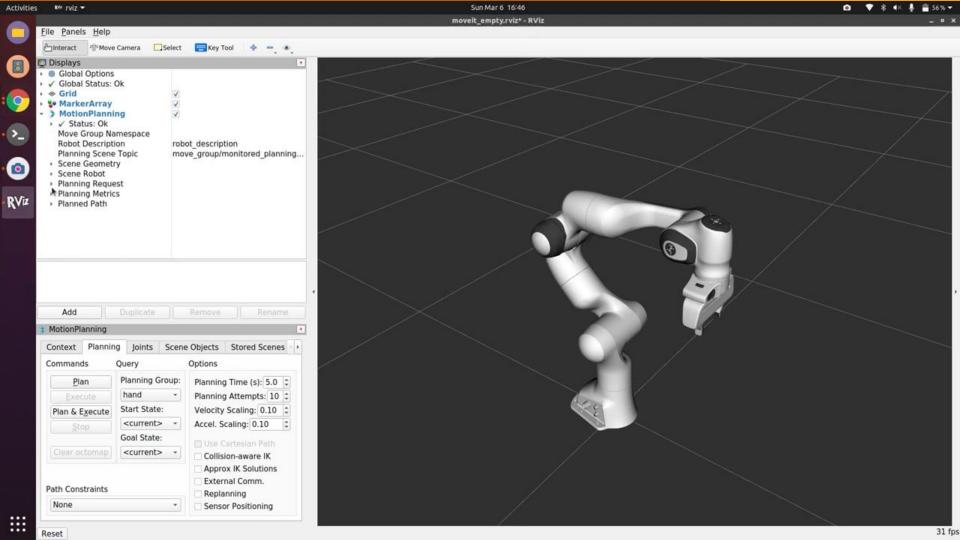




A user-guide to motion planning

- ROS Movelt
 - Library of motion planning algorithms
 - Connection to the ROS environment
 - Get configuration (state) of a robot
 - Uses the viewer from ROS
 - Can execute the plan with a trajectory controller
 - Connects to sensors







Recap

- For large search spaces, discretizing and checking all cells for collisions is unfeasible
- We use sampling (random picked locations) instead
- PRM
 - We sample random locations and connect them. Then use a graph search algorithsm
- RRT
 - We sample at each step and grow the tree until we find a path
- Next: but how do we execute a path that is a sequence of states?

