

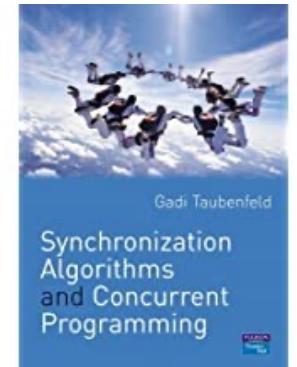
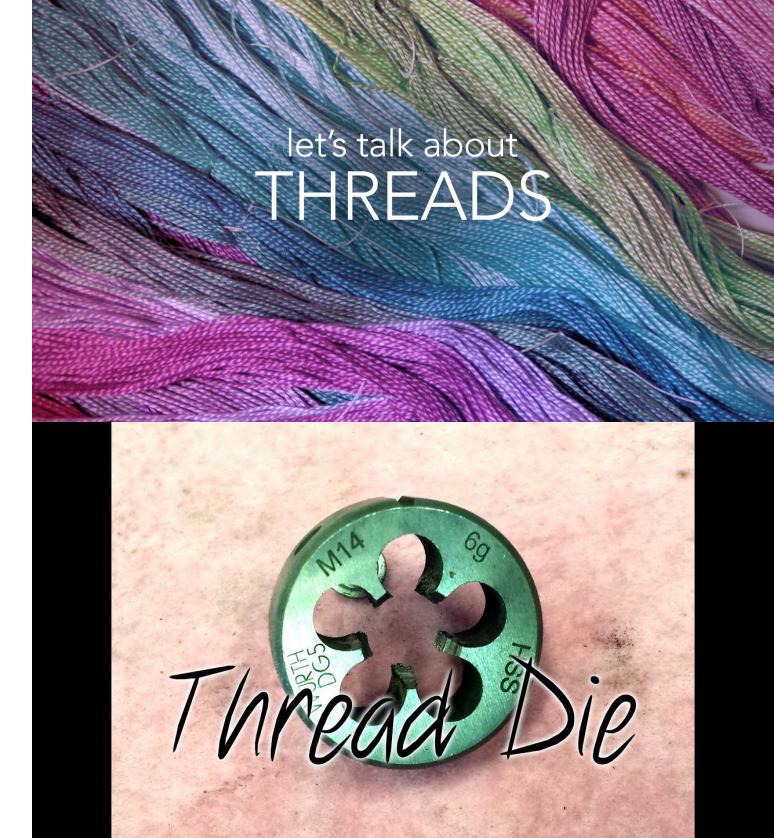
Synchronization Cache Coherence

Chris Rossbach

CS378

Today

- Questions?
- Administrivia
 - Lab 1 due soon
- Material for the day
 - Cache coherence
 - Lock implementation
 - Blocking synchronization
- Acknowledgements
 - Thanks to Gadi Taubenfield: I borrowed from some of his slides on barriers
 - Gadi's materials on synchronization are a great resource



Faux Quiz

(answer any 2, 5 min)

- What is the difference between spinning/busy-wait and blocking synchronization?
- Can you write shared memory parallel applications using single-threaded processes only?
- How do you choose between spinlock/mutex on a multi-processor?
- Define the states of the MESI protocol. Is the E state necessary? Why or why not?
- What is bus locking?
- What is the difference between Mesa and Hoare monitors?
- Why recheck the condition on wakeup from a monitor wait?
- How can you build barriers with spinlocks?
- How can you build barriers with monitors?
- What is the difference between a mutex and a semaphore?

Review: correctness conditions

- Safety
 - Only one thread in the critical region
- Liveness
 - Some thread that enters the entry section eventually enters the critical region
 - Even if other thread takes forever in non-critical region
- Bounded waiting
 - ~~A thread that enters the entry section enters the critical section within some bounded number of operations.~~
 - *If a thread i is in entry section, then there is a bound on the number of times that other threads are allowed to enter the critical section before thread i 's request is granted*

Theorem: Every property is a combination of a safety property and a liveness property.

-Bowen Alpern & Fred Schneider

<https://www.cs.cornell.edu/fbs/publications/defliveness.pdf>

Mutex, spinlock, etc.
are ways to implement

Did we get all the important conditions?
Why is correctness defined in terms of locks?

```
while (1) {  
    Entry section  
    Critical section  
    Exit section  
    Non-critical section  
}
```

Review: Execution Context Management

“Task” == “Flow of Control”, but with less typing

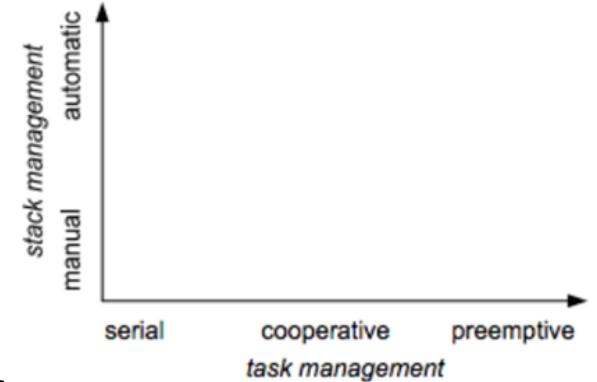
“Stack” == Task State

Task Management

- Preemptive
 - Interleave on uniprocessor
 - Overlap on multiprocessor
- Serial
 - One at a time, no conflict
- Cooperative
 - Yields at well-defined points
 - E.g. wait for long-running I/O

Stack Management

- Manual
 - Inherent in Cooperative
 - Changing at quiescent points
- Automatic
 - Inherent in pre-emptive
 - Downside: Hidden concurrency assumptions

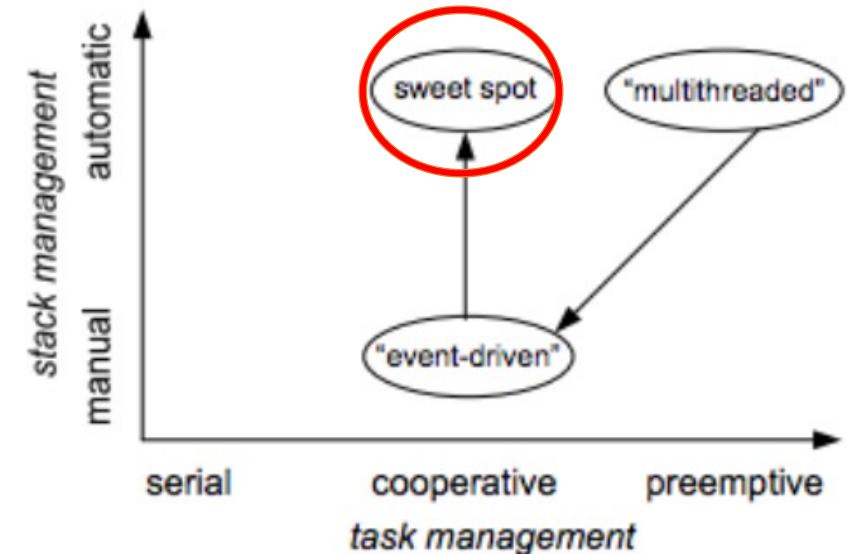


These dimensions can be orthogonal

Review: Fibers: the Sweet Spot?

- Cooperative tasks
 - most desirable when reasoning about concurrency
 - usually associated with event-driven programming
- Automatic stack management
 - most desirable when reading/maintaining code
 - Usually associated with threaded (or serial) programming

Fibers: cooperative threading
with automatic stack
management

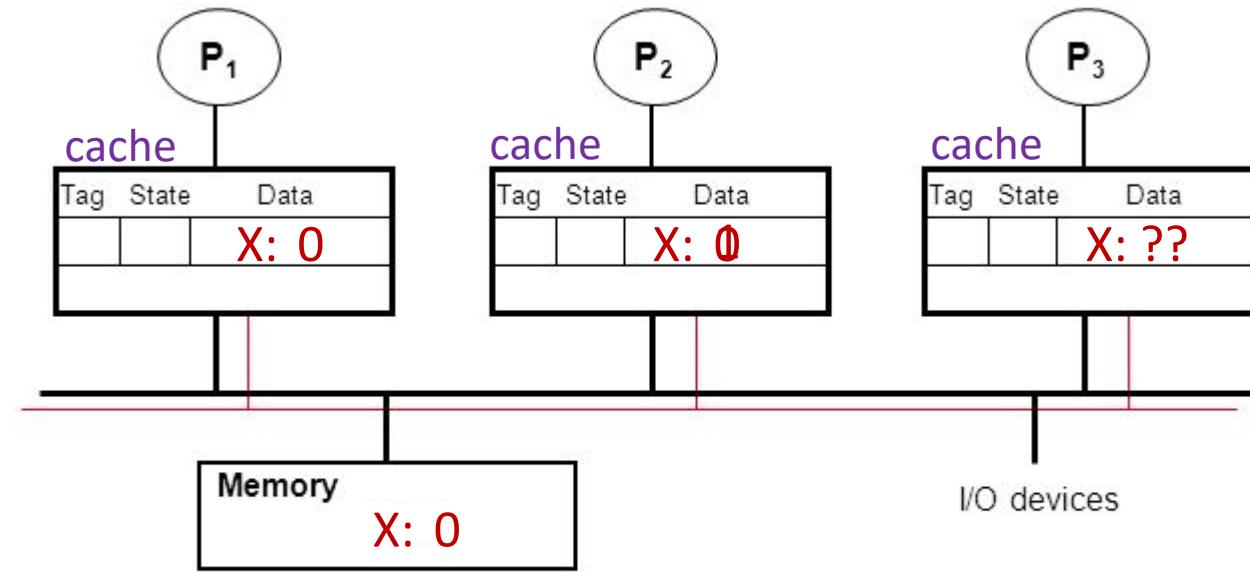


Multiprocessor Cache Coherence

Physics | Concurrency

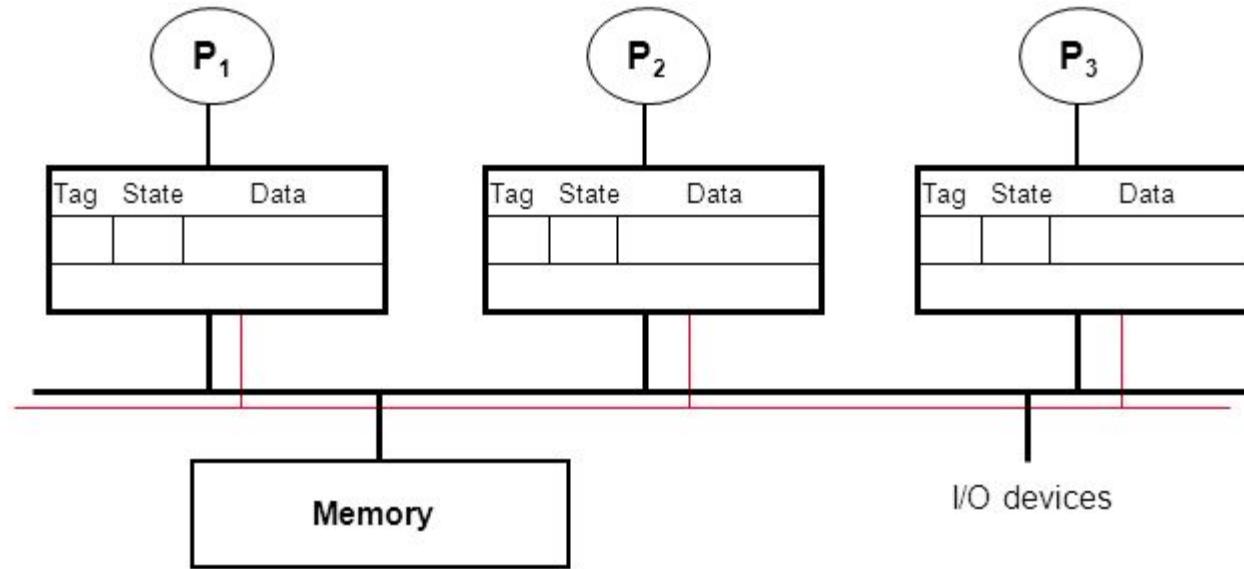
$F = ma \sim coherence$

Multiprocessor Cache Coherence



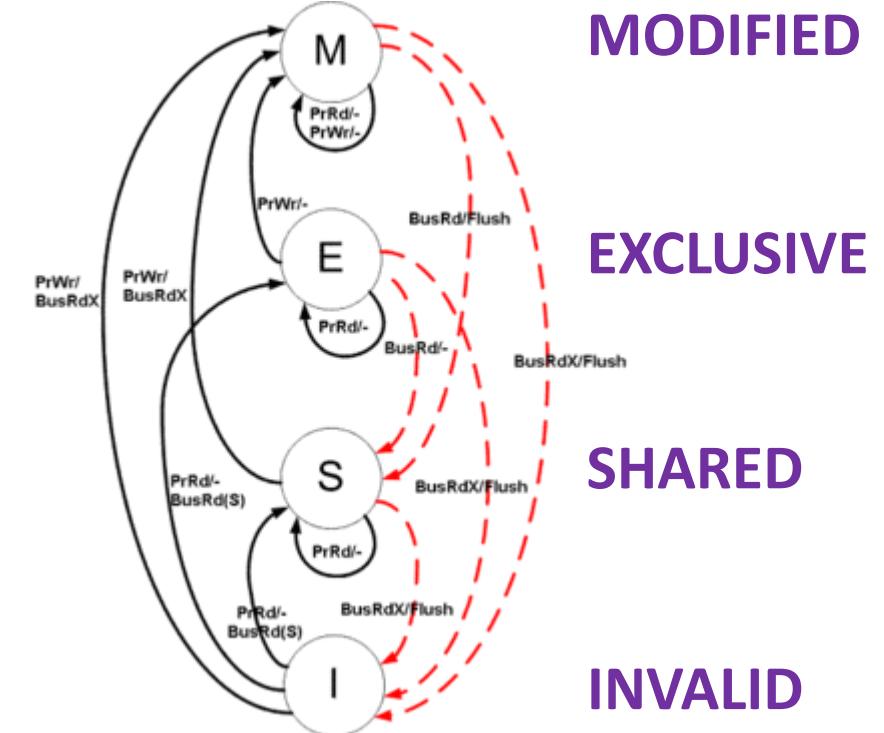
- P_1 : read X
- P_2 : read X
- P_2 : $X++$
- P_3 : read X

Multiprocessor Cache Coherence

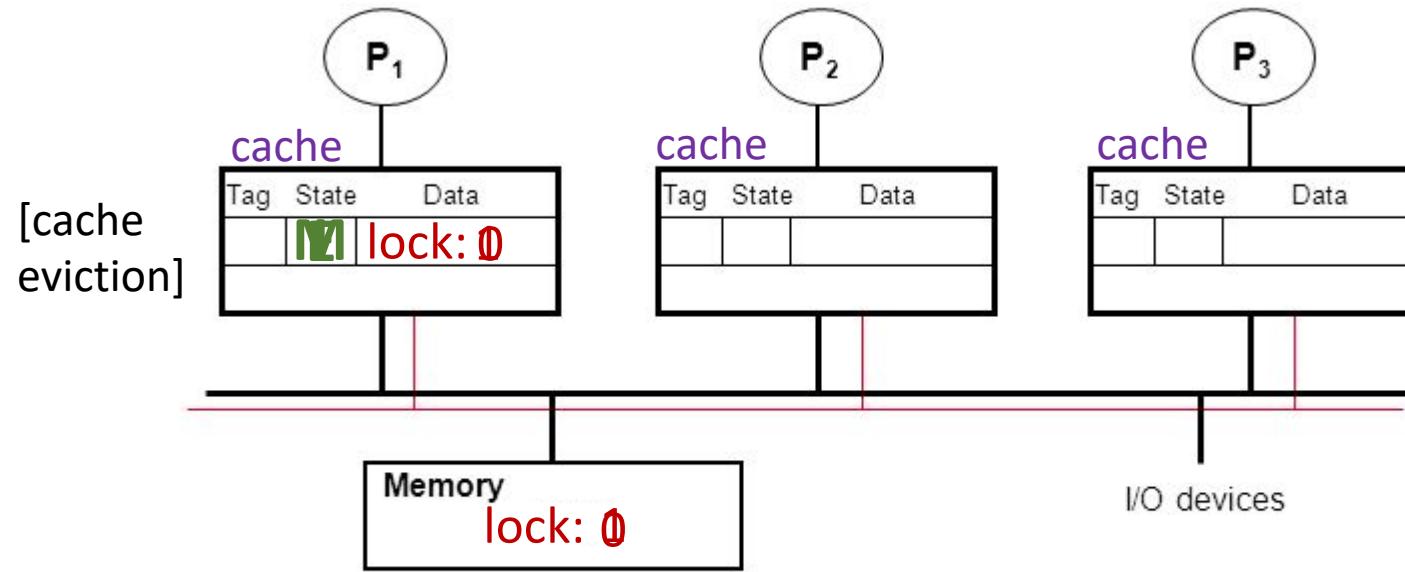


Each cache line has a state (M, E, S, I)

- Processors “snoop” bus to maintain states
- Initially → ‘I’ → Invalid
- Read one → ‘E’ → exclusive
- Reads → ‘S’ → multiple copies possible
- Write → ‘M’ → single copy → lots of cache coherence traffic

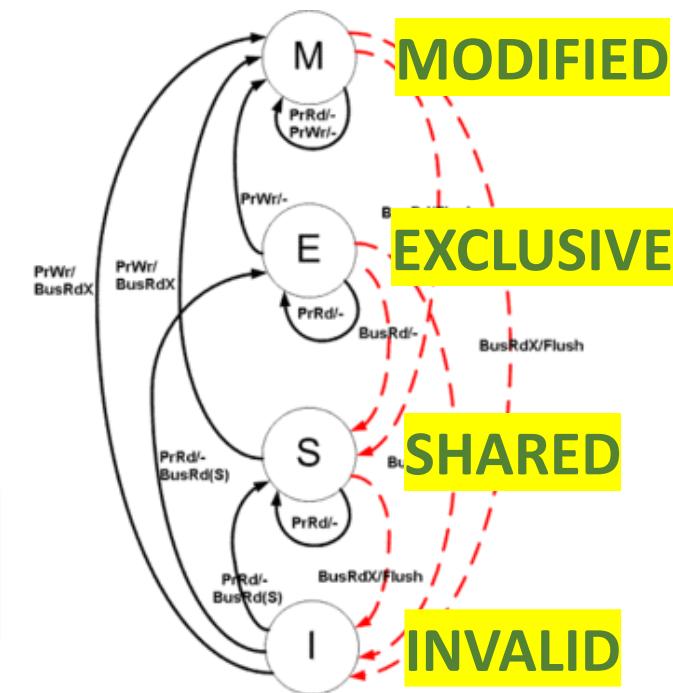
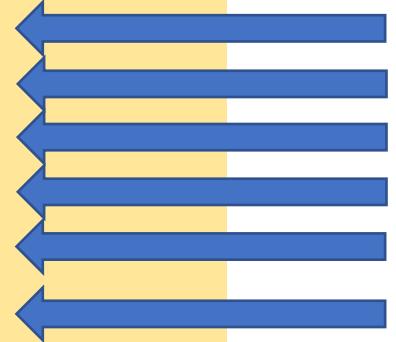


Cache Coherence: single-thread

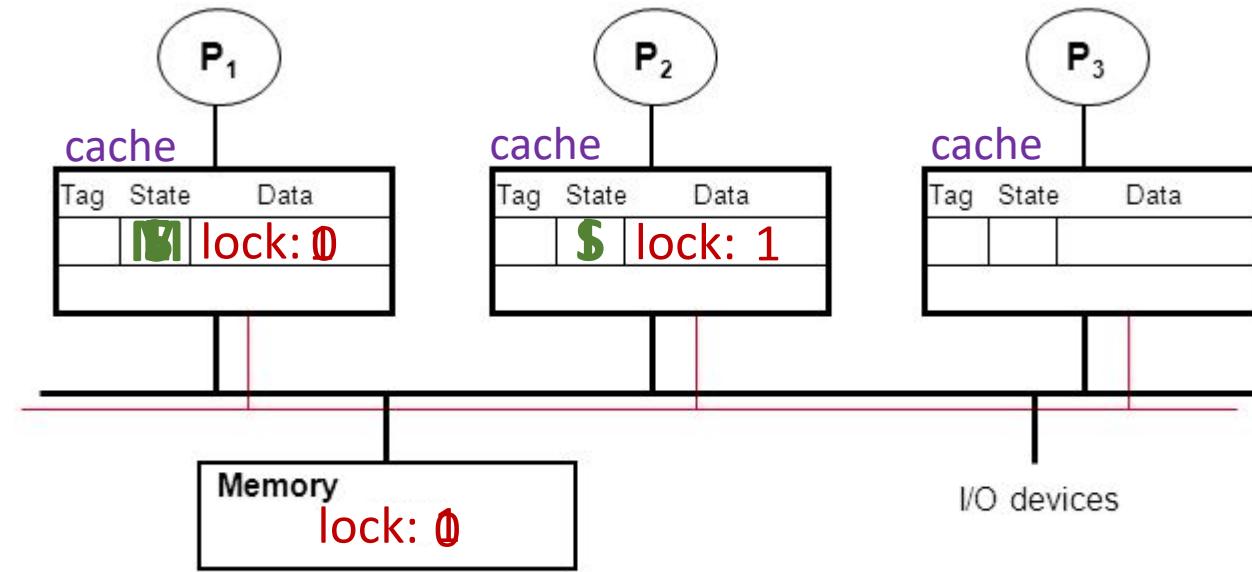


P1

```
// (straw-person lock impl)
// Initially, lock == 0 (unheld)
lock() {
try: load lock, R0
    test R0
    bnz try
    store lock, 1
}
```

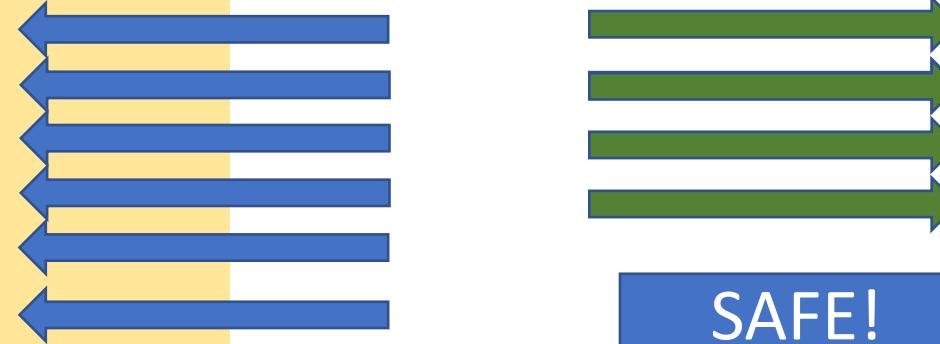


Cache Coherence Action Zone

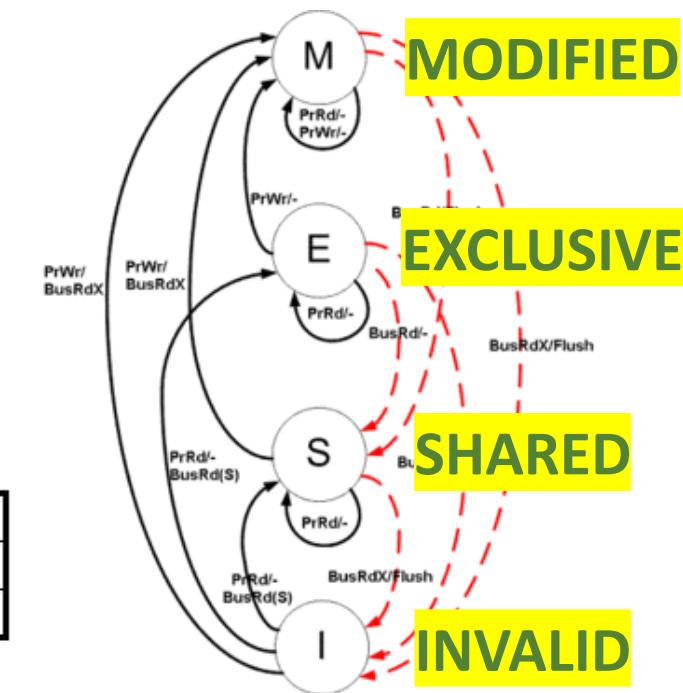


P1

```
// (straw-person lock impl)
// Initially, lock == 0 (unheld)
lock() {
try:    load lock, R0
        test R0
        bnz try
        store lock, 1
}
```



SAFE!

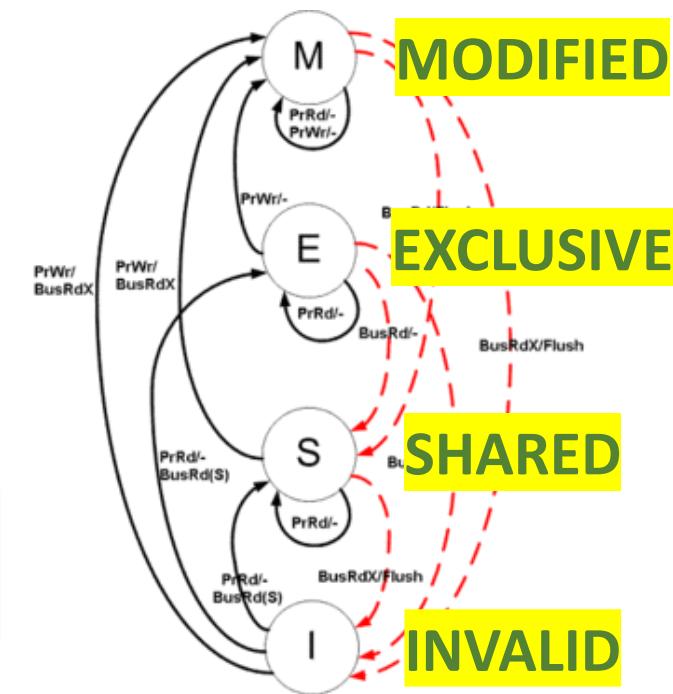
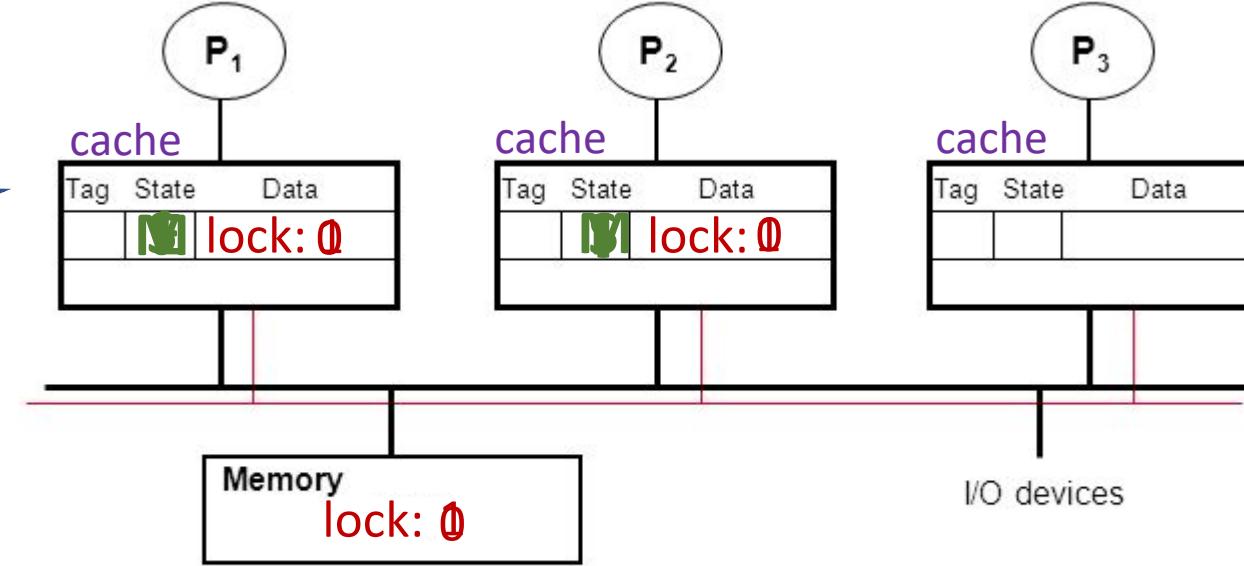


P2

Cache Coherence Action Zone II



P1



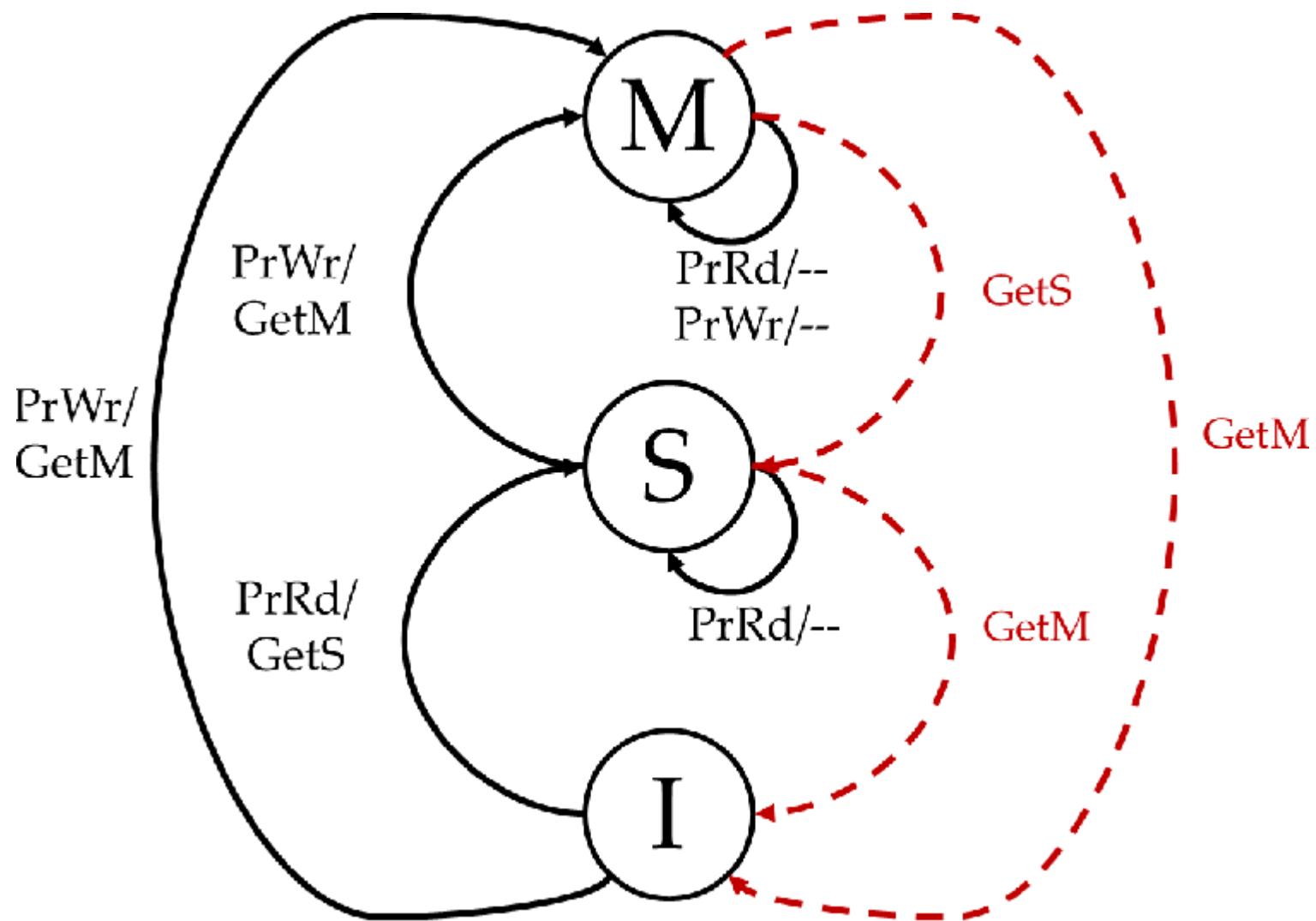
P2

```
// (straw-person lock impl)
// Initially, lock == 0 (unheld)
lock() {
try: load lock, R0
    test R0
    bnz try
    store lock, 1
}
```

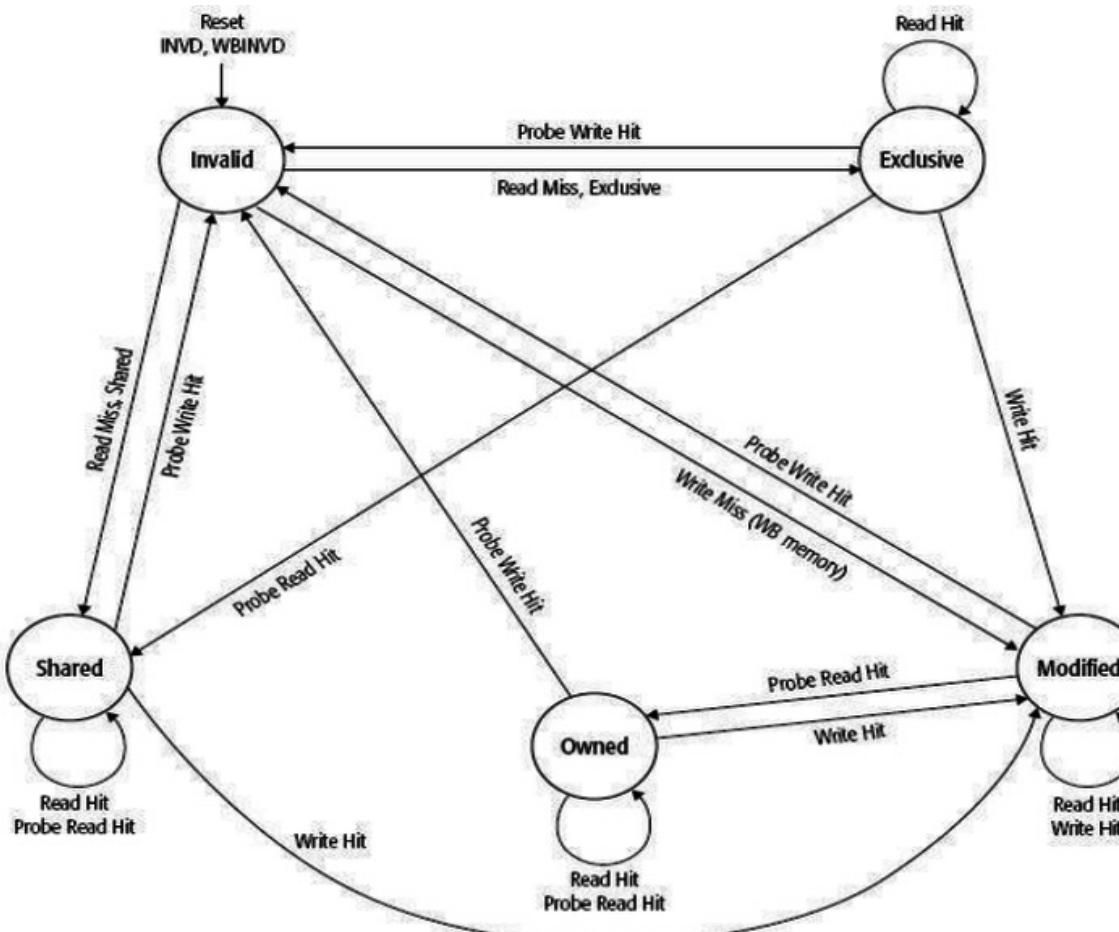


```
// (straw-person lock impl)
// Initially, lock == 0 (unheld)
lock() {
try: load lock, R0
    test R0
    bnz try
    store lock, 1
}
```

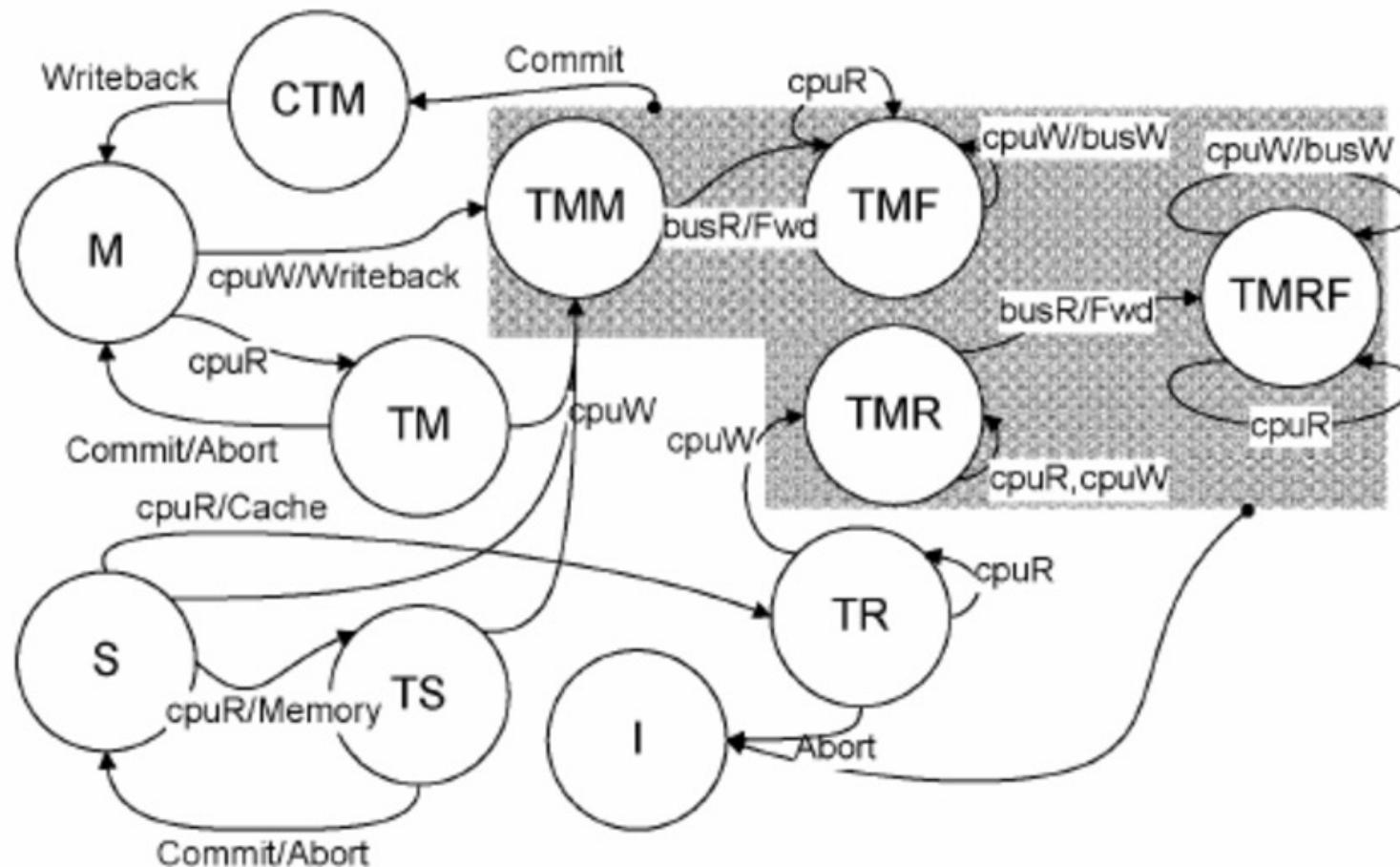
Other Coherence Protocols: MSI



Other Coherence Protocols: MOESI

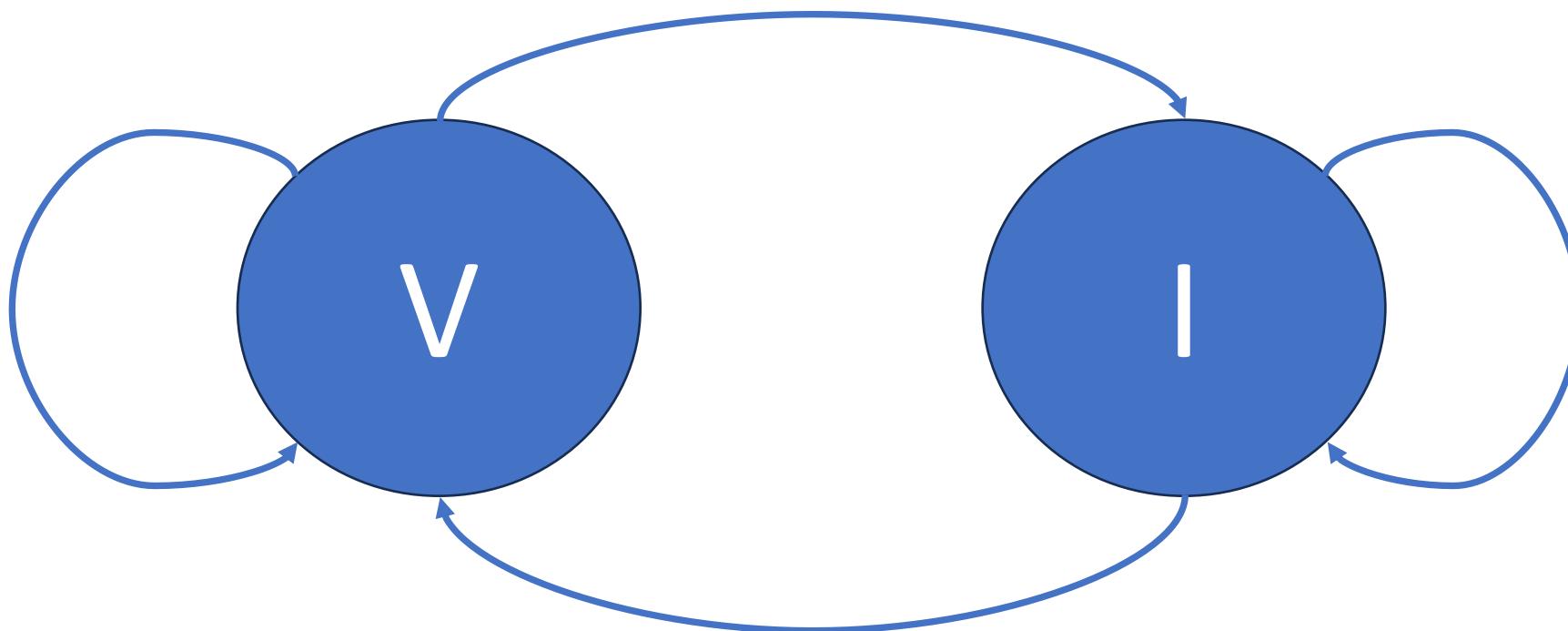


Other Coherence Protocols: FRMSI



Exercise: VI Coherence

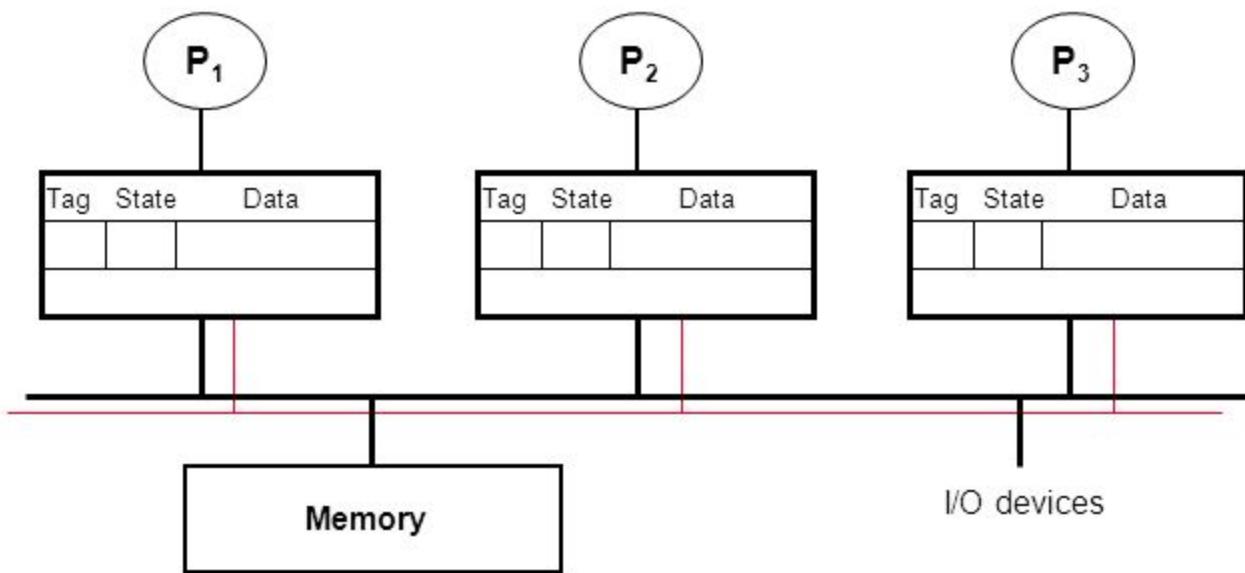
- 2 states: Valid, Invalid
- What are the processor events that drive transitions?
- What are bus events that drive transitions?



Read-Modify-Write (RMW)

- ◆ Implementing locks requires read-modify-write operations
- ◆ Required effect is:
 - An atomic and isolated action
 1. read memory location **AND**
 2. write a new value to the location
 - RMW is *very tricky* in multi-processors
 - Cache coherence alone doesn't solve it

```
// (straw-person lock impl)
// Initially, lock == 0 (unheld)
lock() {
try: load lock, R0
    test R0
    bnz try
    store lock, 1
}
```



Essence of HW-supported RMW

```
// (straw-person lock impl)
// Initially, lock == 0 (unheld)
lock() {
    try: load lock, R0
        test R0
        bnz try
        store lock, 1
}
```

Make this into a single
(atomic hardware instruction)

HW Support for Read-Modify-Write (RMW)

Test & Set	CAS	Exchange, locked increment/decrement,	LLSC: load-linked store-conditional
Most architectures	Many architectures	x86	PPC, Alpha, MIPS
<pre>int TST(addr) { atomic { ret = *addr; if(!*addr) *addr = 1; return ret; } }</pre>	<pre>bool cas(addr, old, new) { atomic { if(*addr == old) { *addr = new; return true; } return false; } }</pre>	<pre>int XCHG(addr, val) { atomic { ret = *addr; *addr = val; return ret; } }</pre>	<pre>bool LLSC(addr, val) { ret = *addr; atomic { if(*addr == ret) { *addr = val; return true; } return false; } }</pre>


```
void CAS_lock(lock) {  
    while(CAS(&lock, 0, 1) != true);  
}
```

HW Support for RMW: LL-SC

LLSC: load-linked store-conditional

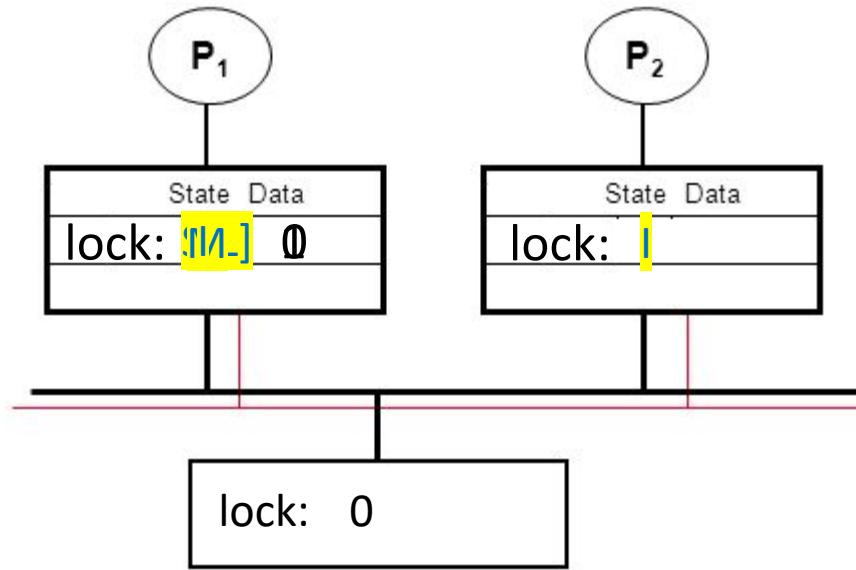
PPC, Alpha, MIPS

```
bool LLSC(addr, val) {
    ret = *addr;
    atomic {
        if(*addr == ret) {
            *addr = val;
            return true;
        }
        return false;
    }
```

```
void LLSC_lock(lock) {
    while(1) {
        old = load-linked(lock);
        if(old == 0 && store-cond(lock, 1))
            return;
    }
}
```

- load-linked is a load that is “linked” to a subsequent store-conditional
- Store-conditional only succeeds if value from linked-load is unchanged

LLSC Lock Action Zone

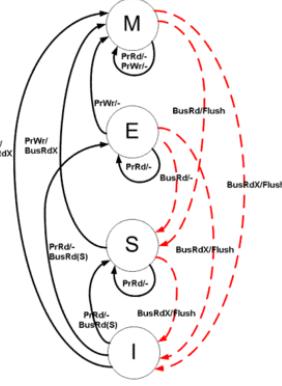


P1

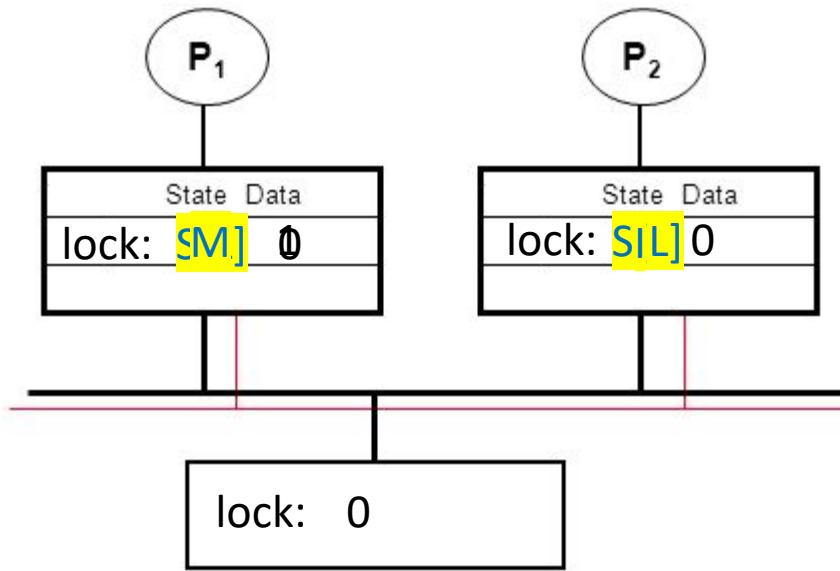
```
lock(lock) {  
    while(1) {  
        old = ll(lock);  
        if(old == 0)  
            if(sc(lock, 1))  
                return;  
    }  
}
```

P2

```
lock(lock) {  
    while(1) {  
        old = ll(lock);  
        if(old == 0)  
            if(sc(lock, 1))  
                return;  
    }  
}
```



LLSC Lock Action Zone II



P1

```
lock(lock) {
    while(1) {
        old = ll(lock);
        if(old == 0)
            if(sc(lock, 1))
                return;
    }
}
```

```
P2  
lock(lock) {  
    while(1) {  
        old = ll(lock);  
        if(old == 0)  
            if(sc(lock, 1))  
                return;  
    }  
}
```



Implementing Locks with Test&set

```
int lock_value = 0;  
int* lock = &lock_value;
```

```
Lock::Acquire() {  
    while (test&set(lock) == 1)  
        ; //spin  
}
```

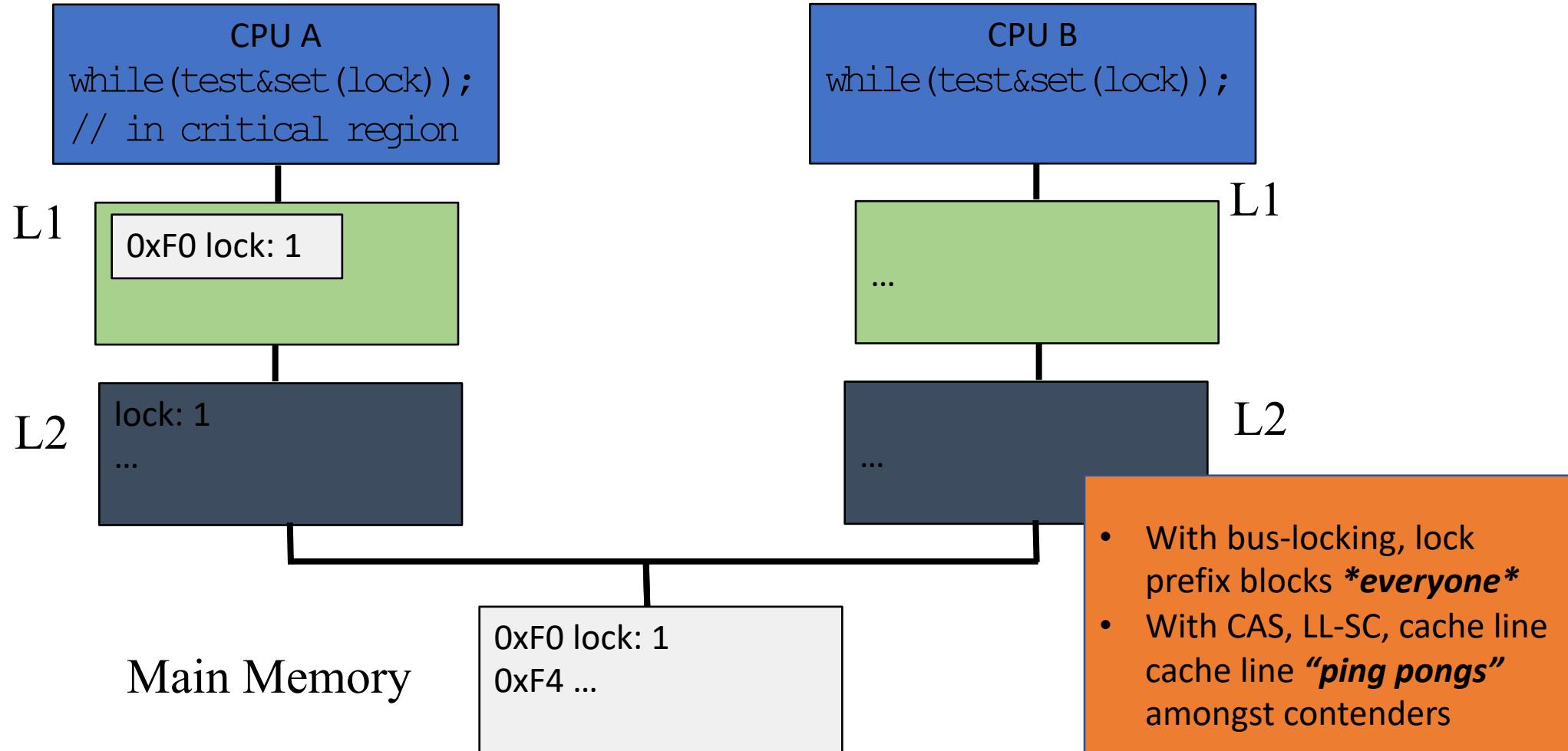
(test & set ~ CAS ~ LLSC)

```
Lock::Release() {  
    *lock = 0;  
}
```

- ◆ What is the problem with this?
 - A. CPU usage B. Memory usage C. Lock::Acquire() latency
 - D. Memory bus usage E. Does not work

Test & Set with Memory Hierarchies

- Initially, lock held by CPU C
- CPU A, B busy-waiting
- What happens to lock variable's cache line when different CPUs contend?



TTS: Reducing busy wait contention

Test&Set

```
Lock::Acquire() {  
    while (test&set(lock) == 1);  
}
```

Busy-wait on in-memory copy

```
Lock::Release() {  
    *lock = 0;  
}
```

Test&Test&Set

```
Lock::Acquire() {  
    while(1) {  
        while (*lock == 1); // spin just reading  
        if (test&set(lock) == 0) break;  
    }  
}
```

Busy-wait on cached copy

```
Lock::Release() {  
    *lock = 0;  
}
```

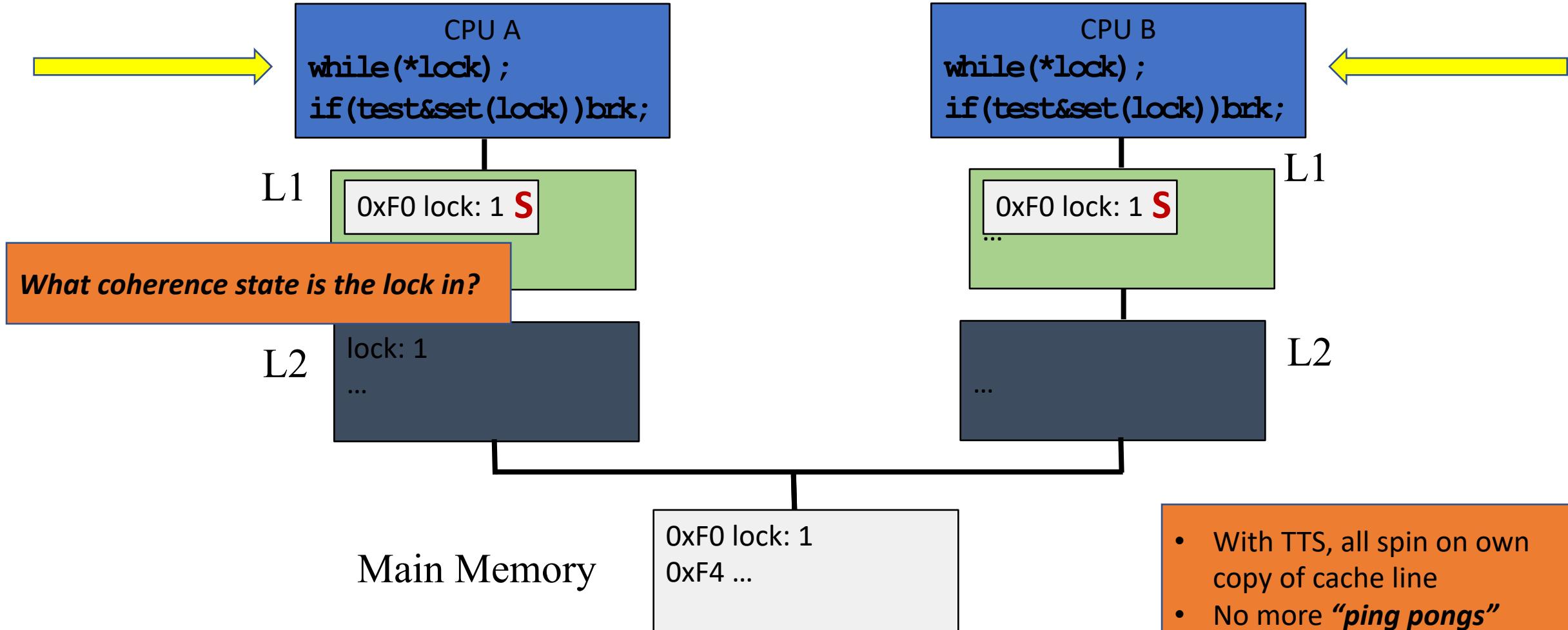
- What is the problem with this?
 - A. CPU usage B. Memory usage C. Lock::Acquire() latency
 - D. Memory bus usage E. Does not work

Test & Test & Set w Memory Hierarchies

CPU C
// in critical region

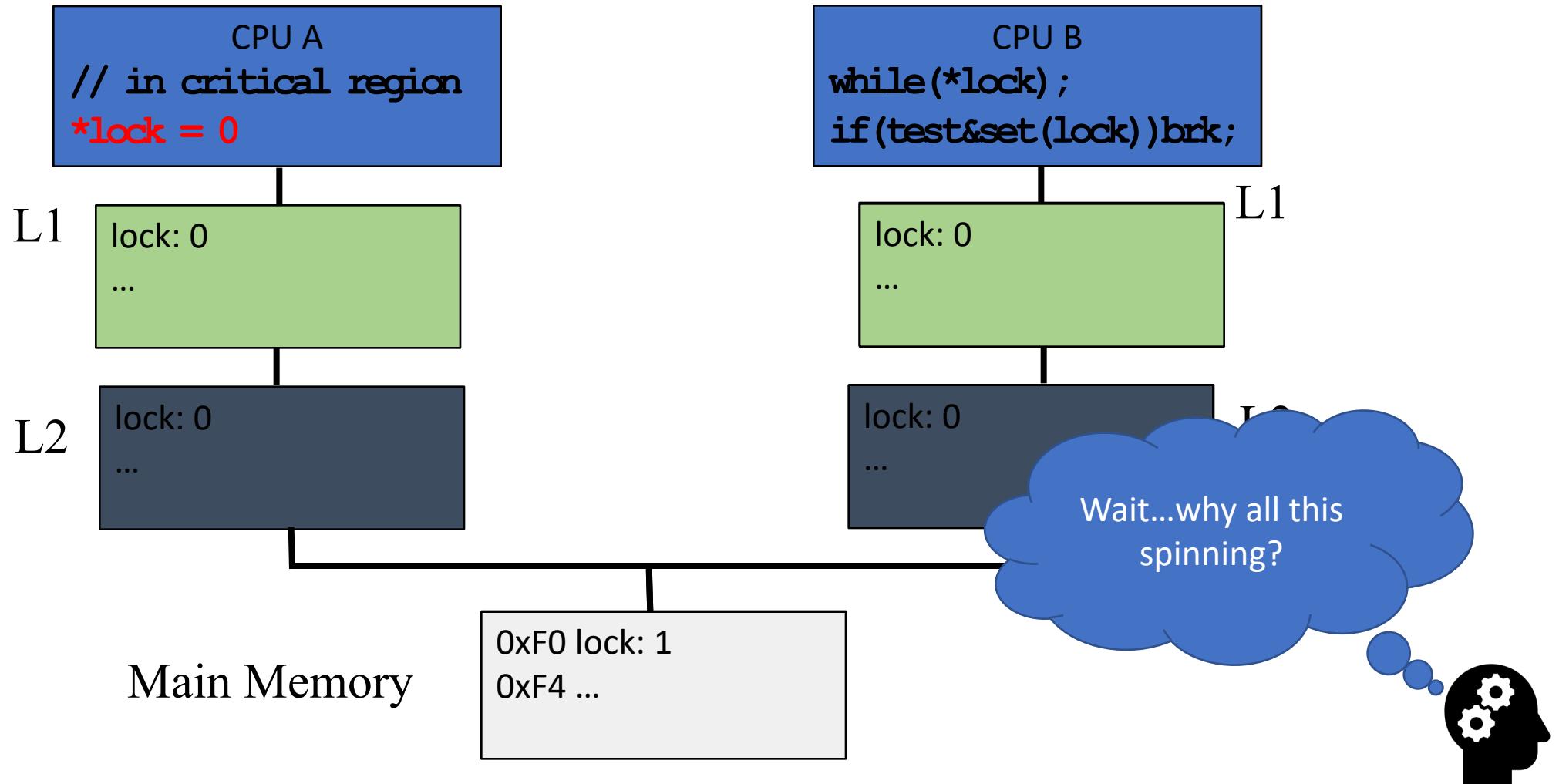


- Initially, lock held by CPU C
- CPU A, B busy-waiting
- Now what happens to lock variable's cache line when different CPUs contend?



Test & Test & Set with Memory Hierarchies

What happens to lock variable's cache line when different cpu's contend for the same lock?



How can we improve over busy-wait?

```
Lock::Acquire() {  
    while(1) {  
        while (*lock == 1); // spin just reading  
        if (test&set(lock) == 0) break;  
    }  
}
```

Mutex

- Same abstraction as spinlock
- But is a “blocking” primitive
 - Lock available → same behavior
 - Lock held → yield/block
- Many ways to yield
- Simplest case of semaphore

```
void cm3_lock(u8_t* M) {  
    u8_t LockedIn = 0;  
    do {  
        if (__LDREXB(Mutex) == 0) {  
            // unlocked: try to obtain lock  
            if (__STREXB(1, Mutex)) { // got lock  
                __CLREX(); // remove __LDREXB() lock  
                LockedIn = 1;  
            }  
            else task_yield(); // give away cpu  
        }  
        else task_yield(); // give away cpu  
    } while (!LockedIn);
```

- Is it better to use a spinlock or mutex on a uni-processor?
- Is it better to use a spinlock or mutex on a multi-processor?
- How do you choose between spinlock/mutex on a multi-processor?

Lock Pitfalls...



A(prio-0) → lock (my_lock) ;

B(prio-100) → lock (my_lock) ;

ACK! Priority Inversion!

Solution?

Priority inheritance: A runs at B's priority

MARS pathfinder failure:

<http://wiki.csie.ncku.edu.tw/embedded/priority-inversion-on-Mars.pdf>

Other ideas?

Can you build a lock without HW RMW?

Dekker's Algorithm

```

variables
    wants_to_enter : array of 2 booleans
    turn : integer

wants_to_enter[0] ← false
wants_to_enter[1] ← false
turn ← 0 // or 1
  
```

```

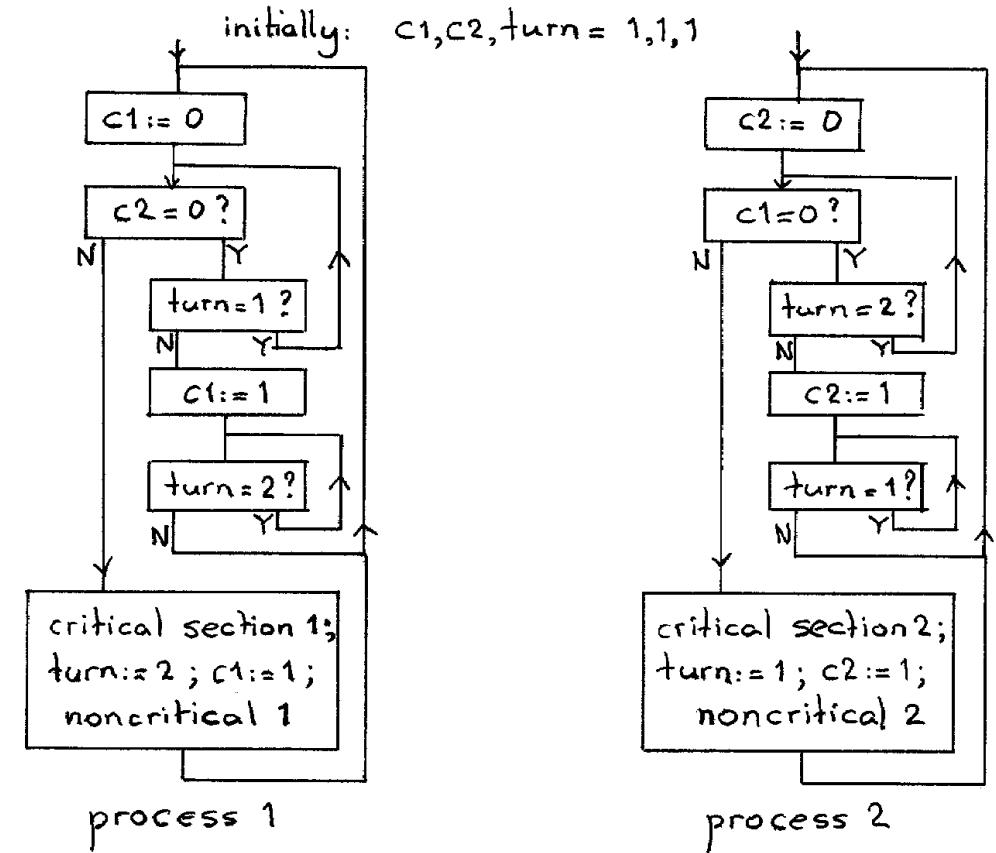
p0:
    wants_to_enter[0] ← true
    while wants_to_enter[1] {
        if turn ≠ 0 {
            wants_to_enter[0] ← false
            while turn ≠ 0 {
                // busy wait
            }
            wants_to_enter[0] ← true
        }
    }

    // critical section
    ...
    turn ← 1
    wants_to_enter[0] ← false
    // remainder section
  
```

```

p1:
    wants_to_enter[1] ← true
    while wants_to_enter[0] {
        if turn ≠ 1 {
            wants_to_enter[1] ← false
            while turn ≠ 1 {
                // busy wait
            }
            wants_to_enter[1] ← true
        }
    }

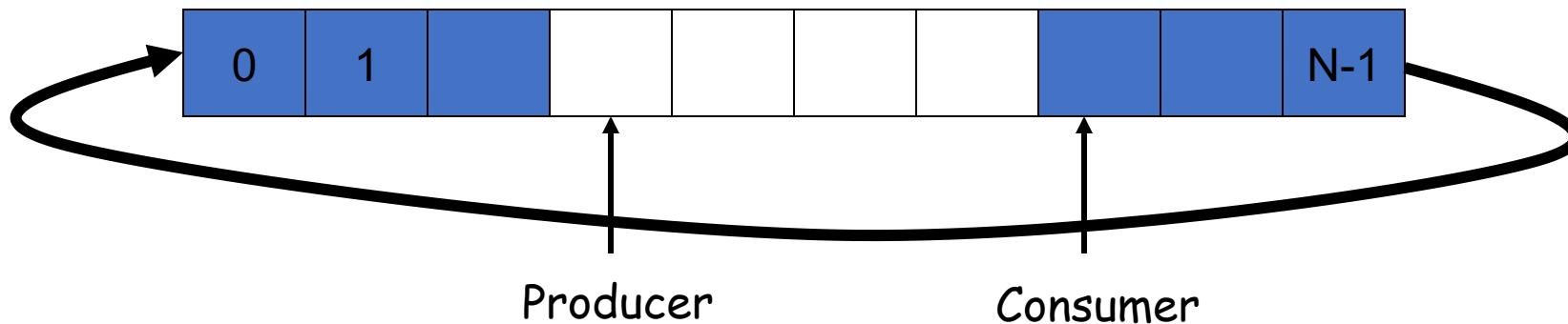
    // critical section
    ...
    turn ← 0
    wants_to_enter[1] ← false
    // remainder section
  
```



Th.J. Dekker's Solution

Producer-Consumer (Bounded-Buffer) Problem

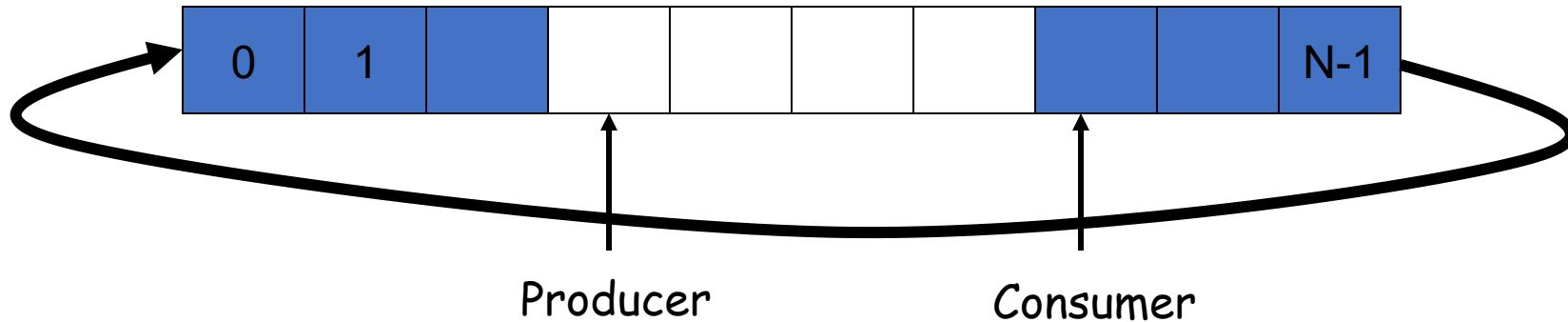
- Bounded buffer: size ‘N’
 - Access entry 0... N-1, then “wrap around” to 0 again
- Producer process writes data to buffer
 - Must not write more than ‘N’ items more than consumer “consumes”
- Consumer process reads data from buffer
 - Should not try to consume if there is no data



OK, let's write some code for this
(using locks only)

- Bounded buffer: size 'N'
 - Access entry 0... N-1, then "wrap around" to 0 again
- Producer writes data
- Consumer reads data

```
object array[N]
void enqueue(object x);
object dequeue();
```



Semaphore Motivation

- Problem with locks: mutual exclusion, but *no ordering*
- Inefficient for producer-consumer (and lots of other things)
 - Producer: creates a resource
 - Consumer: uses a resource
 - bounded buffer between them
 - You need synchronization for correctness, *and...*
 - Scheduling order:
 - producer waits if buffer full, consumer waits if buffer empty

Semaphores

- Synchronization variable
 - Integer value
 - Can't access value directly
 - Must initialize to some value
 - `sem_init(sem_t *s, int pshared, unsigned int value)`
 - Two operations
 - `sem_wait`, or `down()`, `P()`
 - `sem_post`, or `up()`, `V()`

```
int sem_wait(sem_t *s) {
    wait until value of semaphore s
        is greater than 0
    decrement the value of
        semaphore s by 1
}
```

```
function V(semaphore S, integer I):
    [S ← S + I]
function P(semaphore S, integer I):
    repeat:
        if S ≥ I:
            S ← S - I
        break ]
```

```
int sem_post(sem_t *s) {
    increment the value of
        semaphore s by 1
    if there are 1 or more
        threads waiting, wake 1
}
```

Semaphore Uses

- Mutual exclusion
 - Semaphore as mutex
 - What should initial value be?
 - Binary semaphore: X=1
 - (Counting semaphore: X>1)

- Scheduling order
 - One thread waits for another
 - What should initial value be?

```
//thread 0  
... // 1st half of computation  
sem_post(s);
```

```
// initialize to X  
sem_init(s, 0, X)
```

```
sem_wait(s);  
// critical section  
sem_post(s);
```

// thread 1

```
sem_wait(s);  
... // 2nd half of computation
```



Producer-Consumer with semaphores

- Two semaphores
 - `sem_t full; // # of filled slots`
 - `sem_t empty; // # of empty slots`

Is this correct?

- Problem: mutual exclusion?

```
sem_init(&full, 0, 0);
sem_init(&empty, 0, N);
```

```
producer() {
    sem_wait(empty);
    ... // fill a slot
    sem_post(full);
}
```

```
consumer() {
    sem_wait(full);
    ... // empty a slot
    sem_post(empty);
}
```

Producer-Consumer with semaphores

- Three semaphores
 - `sem_t full; // # of filled slots`
 - `sem_t empty; // # of empty slots`
 - `sem_t mutex; // mutual exclusion`

```
sem_init(&full, 0, 0);
sem_init(&empty, 0, N);
sem_init(&mutex, 0, 1);
```

```
producer() {
    sem_wait(empty);
    sem_wait(&mutex);
    ... // fill a slot
    sem_post(&mutex);
    sem_post(full);
}
```

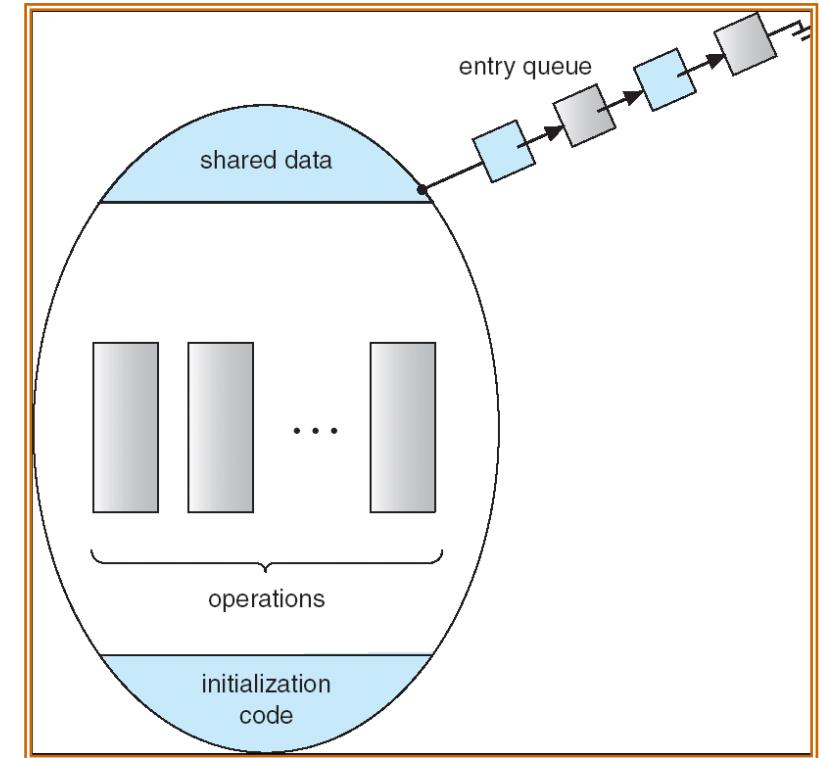
```
consumer() {
    sem_wait(full);
    sem_wait(&mutex);
    ... // empty a slot
    sem_post(&mutex);
    sem_post(empty);
}
```

Pthreads and Semaphores

- `No pthread_semaphore_t` ■ `int sem_wait(sem_t *sem)`
 - Type: `pthread_semaphore_t`
 -
 -
 - `int pthread_semaphore_init(pthread_spinlock_t *lock);`
`int pthread_semaphore_destroy(pthread_spinlock_t *lock);`
...
 ↳ semaphore pointed to by lock
 ↳ shared between threads
 - `????`
 - `int sem_post(sem_t *sem)`
 ↳ value by sem is greater than or equal to current count
 - `int sem_getvalue(sem_t *sem, signed int *val)`
 ↳ value by sem is greater than or equal to current count
- ■ else shared between processes

What is a monitor?

- Monitor: one big lock for set of operations/ methods
- Language-level implementation of mutex
- Entry procedure: called from outside
- Internal procedure: called within monitor
- Wait within monitor releases lock



Many variants...

Pthreads and conditions/monitors

- Type `pthread_cond_t`

Why the `pthread_mutex_t` parameter for `pthread_cond_wait`?

```
int pthread_cond_init(pthread_cond_t *cond,  
                      const pthread_condattr_t *attr);  
int pthread_cond_destroy(pthread_cond_t *cond);  
int pthread_cond_wait(pthread_cond_t *cond,  
                      pthread_mutex_t * mutex);  
int pthread_cond_signal(pthread_cond_t *cond);  
int pthread_cond_broadcast(pthread_cond_t *cond);
```

Java:

synchronized keyword
`wait()` / `notify()` / `notifyAll()`

C#: Monitor class

`Enter()` / `Exit()` /
`Pulse()` / `PulseAll()`

Does this code work?

```
1 public class SynchronizedQueue<T> {
2
3     public void enqueue(T item) {
4         lock.lock();
5         try {
6             if(head == tail - 1)
7                 notFull.wait();
8             Q[head] = item;
9             if(++head == MAX_Q)
10                head = 0;
11             notEmpty.signal();
12         } finally {
13             lock.unlock();
14         }
15     }
16
17     public T dequeue() {
18         T retval = null;
19         lock.lock();
20         try {
21             if(head == tail)
22                 notEmpty.wait();
23             retval = Q[tail];
24             if(++tail == MAX_Q)
25                tail = 0;
26             notFull.signal();
27         } finally {
28             lock.unlock();
29         }
30     }
31 }
```

```
private Lock lock = new ReentrantLock();
private Condition notEmpty = lock.newCondition();
private Condition notFull = lock.newCondition();
private int head = 0;
private int tail = 0;
private int size = MAX_Q;
private T[] Q = new T[size];
```

- Uses “if” to check invariants.
- Why doesn’t **if** work?
- How could we MAKE it work?

Hoare-style Monitors

(aka blocking condition variables)

Given entrance queue 'e', signal queue 's', condition var 'c'

```
enter:  
  if(locked):  
    e.push_back(thread)  
  else  
    lock
```

```
wait C:  
  
  C.q.push_back(thread)  
  schedule // block this thread
```

```
signal C :  
  
  if (C.q.any())  
  
    t = C.q.pop_front() // t → "the signaled thread"  
    s.push_back(t)  
    t.run  
    // block this thread
```

```
schedule:  
  if s.any()  
    t ← s.pop_first()  
    t.run  
  else if e.any()  
    t ← e.pop_first()  
    t.run  
  else  
    unlock // monitor unoccupied
```

- Leave calls schedule
- Signaler must wait, but gets priority over threads on entrance queue
- How is this different from Mesa monitors?
- Is s queue necessary?

Mesa-style monitors

(aka non-blocking condition variables)

```
enter:  
    if locked:  
        e.push_back(thread)  
        block  
    else  
        lock
```

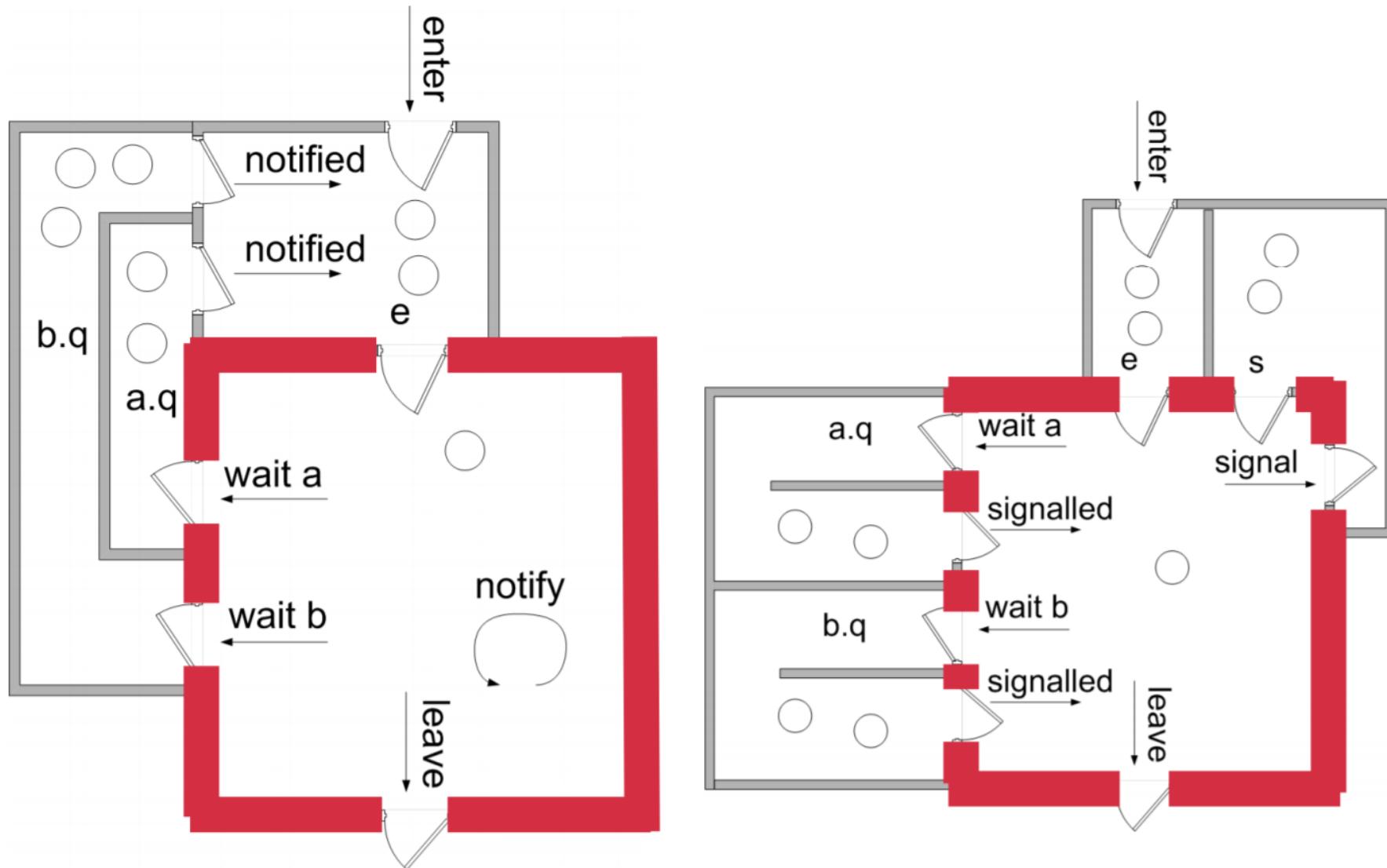
```
schedule:  
    if e.any()  
        t ← e.pop_front  
        t. run  
    else  
        unlock
```

```
notify C:  
    if C.q.any()  
        t ← C.q.pop_front() // t is "notified "  
        e.push_back(t)
```

```
wait C:  
    C.q.push_back(thread)  
    schedule  
    block
```

- (Leave calls schedule)
- Can be extended with extra queues for priority
- What are the differences?

Mesa, Hansen, Hoare



Example: anyone see a bug?

StorageAllocator: MONITOR = BEGIN

availableStorage: INTEGER:

moreAvailable: CONDITION:

Allocate: ENTRY PROCEDURE [*size*: INTEGER]

RETURNS [*p*: POINTER] = BEGIN

 UNTIL *availableStorage* \geq *size*

 DO WAIT *moreAvailable* ENDLOOP;

p \leftarrow <remove chunk of size words & update *availableStorage*>

END;

Free: ENTRY PROCEDURE [*p*: POINTER, *Size*: INTEGER] = BEGIN

 <put back chunk of size words & update *availableStorage*>;

 NOTIFY *moreAvailable* END;

Expand: PUBLIC PROCEDURE [*pOld*: POINTER, *size*: INTEGER] RETURNS [*pNew*: POINTER] = BEGIN

pNew \leftarrow *Allocate*[*size*];

 <copy contents from old block to new block>;

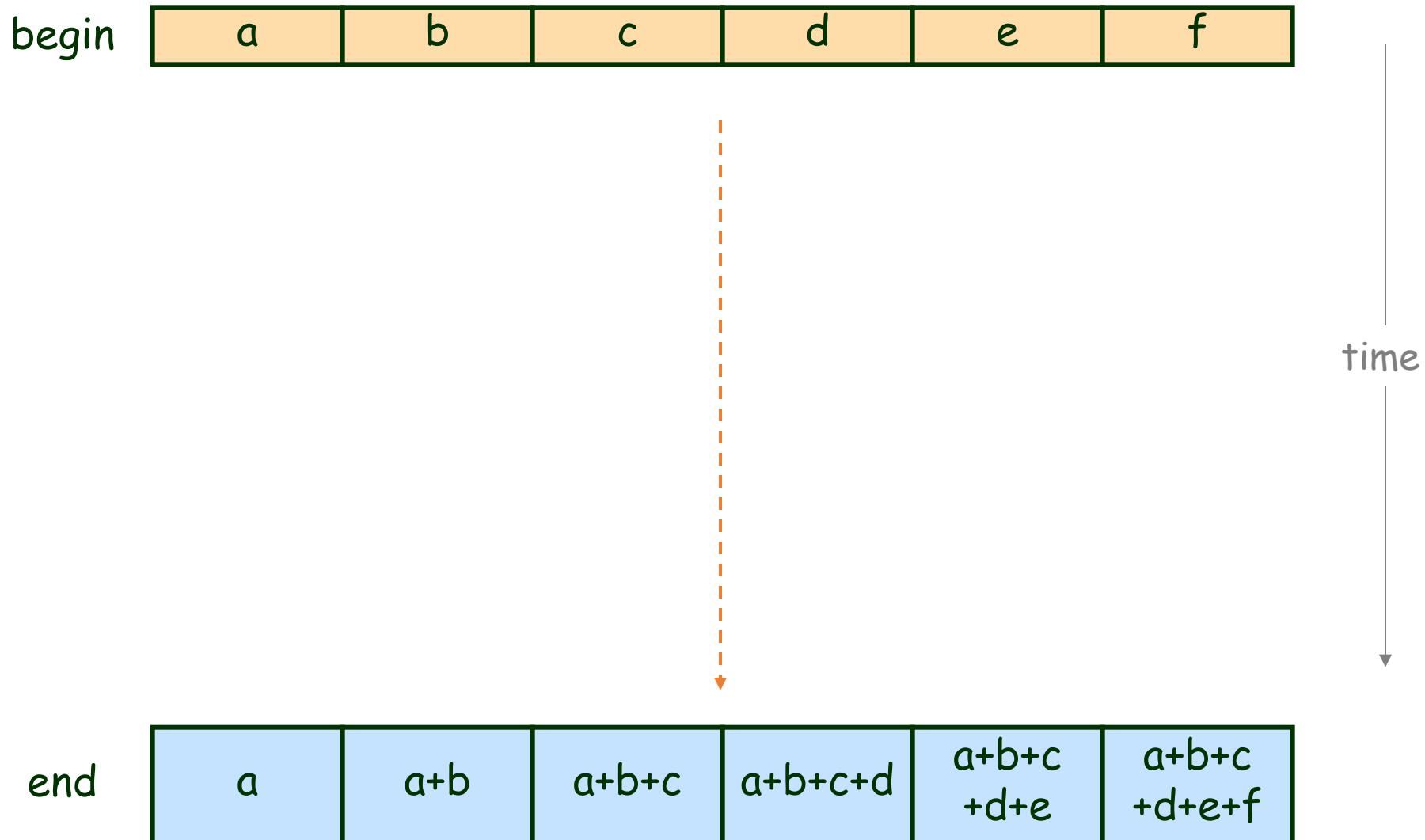
Free[*pOld*] END;

END.

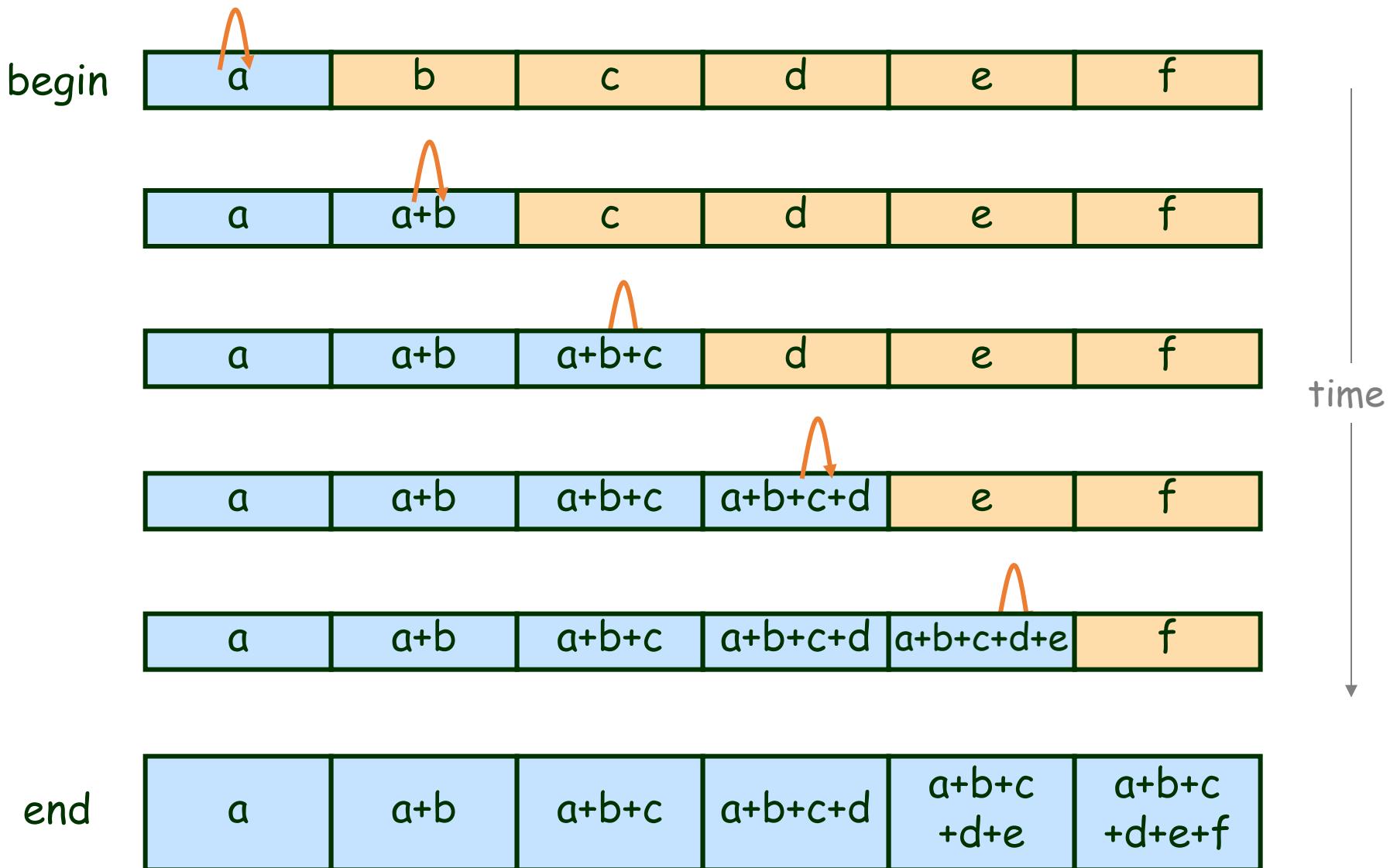
Barriers



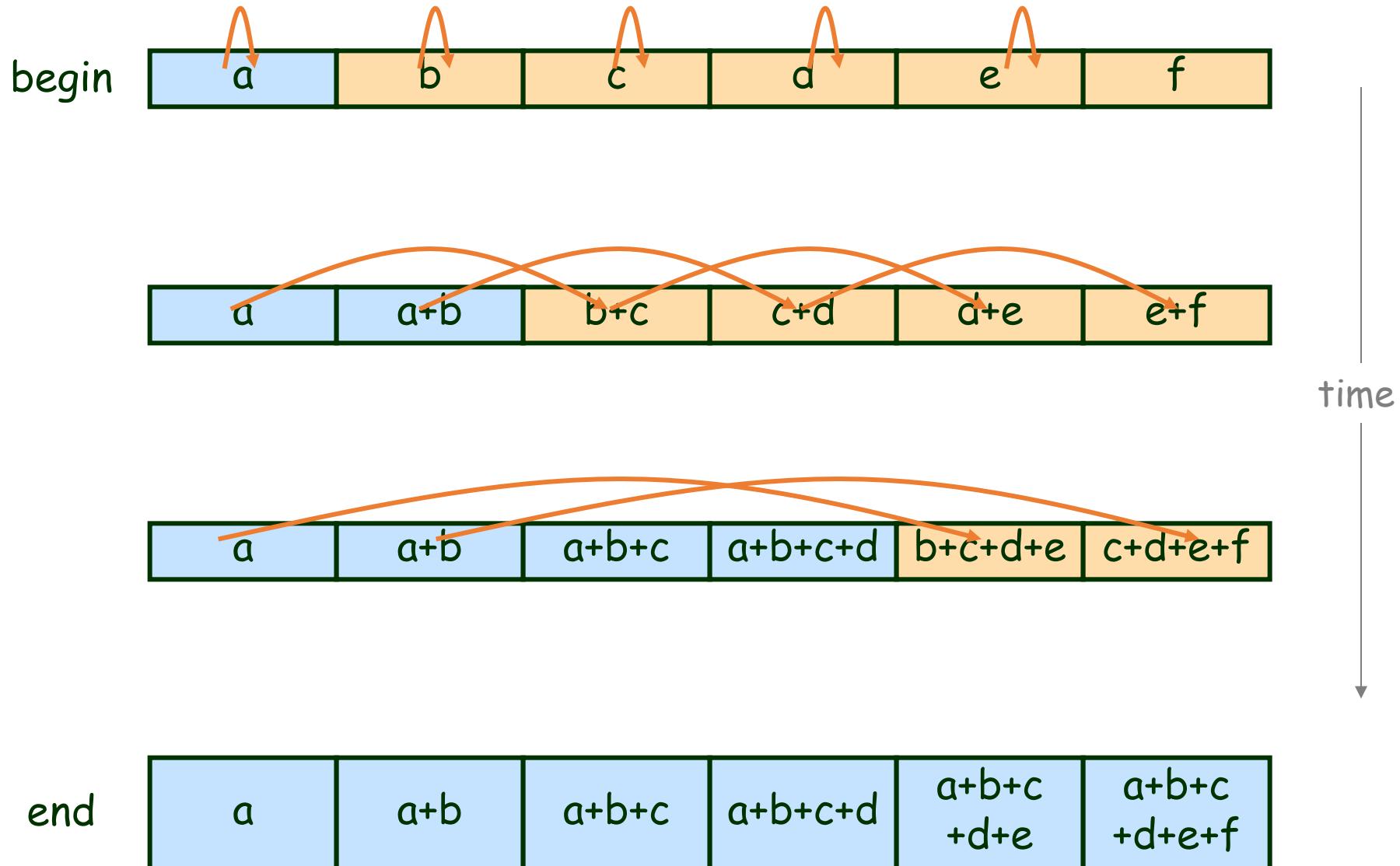
Prefix Sum

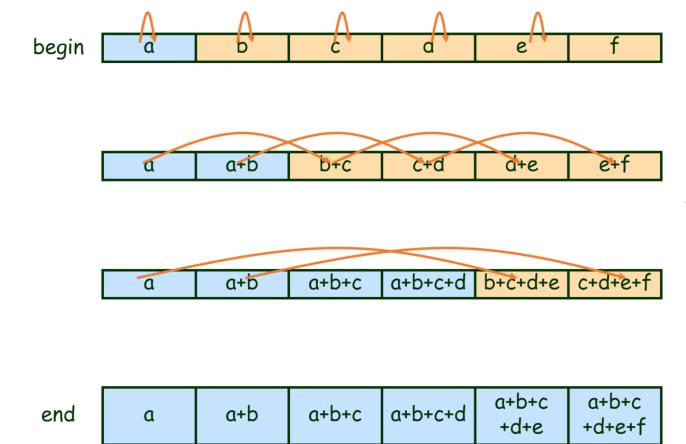


Prefix Sum



Parallel Prefix Sum





PThreads Parallel Prefix Sum

```

int g_values[N] = { a, b, c, d, e, f };

void prefix_sum_thread(void * param) {

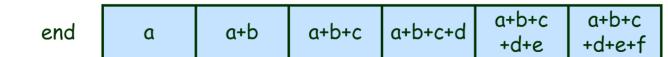
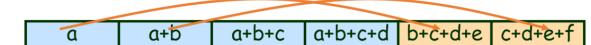
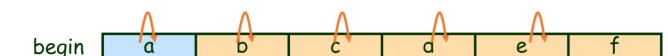
    int i;
    int id = *((int*)param);
    int stride = 0;

    for(stride=1; stride<=N/2; stride<<1) {
        g_values[id+stride] += g_values[id];
    }

}

```

Will this work?



```

pthread_mutex_t g_locks[N] = { MUX_INITIALIZER, ... };
int g_values[N] = { a, b, c, d, e, f };

void prefix_sum_thread(void * param) {

    int i;
    int id = *((int*)param);
    int stride = 0;

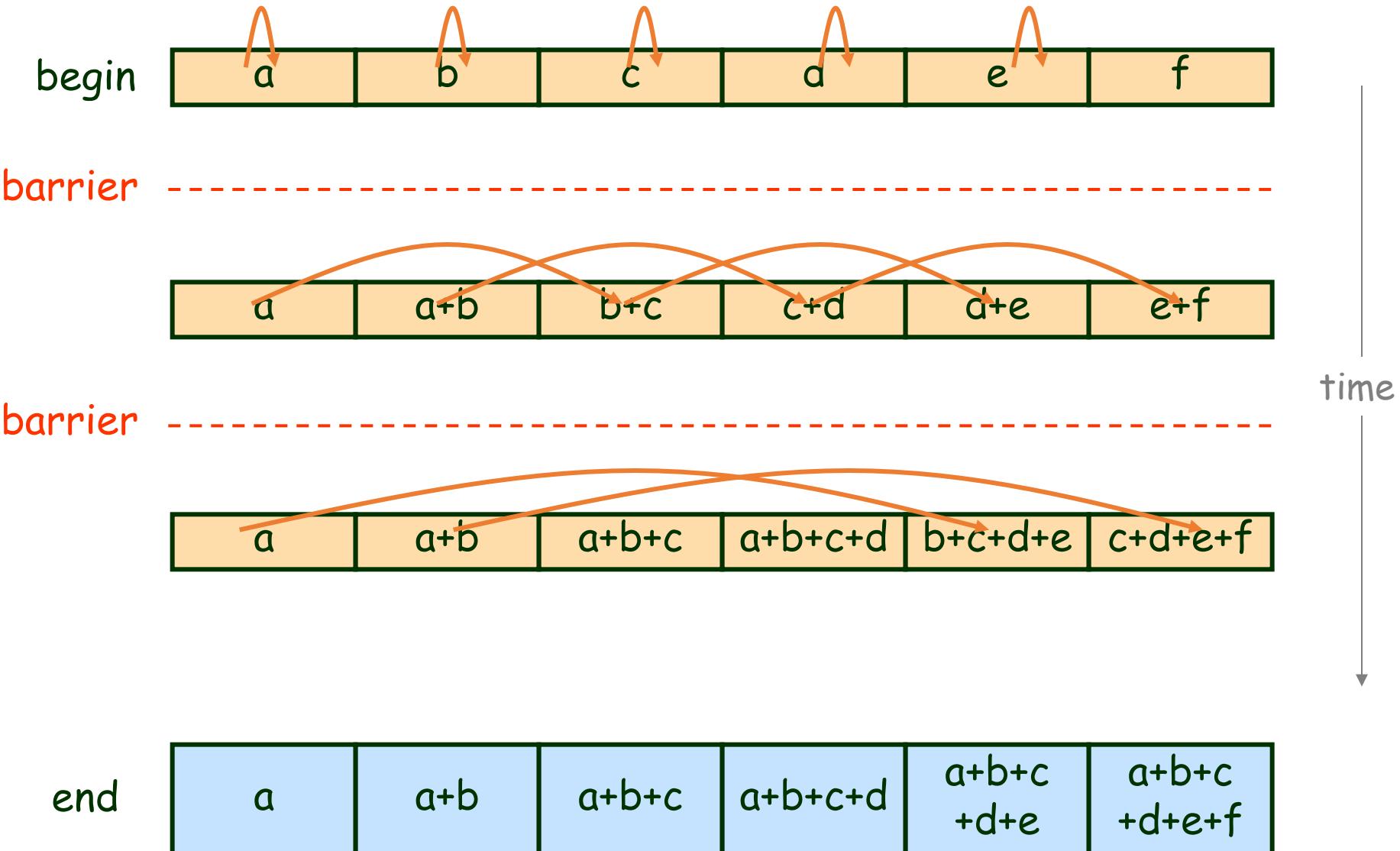
    for(stride=1; stride<=N/2; stride<<1) {
        pthread_mutex_lock(&g_locks[id]);
        pthread_mutex_lock(&g_locks[id+stride]);
        g_values[id+stride] += g_values[id];
        pthread_mutex_unlock(&g_locks[id]);
        pthread_mutex_unlock(&g_locks[id+stride]);
    }

}

```

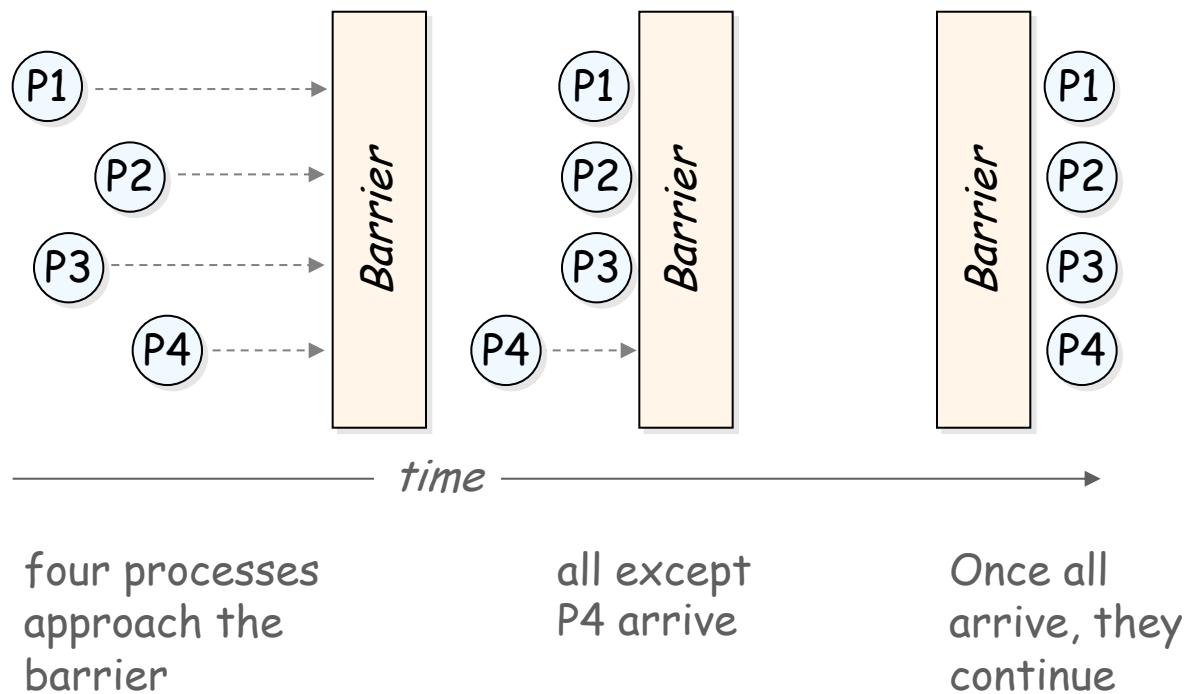
fixed?

Parallel Prefix Sum



What is a Barrier ?

- Coordination mechanism (algorithm)
- forces processes/threads to wait until each one of them has reached a certain point.
- Once all the processes/threads reach barrier, they all can pass the barrier.



four processes
approach the
barrier

all except
P4 arrive

Once all
arrive, they
continue

Pthreads and barriers

- Type `pthread_barrier_t`

```
int pthread_barrier_init(pthread_barrier_t *barrier,  
                         const pthread_barrierattr_t *attr,  
                         unsigned count);  
  
int pthread_barrier_destroy(pthread_barrier_t *barrier);  
int pthread_barrier_wait(pthread_barrier_t *barrier);
```

PThreads Parallel Prefix Sum

```
pthread_barrier_t g_barrier;
pthread_mutex_t g_locks[N];
int g_values[N] = { a, b, c, d, e, f };

void init_stuff() {
    ...
    pthread_barrier_init(&g_barrier, NULL, N-1);
}

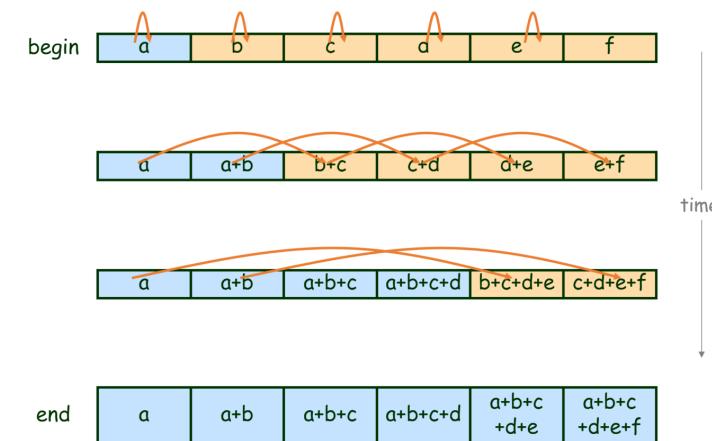
void prefix_sum_thread(void * param) {

    int i;
    int id = *((int*)param);
    int stride = 0;

    for(stride=1; stride<=N/2; stride<<1) {

        pthread_mutex_lock(&g_locks[id]);
        pthread_mutex_lock(&g_locks[id+stride]);
        g_values[id+stride] += g_values[id];
        pthread_mutex_unlock(&g_locks[id]);
        pthread_mutex_unlock(&g_locks[id+stride]);

        pthread_barrier_wait(&g_barrier);
    }
}
```



fixed?

Barrier Goals

Ideal barrier properties:

- Low shared memory space complexity
- Low contention on shared objects
- Low shared memory references per process
- No need for shared memory initialization
- Symmetric-ness (same amount of work for all processes)
- Algorithm simplicity
- Simple basic primitive
- Minimal propagation time
- Reusability of the barrier (**must!**)

Barrier Building Blocks

- Semaphores
- Atomic Bit
- Atomic Register
- Fetch-and-increment register
- Test and set bits
- Read-Modify-Write register

Barrier with Semaphores



Barrier using Semaphores

Algorithm for n processes

```
shared    arrival: binary semaphore, initially 1  
          departure: binary semaphore, initially 0  
          counter: atomic register ranges over {0, ..., n}, initially 0
```

```
1  sem_wait(arrival)  
2  counter := counter + 1           // atomic register  
3  if counter < n then sem_post(arrival) else sem_post(departure)  
4  sem_wait(departure)  
5  counter := counter - 1  
6  if counter > 0 then sem_post(departure) else sem_post(arrival)
```

Question:

Would this barrier be correct if the shared counter won't be an **atomic** register?

Barrier using Semaphores

Properties

- **Pros:**
 - Very Simple
 - Space complexity $O(1)$
 - Symmetric
- **Cons:**
 - Required a strong object
 - Requires some central manager
 - High contention on the semaphores
 - Propagation delay $O(n)$

Questions?