

CUDA

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cs378

Outline for Today

- Questions?
- Administrivia
 - Exam not graded soon!
- Agenda
 - CUDA

Acknowledgements:

- http://developer.download.nvidia.com/compute/developertrainingmaterials/presentations/cuda_language/Introduction_to_CUDA_C.pptx
- <http://www.seas.upenn.edu/~cis565/LECTURES/CUDA%20Tricks.pptx>
- <http://ece757.ece.wisc.edu/lect13-gpgpu.pptx>
- <http://www.cs.utexas.edu/~pingali/CS378/2015sp/lectures/GPU%20Programming.pptx>

Faux Quiz Questions (5 min, any 2)

1. Why do languages like CUDA and OpenCL have both blocks and threads?
2. What does the `_shared_` keyword do? How is it implemented by HW?
3. CUDA kernels have implicit barrier synchronization: `__syncthreads()`. Is it necessary? Why or why not?
4. Is traditional locking implementable on a GPU? What alternatives are there for synchronizing / avoiding races?
5. How is occupancy defined (in CUDA nomenclature)?
6. What is control flow divergence? How does it impact performance?
7. What is a bank conflict?
8. What is the difference between a thread block scheduler and a warp scheduler?
9. Compare/contrast coarse/fine/simultaneous multi-threading.
10. In CUDA, what is the difference between grids, blocks, and threads? What is their counterpart in OpenCL?

Parallel Algorithms Redux

Parallel Algorithms Redux

Key idea:

Parallel Algorithms Redux

Key idea:

Express sequential algorithms as combinations of parallel patterns

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Examples:

Parallel Algorithms Redux

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Express sequential algorithms as combinations of parallel patterns

Examples:

- Map

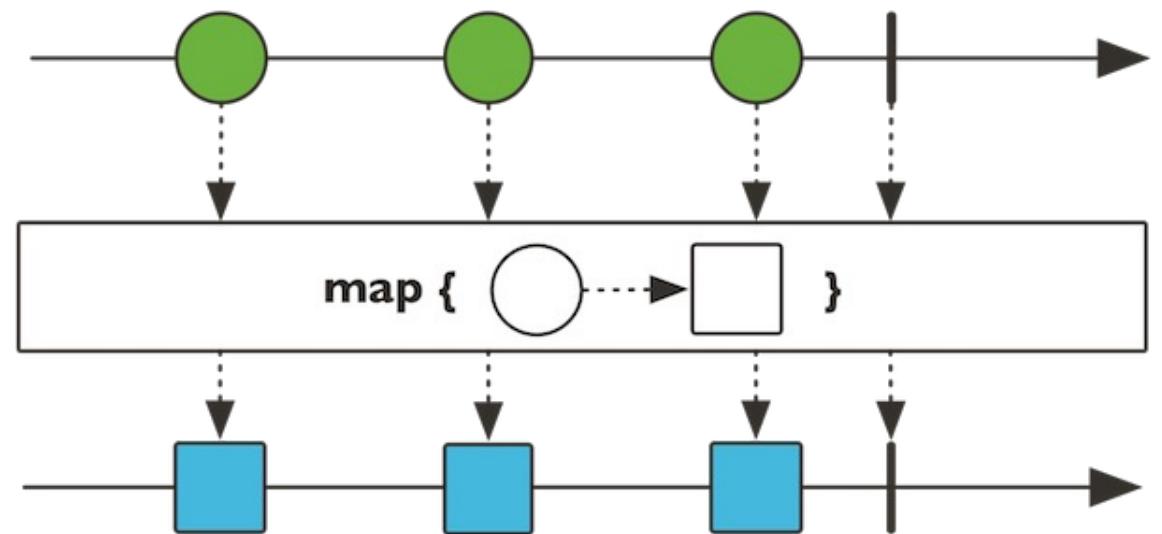
Parallel Algorithms Redux

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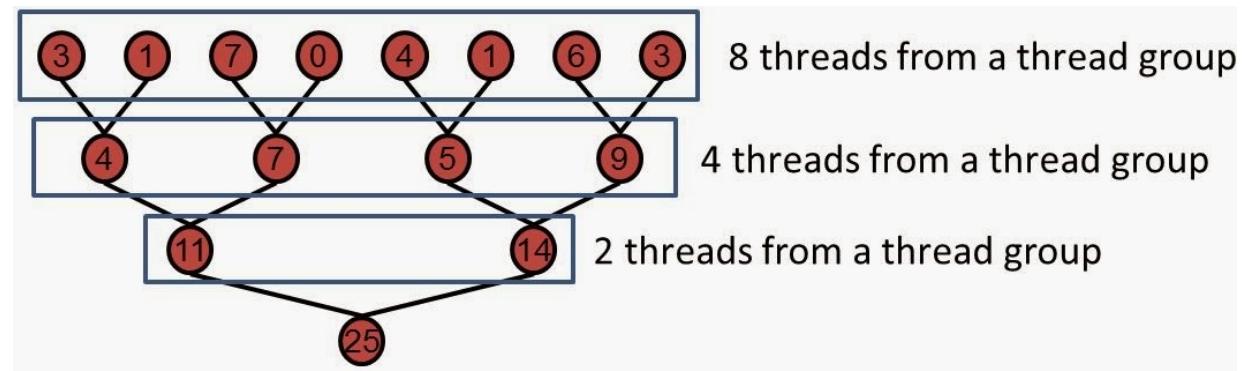
Parallel Algorithms Redux

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Examples:

- Map
- Reductions



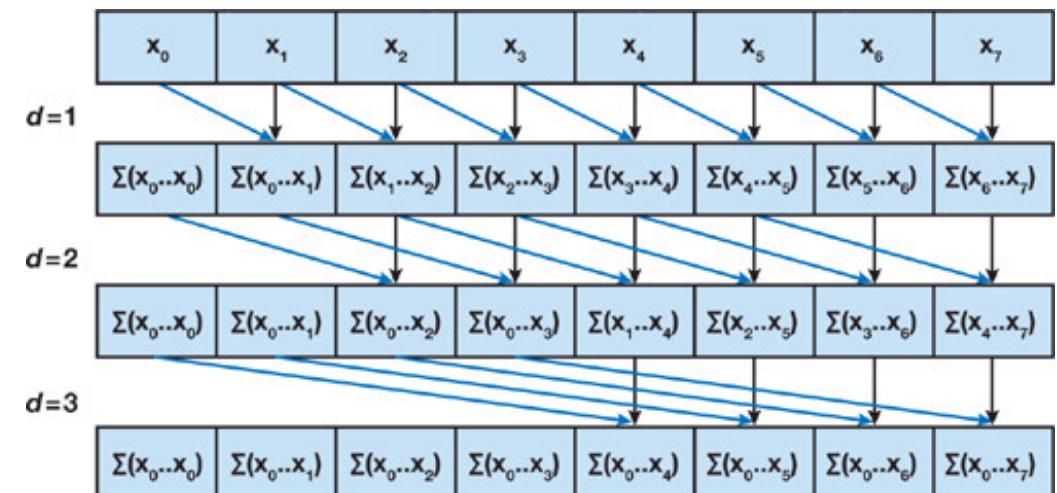
Parallel Algorithms Redux

Key idea:

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Examples:

- Map
- Reductions
- Scans



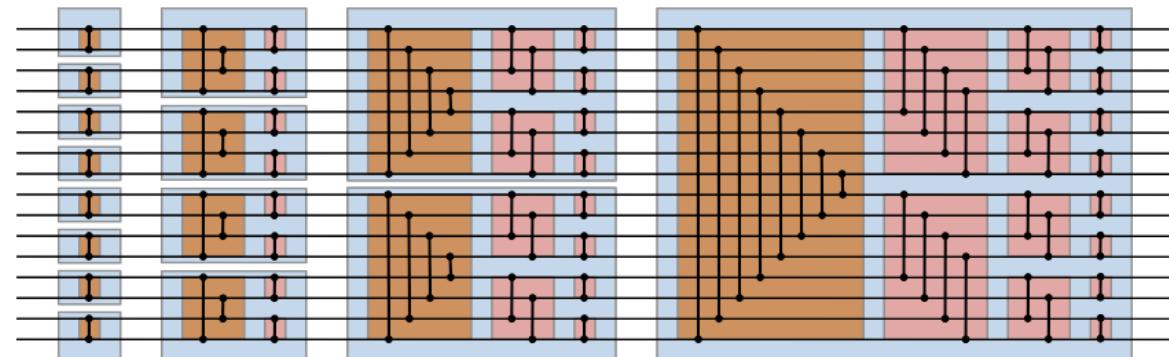
Parallel Algorithms Redux

Key idea:

Express sequential algorithms as combinations of parallel patterns

Examples:

- Map
- Reductions
- Scans
- Re-orderings (scatter/gather/sort)



Review



Review



- Each SM has multiple vector units (4)
 - 32 lanes wide → warp size

Review



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- Vector units use *hardware multi-threading*

Review



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- Execution → a grid of thread blocks (TBs)
 - Each TB has some number of threads

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Review

Thread block scheduler



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Review

Thread block scheduler warp (thread) scheduler

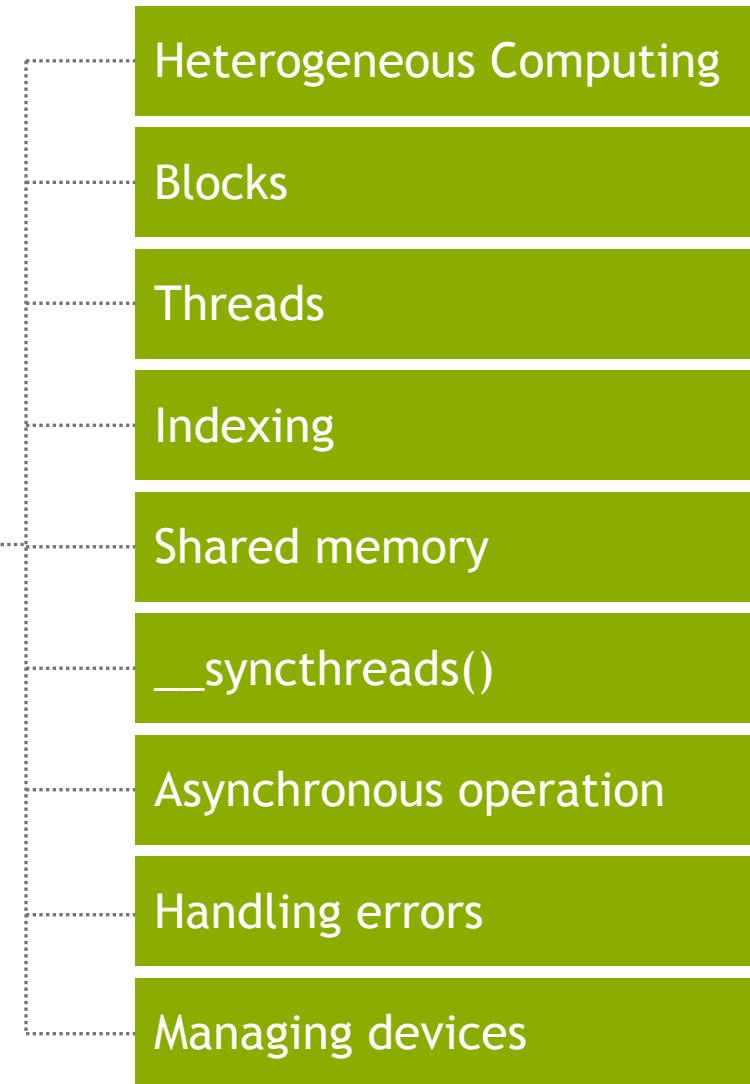


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 - 32 lanes wide → warp size
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What is CUDA?

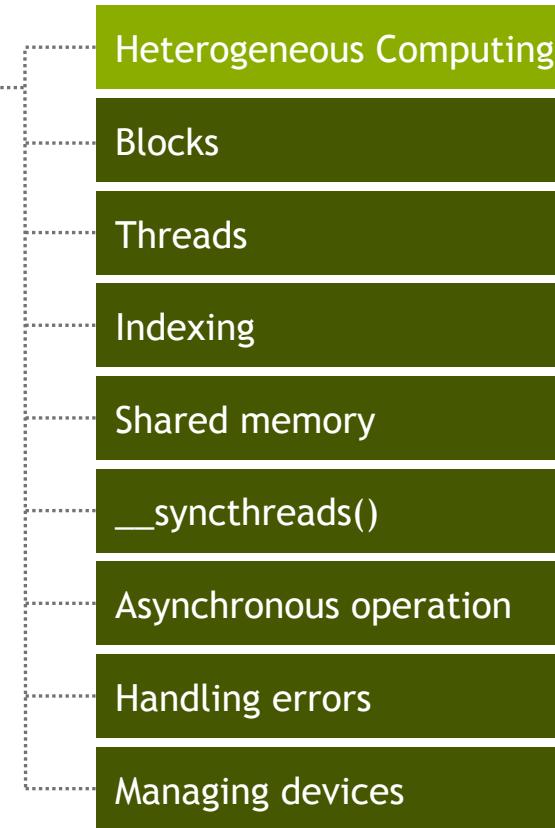
- CUDA Architecture
 - Expose GPU parallelism for general-purpose computing
 - Retain performance
- CUDA C/C++
 - Based on industry-standard C/C++
 - Small set of extensions to enable heterogeneous programming
 - Straightforward APIs to manage devices, memory etc.

CONCEPTS



HELLO WORLD!

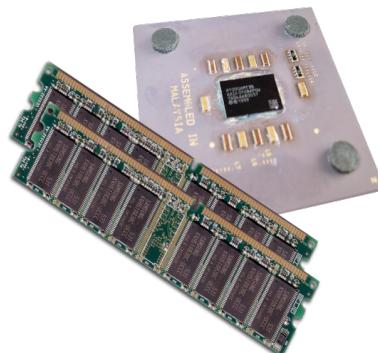
CONCEPTS



Heterogeneous Computing

- Terminology:

- *Host* The CPU and its memory (host memory)
- *Device* The GPU and its memory (device memory)



Host



Device

Heterogeneous Computing

```
#include <iostream>
#include <algorithm>

using namespace std;

#define N          1024
#define RADIUS     3
#define BLOCK_SIZE 16

__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int index = threadIdx.x + blockDim.x * blockIdx.x;
    int gindex = threadIdx.x + blockDim.x * RADIUS;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] = in[gindex + BLOCK_SIZE];
    }

    // Synchronize (ensure all the data is available)
    __syncthreads();

    // Apply the stencil
    int result = 0;
    for (int offset = -RADIUS ; offset <= RADIUS ; offset++)
        result += temp[lindex + offset];

    // Store the result
    out[index] = result;
}

void fill_ints(int *x, int n) {
    fill_n(x, n, 1);
}

int main(void) {
    int *in, *out;           // host copies of a, b, c
    int *d_in, *d_out;       // device copies of a, b, c
    int size = (N + 2*RADIUS) * sizeof(int);

    // Alloc space for host copies and setup values
    in = (int *)malloc(size); fill_ints(in, N + 2*RADIUS);
    out = (int *)malloc(size); fill_ints(out, N + 2*RADIUS);

    // Alloc space for device copies
    cudaMalloc((void **) &d_in, size);
    cudaMalloc((void **) &d_out, size);

    // Copy to device
    cudaMemcpy(d_in, in, size, cudaMemcpyHostToDevice);
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    // Launch stencil_1d() kernel on GPU
    stencil_1d<<<N/BLOCK_SIZE,BLOCK_SIZE>>>(d_in + RADIUS,
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    // Cleanup
    free(in); free(out);
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}
```

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    int tempIndex = index - RADIUS;
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serial code

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```

parallel fn

serial code

parallel code

Heterogeneous Computing

The diagram illustrates a nested structure of code regions, each represented by a green rectangular box. The regions are labeled from top to bottom as follows:

- parallel fn
- serial code
- parallel code
- serial code

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Heterogeneous Computing

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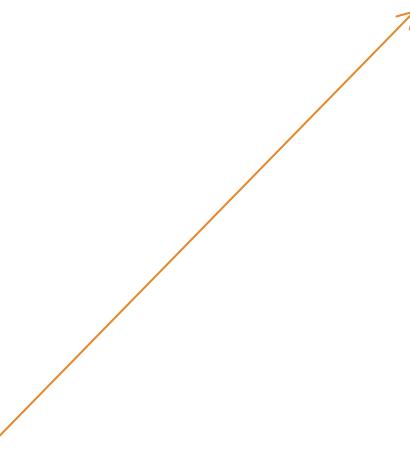
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serial code

parallel code

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Heterogeneous Computing

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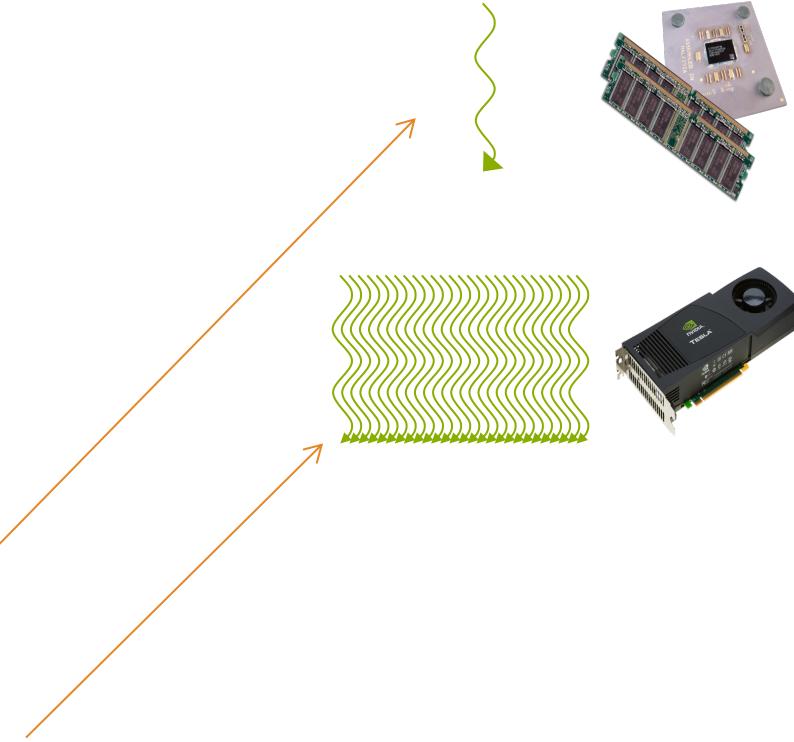
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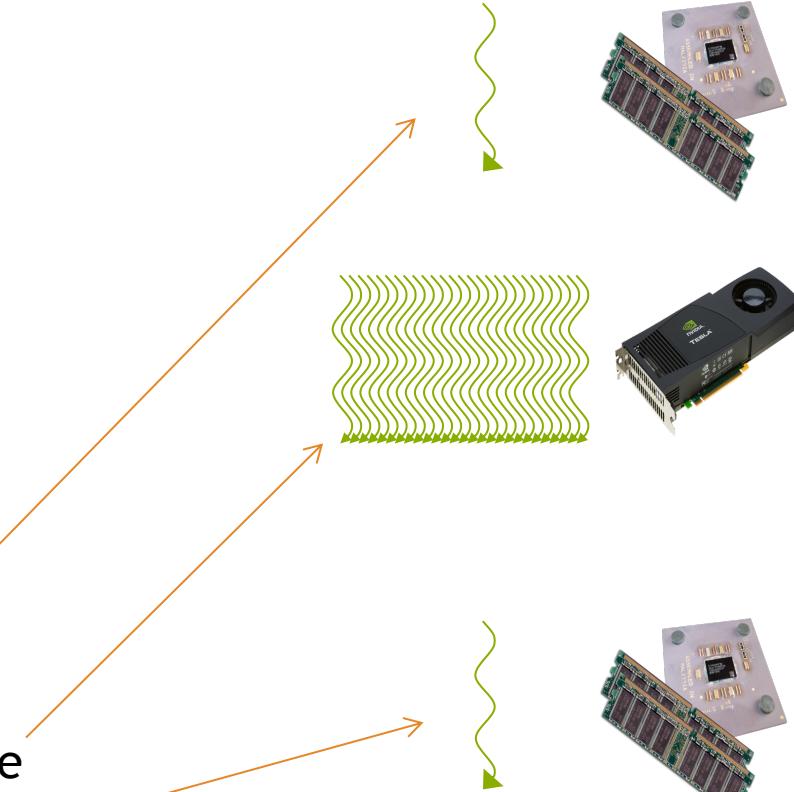
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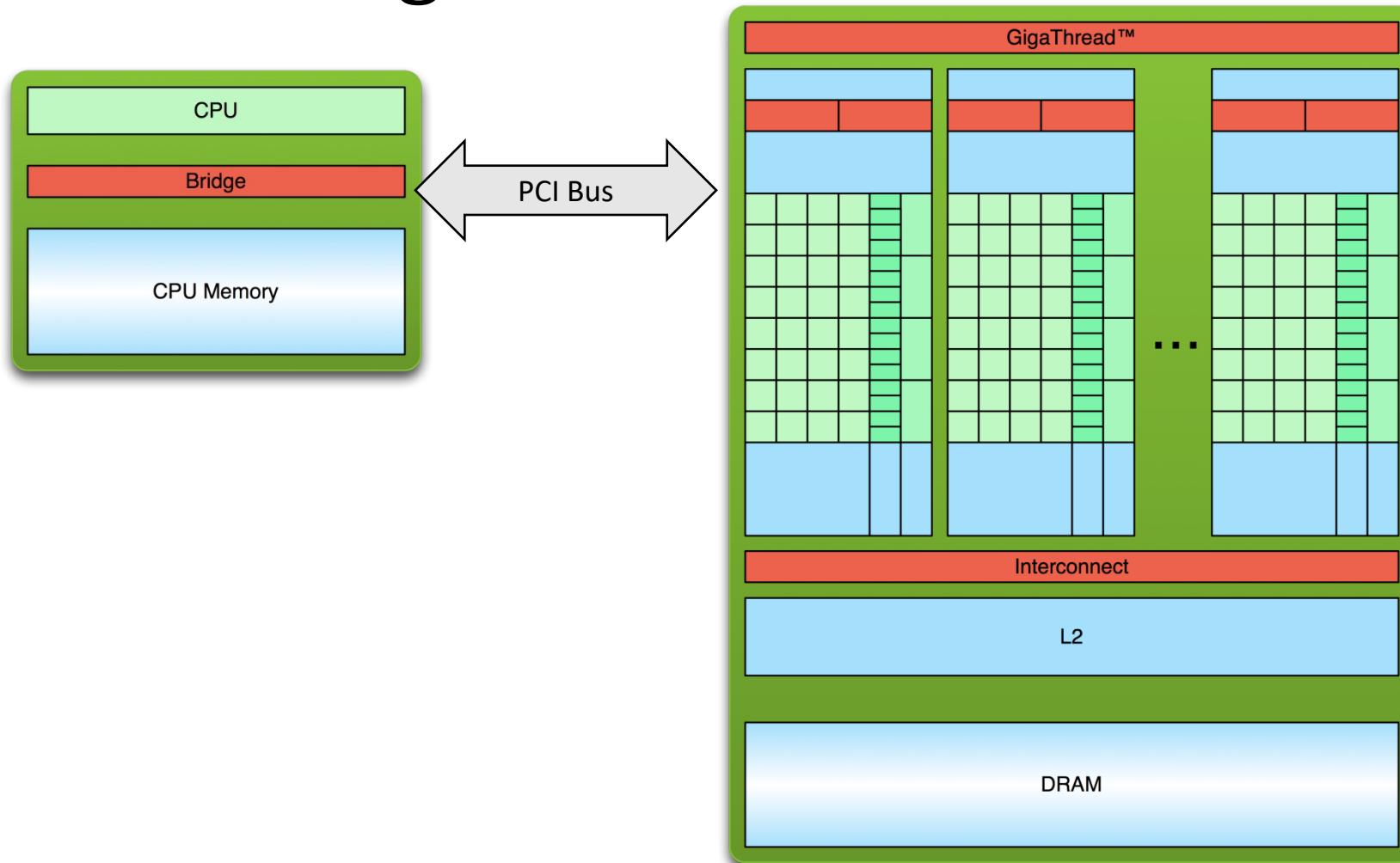
parallel fn

serial code

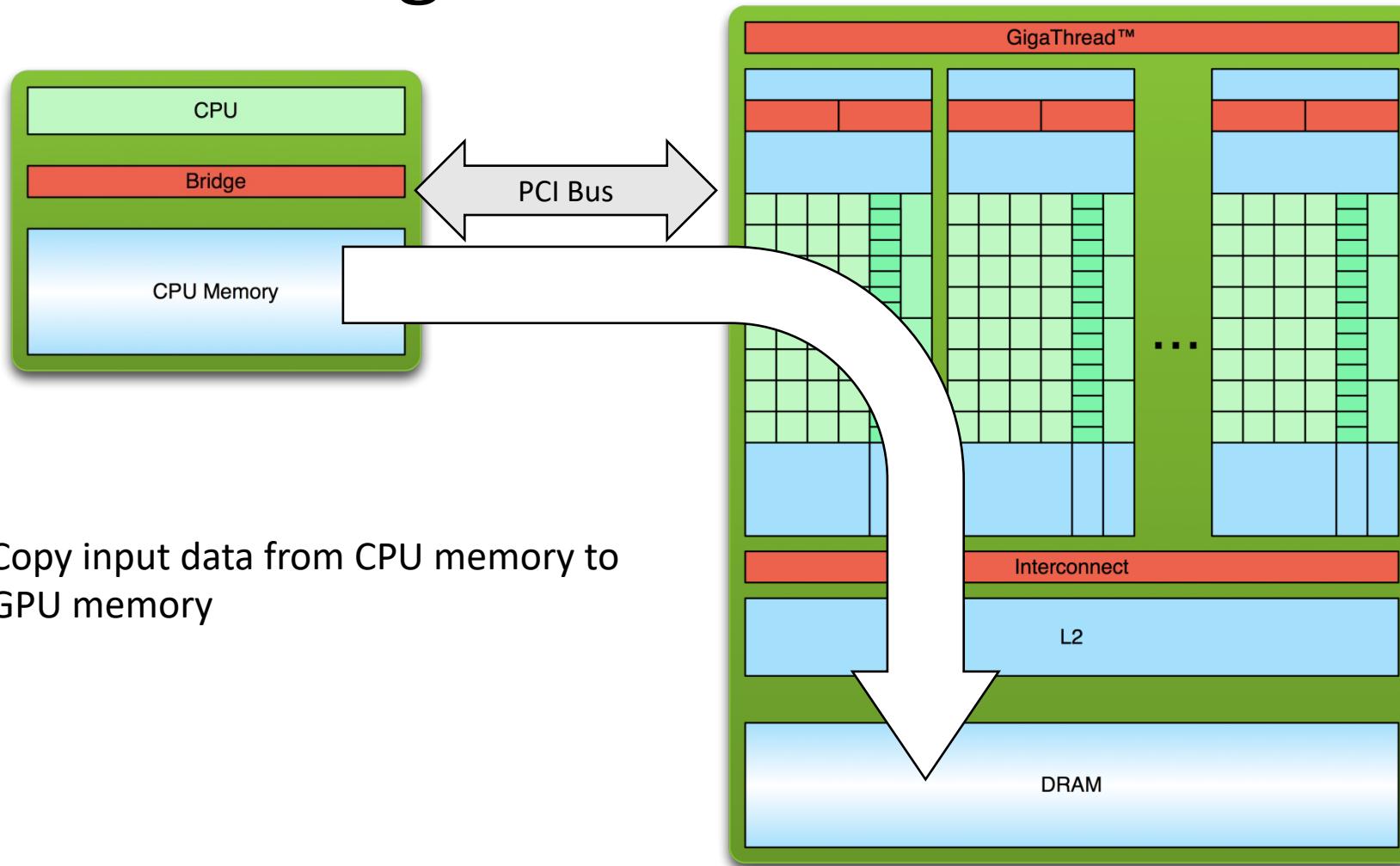
parallel code
serial code



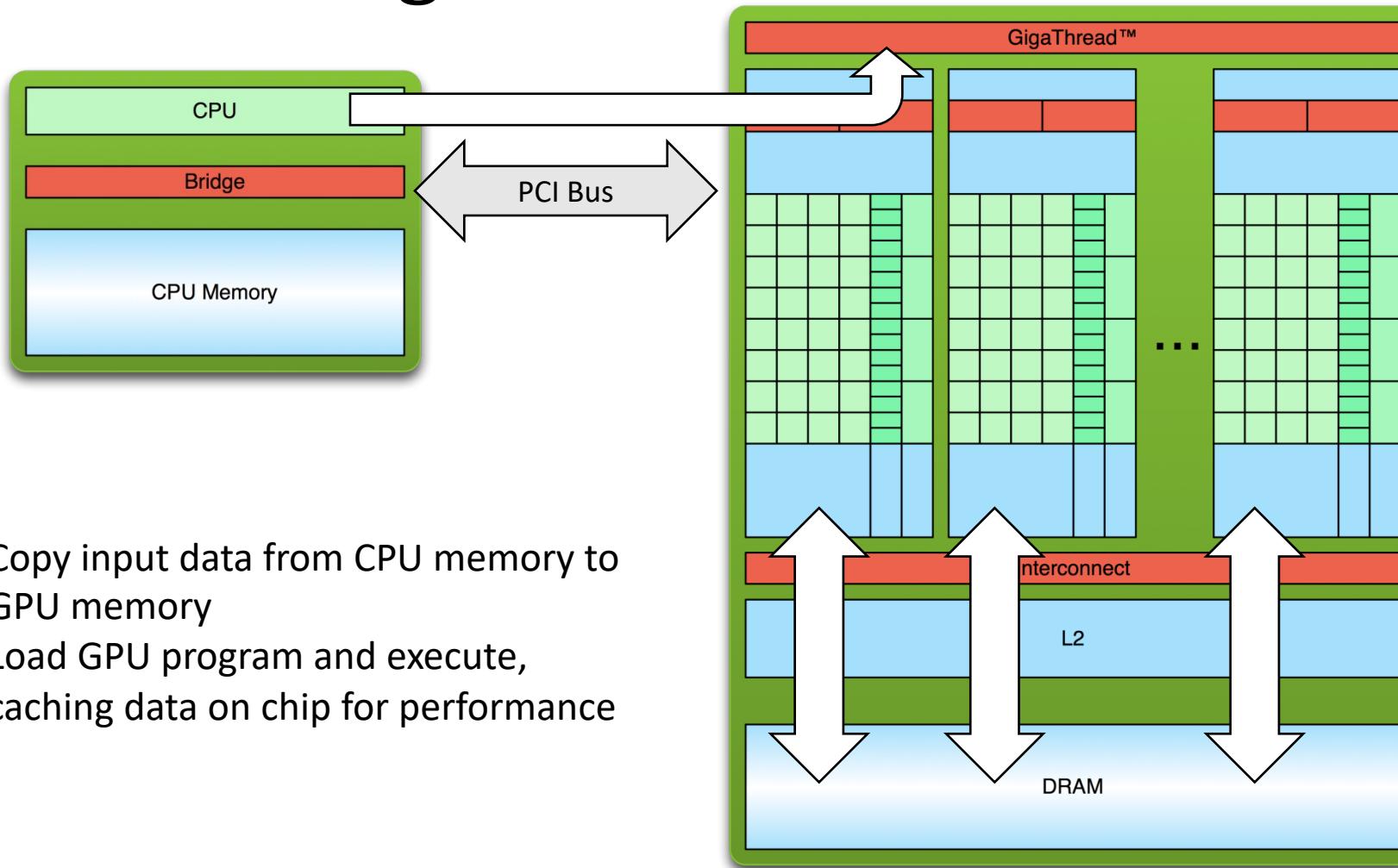
Simple Processing Flow



Simple Processing Flow

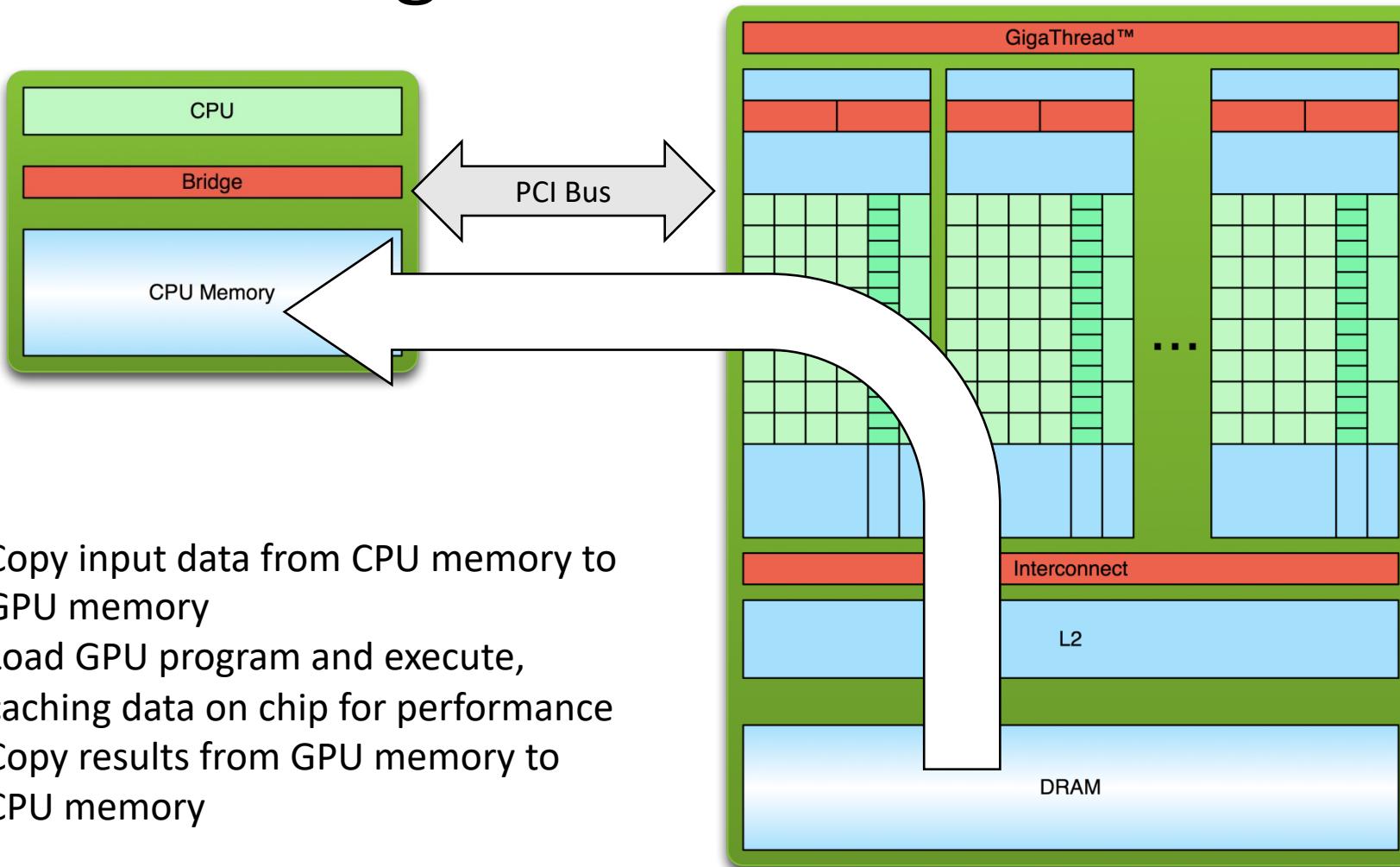


Simple Processing Flow



1. Copy input data from CPU memory to GPU memory
2. Load GPU program and execute, caching data on chip for performance

Simple Processing Flow



Hello World!

```
int main(void) {  
    printf("Hello World!\n");  
    return 0;  
}
```

Hello World!

```
int main(void) {
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```

- Standard C that runs on the host
- NVIDIA compiler (nvcc) can be used to compile programs with no *device* code

Output:

```
$ nvcc
hello_world.
cu
$ a.out
Hello World!
$
```

Hello World! with Device Code

```
__global__ void mykernel(void) {  
}  
  
int main(void) {  
    mykernel<<<1,1>>>();  
    printf("Hello World!\n");  
    return 0;  
}
```

Hello World! with Device Code

```
__global__ void mykernel(void) {  
}  
  
int main(void) {  
    mykernel<<<1,1>>>();  
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}
```

- Two new syntactic elements...

Hello World! with Device Code

```
__global__ void mykernel(void) {  
}
```

Hello World! with Device Code

```
__global__ void mykernel(void) {  
}
```

- CUDA C/C++ keyword `__global__` indicates a function that:
 - Runs on the device
 - Is called from host code
- nvcc separates source code into host and device components
 - Device functions (e.g. `mykernel()`) processed by NVIDIA compiler
 - Host functions (e.g. `main()`) processed by standard host compiler
 - `gcc, cl.exe`

Hello World! with Device COde

```
mykernel<<<1,1>>>();
```

Hello World! with Device COde

```
mykernel<<<1,1>>>();
```

- Triple angle brackets mark a call from *host* code to *device* code
 - Also called a “kernel launch”
 - We’ll return to the parameters (1,1) in a moment
- That’s all that is required to execute a function on the GPU!

Hello World! with Device Code

```
__global__ void mykernel(void) {  
}  
  
int main(void) {  
    mykernel<<<1,1>>>();  
    printf("Hello World!\n");  
    return 0;  
}
```

Hello World! with Device Code

```
__global__ void mykernel(void) {  
}
```

```
int main(void) {  
    mykernel<<<1,1>>>();  
    printf("Hello World!\n");  
    return 0;  
}
```

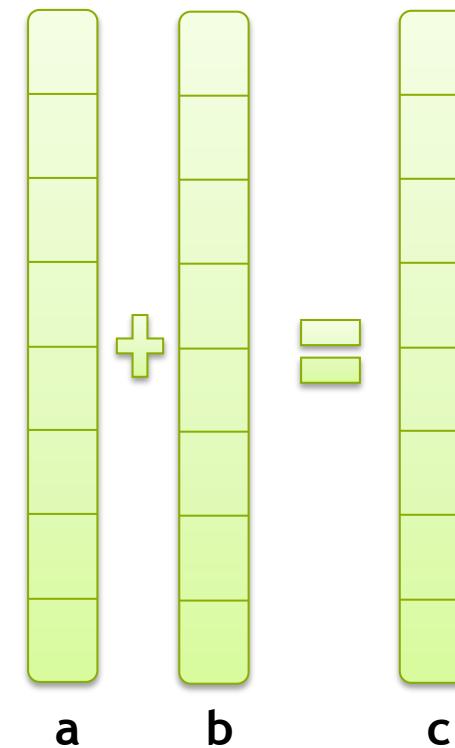
- `mykernel()` does nothing,
somewhat anticlimactic!

Output:

```
$ nvcc  
hello.cu  
$ a.out  
Hello World!  
$
```

Parallel Programming in CUDA C/C++

- But wait... GPU computing is about massive parallelism!
- We need a more interesting example...
- We'll start by adding two integers and build up to vector addition



Addition on the Device

- A simple kernel to add two integers

```
__global__ void add(int *a, int *b, int *c) {  
    *c = *a + *b;  
}
```

Addition on the Device

- A simple kernel to add two integers

```
__global__ void add(int *a, int *b, int *c) {  
    *c = *a + *b;  
}
```

- As before `__global__` is a CUDA C/C++ keyword meaning
 - `add()` will execute on the device
 - `add()` will be called from the host

Addition on the Device

- Note that we use pointers for the variables

```
__global__ void add(int *a, int *b, int *c) {  
    *c = *a + *b;  
}
```

Addition on the Device

- Note that we use pointers for the variables

```
__global__ void add(int *a, int *b, int *c) {  
    *c = *a + *b;  
}
```

- `add()` runs on the device, so `a`, `b` and `c` must point to device memory
- We need to allocate memory on the GPU

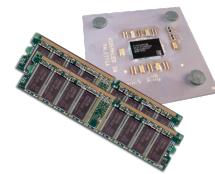
Memory Management

- Host and device memory are separate entities
 - *Device* pointers point to GPU memory
 - May be passed to/from host code
 - May *not* be dereferenced in host code
 - *Host* pointers point to CPU memory
 - May be passed to/from device code
 - May *not* be dereferenced in device code



Memory Management

- Host and device memory are separate entities
 - *Device* pointers point to GPU memory
 - May be passed to/from host code
 - May *not* be dereferenced in host code
 - *Host* pointers point to CPU memory
 - May be passed to/from device code
 - May *not* be dereferenced in device code
- Simple CUDA API for handling device memory
 - `cudaMalloc()`, `cudaFree()`, `cudaMemcpy()`
 - Similar to the C equivalents `malloc()`, `free()`, `memcpy()`



Addition on the Device: add()

- Returning to our add() kernel

```
__global__ void add(int *a, int *b, int *c) {  
    *c = *a + *b;  
}
```

- Let's take a look at main()...

Addition on the Device: main()

```
int main(void) {  
    int a, b, c;                      // host copies of a, b, c  
    int *d_a, *d_b, *d_c;              // device copies of a, b, c
```

Addition on the Device: main()

```
int main(void) {
    int a, b, c;                      // host copies of a, b, c
    int *d_a, *d_b, *d_c;              // device copies of a, b, c
    int size = sizeof(int);

    // Allocate space for device copies of a, b, c
    cudaMalloc((void **) &d_a, size);
    cudaMalloc((void **) &d_b, size);
    cudaMalloc((void **) &d_c, size);
```

Addition on the Device: main()

```
int main(void) {
    int a, b, c;                      // host copies of a, b, c
    int *d_a, *d_b, *d_c;              // device copies of a, b, c
    int size = sizeof(int);

    // Allocate space for device copies of a, b, c
    cudaMalloc((void **) &d_a, size);
    cudaMalloc((void **) &d_b, size);
    cudaMalloc((void **) &d_c, size);

    // Setup input values
    a = 2;
    b = 7;
```

Addition on the Device: main()

```
// Copy inputs to device
cudaMemcpy(d_a, &a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, &b, size, cudaMemcpyHostToDevice);
```

Addition on the Device: main()

```
// Copy inputs to device
cudaMemcpy(d_a, &a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, &b, size, cudaMemcpyHostToDevice);

// Launch add() kernel on GPU
add<<<1,1>>>(d_a, d_b, d_c);
```

Addition on the Device: main()

```
// Copy inputs to device
cudaMemcpy(d_a, &a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, &b, size, cudaMemcpyHostToDevice);

// Launch add() kernel on GPU
add<<<1,1>>>(d_a, d_b, d_c);

// Copy result back to host
cudaMemcpy(&c, d_c, size, cudaMemcpyDeviceToHost);
```

Addition on the Device: main()

```
// Copy inputs to device
cudaMemcpy(d_a, &a, size, cudaMemcpyHostToDevice);
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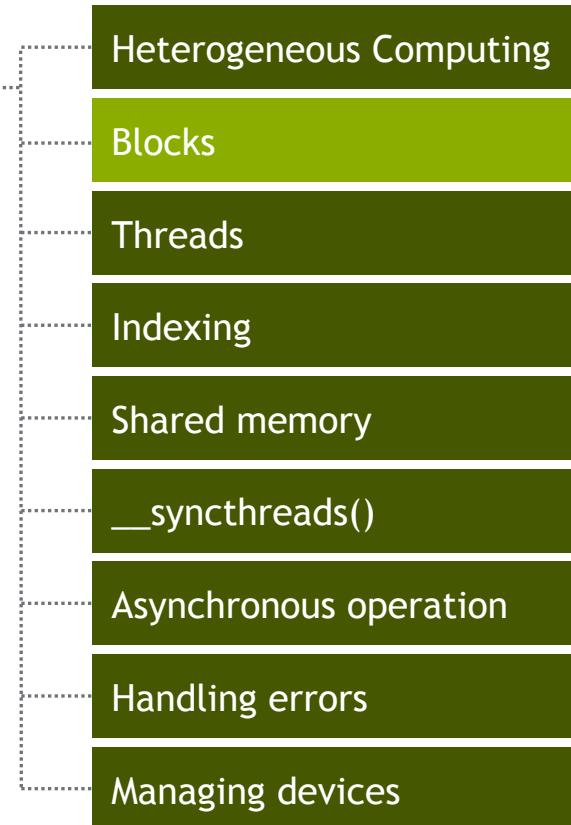
// Launch add() kernel on GPU
add<<<1,1>>>(d_a, d_b, d_c);

// Copy result back to host
cudaMemcpy(&c, d_c, size, cudaMemcpyDeviceToHost);

// Cleanup
cudaFree(d_a); cudaFree(d_b); cudaFree(d_c);
return 0;
}
```

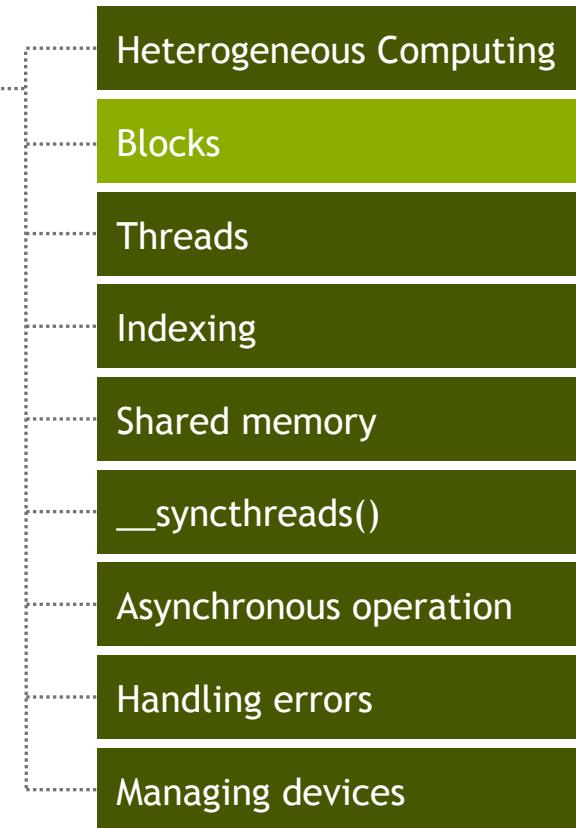
RUNNING IN PARALLEL

CONCEPTS



RUNNING IN PARALLEL

CONCEPTS



Getting Parallel

- GPU computing is about massive parallelism
 - So how do we run code in parallel on the device?

Getting Parallel

- GPU computing is about massive parallelism
 - So how do we run code in parallel on the device?

```
add<<< 1, 1 >>>();  
          ↓  
add<<< N, 1 >>>();
```

- Instead of executing `add()` once, execute N times in parallel

Vector Addition on the Device

- With `add()` running in parallel we can do vector addition

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- Terminology: each parallel invocation of `add()` is a **block**

Vector Addition on the Device

- With `add()` running in parallel we can do vector addition
- Terminology: each parallel invocation of `add()` is a **block**
 - The set of blocks is referred to as a **grid**
 - Each invocation can refer to its block index using `blockIdx.x`

```
__global__ void add(int *a, int *b, int *c) {  
    c[blockIdx.x] = a[blockIdx.x] + b[blockIdx.x];  
}
```

- By using `blockIdx.x` to index into the array, each block handles a different index

Vector Addition on the Device

```
__global__ void add(int *a, int *b, int *c) {  
    c[blockIdx.x] = a[blockIdx.x] + b[blockIdx.x];  
}
```

Vector Addition on the Device

```
__global__ void add(int *a, int *b, int *c) {  
    c[blockIdx.x] = a[blockIdx.x] + b[blockIdx.x];  
}
```

- On the device, each block can execute in parallel:

Block 0

```
c[0] = a[0] + b[0];
```

Block 1

```
c[1] = a[1] + b[1];
```

Block 2

```
c[2] = a[2] + b[2];
```

Block 3

```
c[3] = a[3] + b[3];
```

Vector Addition on the Device: add()

- Returning to our parallelized `add()` kernel

```
__global__ void add(int *a, int *b, int *c) {  
    c[blockIdx.x] = a[blockIdx.x] + b[blockIdx.x];  
}
```

- Let's take a look at `main()`...

Vector Addition on the Device: main()

```
#define N 512
int main(void) {
    int *a  *b  *c           // host copies of a, b, c
    int *d_a, *d_b, *d_c;    // device copies of a, b, c
```

Vector Addition on the Device: main()

```
#define N 512

int main(void) {
    int *a    *b    *c           // host copies of a, b, c
    int *d_a, *d_b, *d_c;       // device copies of a, b, c
    int size = N * sizeof(int);

    // Alloc space for device copies of a, b, c
    cudaMalloc((void **) &d_a, size);
    cudaMalloc((void **) &d_b, size);
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```

Vector Addition on the Device: main()

```
#define N 512

int main(void) {
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    cudaMalloc((void **) &d_a, size);
    cudaMalloc((void **) &d_b, size);
    cudaMalloc((void **) &d_c, size);

    // Alloc space for host copies of a, b, c and setup input values
    a = (int *)malloc(size); random_ints(a, N);
    b = (int *)malloc(size); random_ints(b, N);
    c = (int *)malloc(size);
```

Vector Addition on the Device: main()

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, b, size, cudaMemcpyHostToDevice);
```

Vector Addition on the Device: main()

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, b, size, cudaMemcpyHostToDevice);

// Launch add() kernel on GPU with N blocks
add<<<N,1>>>(d_a, d_b, d_c);
```

Vector Addition on the Device: main()

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, b, size, cudaMemcpyHostToDevice);

// Launch add() kernel on GPU with N blocks
add<<<N,1>>>(d_a, d_b, d_c);

// Copy result back to host
cudaMemcpy(c, d_c, size, cudaMemcpyDeviceToHost);
```

Vector Addition on the Device: main()

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
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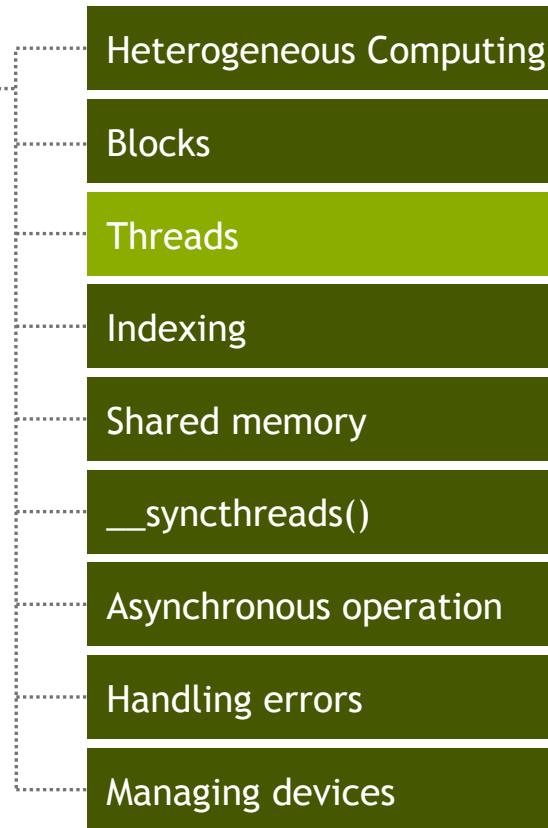
// Launch add() kernel on GPU with N blocks
add<<<N,1>>>(d_a, d_b, d_c);

// Copy result back to host
cudaMemcpy(c, d_c, size, cudaMemcpyDeviceToHost);

// Cleanup
free(a); free(b); free(c);
cudaFree(d_a); cudaFree(d_b); cudaFree(d_c);
return 0;
}
```

INTRODUCING THREADS

CONCEPTS



CUDA Threads

- Terminology: a block can be split into parallel **threads**
- Change `add()` to use parallel *threads* instead of parallel *blocks*:
- Use **threadIdx.x** instead of **blockIdx.x**

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CUDA Threads

- Terminology: a block can be split into parallel *threads*
- Change `add()` to use parallel *threads* instead of parallel *blocks*:

```
__global__ void add(int *a, int *b, int *c) {  
    c[threadIdx.x] = a[threadIdx.x] + b[threadIdx.x];  
}
```

- Use `threadIdx.x` instead of `blockIdx.x`
- Need to make one change in `main()` ...

Vector Addition Using Threads: main()

```
#define N 512

int main(void) {
    int *a, *b, *c;                                // host copies of a, b, c
    int *d_a, *d_b, *d_c;                            // device copies of a, b, c
    int size = N * sizeof(int);

    // Alloc space for device copies of a, b, c
    cudaMalloc((void **) &d_a, size);
    cudaMalloc((void **) &d_b, size);
    cudaMalloc((void **) &d_c, size);

    // Alloc space for host copies of a, b, c and setup input values
    a = (int *)malloc(size); random_ints(a, N);
    b = (int *)malloc(size); random_ints(b, N);
    c = (int *)malloc(size);
```

Vector Addition Using Threads: main()

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, b, size, cudaMemcpyHostToDevice);

// Launch add() kernel on GPU with N threads
add<<<1,N>>>(d_a, d_b, d_c);

// Copy result back to host
cudaMemcpy(c, d_c, size, cudaMemcpyDeviceToHost);

// Cleanup
free(a); free(b); free(c);
cudaFree(d_a); cudaFree(d_b); cudaFree(d_c);
return 0;
}
```

Vector Addition Using Threads: main()

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
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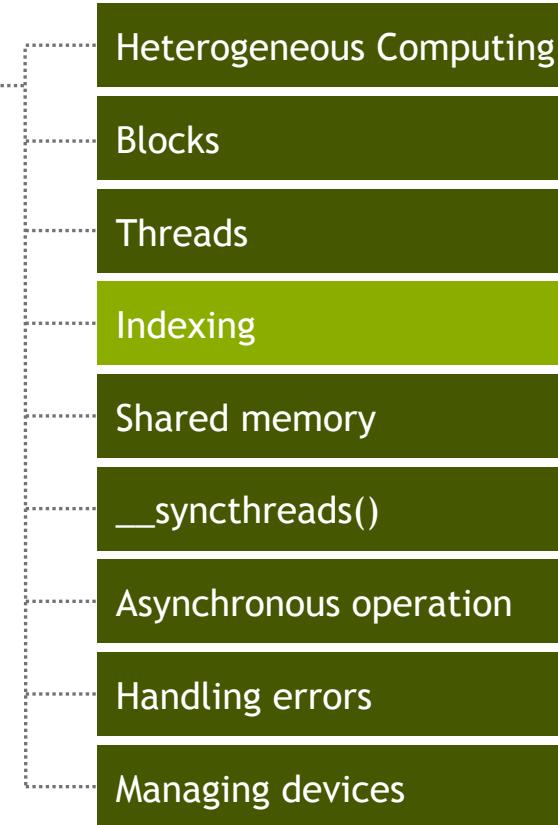
// Copy result back to host
cudaMemcpy(c, d_c, size, cudaMemcpyDeviceToHost);
```

```
// Cleanup
free(a);
cudaFree(d_a);
cudaFree(d_b);
return 0;
}
```

	Traditional CPU	Graphics Shaders	CUDA	OpenCL
free(a);	SIMD lane	thread	thread	work-item
cudaFree(d_a);	~thread	-	warp	-
cudaFree(d_b);		thread group	block	work group
return 0;		-	grid	N-D range

COMBINING THREADS AND BLOCKS

CONCEPTS



Combining Blocks and Threads

- We've seen parallel vector addition using:
 - Many blocks with *one thread* each ($M:1$)
 - One block with *many threads* ($1:M$)

Combining Blocks and Threads

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- How to make vector addition to use both blocks and threads?

Combining Blocks and Threads

- We've seen parallel vector addition using:
 - Many blocks with *one thread* each ($M:1$)
 - One block with *many threads* ($1:M$)
- How to make vector addition to use both blocks and threads?
- How to deal with `blockIdx.*` vs `threadIdx.*`?

Indexing Arrays with Blocks and Threads

- Most kernels use ***both*** `blockIdx.x` and `threadIdx.x`
 - Index an array with one elem. per thread (8 threads/block)

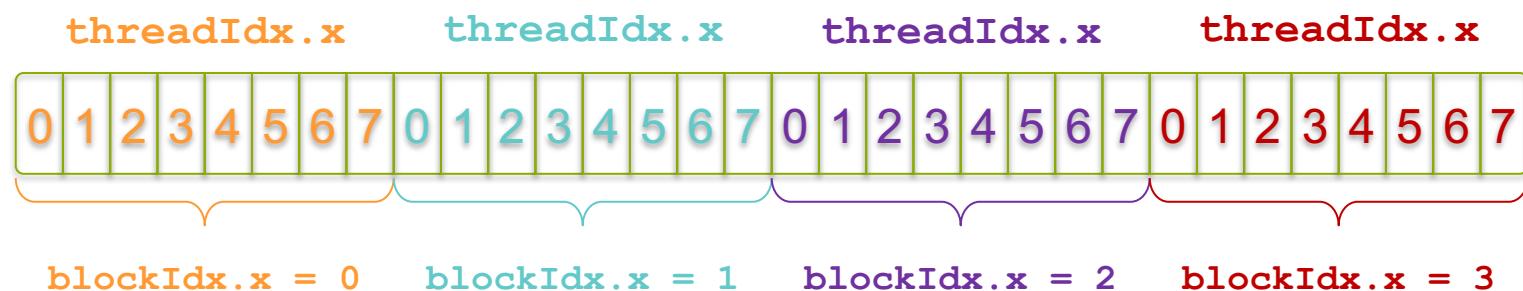
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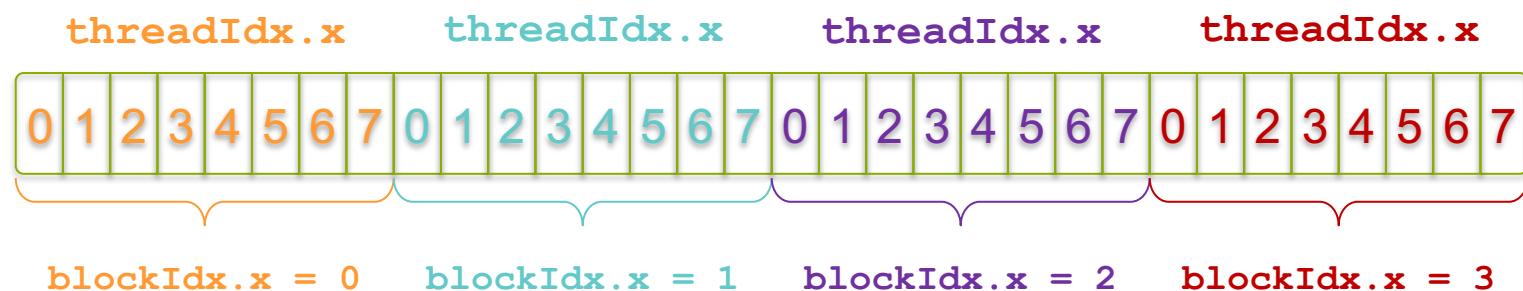
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Indexing Arrays with Blocks and Threads

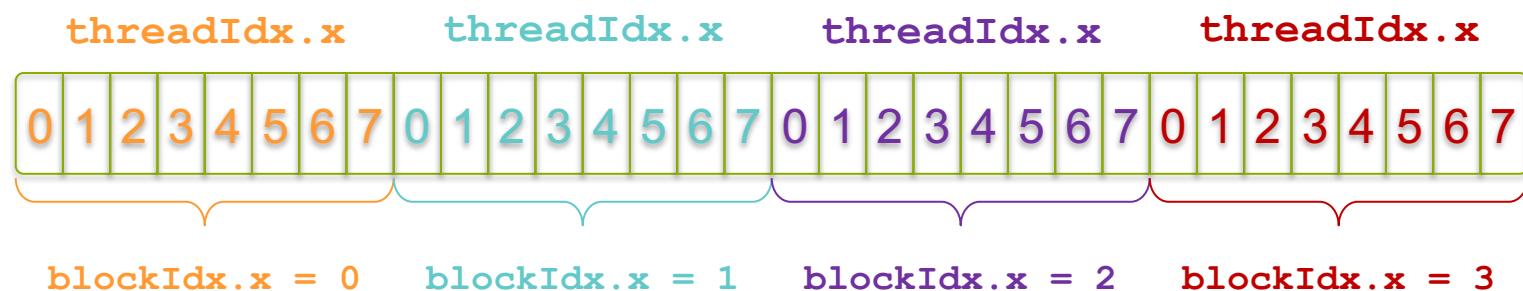
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- With M threads/block, unique index per thread is :

Indexing Arrays with Blocks and Threads

- Most kernels use **both** `blockIdx.x` and `threadIdx.x`
 - Index an array with one elem. per thread (8 threads/block)



- With M threads/block, unique index per thread is :

```
int index = threadIdx.x + blockIdx.x * M;
```

Indexing Arrays: Example

- Which thread will operate on the red element?
 - M=8 Threads, 4 blocks



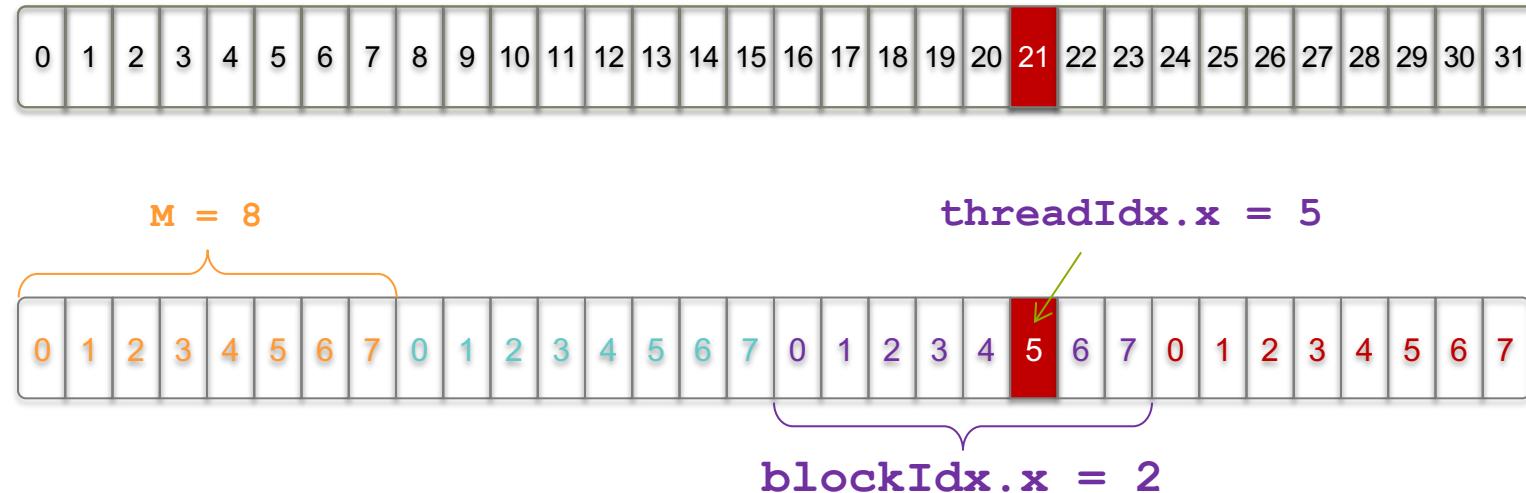
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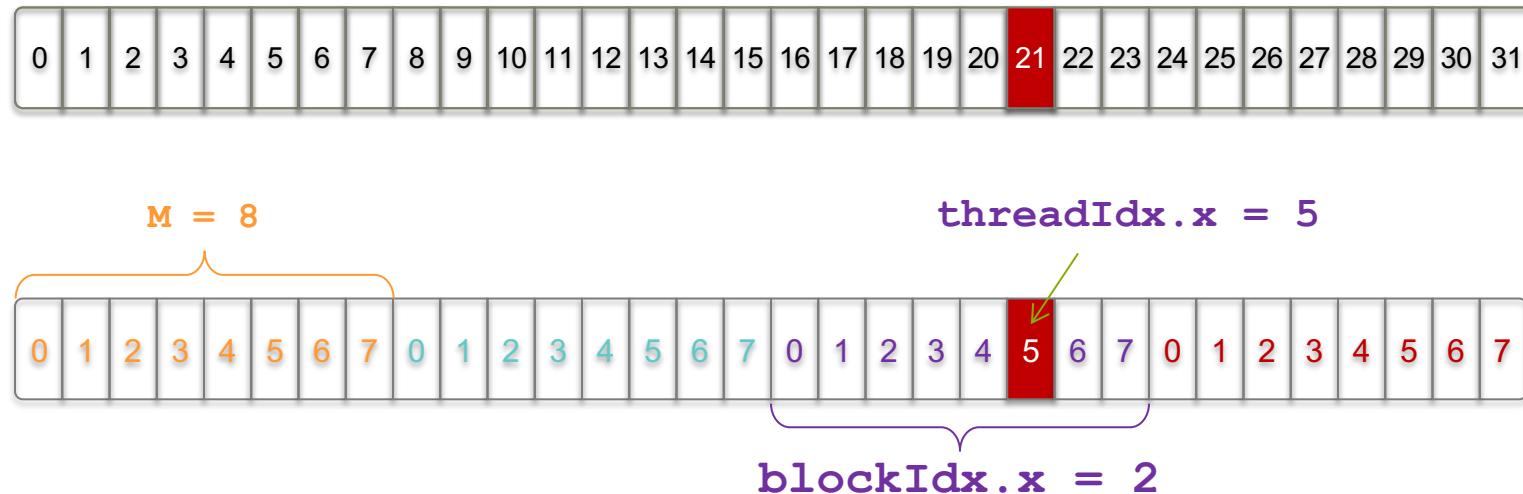
Indexing Arrays: Example

- Which thread will operate on the red element?
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Indexing Arrays: Example

- Which thread will operate on the red element?
 - M=8 Threads, 4 blocks



```
int index = threadIdx.x + blockIdx.x * M;  
= 5 + 2 * 8;  
= 21;
```

Vector Addition with Blocks and Threads

- Use the built-in variable `blockDim.x` for threads per block

```
int index = threadIdx.x + blockIdx.x * blockDim.x;
```

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Vector Addition with Blocks and Threads

- Use the built-in variable `blockDim.x` for threads per block

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int index = threadIdx.x + blockIdx.x * blockDim.x;
```

- Combined add () using parallel threads *and* blocks

```
__global__ void add(int *a, int *b, int *c) {
    int index = threadIdx.x + blockIdx.x * blockDim.x;
    c[index] = a[index] + b[index];
}
```

- What changes need to be made in `main()`?

Addition with Blocks and Threads:

```
main ()  
{  
    #define N (2048*2048)  
    #define THREADS_PER_BLOCK 512  
  
    int main(void) {  
        int *a, *b, *c;                                // host copies of a, b, c  
        int *d_a, *d_b, *d_c;                          // device copies of a, b, c  
        int size = N * sizeof(int);  
  
        // Alloc space for device copies of a, b, c  
        cudaMalloc((void **) &d_a, size);  
        cudaMalloc((void **) &d_b, size);  
        cudaMalloc((void **) &d_c, size);  
  
        // Alloc space for host copies of a, b, c and setup input values  
        a = (int *)malloc(size); random_ints(a, N);  
        b = (int *)malloc(size); random_ints(b, N);  
        c = (int *)malloc(size);
```

Addition with Blocks and Threads:

```
main()
```

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, b, size, cudaMemcpyHostToDevice);

// Launch add() kernel on GPU
add<<<N/THREADS_PER_BLOCK, THREADS_PER_BLOCK>>>(d_a, d_b, d_c);

// Copy result back to host
cudaMemcpy(c, d_c, size, cudaMemcpyDeviceToHost);

// Cleanup
free(a); free(b); free(c);
cudaFree(d_a); cudaFree(d_b); cudaFree(d_c);
return 0;
}
```

Addition with Blocks and Threads:

```
main()
```

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
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// Launch add() kernel on GPU
add<<<N/THREADS_PER_BLOCK, THREADS_PER_BLOCK>>>(d_a, d_b, d_c);

// Copy result back to host
cudaMemcpy(c, d_c, size, cudaMemcpyDeviceToHost);

// Cleanup
free(a); free(b); free(c);
cudaFree(d_a); cudaFree(d_b); cudaFree(d_c);
return 0;
}
```

Anyone see a problem?

Handling Arbitrary Vector Sizes

- Typical problems are not friendly multiples of `blockDim.x`

Handling Arbitrary Vector Sizes

- Typical problems are not friendly multiples of `blockDim.x`
- Avoid accessing beyond the end of the arrays:

Handling Arbitrary Vector Sizes

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- Update the kernel launch:

Handling Arbitrary Vector Sizes

- Typical problems are not friendly multiples of `blockDim.x`
- Avoid accessing beyond the end of the arrays:

```
__global__ void add(int *a, int *b, int *c, int n) {
    int index = threadIdx.x + blockIdx.x * blockDim.x;
    if (index < n)
        c[index] = a[index] + b[index];
}
```

- Update the kernel launch:

```
add<<< (N + M-1) / M, M>>>(d_a, d_b, d_c, N);
```

Why Bother with Threads?

- Threads seem unnecessary
 - They add a level of complexity
 - What do we gain?

Why Bother with Threads?

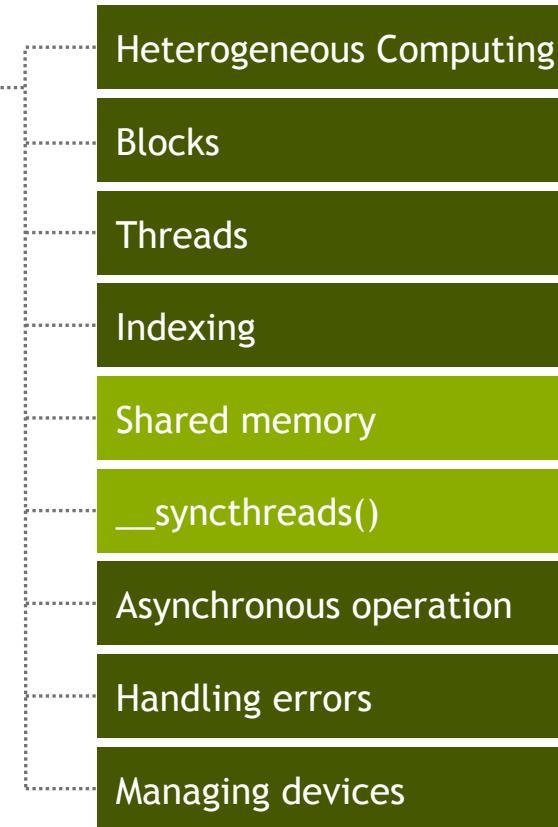
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 - They add a level of complexity
 - What do we gain?
- Unlike parallel blocks, threads have mechanisms to:
 - Communicate
 - Synchronize

Why Bother with Threads?

- Threads seem unnecessary
 - They add a level of complexity
 - What do we gain?
- Unlike parallel blocks, threads have mechanisms to:
 - Communicate
 - Synchronize
- To look closer, we need a new example...

COOPERATING THREADS

CONCEPTS



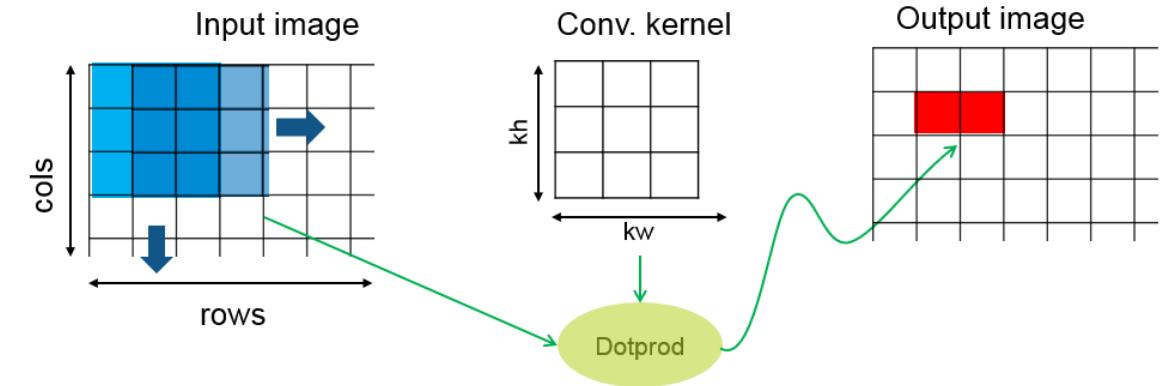
Stencils

Stencils

- Each pixel → function of neighbors

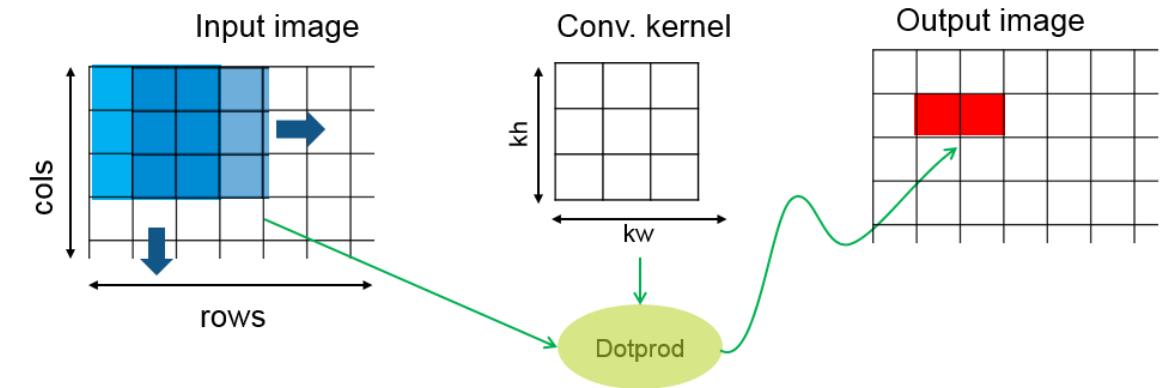
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Stencils

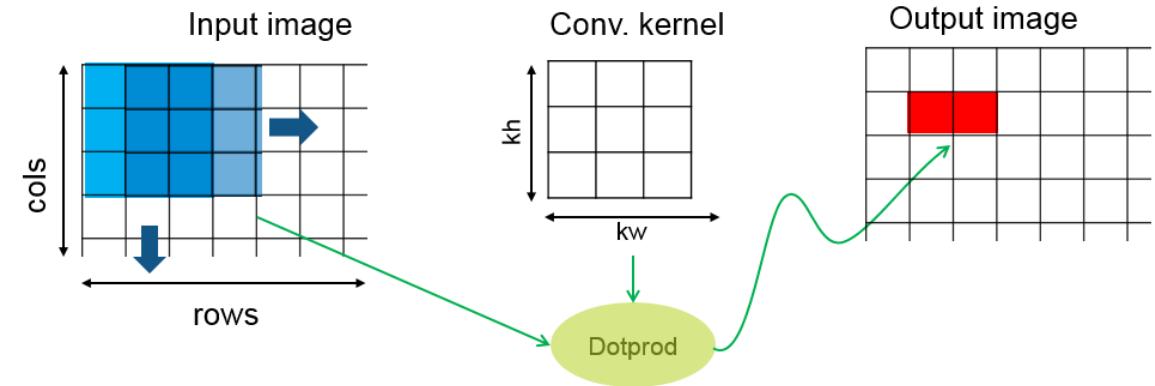
- Each pixel → function of neighbors
- Edge detection:



Stencils

- Each pixel → function of neighbors
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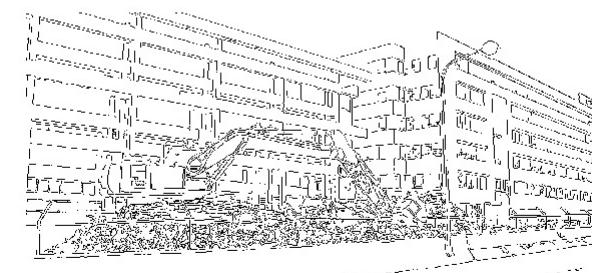
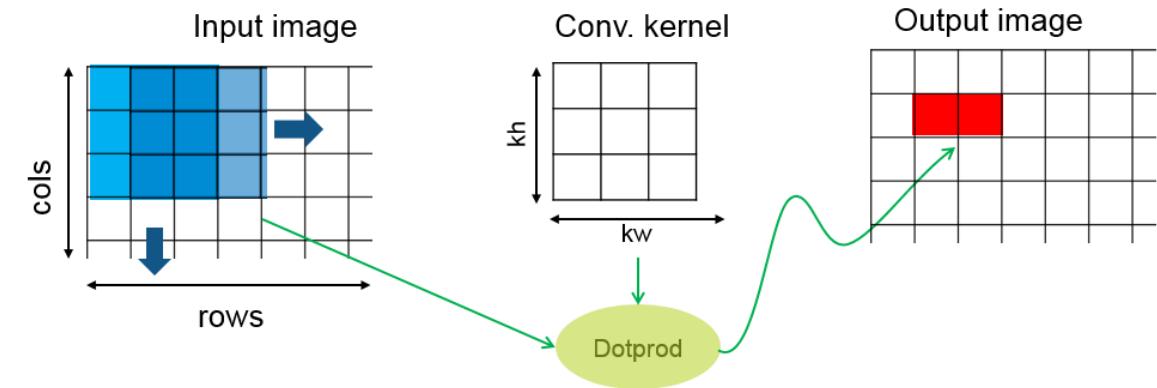
$$\mathbf{G}_x = \begin{bmatrix} +1 & 0 & -1 \\ +2 & 0 & -2 \\ +1 & 0 & -1 \end{bmatrix} * \mathbf{A} \quad \text{and} \quad \mathbf{G}_y = \begin{bmatrix} +1 & +2 & +1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix} * \mathbf{A}$$



Stencils

- Each pixel → function of neighbors
- Edge detection:

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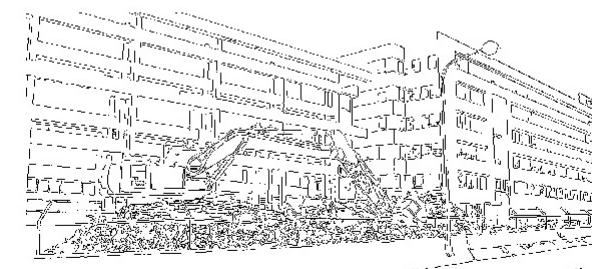
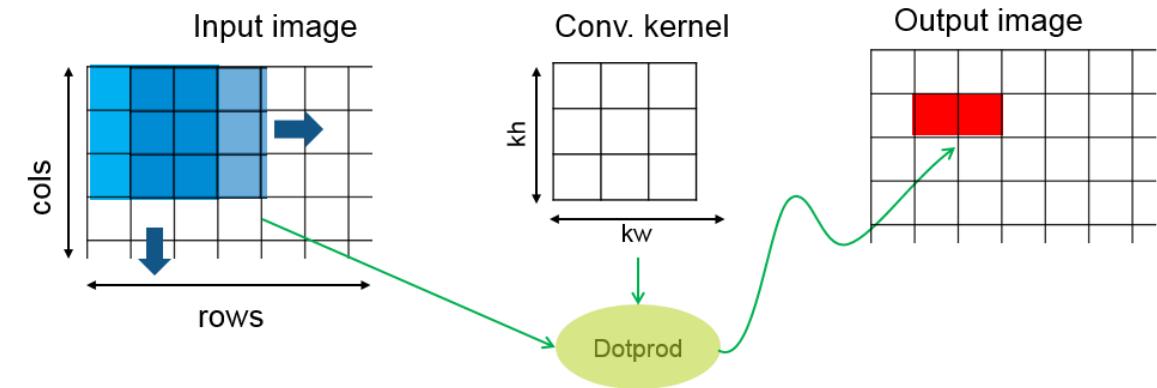


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- Blur:



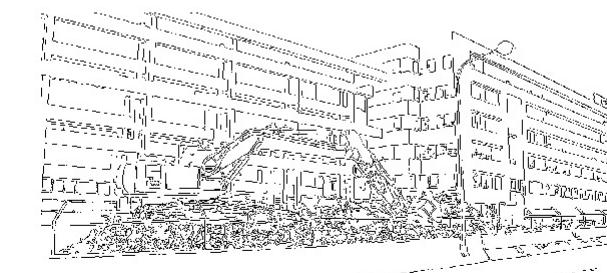
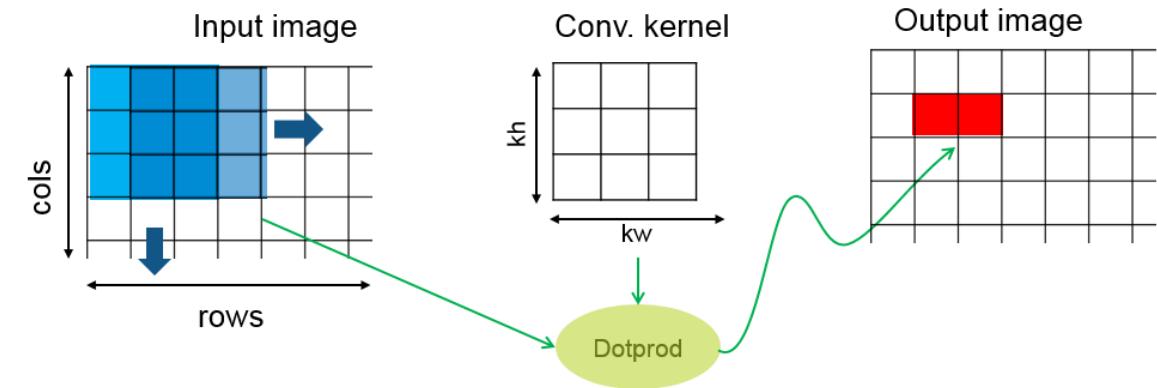
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- Blur:

1/16	1/8	1/16
1/8	1/4	1/8
1/16	1/8	1/16



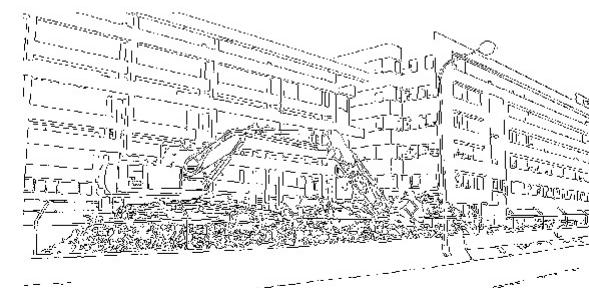
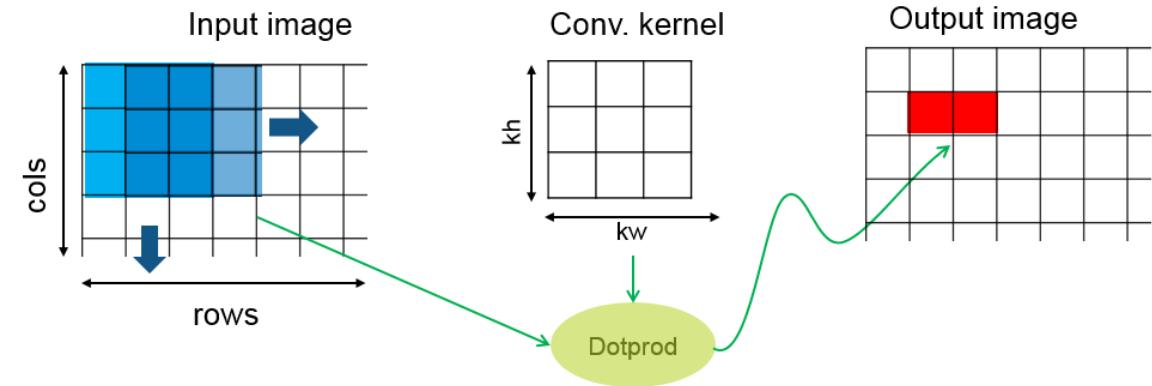
Stencils

- Each pixel → function of neighbors
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1D Stencil

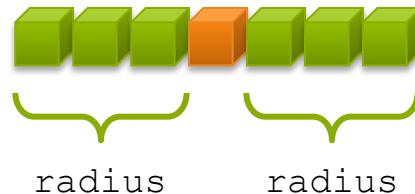
- Consider 1D stencil over 1D array of elements
 - Each output element is the sum of input elements within a radius

1D Stencil

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- Radius == 3 → each output element is sum of 7 input elements:

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Implementation within a block

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- Each thread: process 1 output element
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```
_global_ void stencil_1d(int *in, int *out) {
    // note: idx comp & edge conditions omitted...
    int result = 0;
    for (int offset = -R; offset <= R; offset++)
        result += in[idx + offset];

    // Store the result
    out[idx] = result;
}
```

Implementation within a block

- Each thread: process 1 output element
 - blockDim.x elements per block
- Input elements read many times
 - With radius 3, each input element is read seven times

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__global__ void stencil_1d(int *in, int *out) {
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Why is this a problem?

Sharing Data Between Threads

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- Terminology: within a block, threads share data via *shared memory*

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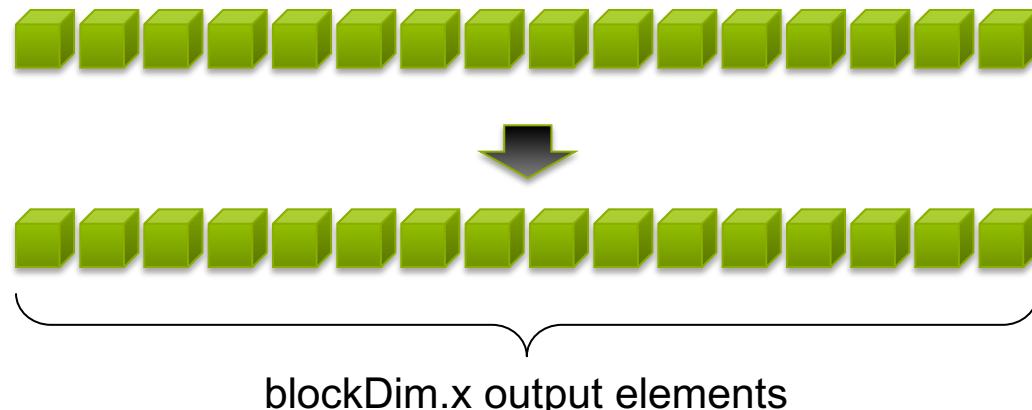
- Terminology: within a block, threads share data via *shared memory*
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- Declare using `__shared__`, allocated per block

Sharing Data Between Threads

- Terminology: within a block, threads share data via *shared memory*
- Extremely fast on-chip memory, user-managed
- Declare using `__shared__`, allocated per block
- Data is *not visible* to threads in other blocks

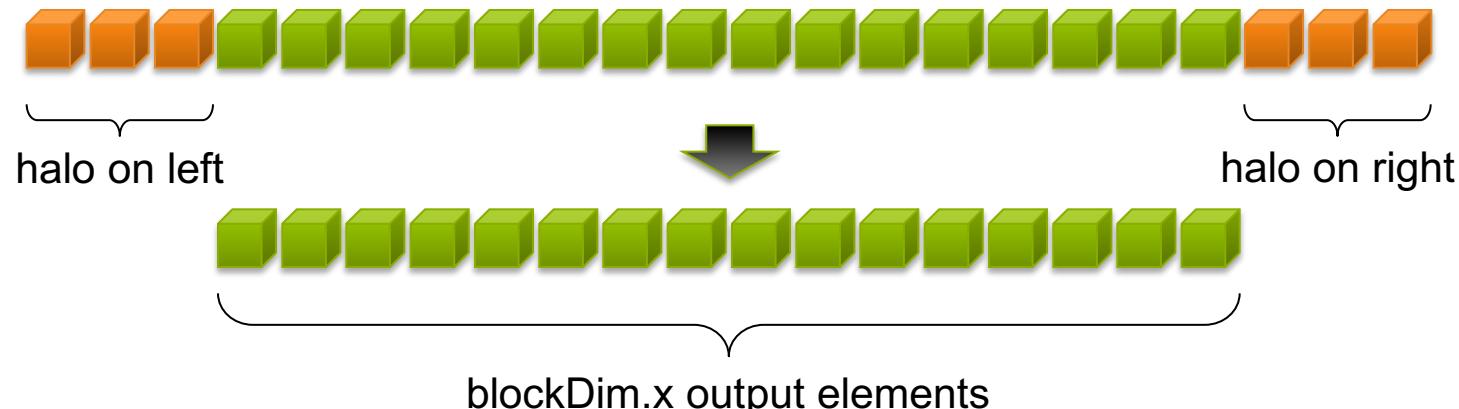
Stencil with Shared Memory

- Cache data in shared memory
 - Read $(blockDim.x + 2 * radius)$ elements from memory to shared
 - Compute $blockDim.x$ output elements
 - Write $blockDim.x$ output elements to global memory



Stencil with Shared Memory

- Cache data in shared memory
 - Read $(blockDim.x + 2 * radius)$ elements from memory to shared
 - Compute $blockDim.x$ output elements
 - Write $blockDim.x$ output elements to global memory
 - Each block needs a **halo** of $radius$ elements at each boundary



Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
```

Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {  
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
```



Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;
```

Stencil Kernel

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__global__ void stencil_1d(int *in, int *out) {
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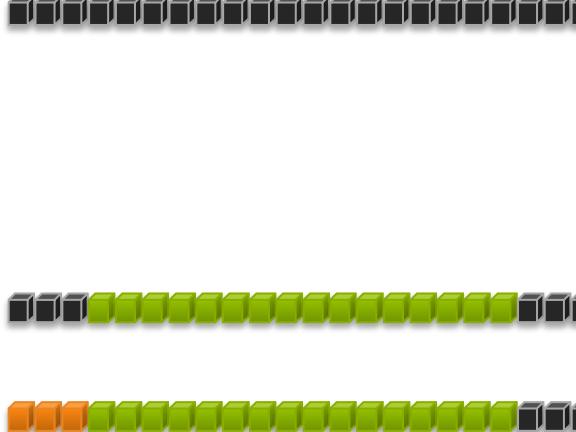
    // Read input elements into shared memory
    temp[lindex] = in[gindex];
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Stencil Kernel

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__global__ void stencil_1d(int *in, int *out) {
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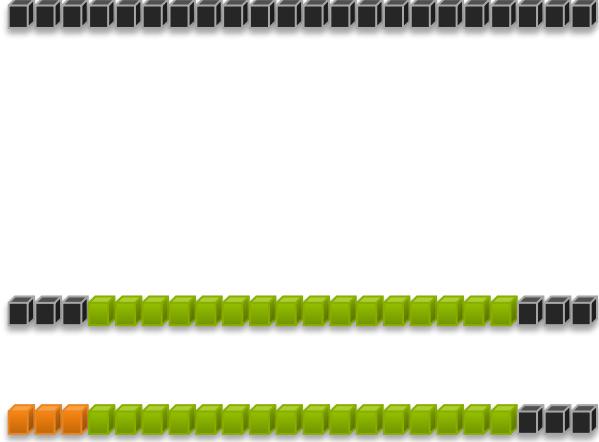
    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
```



Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] =
```



Stencil Kernel

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__global__ void stencil_1d(int *in, int *out) {
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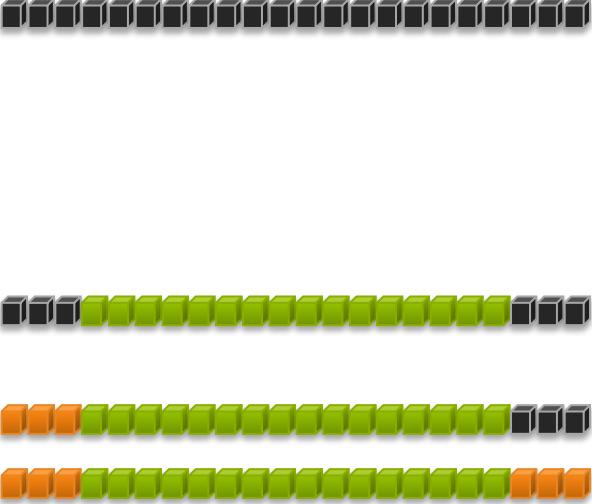
    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
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        temp[lindex + BLOCK_SIZE] =
            in[gindex + BLOCK_SIZE];
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Stencil Kernel

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__global__ void stencil_1d(int *in, int *out) {
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    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] =
            in[gindex + BLOCK_SIZE];
    }
}
```



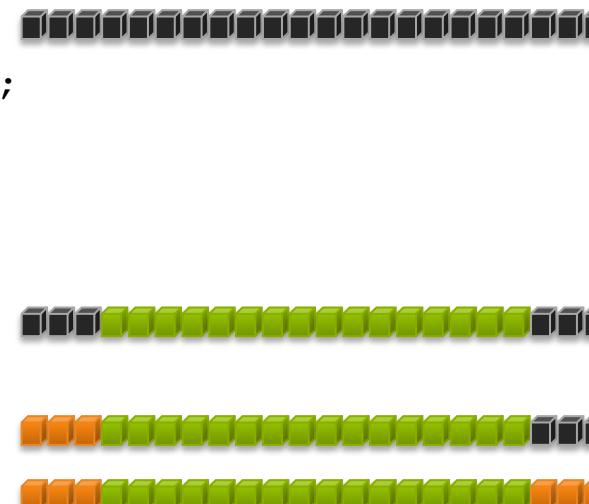
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__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] =
            in[gindex + BLOCK_SIZE];
    }

    // Apply the stencil
    int result = 0;
    for (int offset = -RADIUS ; offset <= RADIUS ; offset++)
        result += temp[lindex + offset];

    // Store the result
    out[gindex] = result;
}
```



Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] =
            in[gindex + BLOCK_SIZE];
    }

    // Apply the stencil
    int result = 0;
    for (int offset = -RADIUS ; offset <= RADIUS ; offset++)
        result += temp[lindex + offset];

    // Store the result
    out[gindex] = result;
}
```

Are we done?

Data Race!

- The stencil example will not work...

Data Race!

- The stencil example will not work...
- Suppose thread 15 reads the halo before thread 0 has fetched it...

```
temp[lindex] = in[gindex];
if (threadIdx.x < RADIUS) {
    temp[lindex - RADIUS] = in[gindex - RADIUS];
    temp[lindex + BLOCK_SIZE] = in[gindex + BLOCK_SIZE];
}

int result = 0;
result += temp[lindex + 1];
```

Data Race!

- The stencil example will not work...
- Suppose thread 15 reads the halo before thread 0 has fetched it...

```
temp[lindex] = in[gindex];           Store at temp[18] ████  
if (threadIdx.x < RADIUS) {  
    temp[lindex - RADIUS] = in[gindex - RADIUS];  
    temp[lindex + BLOCK_SIZE] = in[gindex + BLOCK_SIZE];  
}  
  
int result = 0;  
result += temp[lindex + 1];
```

Data Race!

- The stencil example will not work...
- Suppose thread 15 reads the halo before thread 0 has fetched it...

```
temp[lindex] = in[gindex];           Store at temp[18] ████  
if (threadIdx.x < RADIUS) {  
    temp[lindex - RADIUS] = in[gindex - RADIUS];   Skipped, threadIdx > RADIUS  
    temp[lindex + BLOCK_SIZE] = in[gindex + BLOCK_SIZE];  
}  
  
int result = 0;  
result += temp[lindex + 1];
```

Data Race!

- The stencil example will not work...
- Suppose thread 15 reads the halo before thread 0 has fetched it...

```
temp[lindex] = in[gindex];           Store at temp[18]   
if (threadIdx.x < RADIUS) {  
    temp[lindex - RADIUS] = in[gindex - RADIUS];   Skipped, threadIdx > RADIUS  
    temp[lindex + BLOCK_SIZE] = in[gindex + BLOCK_SIZE];  
}  
  
int result = 0;  
result += temp[lindex + 1];           Load from temp[19] 
```

__syncthreads()

- `void __syncthreads();`
- Synchronizes all threads within a block
 - Used to prevent RAW / WAR / WAW hazards
- All threads must reach the barrier
 - In conditional code, the condition must be uniform across the block

Correct Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
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Correct Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {  
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
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```
__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;
```

Correct Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
```



Correct Stencil Kernel

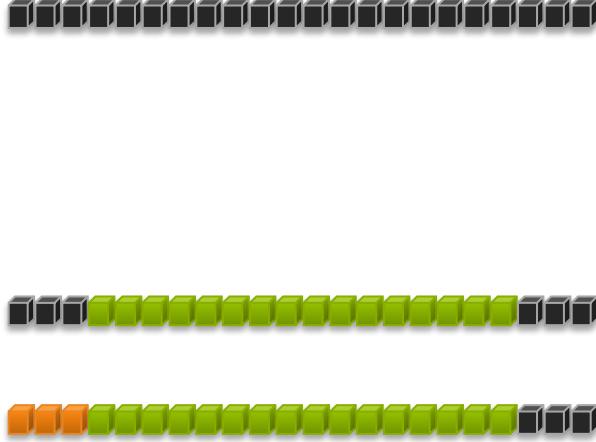
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__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
```

Correct Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] =
```



Correct Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] =
            in[gindex + BLOCK_SIZE];
```



Correct Stencil Kernel

```
__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
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    temp[lindex] = in[gindex];
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        temp[lindex - RADIUS] = in[gindex - RADIUS];
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            in[gindex + BLOCK_SIZE];
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}
```



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__global__ void stencil_1d(int *in, int *out) {
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    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
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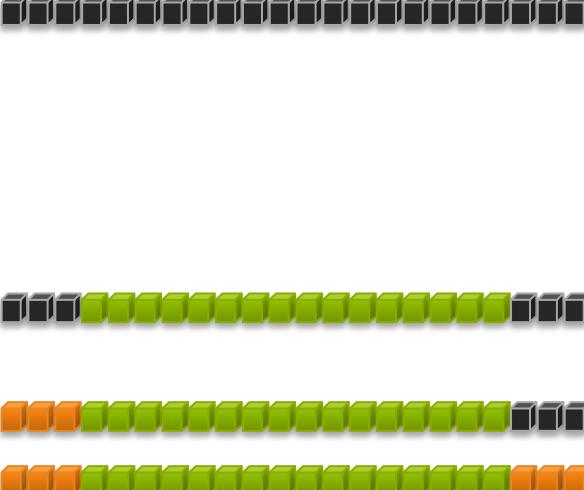
    // Read input elements into shared memory
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        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] =
            in[gindex + BLOCK_SIZE];
    }
    __syncthreads();
```



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__global__ void stencil_1d(int *in, int *out) {
    __shared__ int temp[BLOCK_SIZE + 2 * RADIUS];
    int gindex = threadIdx.x + blockIdx.x * blockDim.x;
    int lindex = threadIdx.x + RADIUS;

    // Read input elements into shared memory
    temp[lindex] = in[gindex];
    if (threadIdx.x < RADIUS) {
        temp[lindex - RADIUS] = in[gindex - RADIUS];
        temp[lindex + BLOCK_SIZE] =
            in[gindex + BLOCK_SIZE];
    }
    __syncthreads();
    // Apply the stencil
    int result = 0;
    for (int offset = -RADIUS ; offset <= RADIUS ; offset++)
        result += temp[lindex + offset];
    __syncthreads();
    // Store the result
    out[gindex] = result;
}
```



Notes on __syncthreads()

- `void __syncthreads();`
- Synchronizes all threads within a block
 - Used to prevent RAW / WAR / WAW hazards
- All threads must reach the barrier
 - In conditional code, the condition must be uniform across the block

Notes on __syncthreads()

- void __syncthreads();

- Synchronizes all threads within a block

- Used to prevent RAW / WAR / WAW hazards

```
__global__ void some_kernel(int *in, int *out) {
    // good idea?
    if(threadIdx.x == SOME_VALUE)
        __syncthreads();
}
```

- All threads must reach the barrier

- In conditional code, the condition must be uniform across the block

Notes on __syncthreads()

- `void __syncthreads();`
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Notes on __syncthreads()

- `void __syncthreads();`
- Synchronizes all threads within a block
 - Used to prevent RAW / WAR / WAW hazards
- All threads must reach the barrier
 - In conditional code, the condition must be uniform across the block

```
__device__ void lock_trick(int *in, int *out) {
    __syncthreads();
    if(myIndex == 0)
        critical_section();
    __syncthreads();
}
```

Atomics

Race conditions –

- Traditional locks are to be avoided
- How do we synchronize?

Read-Modify-Write – atomic

atomicAdd()	atomicInc()
atomicSub()	atomicDec()
atomicMin()	atomicExch()
atomicMax()	atomicCAS()

Atomics

Race conditions –

- Traditional locks are to be avoided
- How do we synchronize?

Read

Modify, Write, atomic

```
__device__ double atomicAdd(double* address, double val) {
    unsigned long long int* address_as_ull = (unsigned long long int*)address;
    unsigned long long int old = *address_as_ull, assumed;
    do {
        assumed = old;
        old = atomicCAS(address_as_ull,
                        assumed,
                        __double_as_longlong(val + __longlong_as_double(assumed)));
    } while (assumed != old);
    return __longlong_as_double(old);
}
```

Recap

- Launching parallel threads
 - Launch N blocks with M threads per block with `kernel<<<N,M>>>(...);`
 - Use `blockIdx.x` to access block index within grid
 - Use `threadIdx.x` to access thread index within block
- Allocate elements to threads:

```
int index = threadIdx.x + blockIdx.x * blockDim.x
```

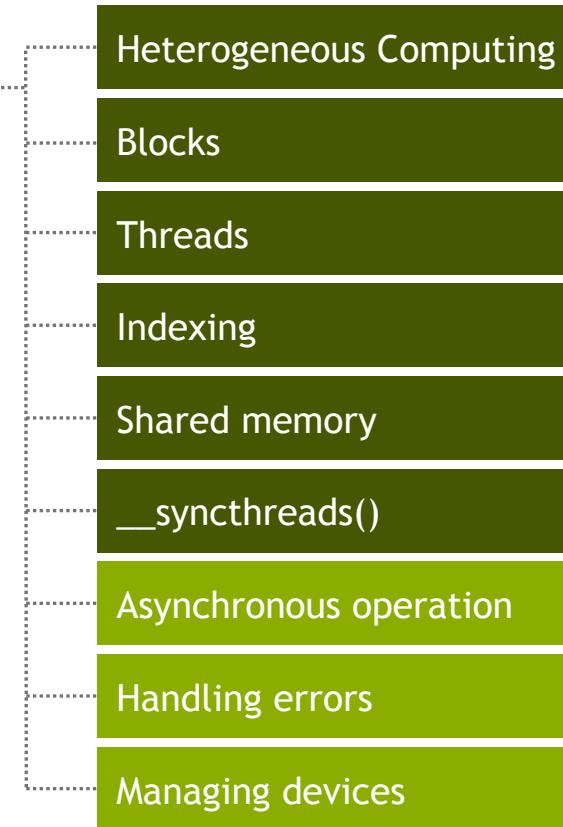
Use `__shared__` to declare a variable/array in shared memory

Data is shared between threads in a block
Not visible to threads in other blocks

Use `__syncthreads()` as a barrier
Use to prevent data hazards

MANAGING THE DEVICE

CONCEPTS



Coordinating Host & Device

- Kernel launches are **asynchronous**
 - Control returns to the CPU immediately
- CPU needs to synchronize before consuming the results

cudaMemcpy()

Blocks the CPU until the copy is complete
Copy begins when all preceding CUDA calls have completed

cudaMemcpyAsync()

Asynchronous, does not block the CPU

cudaDeviceSynchronize()

Blocks the CPU until all preceding CUDA calls have completed

Reporting Errors

- All CUDA API calls return an error code (`cudaError_t`)
 - Error in the API call itself
 - OR
 - Error in an earlier asynchronous operation (e.g. kernel)

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`cudaError_t cudaGetLastError(void)`
- Get a string to describe the error:
`char *cudaGetErrorString(cudaError_t)`

Reporting Errors

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`cudaError_t cudaGetLastError(void)`
- Get a string to describe the error:
`char *cudaGetString(cudaError_t)`

`printf("%s\n", cudaGetString(cudaGetLastError()));`

Device Management

- Application can query and select GPUs

```
cudaGetDeviceCount(int *count)
cudaSetDevice(int device)
cudaGetDevice(int *device)
cudaGetDeviceProperties(cudaDeviceProp *prop, int
device)
```

- Multiple threads can share a device
- A single thread can manage multiple devices

```
cudaSetDevice(i) to select current device
cudaMemcpy(...) for peer-to-peer copies†
```

[†] requires OS and device support

CUDA Events: Measuring Performance

```
float memsettime;
cudaEvent_t start, stop;

// initialize CUDA timer
cudaEventCreate(&start);  cudaEventCreate(&stop);
cudaEventRecord(start,0);

// CUDA Kernel
. . .

// stop CUDA timer
cudaEventRecord(stop,0);
cudaEventSynchronize(stop);
cudaEventElapsedTime(&memsettime,start,stop);
printf(" *** CUDA execution time: %f *** \n", memsettime);
cudaEventDestroy(start);
cudaEventDestroy(stop);
```

Compute Capability

- The **compute capability** of a device describes its architecture, e.g.
 - Number of registers
 - Sizes of memories
 - Features & capabilities

Compute Capability

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Compute Capability <small>(see CUDA C Programming Guide for complete list)</small>	Selected Features	Tesla models
1.0	Fundamental CUDA support	870
1.3	Double precision, improved memory accesses, atomics	10-series
2.0	Caches, fused multiply-add, 3D grids, surfaces, ECC, P2P, concurrent kernels/copies, function pointers, recursion	20-series

Compute Capability

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- The following presentations concentrate on Fermi devices
 - Compute Capability ≥ 2.0

Compute Capability

- The compute capability
- Number of cores
- Sizes of memory
- Features & Capabilities



Feature Support	Compute Capability				
(Unlisted features are supported for all compute capabilities)	3.5, 3.7, 5.0, 5.2	5.3	6.x	7.x	8.x
Atomic functions operating on 32-bit integer values in global memory (Atomic Functions)			Yes		
Atomic functions operating on 32-bit integer values in shared memory (Atomic Functions)			Yes		
Atomic functions operating on 64-bit integer values in global memory (Atomic Functions)			Yes		
Atomic functions operating on 64-bit integer values in shared memory (Atomic Functions)			Yes		
Atomic addition operating on 32-bit floating point values in global and shared memory (atomicAdd())			Yes		
Atomic addition operating on 64-bit floating point values in global memory and shared memory (atomicAdd())	No			Yes	
Warp vote functions (Warp Vote Functions)					
Memory fence functions (Memory Fence Functions)					
Synchronization functions (Synchronization Functions)			Yes		
Surface functions (Surface Functions)					
Unified Memory Programming (Unified Memory Programming)			Yes		
Dynamic Parallelism (CUDA Dynamic Parallelism)					
Half-precision floating-point operations: addition, subtraction, multiplication, comparison, warp shuffle functions, conversion	No		Yes		
Bfloat16-precision floating-point operations: addition, subtraction, multiplication, comparison, warp shuffle functions, conversion		No			Yes
Tensor Cores		No		Yes	
Mixed Precision Warp-Matrix Functions (Warp matrix functions)		No		Yes	
Hardware-accelerated <code>memcpy_async</code> (Asynchronous Data Copies)		No			Yes
Hardware-accelerated Split Arrive/Wait Barrier (Asynchronous Barrier)		No			Yes
L2 Cache Residency Management (Device Memory L2 Access Management)		No			Yes

Note that the KB and K units used in the following table correspond to 1024 bytes (i.e., a KiB) and 1024 respectively.



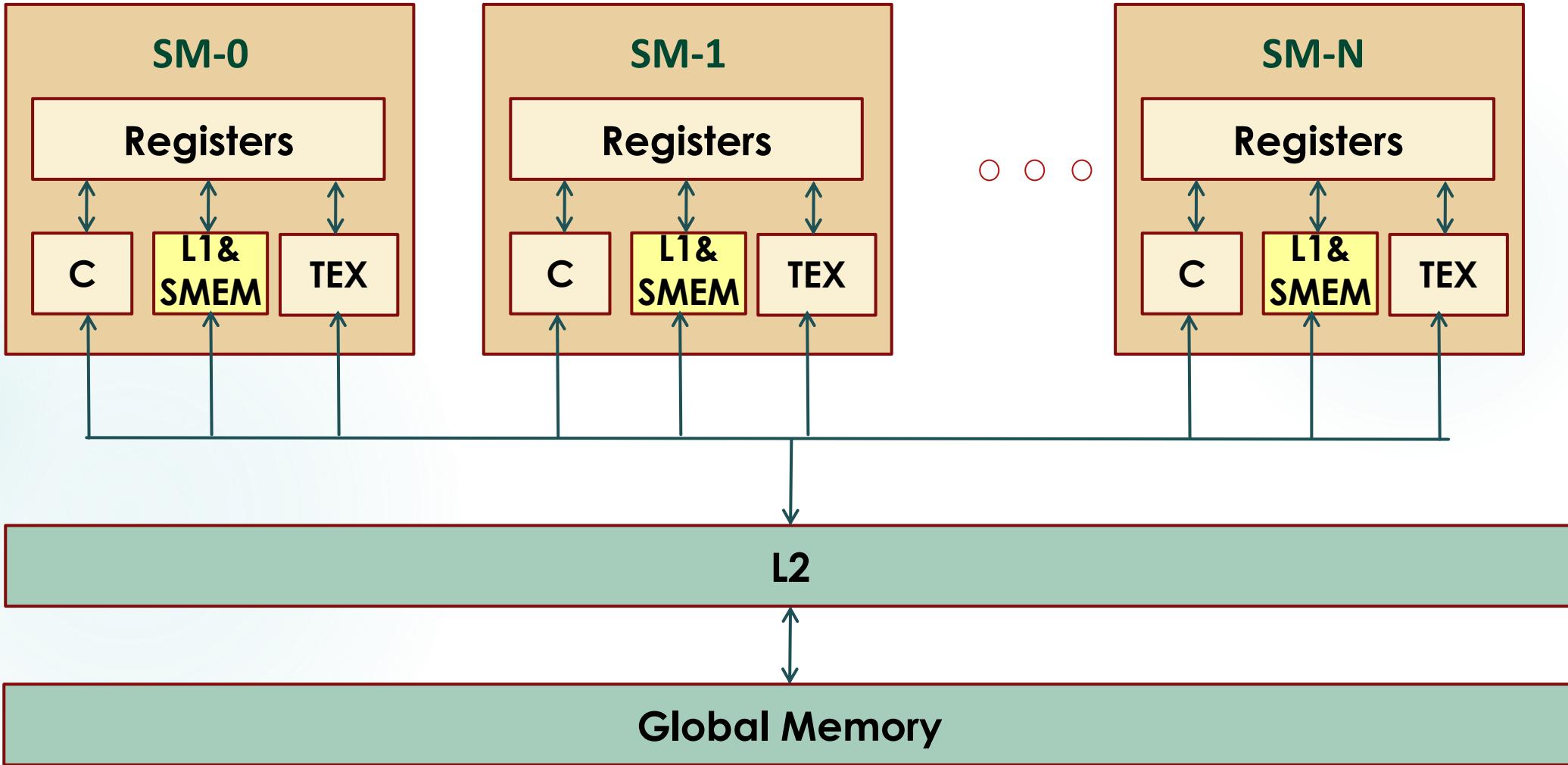
- Thread block dimensions
- Compute Capability ≥ 2.0

Table 15. Technical Specifications per Compute Capability

Technical Specifications	3.5	3.7	5.0	5.2	5.3	6.0	6.1	6.2	7.0
Maximum number of resident grids per device (Concurrent Kernel Execution)		32		16	128	32	16		
Maximum dimensionality of grid of thread blocks						3			
Maximum x-dimension of a grid of thread blocks						$2^{31.1}$			
Maximum y- or z-dimension of a grid of thread blocks						65535			
Maximum dimensionality of a thread block						3			
Maximum x- or y-dimension of a block						1024			
Maximum z-dimension of a block						64			
Maximum number of threads per block						1024			
Warp size						32			
Maximum number of resident blocks per SM	16					32			
Maximum number of resident warps per SM						64			

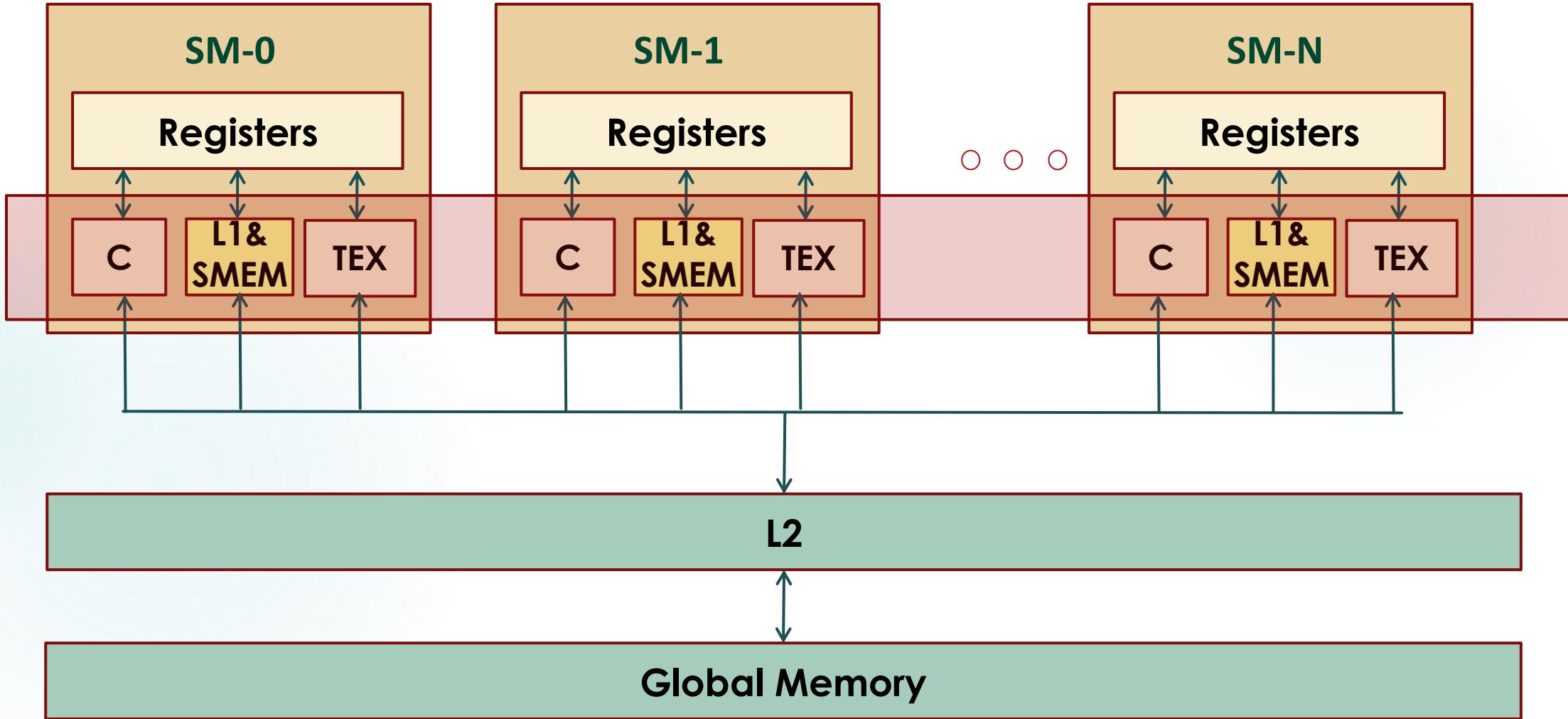
GPU Memory Hierarchy

73



GPU Memory Hierarchy

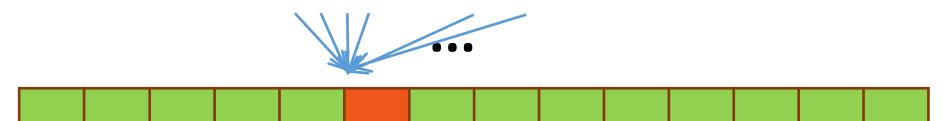
73



Constant Cache

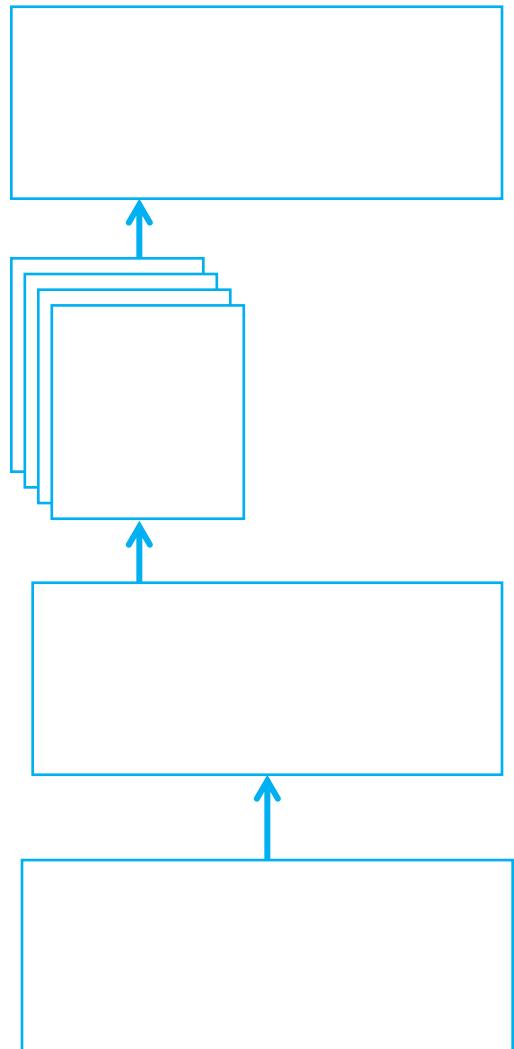
- Global variables marked by `__constant__`
 - constant and can't be changed in device.
- Will be cached by Constant Cache
- Located in global memory
- Good for threads that access the same address

```
__constant__ int a=10;  
  
__global__ void kernel()  
{  
    a++; //error  
}
```



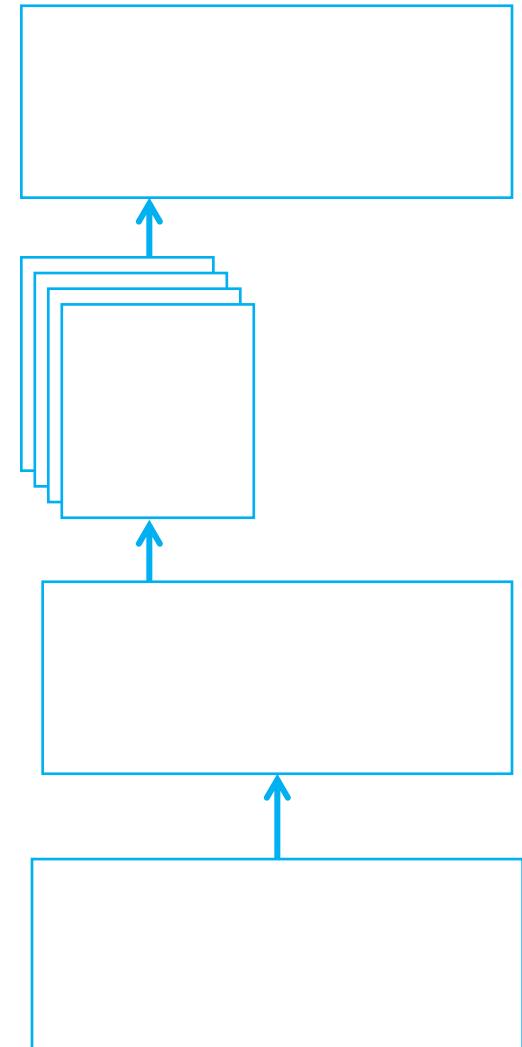
Memory addresses

Texture Cache



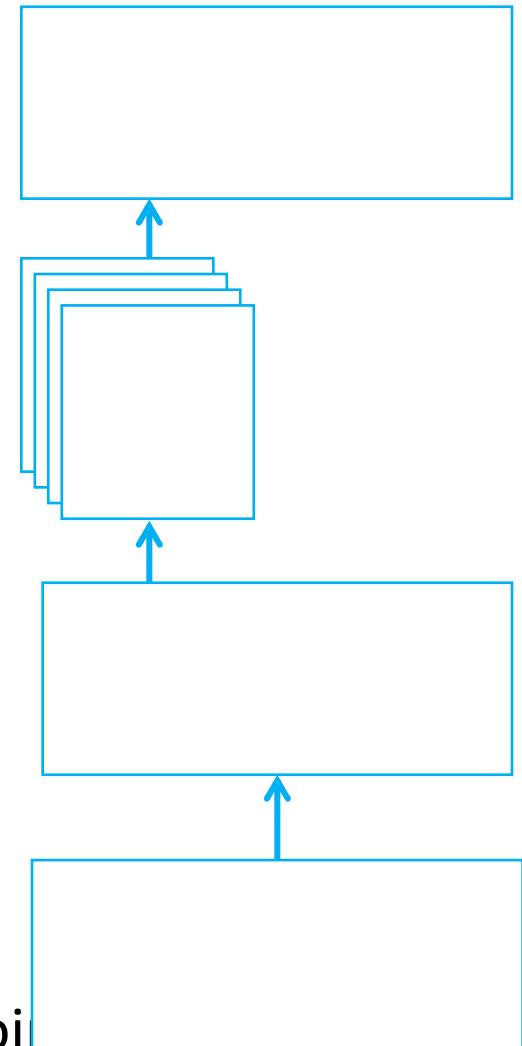
Texture Cache

- Save Data as Texture :
 - Provides hardware accelerated filtered sampling of data (1D, 2D, 3D)
 - Read-only data cache holds fetched samples
 - Backed up by the L2 cache



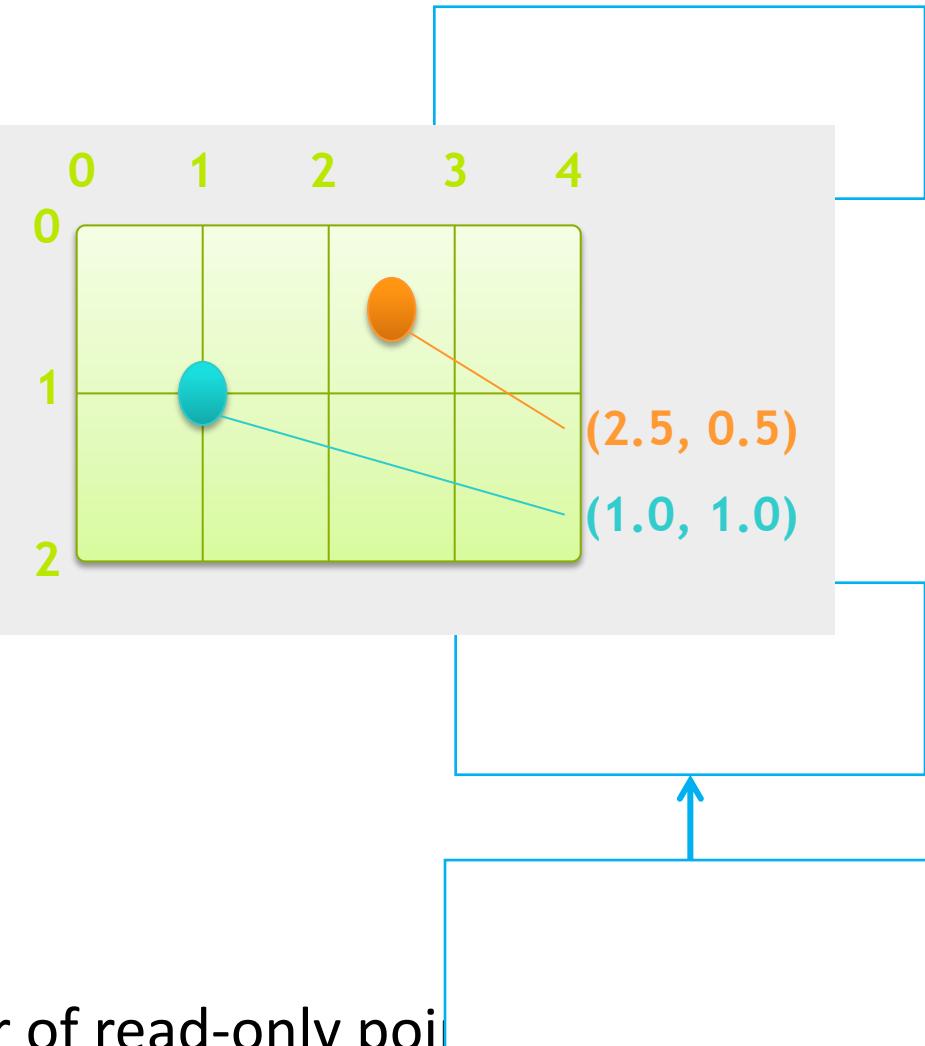
Texture Cache

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 - Provides hardware accelerated filtered sampling of data (1D, 2D, 3D)
 - Read-only data cache holds fetched samples
 - Backed up by the L2 cache
- Why use it?
 - Separate pipeline from shared/L1
 - Highest miss bandwidth
 - Flexible, e.g. unaligned accesses
 - What if your problem takes a large number of read-only point input?



Texture Cache

- Save Data as Texture
 - Provides hardware sampling of data
 - Read-only data cache
 - Backed up by the memory system
- Why use it?
 - Separate pipeline from shared/L1
 - Highest miss bandwidth
 - Flexible, e.g. unaligned accesses
 - What if your problem takes a large number of read-only points as input?



How many threads/blocks should I use?

```
// Copy inputs to device
cudaMemcpy(d_a, a, size, cudaMemcpyHostToDevice);
cudaMemcpy(d_b, b, size, cudaMemcpyHostToDevice);

// Launch add() kernel on GPU
add<<<N/THREADS_PER_BLOCK, THREADS_PER_BLOCK>>>(d_a, d_b, d_c);

// Copy result back to host
cudaMemcpy(c, d_c, size, cudaMemcpyDeviceToHost);

// Cleanup
free(a); free(b); free(c);
cudaFree(d_a); cudaFree(d_b); cudaFree(d_c);
return 0;
}
```

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cudaFree(d_a); cudaFree(d_b); cudaFree(d_c);
return 0;
}
```

- Usually things are correct if grid*block dims >= input size
- Getting good performance is another matter



Internals

```
host
Void vecAdd()
{
    dim3 DimGrid = (ceil(n/256,1,1);
    dim3 DimBlock = (256,1,1);
    vecAddKernel<<<DGrid,DBlock>>>(A_d,B_d,C_d,n);
}
```

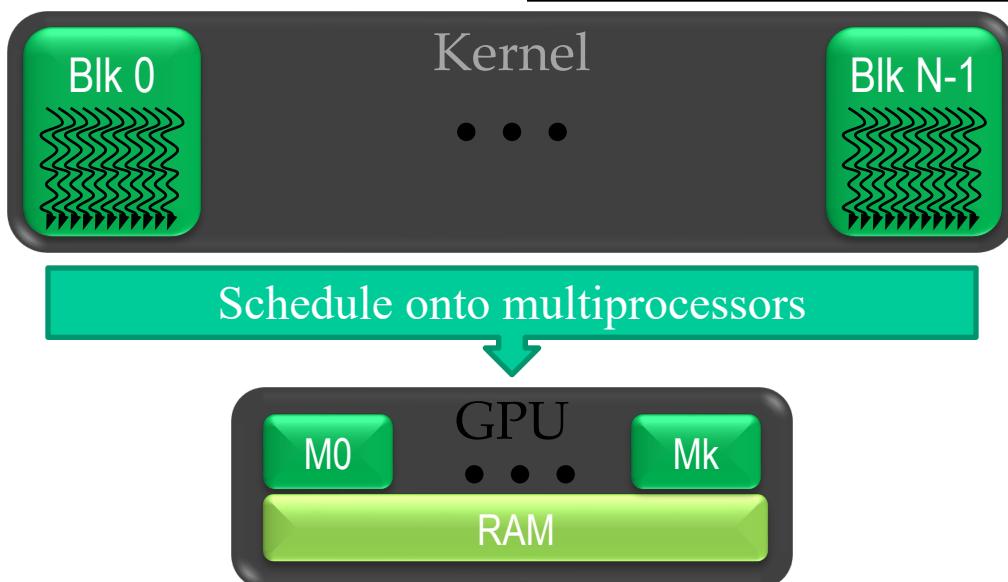
```
global
void vecAddKernel(float *A_d,
                  float *B_d, float *C_d, int n)
{
    int i = blockIdx.x * blockDim.x
           + threadIdx.x;
    if( i<n ) C_d[i] = A_d[i]+B_d[i];
}
```

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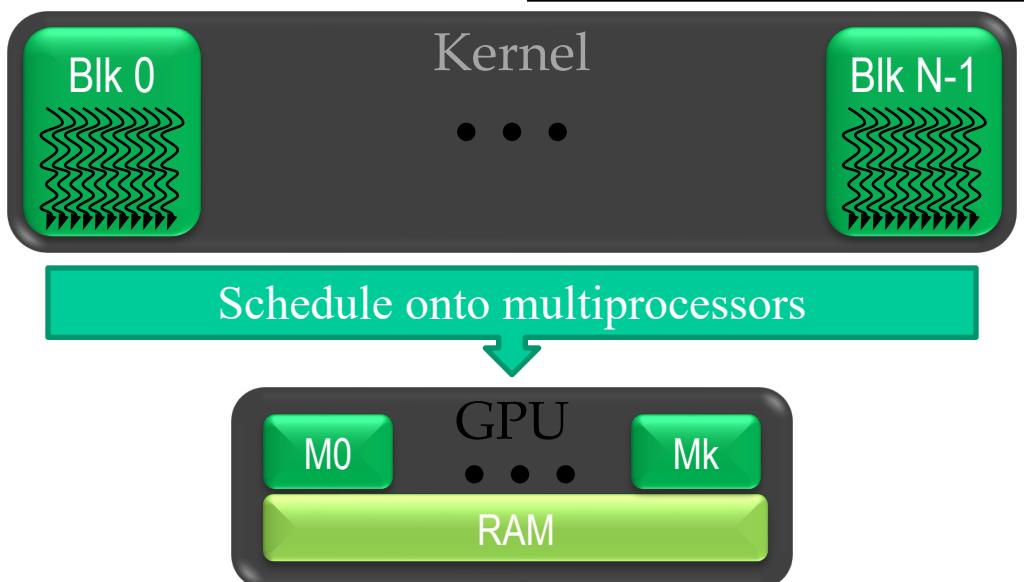
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```



How are threads scheduled?

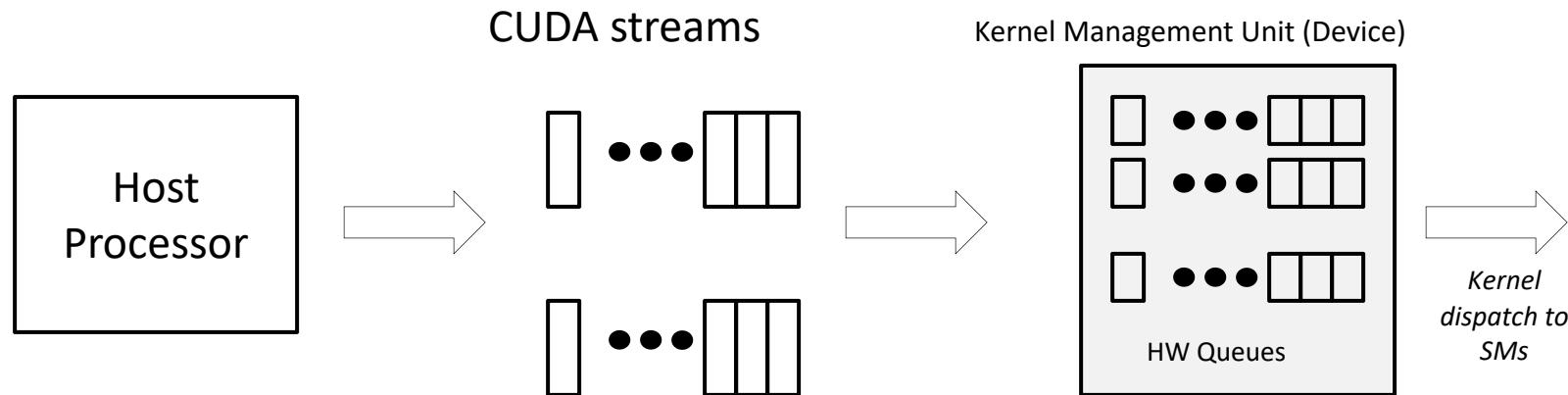
Kernel Launch

Kernel Launch

- Commands by host issued through *streams*

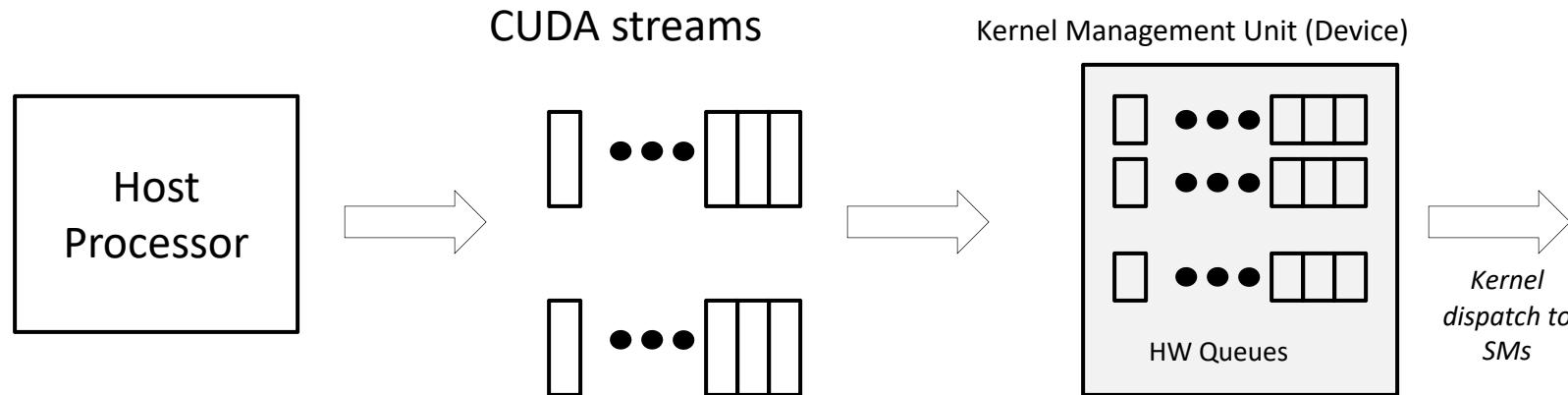
Kernel Launch

- Commands by host issued through *streams*



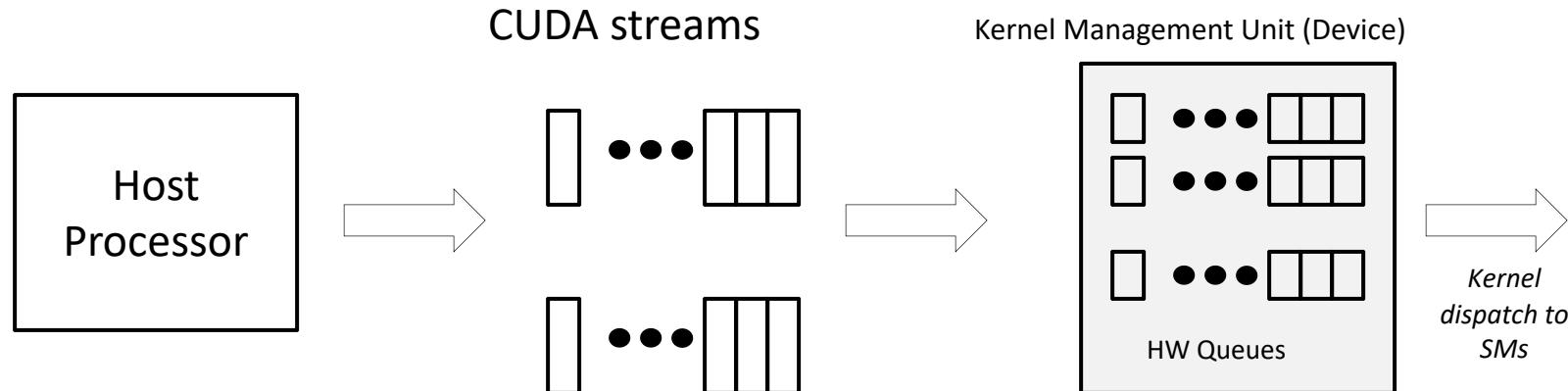
Kernel Launch

- Commands by host issued through *streams*
 - ❖ Kernels in the same stream executed sequentially



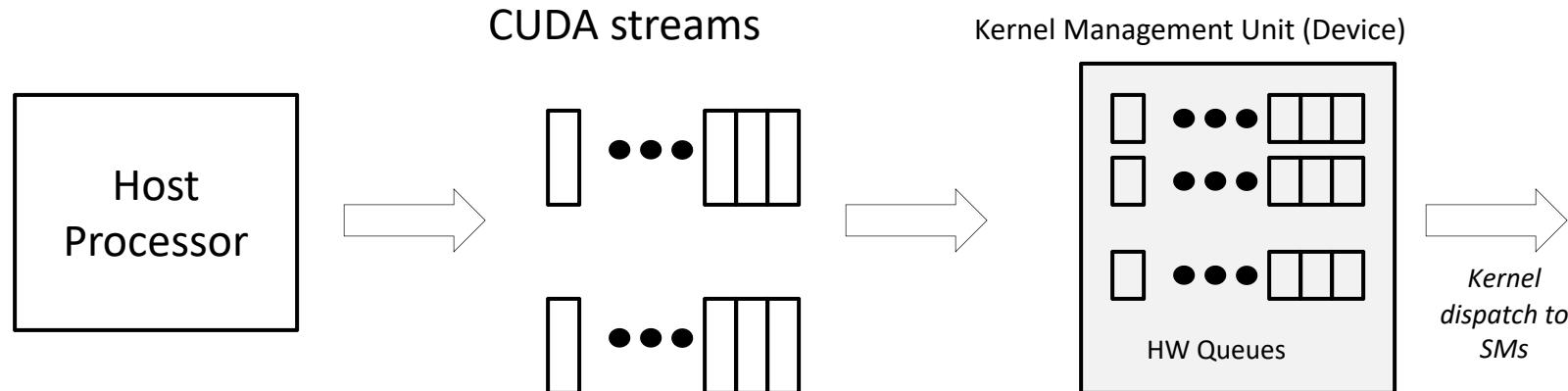
Kernel Launch

- Commands by host issued through *streams*
 - ❖ Kernels in the same stream executed sequentially
 - ❖ Kernels in different streams may be executed concurrently



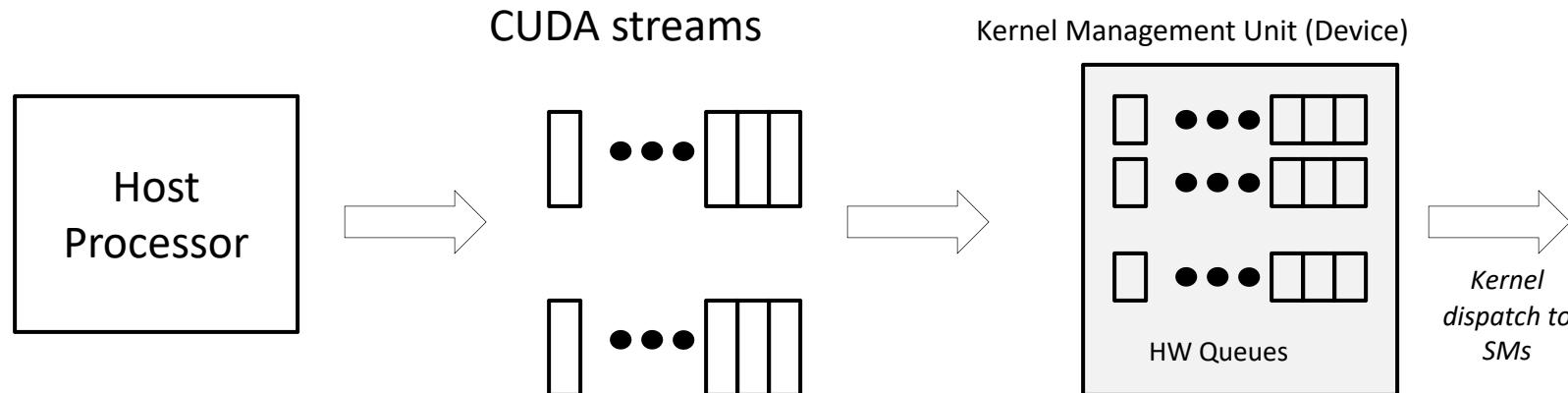
Kernel Launch

- Commands by host issued through *streams*
 - ❖ Kernels in the same stream executed sequentially
 - ❖ Kernels in different streams may be executed concurrently
- Streams mapped to GPU HW queues



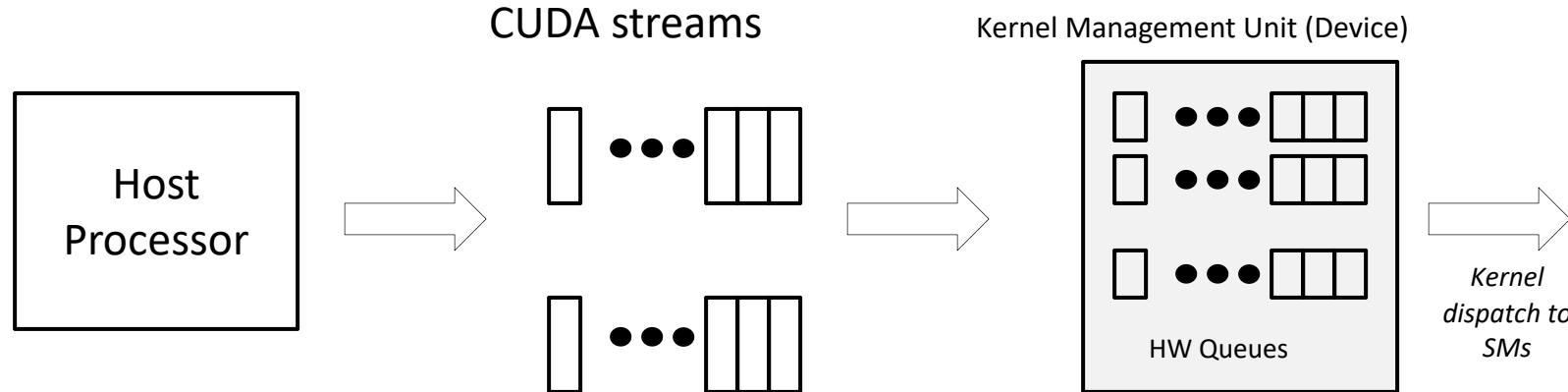
Kernel Launch

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 - ❖ Done by “kernel management unit” (KMU)



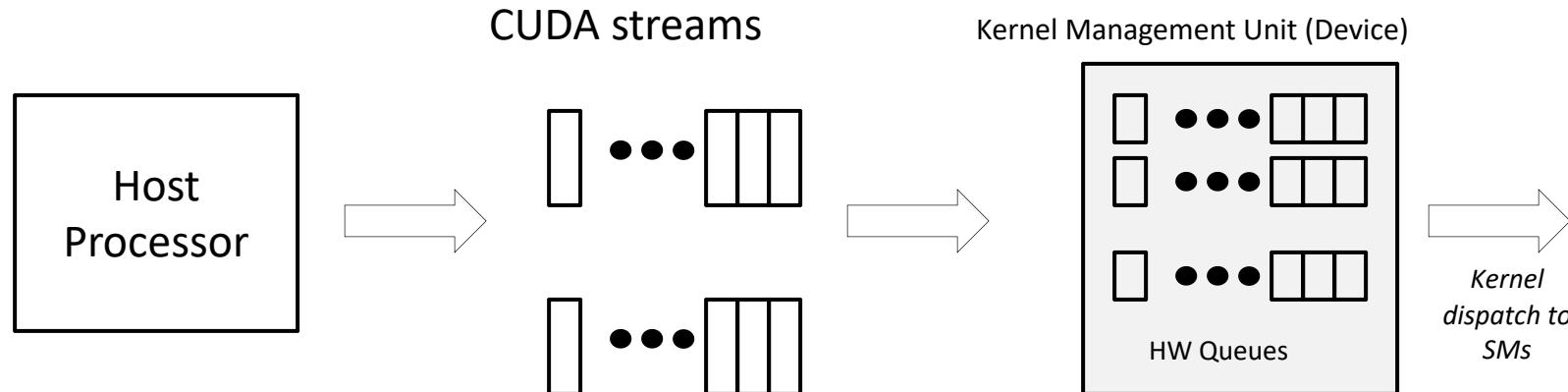
Kernel Launch

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Kernel Launch

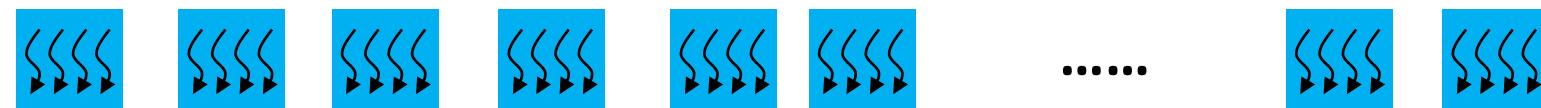
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- Streams mapped to GPU HW queues
 - ❖ Done by “kernel management unit” (KMU)
 - ❖ Multiple streams mapped to each queue → serializes some kernels
- Kernel launch distributes thread blocks to SMs



Thread Blocks, Warps, Scheduling

- What's a warp?
- Imagine one TB (threadblock) has 64 threads (2 warps)
 - On K20c GK110 GPU: 13 SMs, max 64 warps/SM, max 32 concurrent kernels

Thread Blocks



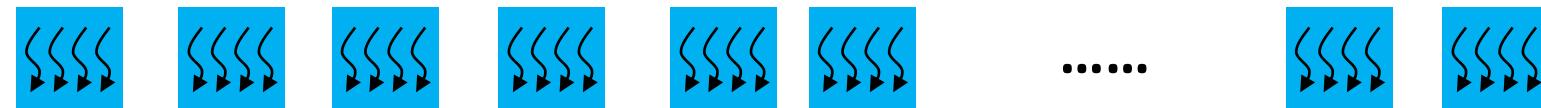
SMs



Thread Blocks, Warps, Scheduling

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Thread Blocks



SMs



- SMs split blocks into warps
- Unit of HW scheduling for SM
- 32 threads each

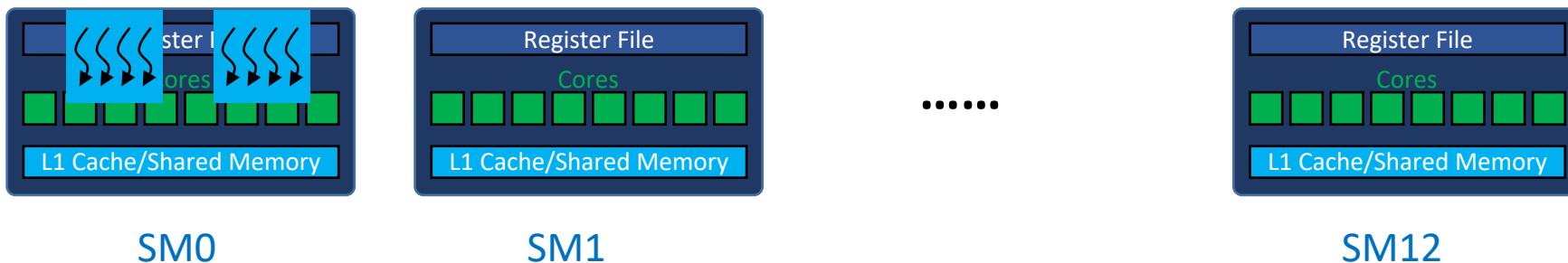
TBs, Warps, & Utilization

- One TB has 64 threads or 2 warps
 - On K20c GK110 GPU: 13 SMX, max 64 warps/SM, max 32 concurrent kernels

Thread Blocks



SMs



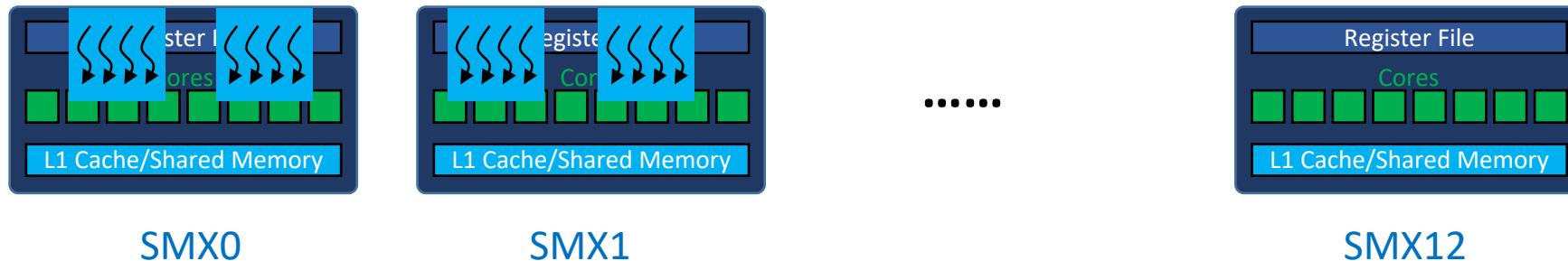
TBs, Warps, & Utilization

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Thread Blocks



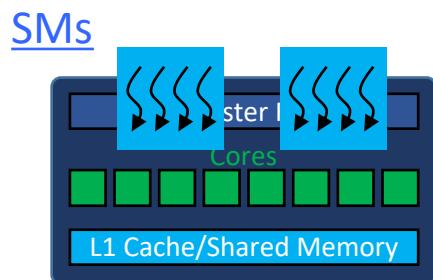
SMXs



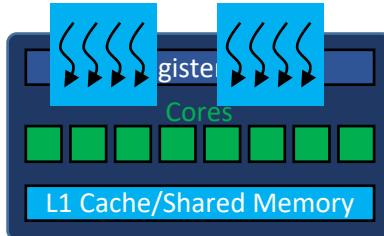
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Thread Blocks



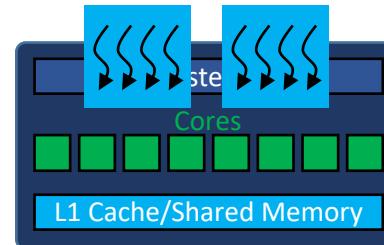
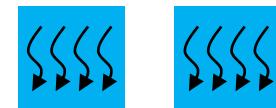
SM0



SM1

Remaining TBs are queued

.....



SM12

NVIDIA GK110 (Kepler)

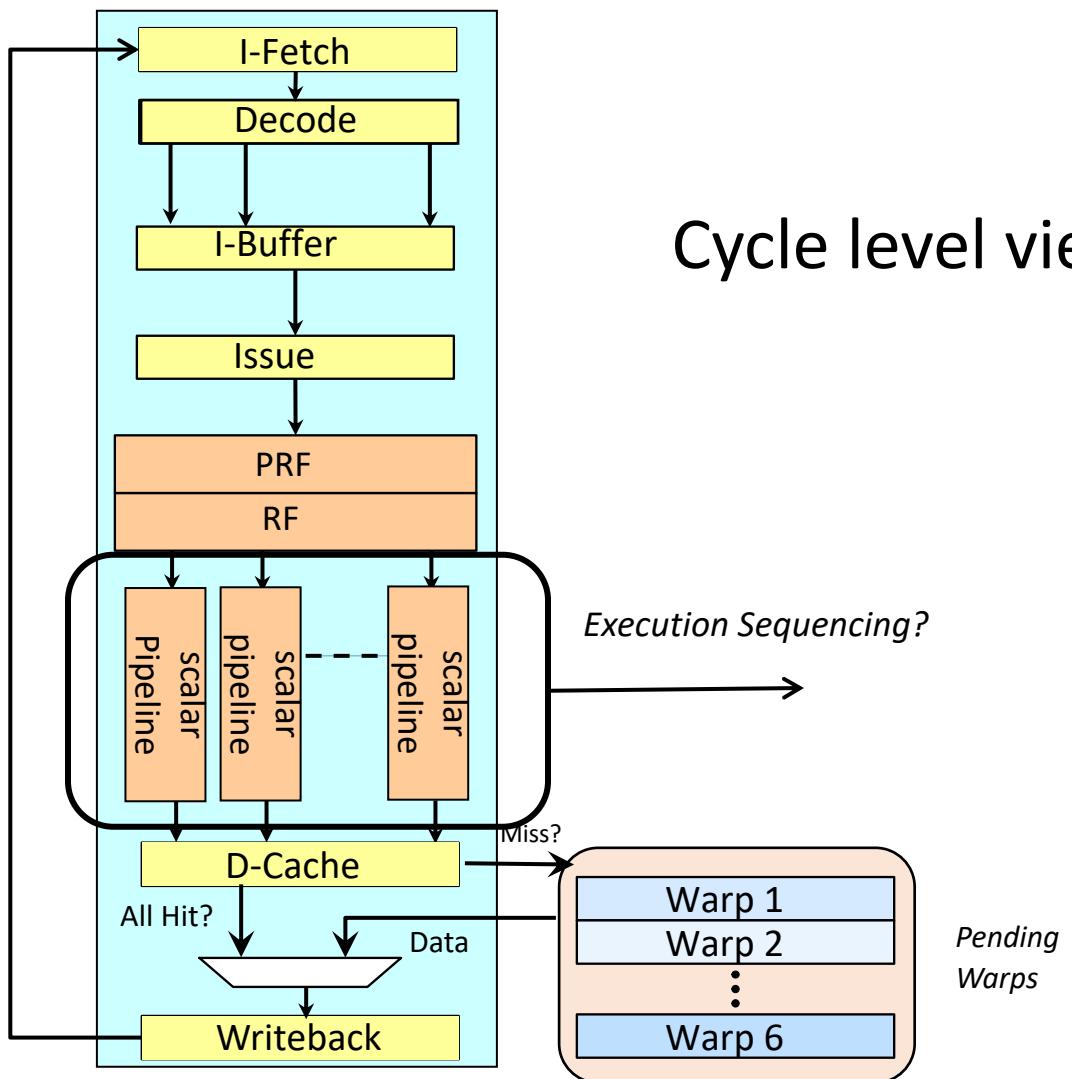


Image from <http://mandetech.com/2012/05/20/nvidia-new-gpu-and-visualization/>

NVIDIA GK110 (Kepler)



Execution Sequencing in a Single SM



Cycle level view: GPU kernel execution

Example: VectorAdd on GPU

CUDA:

```
__global__ vector_add
( float *a, float *b, float *c, int N) {
int index = blockIdx.x * blockDim.x +
threadIdx.x;

if (index < N)
    c[index] = a[index]+b[index];
}
```

PTX (Assembly):

```
setp.lt.s32 %p, %r5, %rd4; //r5 = index, rd4 = N
@p bra L1;
bra L2;

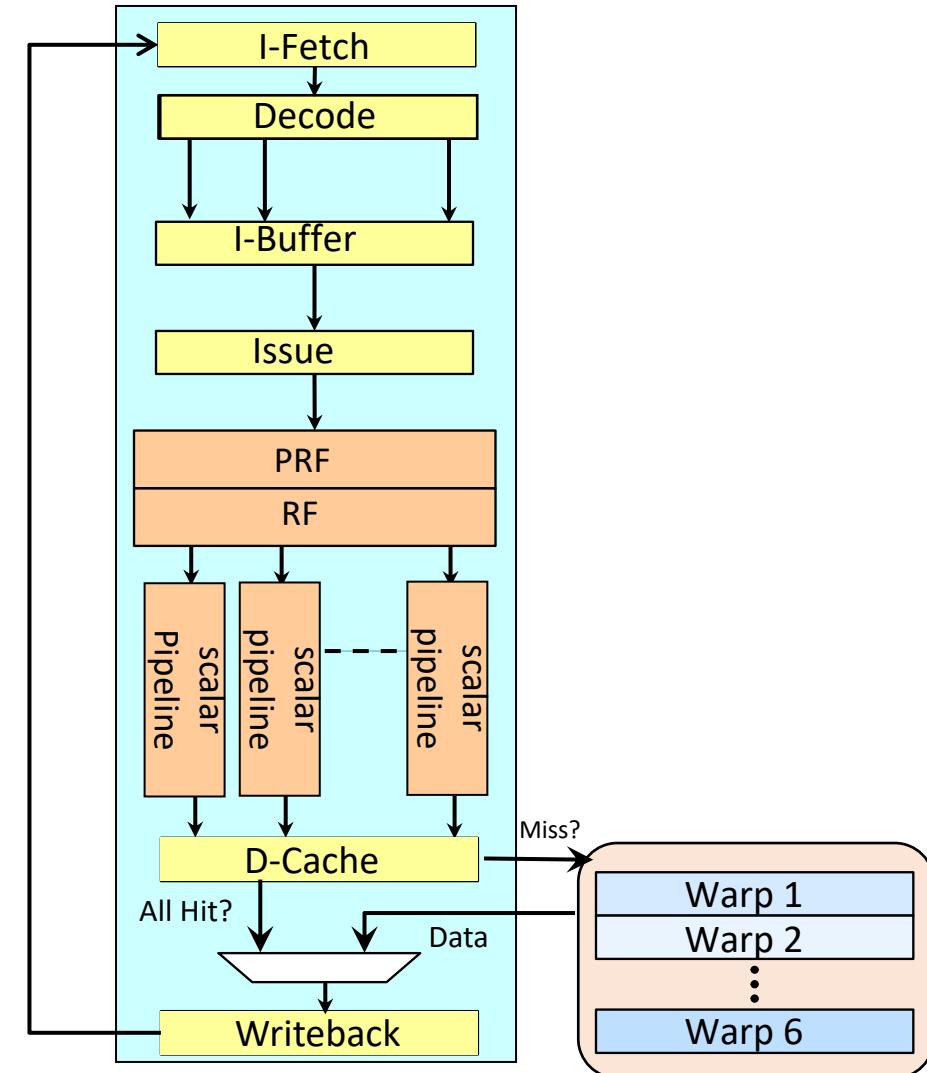
L1:
ld.global.f32 %f1, [%r6]; //r6 = &a[index]
ld.global.f32 %f2, [%r7]; //r7 = &b[index]
add.f32 %f3, %f1, %f2;

st.global.f32 [%r8], %f3; //r8 = &c[index]

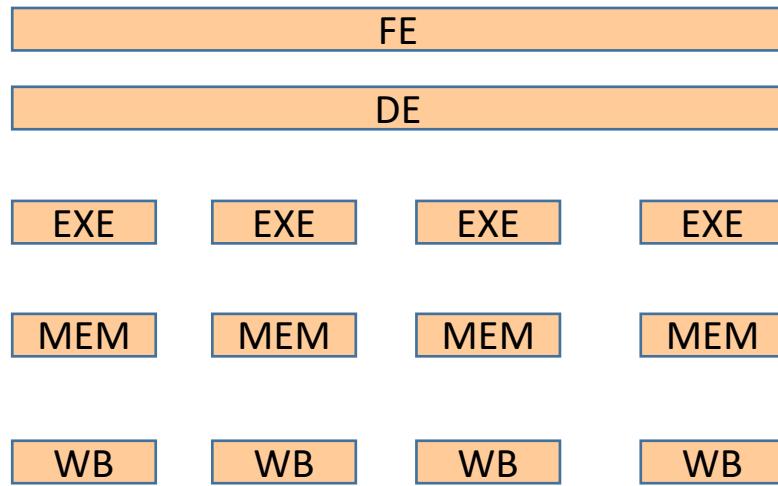
L2:
ret;
```

Example: VectorAdd on GPU

- N=8, 8 Threads, 1 block, warp size = 4
- 1 SM, 4 Cores
- Pipeline:
 - Fetch:
 - One instruction from each warp
 - Round-robin through all warps
 - Execution:
 - In-order execution within warps
 - With proper data forwarding
 - 1 Cycle each stage
- How many warps?



Execution Sequence



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

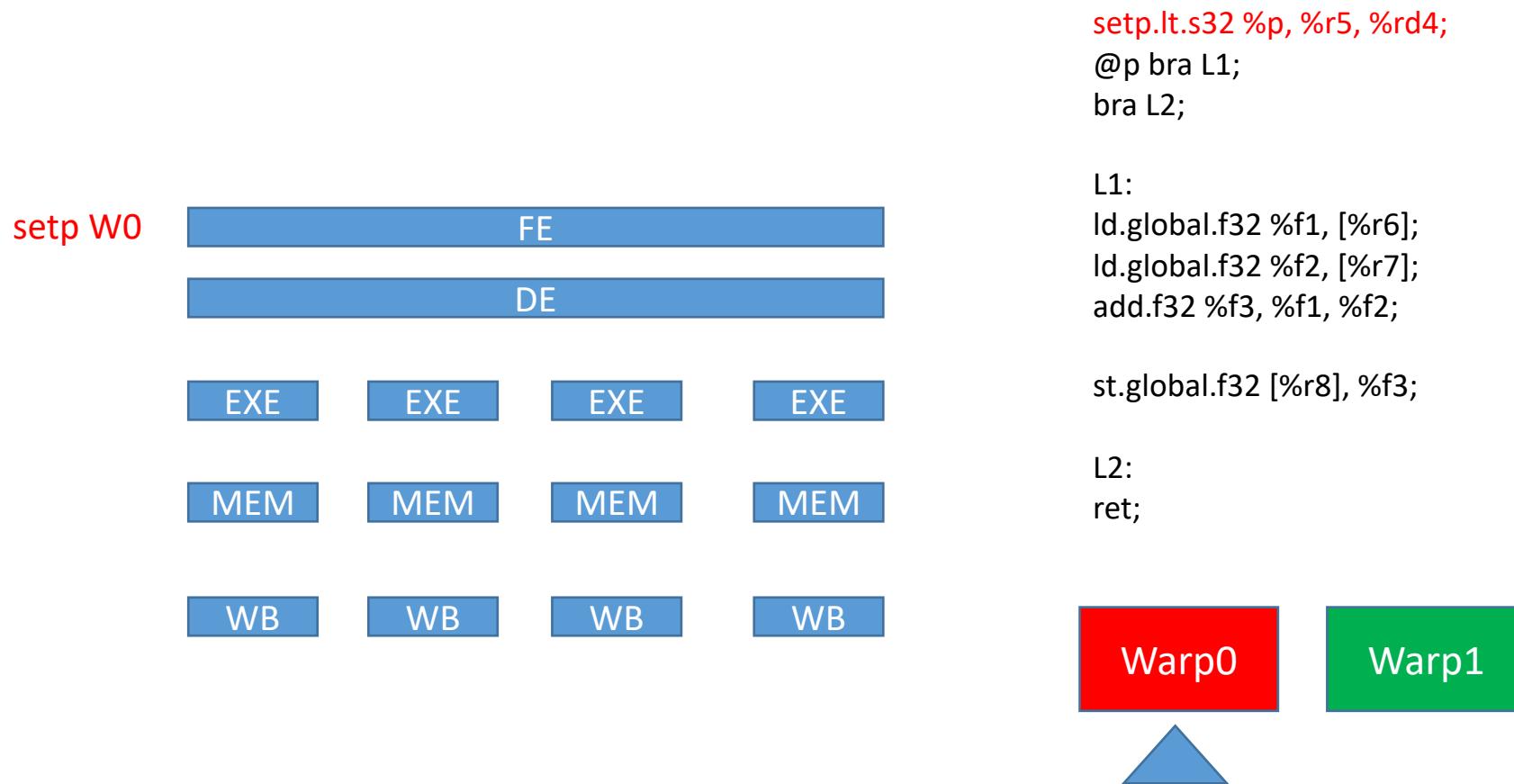
```
L1:  
ld.global.f32 %f1, [%r6];  
ld.global.f32 %f2, [%r7];  
add.f32 %f3, %f1, %f2;
```

```
st.global.f32 [%r8], %f3;
```

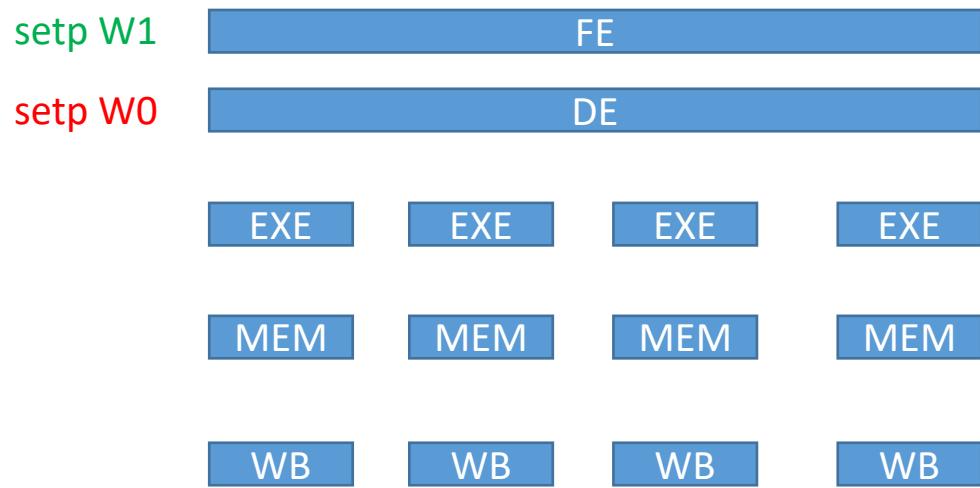
```
L2:  
ret;
```



Execution Sequence (cont.)



Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

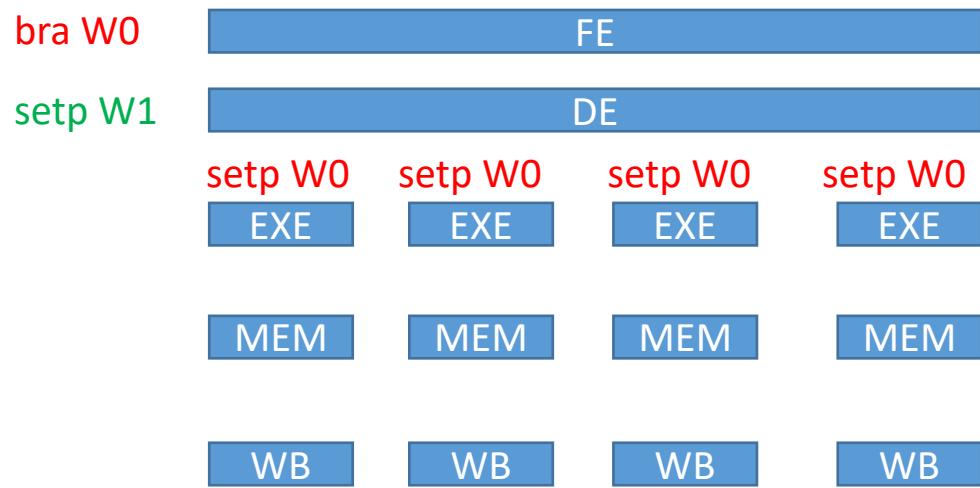
L1:
ld.global.f32 %f1, [%r6];
ld.global.f32 %f2, [%r7];
add.f32 %f3, %f1, %f2;

st.global.f32 [%r8], %f3;

L2:
ret;



Execution Sequence (cont.)

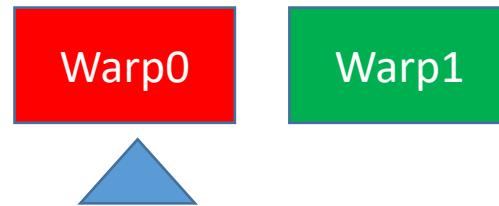


```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

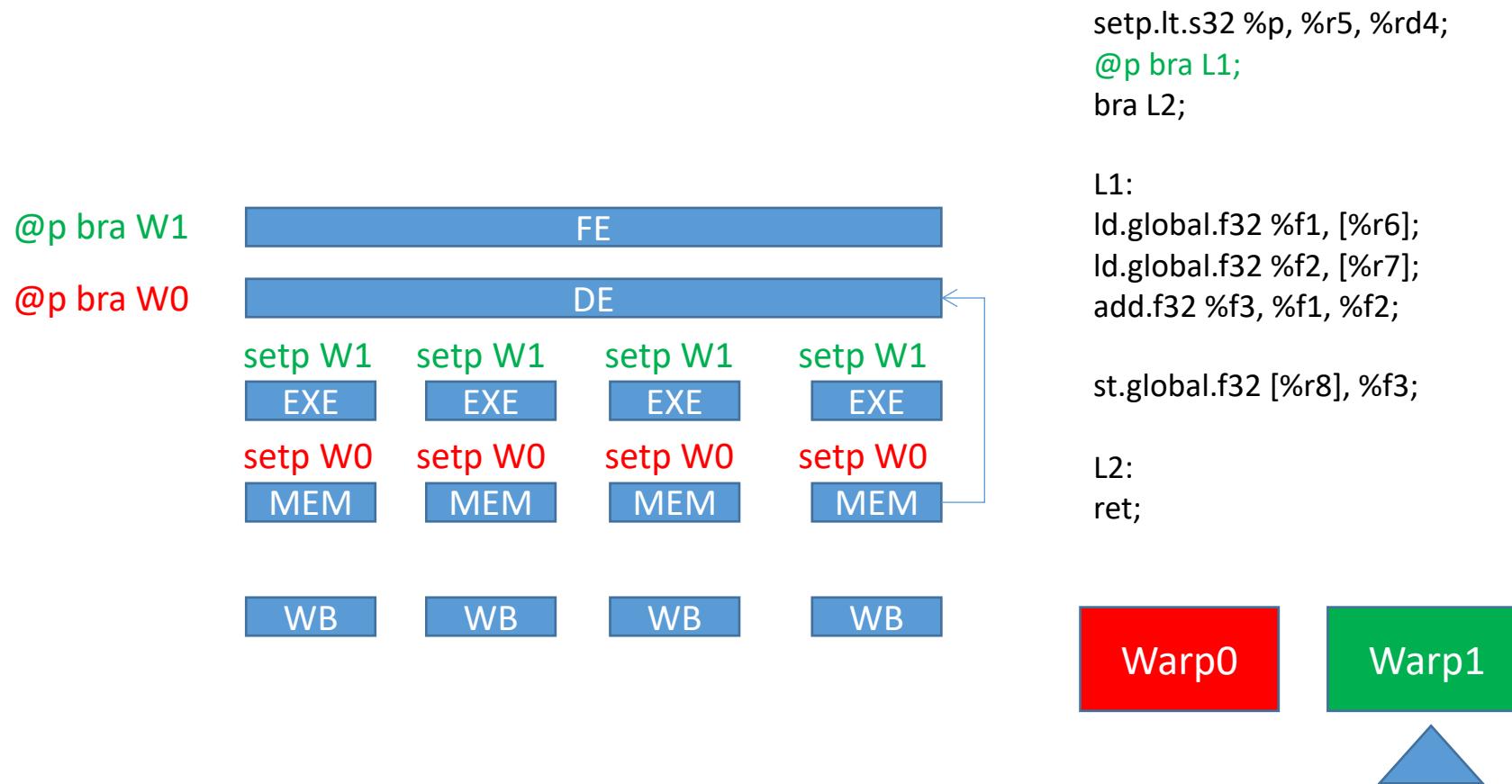
L1:
ld.global.f32 %f1, [%r6];
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add.f32 %f3, %f1, %f2;

st.global.f32 [%r8], %f3;

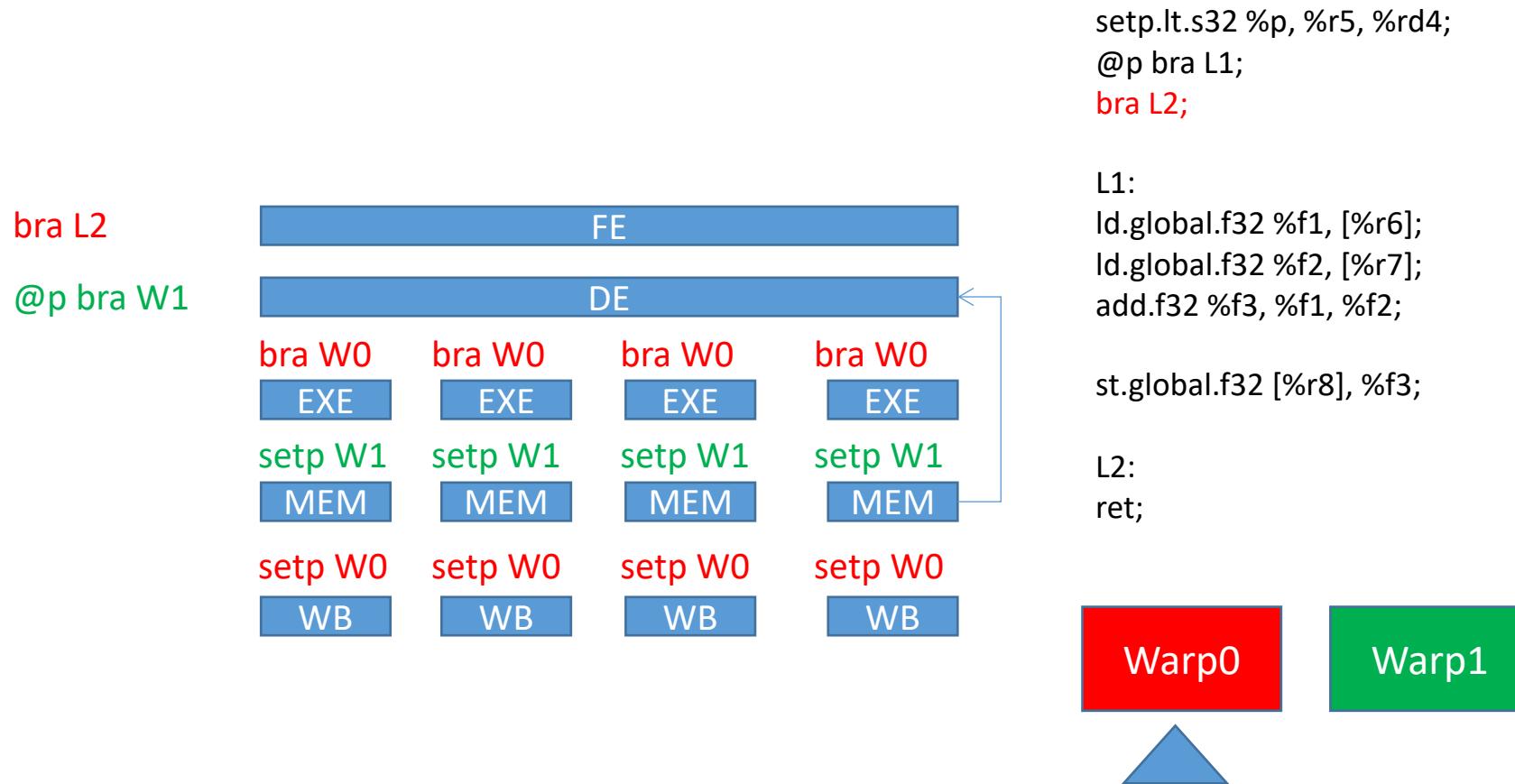
L2:
ret;



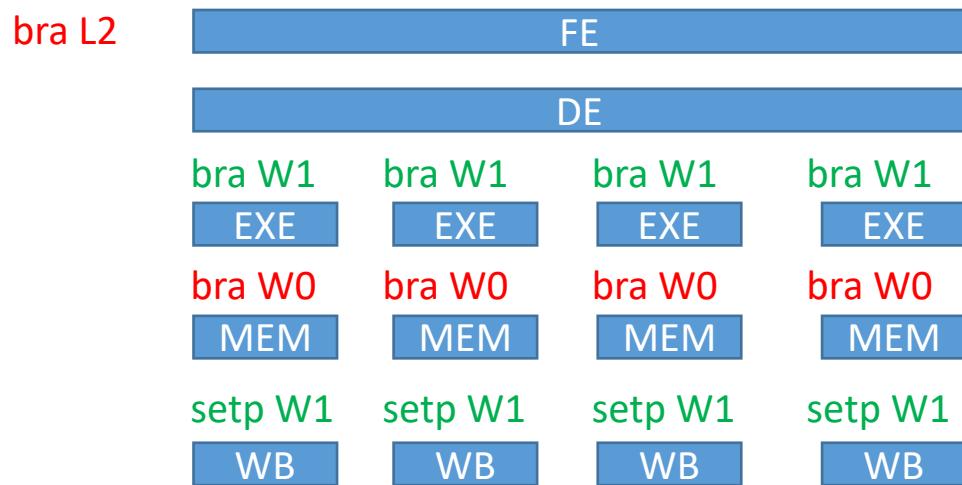
Execution Sequence (cont.)



Execution Sequence (cont.)



Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
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```

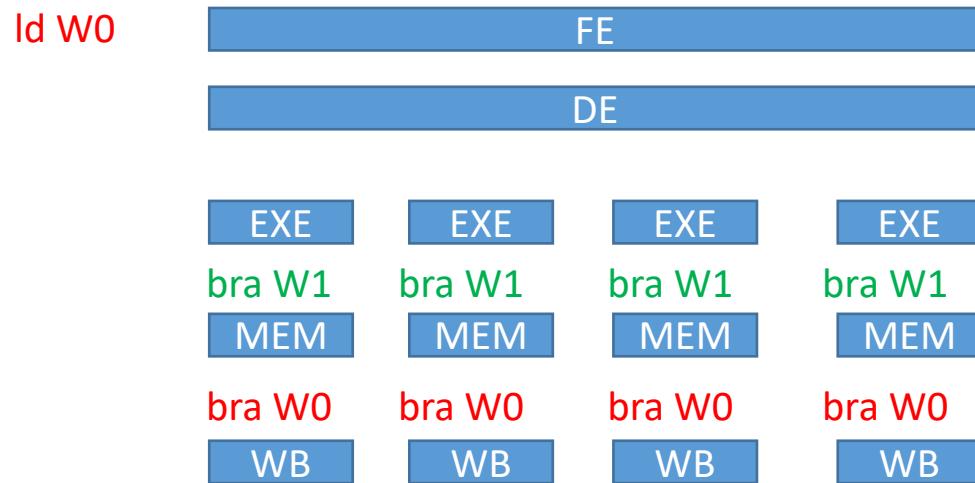
L1:
ld.global.f32 %f1, [%r6];
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add.f32 %f3, %f1, %f2;

st.global.f32 [%r8], %f3;

L2:
ret;



Execution Sequence (cont.)

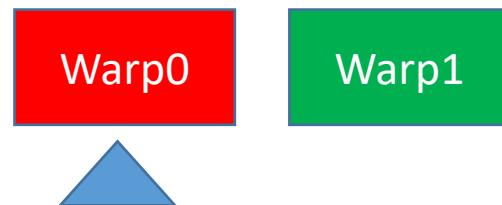


```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

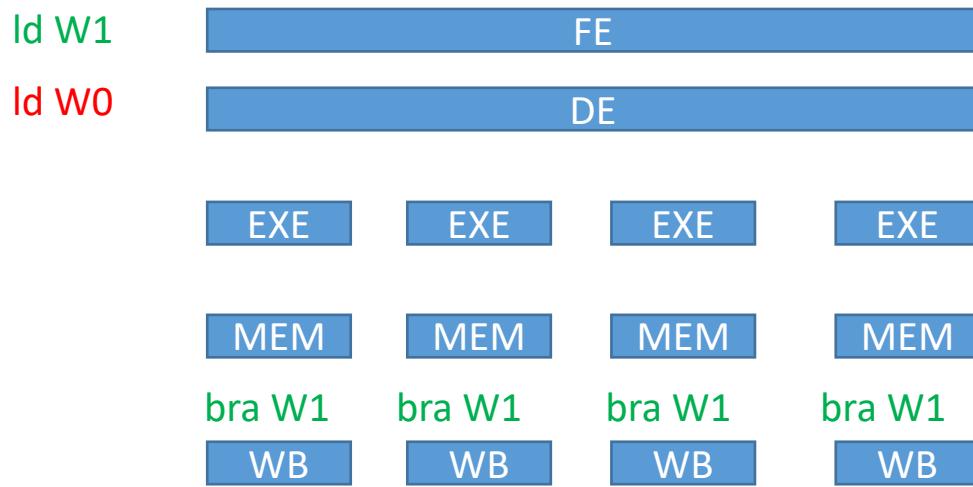
L1:
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Id.global.f32 %f2, [%r7];
add.f32 %f3, %f1, %f2;

```
st.global.f32 [%r8], %f3;
```

L2:
ret;



Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

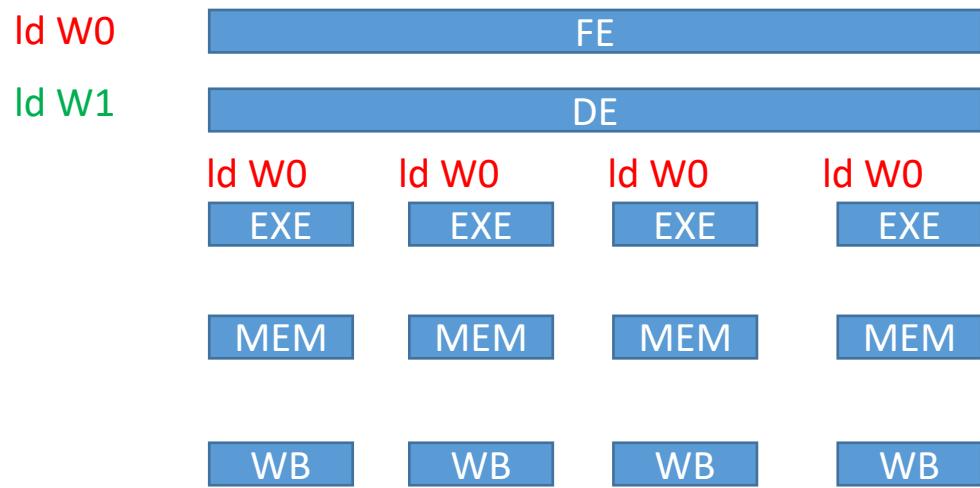
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Id.global.f32 %f2, [%r7];
add.f32 %f3, %f1, %f2;

st.global.f32 [%r8], %f3;

L2:
ret;



Execution Sequence (cont.)

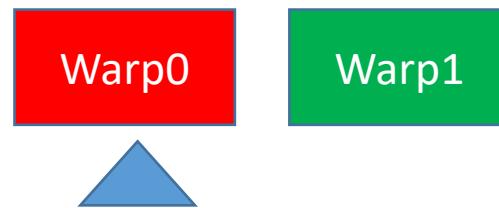


```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

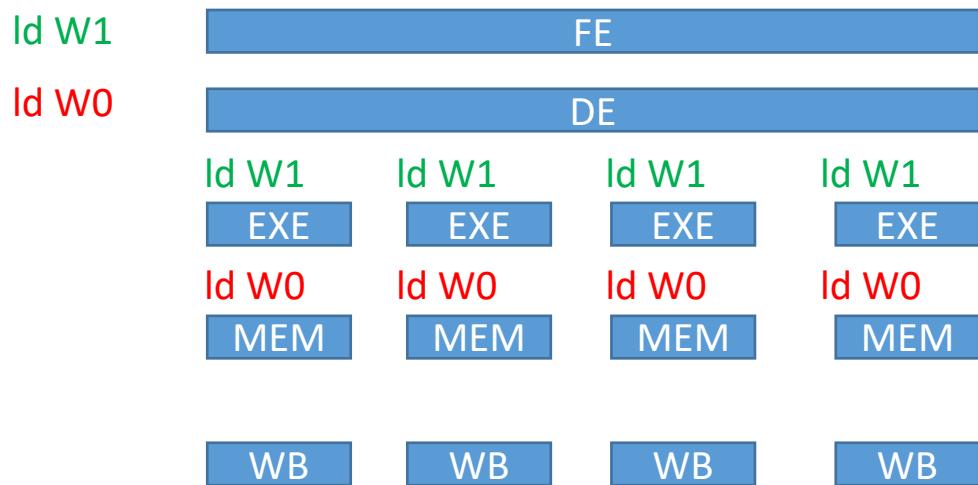
L1:
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ld.global.f32 %f2, [%r7];
add.f32 %f3, %f1, %f2;

st.global.f32 [%r8], %f3;

L2:
ret;



Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
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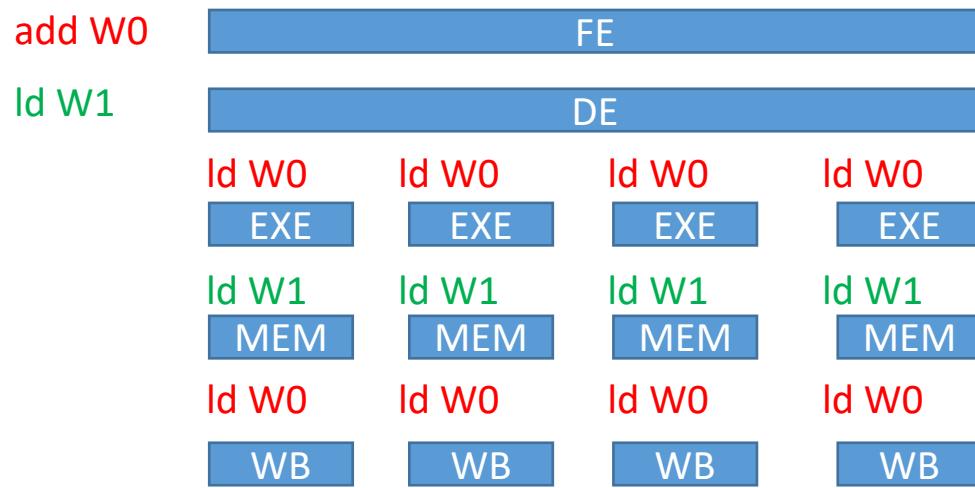
```
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ld.global.f32 %f2, [%r7];  
add.f32 %f3, %f1, %f2;
```

```
st.global.f32 [%r8], %f3;
```

```
L2:  
ret;
```



Execution Sequence (cont.)

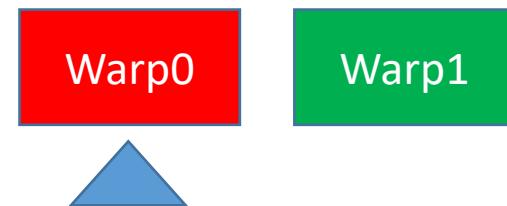


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setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

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`add.f32 %f3, %f1, %f2;`

`st.global.f32 [%r8], %f3;`

L2:
`ret;`



Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
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L1:  
ld.global.f32 %f1, [%r6];  
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add.f32 %f3, %f1, %f2;
```

```
st.global.f32 [%r8], %f3;
```

```
L2:  
ret;
```



Execution Sequence (cont.)

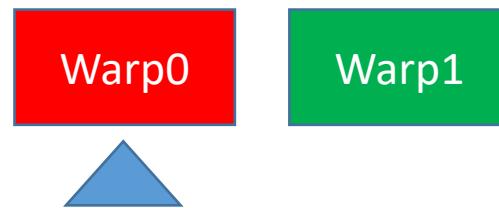


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setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

L1:
ld.global.f32 %f1, [%r6];
ld.global.f32 %f2, [%r7];
add.f32 %f3, %f1, %f2;

st.global.f32 [%r8], %f3;

L2:
ret;



Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
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L1:  
ld.global.f32 %f1, [%r6];  
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add.f32 %f3, %f1, %f2;
```

```
st.global.f32 [%r8], %f3;
```

```
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ret;
```



Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

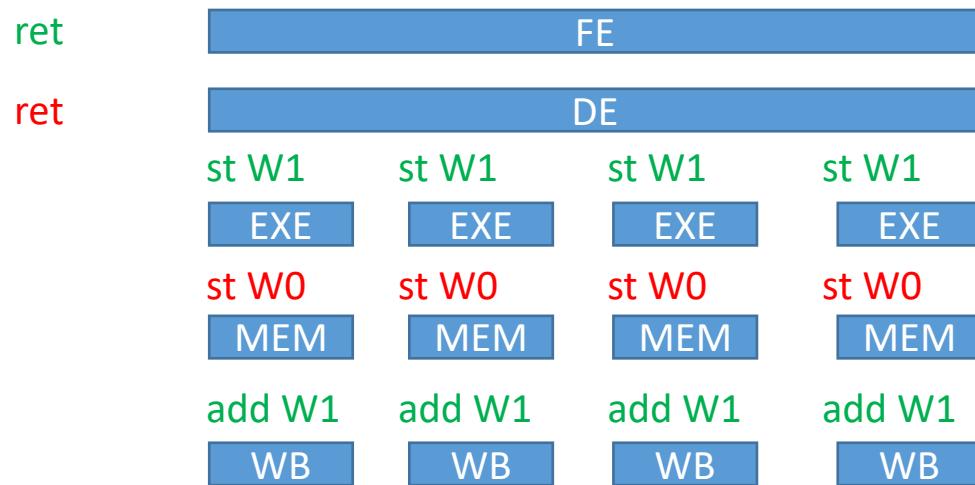
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ld.global.f32 %f2, [%r7];  
add.f32 %f3, %f1, %f2;
```

```
st.global.f32 [%r8], %f3;
```

```
L2:  
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```



Execution Sequence (cont.)

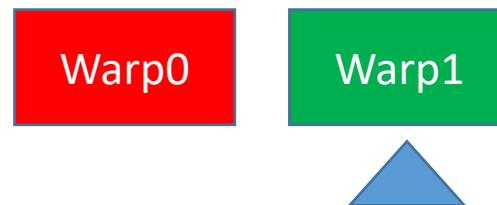


```
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```

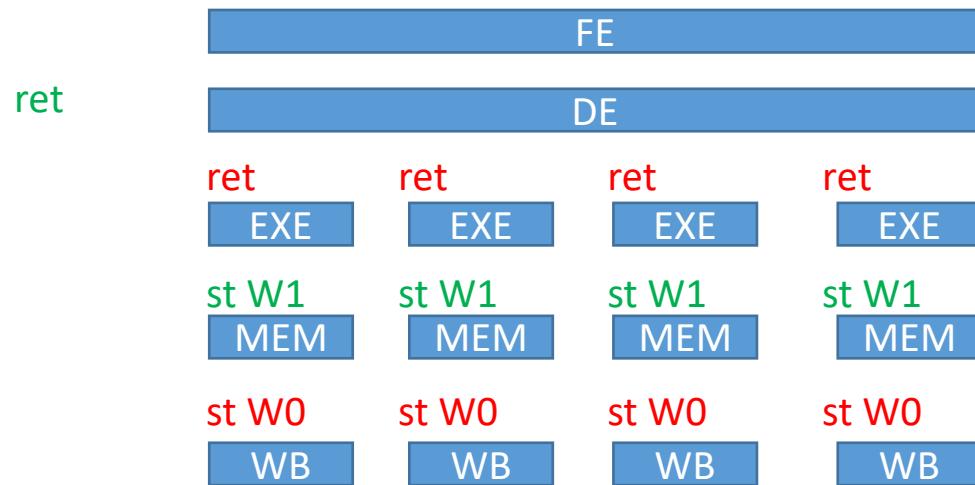
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L2:
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Execution Sequence (cont.)



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setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
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ld.global.f32 %f1, [%r6];  
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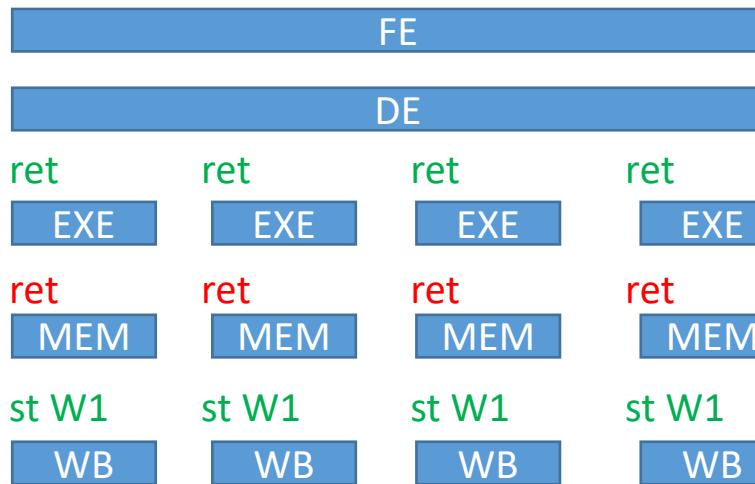
```
st.global.f32 [%r8], %f3;
```

L2:

```
ret;
```



Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
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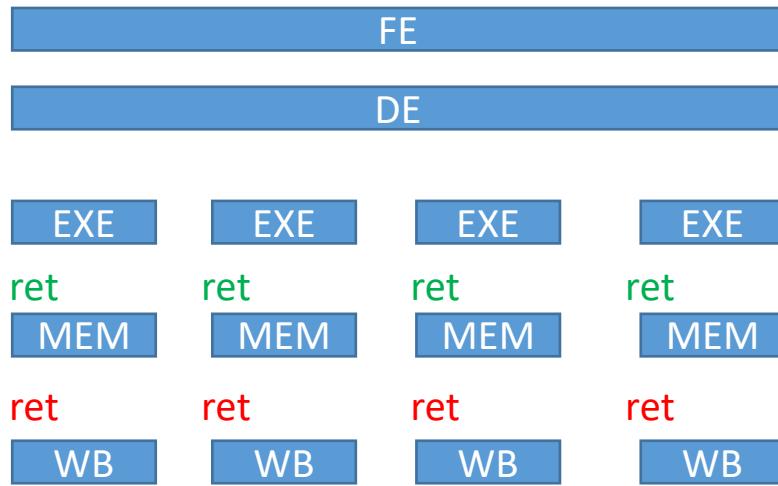
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Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
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```

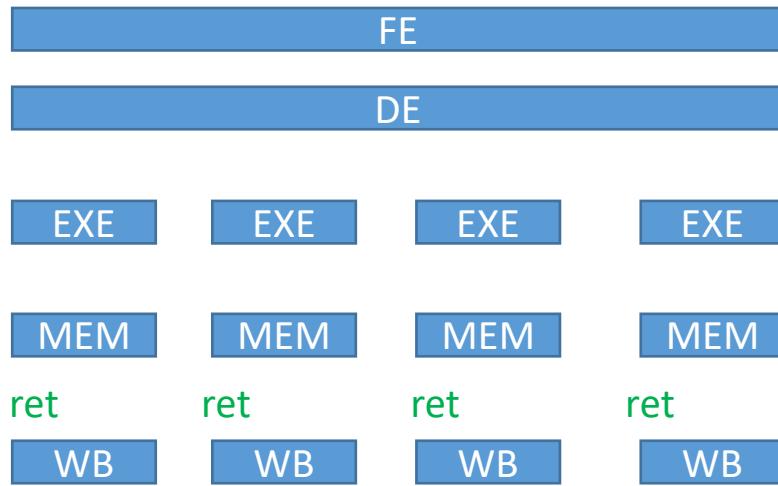
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ld.global.f32 %f2, [%r7];
add.f32 %f3, %f1, %f2;

```
st.global.f32 [%r8], %f3;
```

L2:
ret;

Warp0 Warp1

Execution Sequence (cont.)



```
setp.lt.s32 %p, %r5, %rd4;  
@p bra L1;  
bra L2;
```

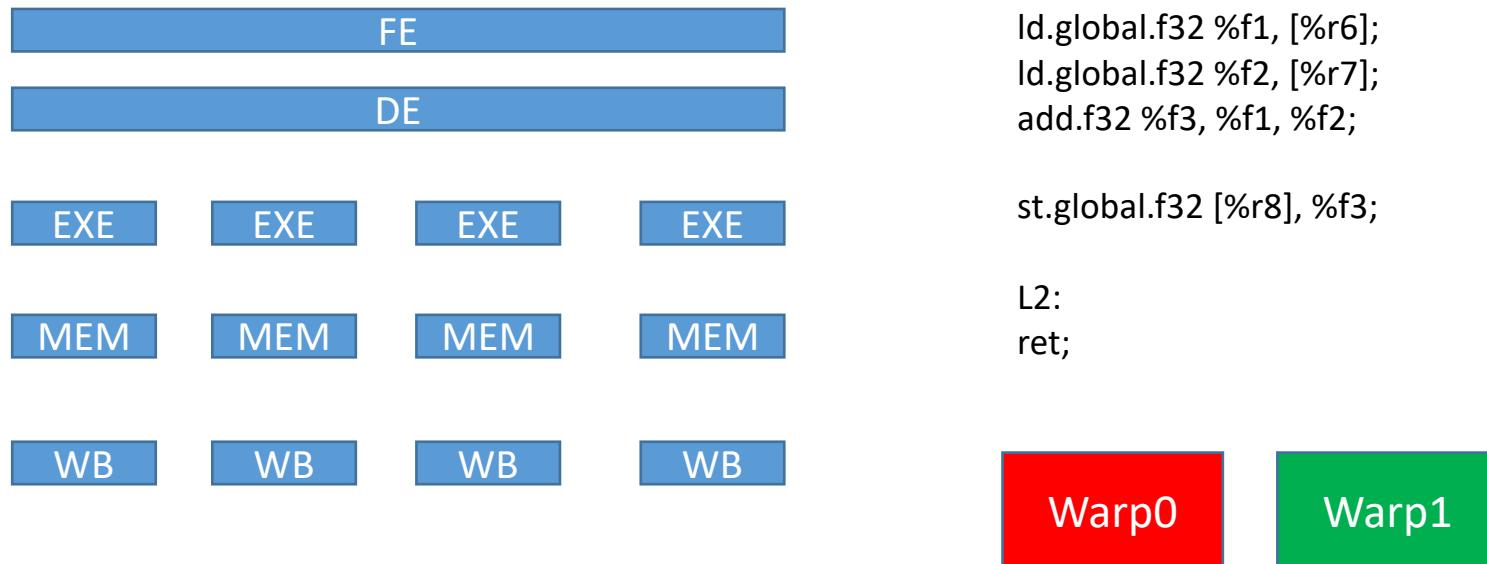
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L1:  
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add.f32 %f3, %f1, %f2;
```

```
st.global.f32 [%r8], %f3;
```

```
L2:  
ret;
```

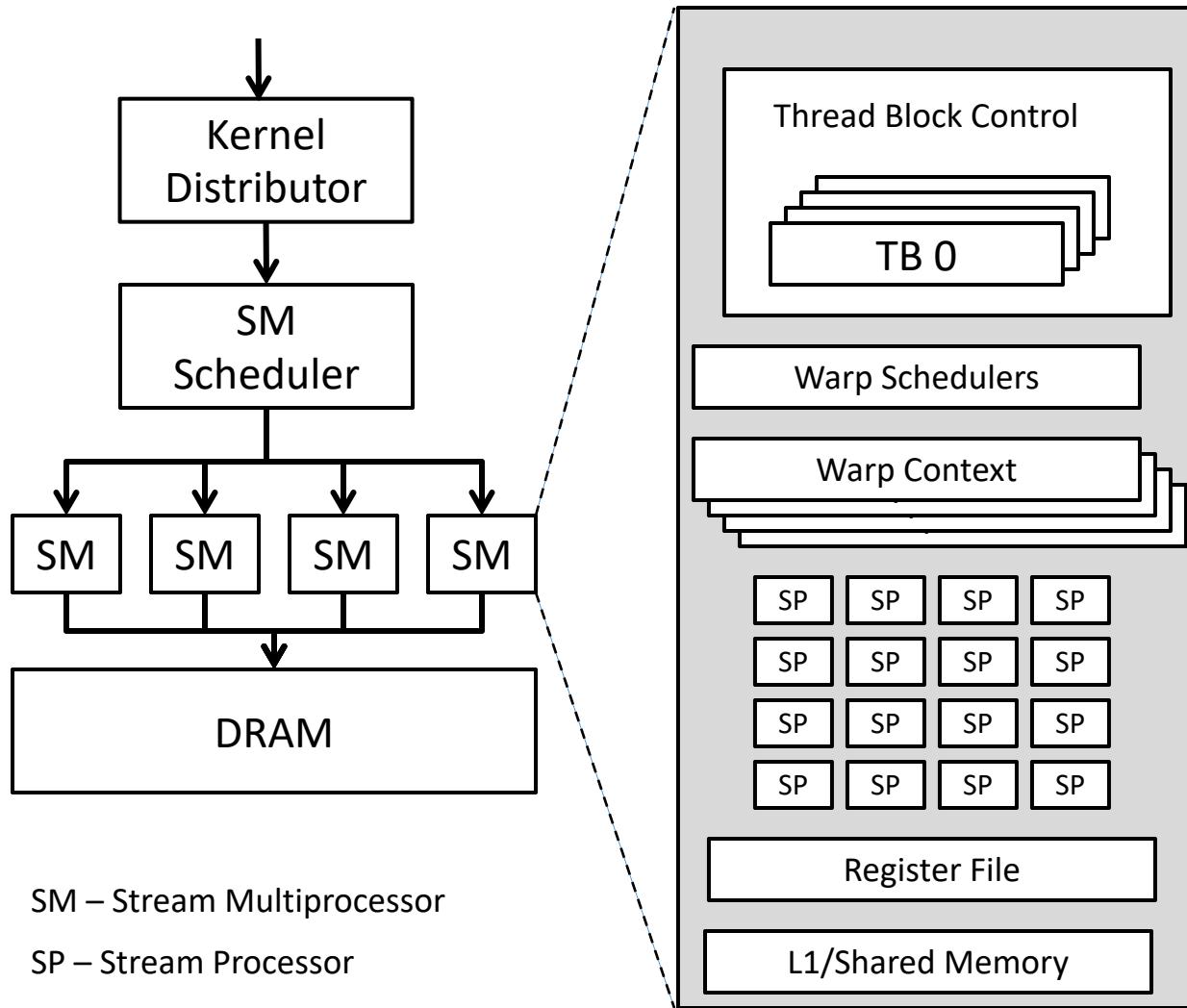


Execution Sequence (cont.)

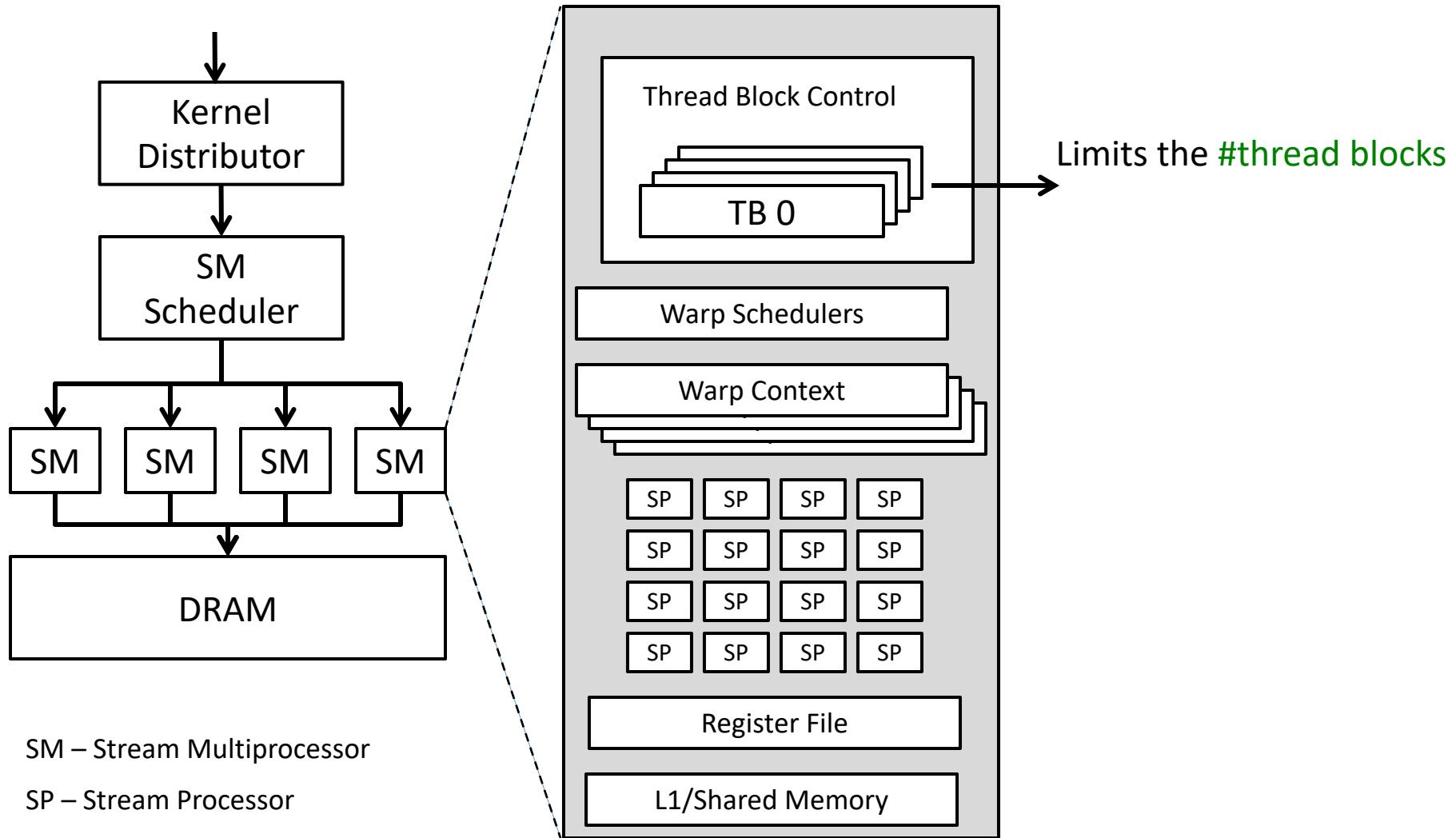


Note: Idealized execution without memory or special function delays

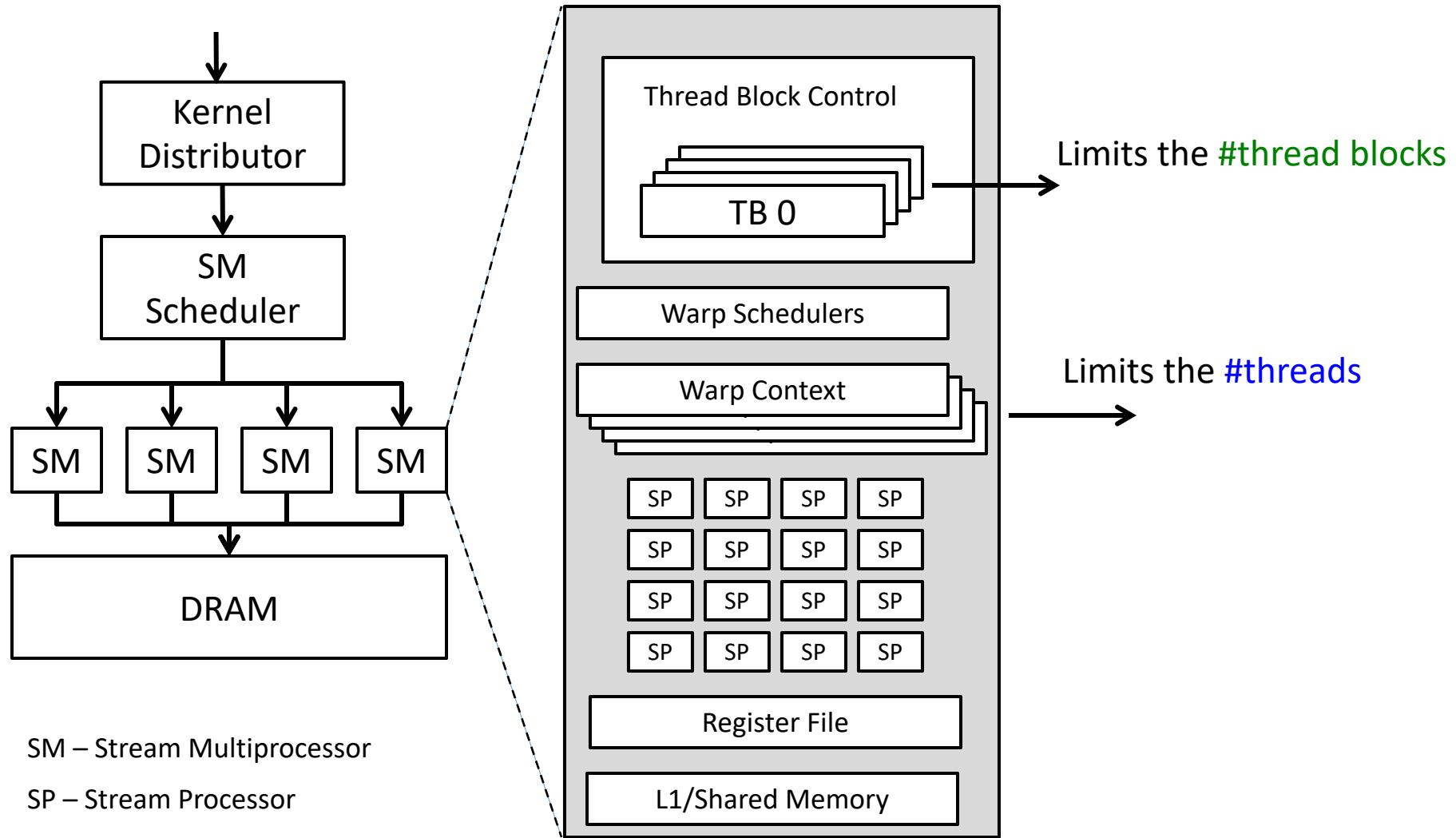
Resource Limits



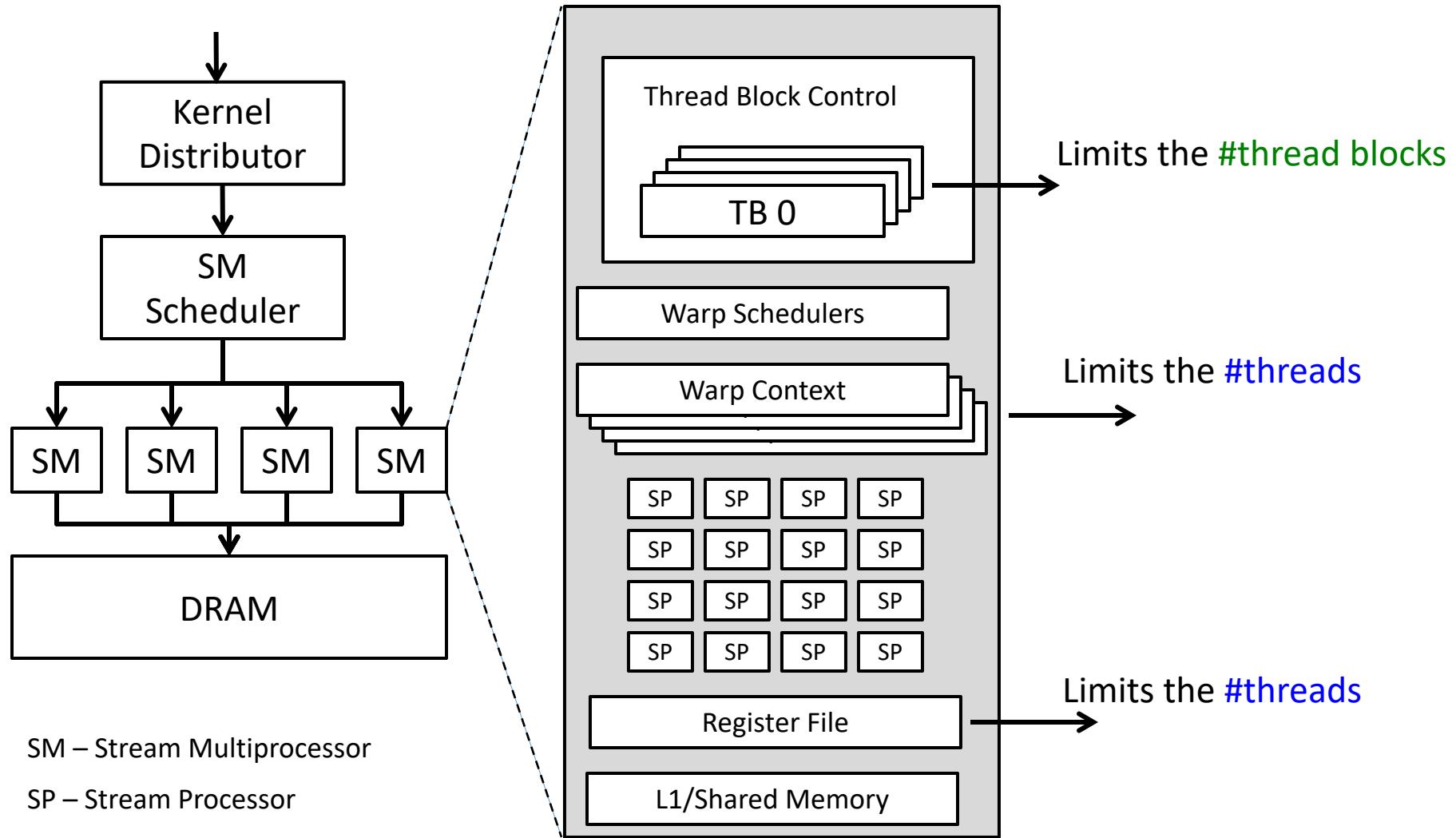
Resource Limits



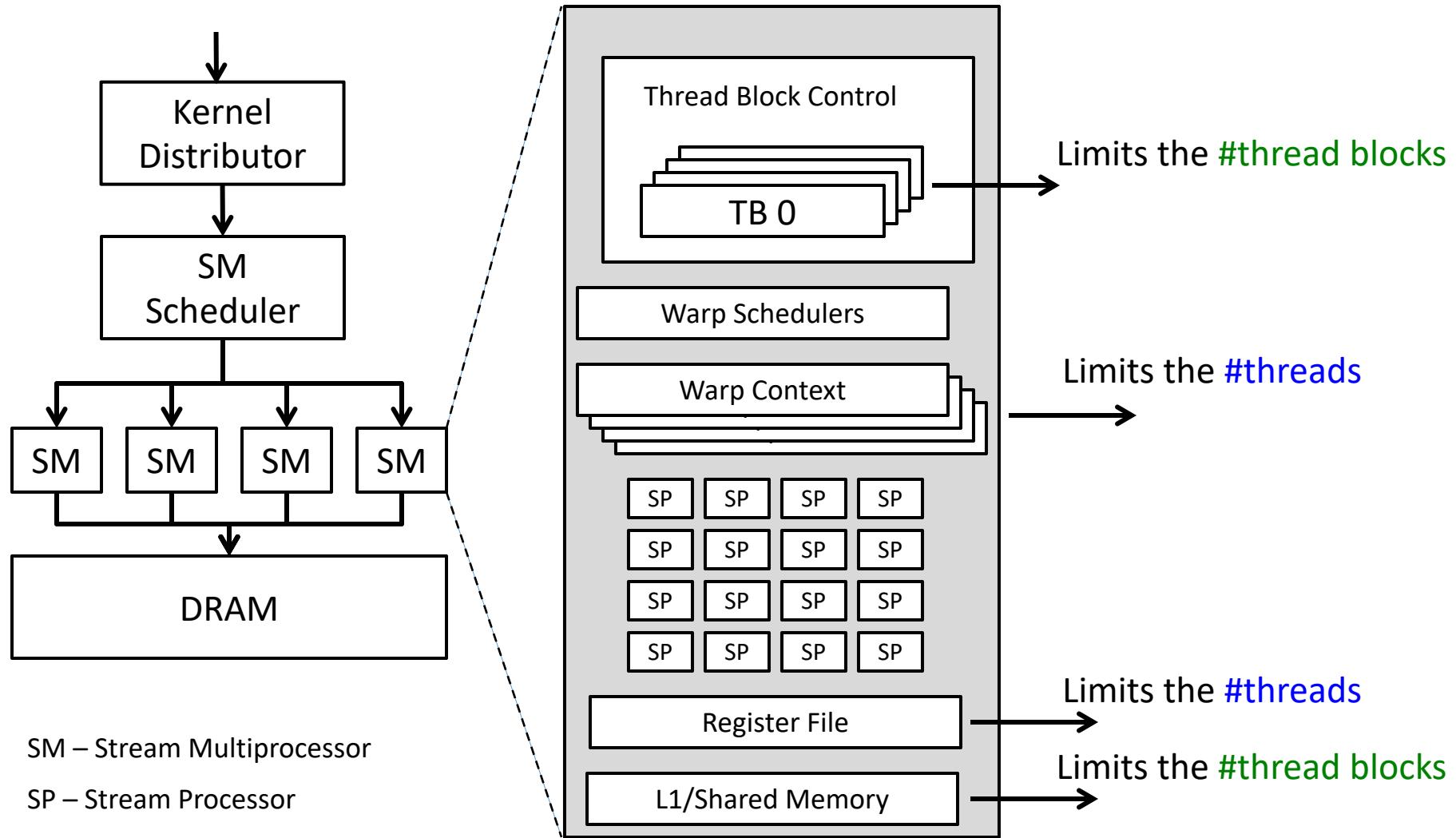
Resource Limits



Resource Limits



Resource Limits



Performance Metrics: *Occupancy*

- Performance implications of programming model properties
 - Warps
 - Thread blocks
 - Register file usage
- Occupancy captures
 - which resources can be dynamically shared
 - how to reason about resource demands of a CUDA kernel
 - Enable device-specific online tuning of kernel parameters

CUDA Occupancy

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 - Measure of how well max capacity is utilized

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 - Shared memory/thread block
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CUDA Occupancy

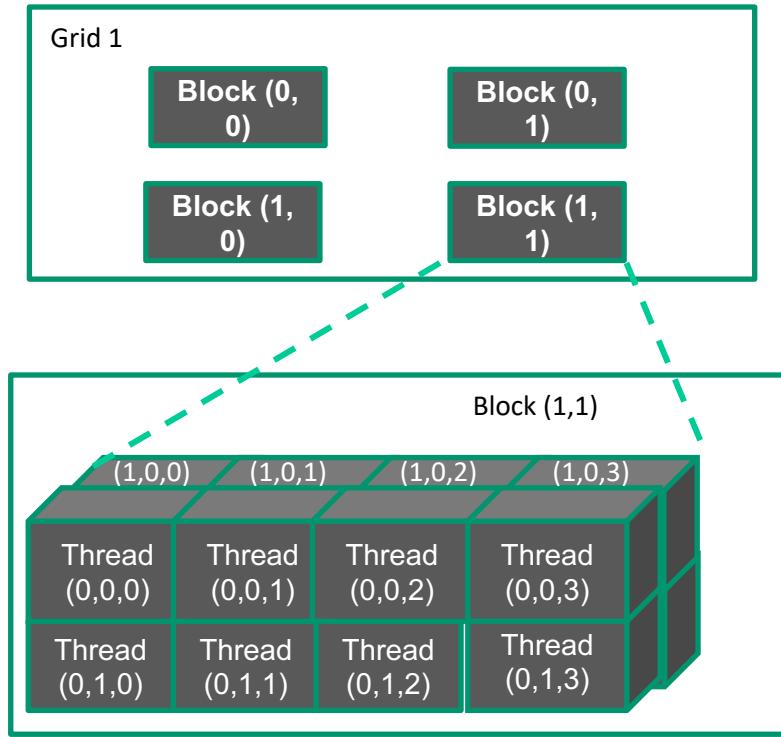
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 - Measure of how well max capacity is utilized
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 - Memory bandwidth
 - Scheduler slots

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 - Registers/thread
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- Limits on the denominator:
 - Memory bandwidth
 - Scheduler slots

What is the performance impact of varying kernel resource demands?

Programming Model Attributes



- #SMs
- Max Threads/Block
- Max Threads/Dim
- Warp size

To maximize ***occupancy***

- Know micro-architecture of target processor
- Exercise kernel configuration parameters

Impact of Thread Block Size

Impact of Thread Block Size

- Consider Fermi with 1536 threads/SM
 - With 512 threads/block, can only up to 3 thread blocks executing at an instant
 - With 128 threads/block → 12 thread blocks per SM
 - Consider how many instructions can be in flight?

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- Consider limit of 8 thread blocks/SM?
 - Only 1024 active threads at a time
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- Consider limit of 8 thread blocks/SM?
 - Only 1024 active threads at a time
 - Occupancy = 0.666
- To maximize utilization, thread block size should balance
 - demand for thread blocks vs.
 - thread slots

Impact of #Registers Per Thread

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- Assume 10 registers/thread and a thread block size of 256

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- A TB requires 2560 registers for a maximum of 6 thread blocks per SM
 - Uses all 1536 thread slots

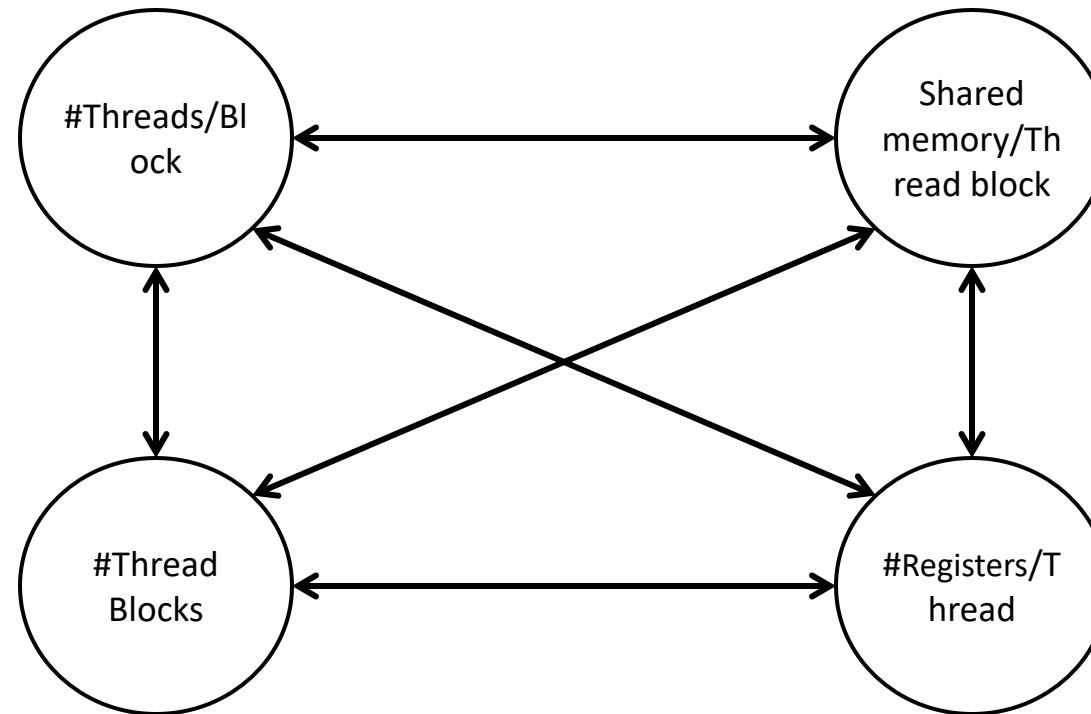
Impact of #Registers Per Thread

- Assume 10 registers/thread and a thread block size of 256
- Number of registers per SM = 16K
- A TB requires 2560 registers for a maximum of 6 thread blocks per SM
 - Uses all 1536 thread slots
- What is the impact of increasing number of registers by 2?
 - Granularity of management is a thread block!
 - Loss of concurrency of 256 threads!

Impact of Shared Memory

- Shared memory is allocated per thread block
 - Can limit the number of thread blocks executing concurrently per SM
- `gridDim` and `blockDim` parameters impact demand for
 - shared memory
 - number of thread slots
 - number of thread block slots

Balance



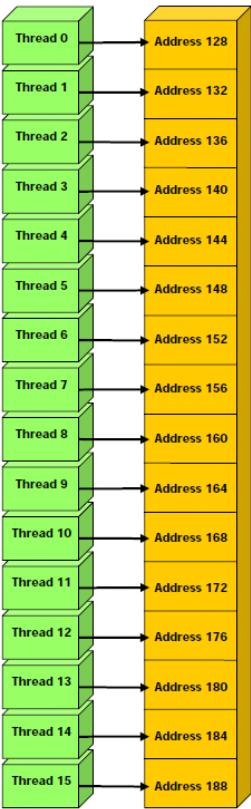
- Navigate the tradeoffs
 - ❖ maximize core utilization and memory bandwidth utilization
 - ❖ Device-specific
- **Goal:** Increase occupancy until one or the other is saturated

Parallel Memory Accesses

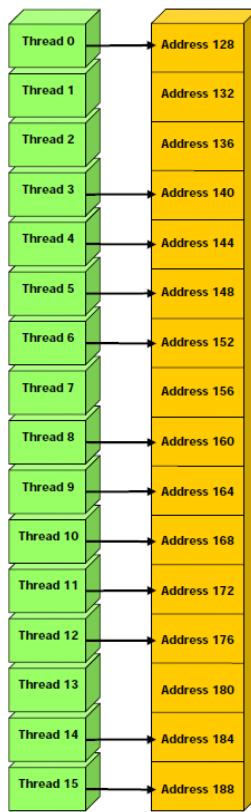
- **Coalesced main memory access (16/32x faster)**
 - Under some conditions, HW combines multiple (half) warp memory accesses into a single coalesced access
 - CC 1.3: 64-byte aligned 64-byte line (any permutation)
 - CC 2.x+3.0: 128-byte aligned 128-byte line (cached)
- **Bank-conflict-free shared memory access (16/32)**
 - No superword alignment or contiguity requirements
 - CC 1.3: 16 different banks per half warp or same word
 - CC 2.x+3.0 : 32 different banks + 1-word broadcast each

Coalesced Main Memory Accesses

single coalesced

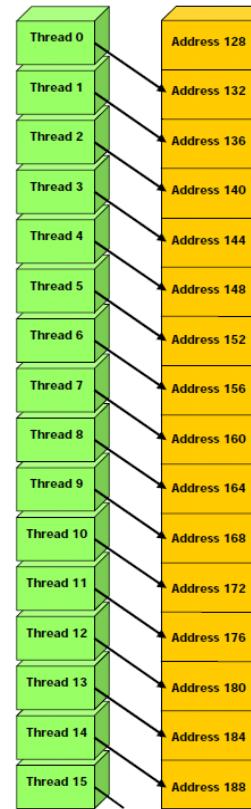
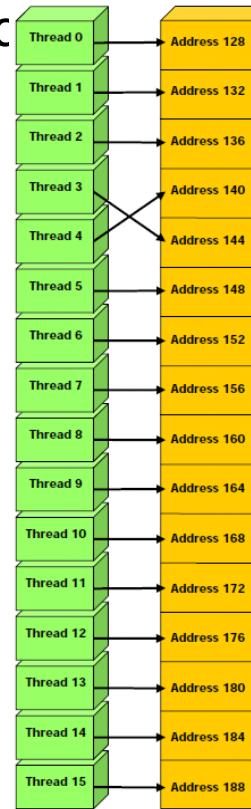


NVIDIA



NVIDIA

and two coalesced



Device Properties

```
cudaError_t cudaGetDeviceProperties ( struct cudaDeviceProp * prop,  
                                     int device  
                                     )
```

Returns in *prop the properties of device dev. The **cudaDeviceProp** structure is defined as:

```
struct cudaDeviceProp {  
    char name[256];  
    size_t totalGlobalMem;  
    size_t sharedMemPerBlock;  
    int regsPerBlock;  
    int warpSize;  
    size_t memPitch;  
    int maxThreadsPerBlock;  
    int maxThreadsDim[3];  
    int maxGridSize[3];  
    int clockRate;  
    size_t totalConstMem;  
    int major;  
    int minor;  
    size_t textureAlignment;  
    size_t texturePitchAlignment;  
    int deviceOverlap;  
    int multiProcessorCount;
```

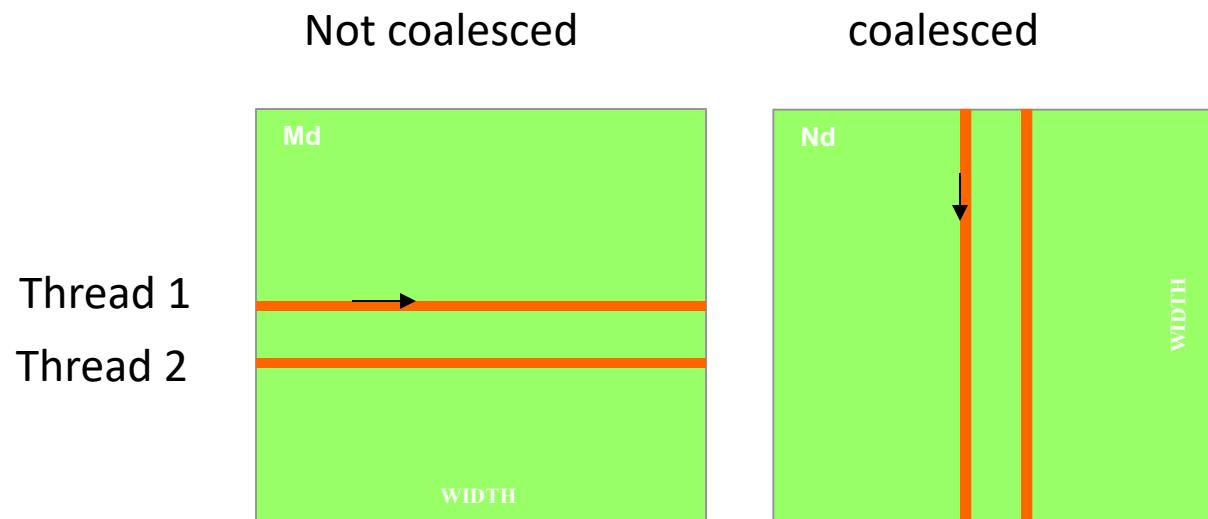
CUDA Variable Type Qualifiers

Variable declaration	Memory	Scope	Lifetime
<code>__device__ __local__ int LocalVar;</code>	local	thread	thread
<code>__device__ __shared__ int SharedVar;</code>	shared	block	block
<code>__device__ int GlobalVar;</code>	global	grid	application
<code>__device__ __constant__ int ConstantVar;</code>	constant	grid	application

- `__device__` is optional when used with `__local__`, `__shared__`, or `__constant__`
- Automatic variables without any qualifier reside in a register
 - Except arrays that reside in local memory

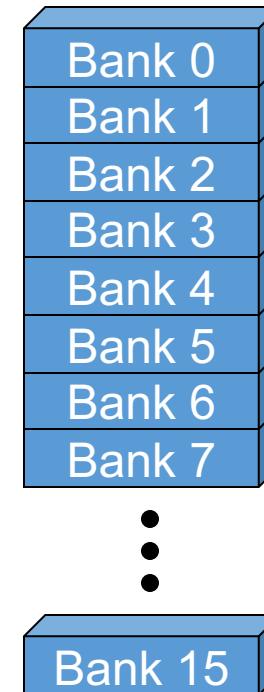
Memory Coalescing

- When accessing global memory, peak performance utilization occurs when all threads in a half warp access continuous memory locations.



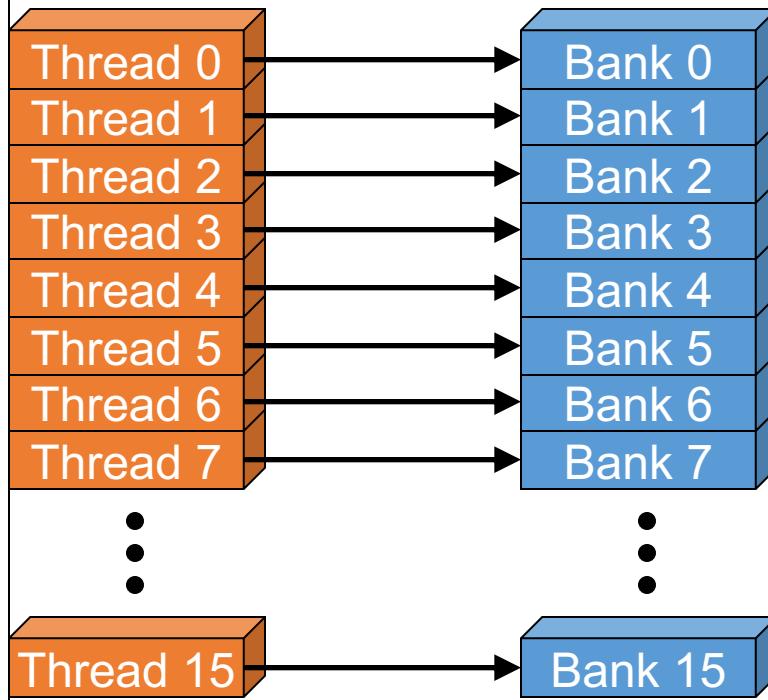
Parallel Memory Architecture

- In a parallel machine, many threads access memory
 - Therefore, memory is divided into **banks**
 - Essential to achieve high bandwidth
- Each bank can service one address per cycle
 - A memory can service as many simultaneous accesses as it has banks
- Multiple simultaneous accesses to a bank result in a **bank conflict**
 - Conflicting accesses are serialized

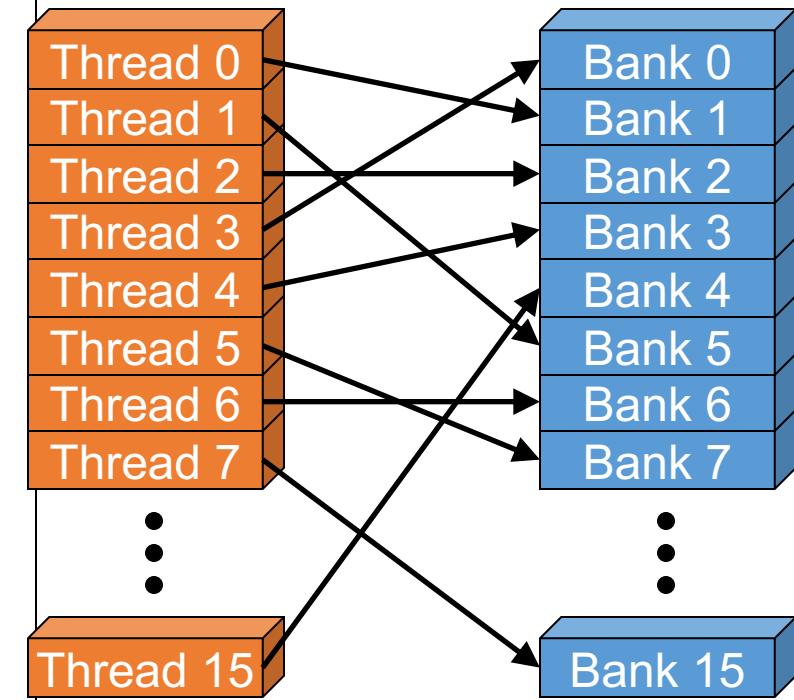


Bank Addressing Examples

- No Bank Conflicts
 - Linear addressing
stride == 1

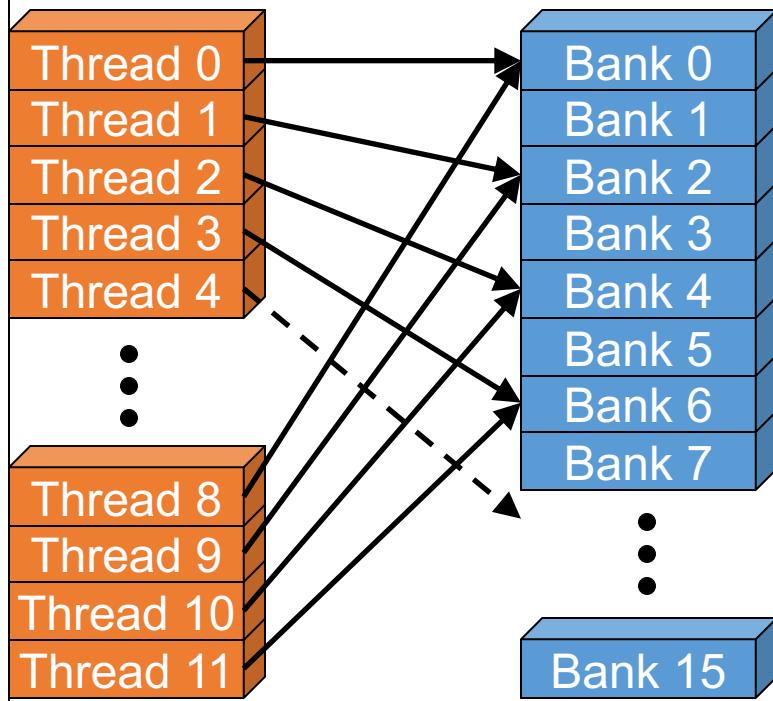


- No Bank Conflicts
 - Random 1:1 Permutation

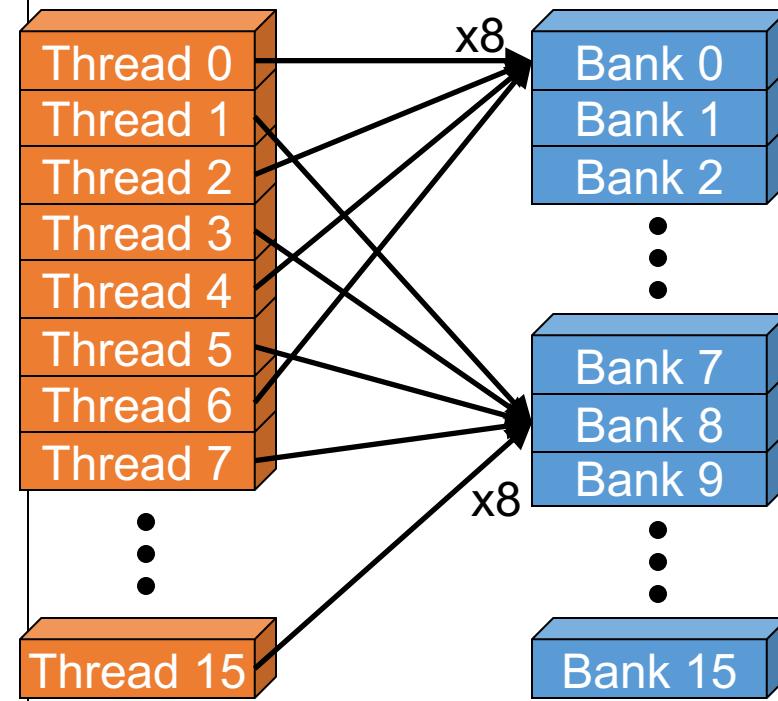


Bank Addressing Examples

- 2-way Bank Conflicts
 - Linear addressing
stride == 2



- 8-way Bank Conflicts
 - Linear addressing
stride == 8



How addresses map to banks on G80

- Each bank has a bandwidth of 32 bits per clock cycle
- Successive 32-bit words are assigned to successive banks
- G80 has 16 banks
 - So bank = address % 16
 - Same as the size of a half-warp
 - No bank conflicts between different half-warps, only within a single half-warp

Shared memory bank conflicts

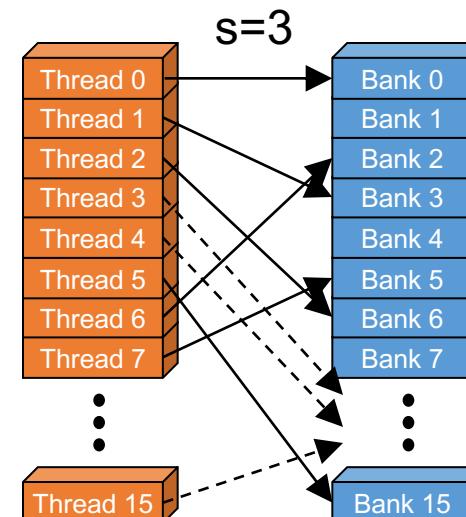
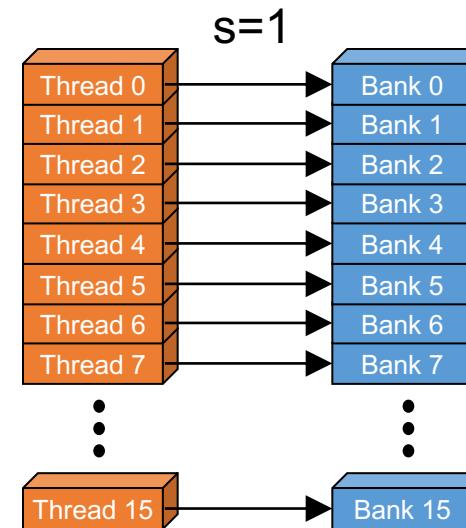
- Shared memory is as fast as registers if there are no bank conflicts
- The fast case:
 - If all threads of a half-warp access different banks, there is no bank conflict
 - If all threads of a half-warp access the identical address, there is no bank conflict (broadcast)
- The slow case:
 - Bank Conflict: multiple threads in the same half-warp access the same bank
 - Must serialize the accesses
 - Cost = max # of simultaneous accesses to a single bank

Linear Addressing

- Given:

```
__shared__ float shared[256];  
float foo =  
    shared[baseIndex + s *  
        threadIdx.x];
```

- This is only bank-conflict-free if s shares no common factors with the number of banks
 - 16 on G80, so s must be odd



Advanced topics: Prefix-Sum

- in: 3 1 7 0 4 1 6 3
- out: 0 3 4 11 11 14 16 22

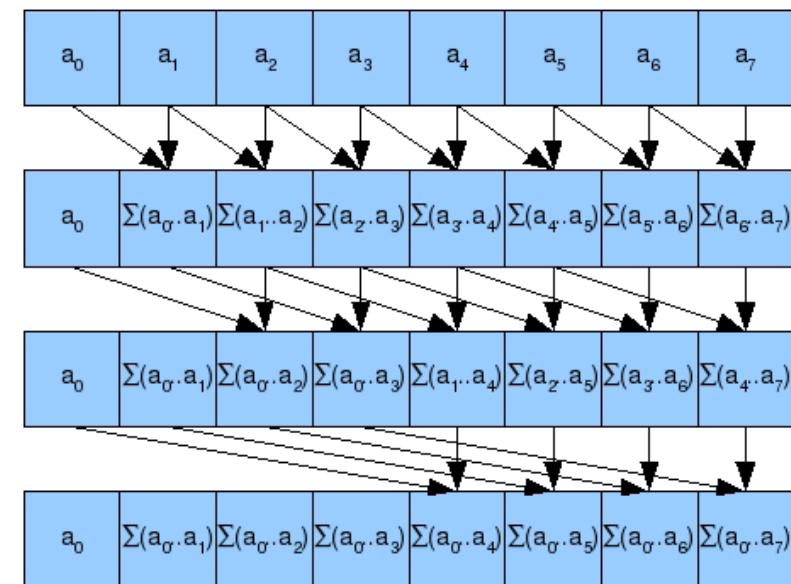
Trivial Sequential Implementation

```
void scan(int* in, int* out, int n)
{
    out[0] = 0;
    for (int i = 1; i < n; i++)
        out[i] = in[i-1] + out[i-1];
}
```

Parallel Scan

```
for(d = 1; d < log2n; d++)  
    for all k in parallel  
        if( k >= 2d )  
            x[out][k] = x[in][k - 2d-1] + x[in][k]  
        else  
            x[out][k] = x[in][k]
```

Complexity $O(n \log_2 n)$



A work efficient parallel scan

- Goal is a parallel scan that is $O(n)$ instead of $O(n \log_2 n)$
 - Solution:
 - Balanced Trees: Build a binary tree, sweep it to and from the root.
 - Binary tree with n leaves has
 - $d = \log_2 n$ levels,
 - each level d has 2^d nodes
- * One add is performed per node → $O(n)$ add on a single traversal of the tree.

$O(n)$ unsegmented scan

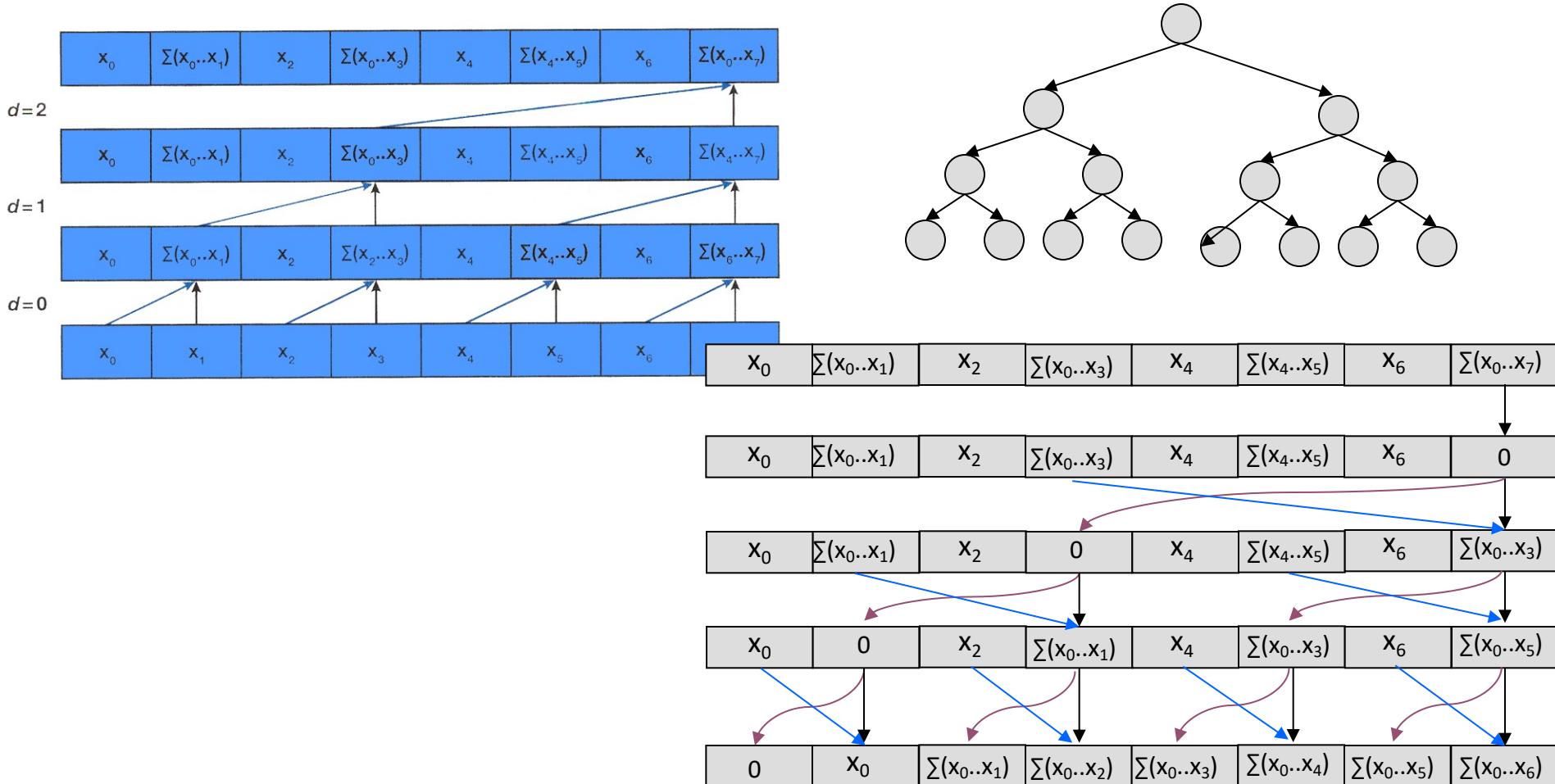
- Reduce/Up-Sweep

```
for(d = 0; d < log2n-1; d++)  
    for all k=0; k < n-1; k+=2d+1 in parallel  
        x[k+2d+1-1] = x[k+2d-1] + x[k+2d+1-1]
```

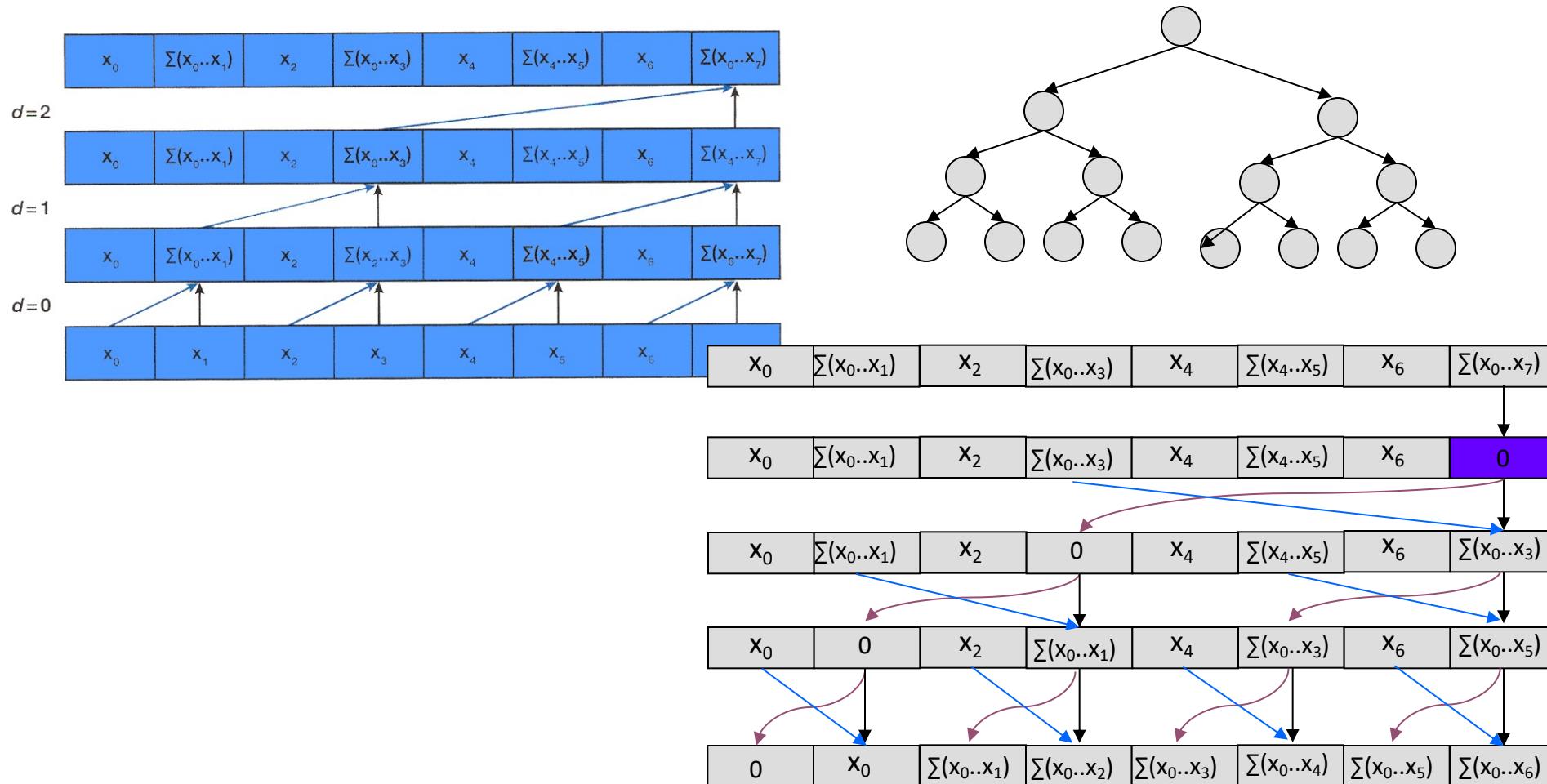
- Down-Sweep

```
x[n-1] = 0;  
for(d = log2n - 1; d >=0; d--)  
    for all k = 0; k < n-1; k += 2d+1 in parallel  
        t = x[k + 2d - 1]  
        x[k + 2d - 1] = x[k + 2d+1 -1]  
        x[k + 2d+1 - 1] = t + x[k + 2d+1 - 1]
```

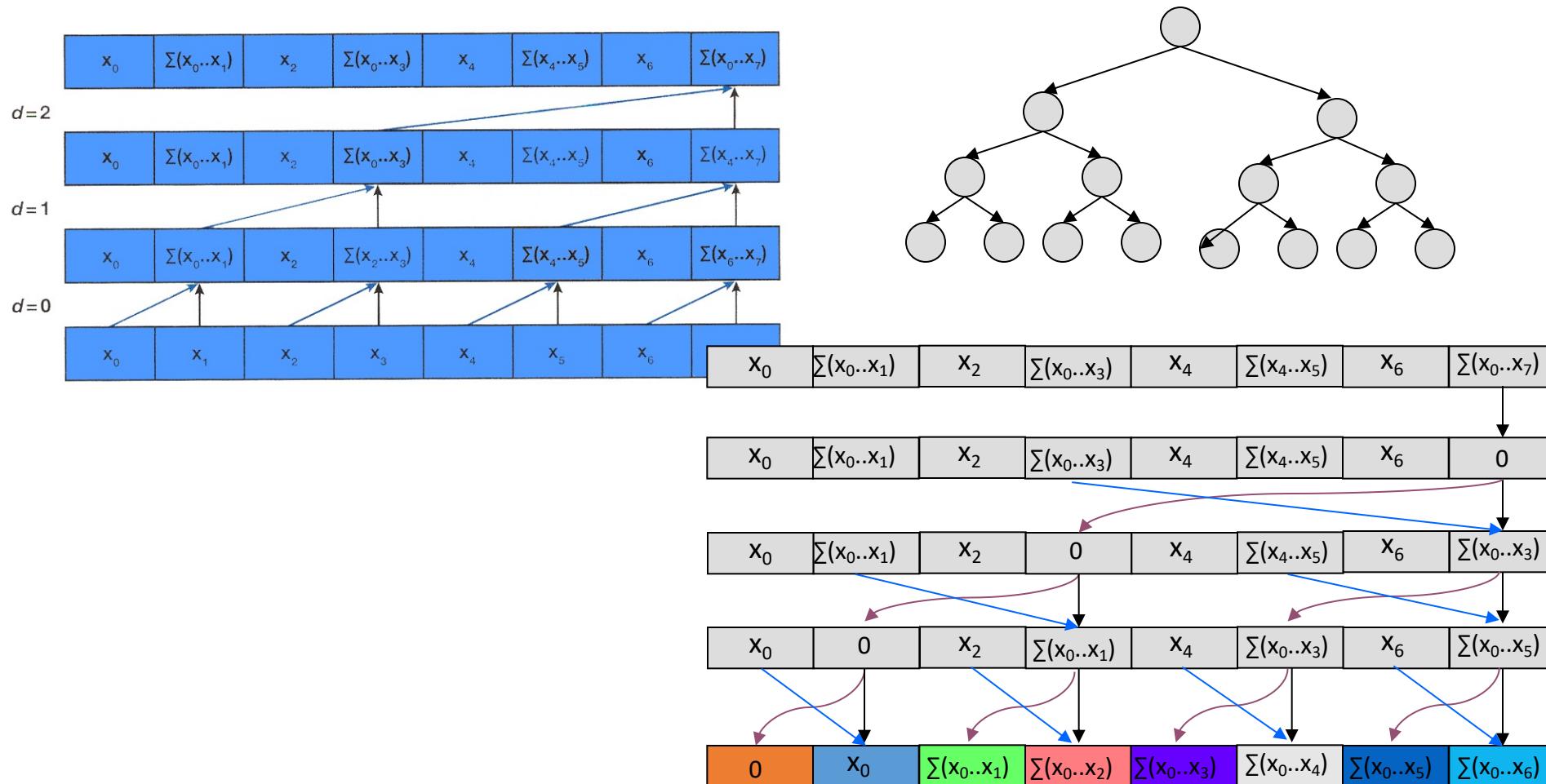
Tree analogy



Tree analogy



Tree analogy



$O(n)$ Segmented Scan

Up-Sweep

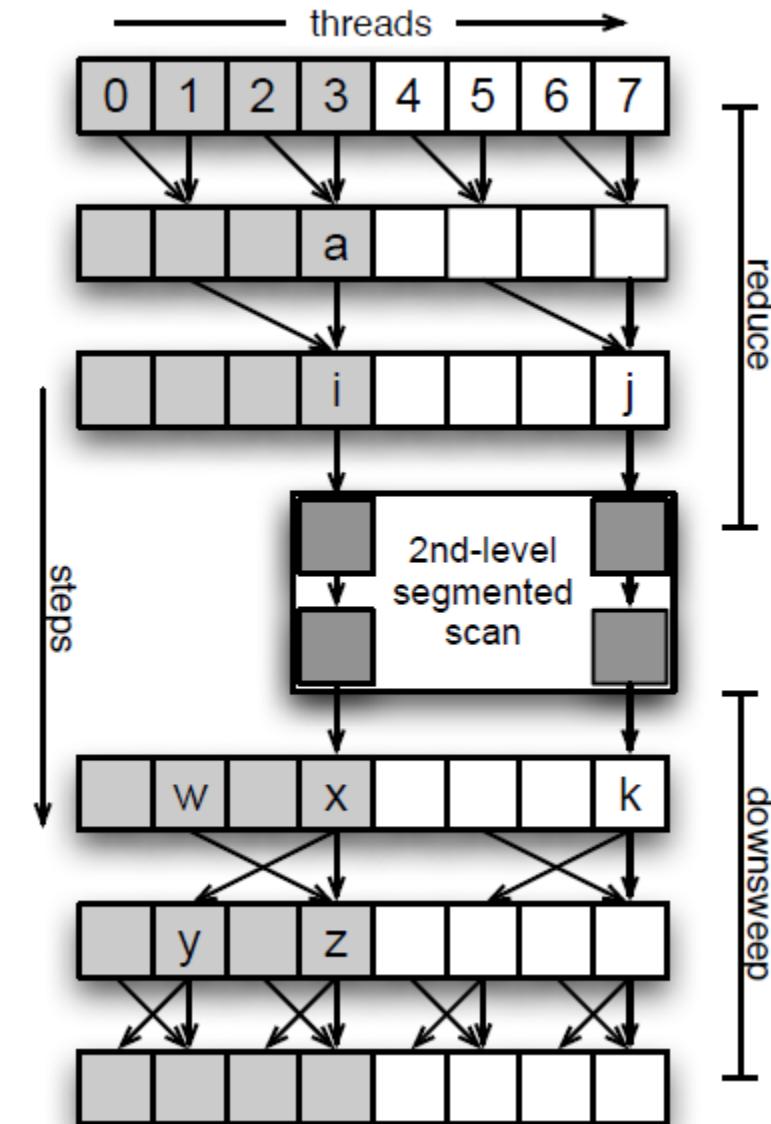
```
1: for  $d = 1$  to  $\log_2 n - 1$  do
2:   for all  $k = 0$  to  $n - 1$  by  $2^{d+1}$  in parallel do
3:     if  $f[k + 2^{d+1} - 1]$  is not set then
4:        $x[k + 2^{d+1} - 1] \leftarrow x[k + 2^d - 1] + x[k + 2^{d+1} - 1]$ 
5:        $f[k + 2^{d+1} - 1] \leftarrow f[k + 2^d - 1] | f[k + 2^{d+1} - 1]$ 
```

- Down-Sweep

```

1:  $x[n - 1] \leftarrow 0$ 
2: for  $d = \log_2 n - 1$  down to 0 do
3:   for all  $k = 0$  to  $n - 1$  by  $2^{d+1}$  in parallel do
4:      $t \leftarrow x[k + 2^d - 1]$ 
5:      $x[k + 2^d - 1] \leftarrow x[k + 2^{d+1} - 1]$ 
6:     if  $f_i[k + 2^d]$  is set then
7:        $x[k + 2^{d+1} - 1] \leftarrow 0$ 
8:     else if  $f[k + 2^d - 1]$  is set then
9:        $x[k + 2^{d+1} - 1] \leftarrow t$ 
10:    else
11:       $x[k + 2^{d+1} - 1] \leftarrow t + x[k + 2^{d+1} - 1]$ 
12:    Unset flag  $f[k + 2^d - 1]$ 

```



Features of segmented scan

- 3 times slower than unsegmented scan
- Useful for building broad variety of applications which are not possible with unsegmented scan.

Primitives built on scan

- Enumerate
 - $\text{enumerate}([t\ f\ f\ t\ f\ t\ t]) = [0\ 1\ 1\ 1\ 2\ 2\ 3]$
 - Exclusive scan of input vector
- Distribute (copy)
 - $\text{distribute}([a\ b\ c][d\ e]) = [a\ a\ a][d\ d]$
 - Inclusive scan of input vector
- Split and split-and-segment

Split divides the input vector into two pieces, with all the elements marked false on the left side of the output vector and all the elements marked true on the right.

Applications

- Quicksort
- Sparse Matrix-Vector Multiply
- Tridiagonal Matrix Solvers and Fluid Simulation
- Radix Sort
- Stream Compaction
- Summed-Area Tables

Quicksort

```
[5 3 7 4 6]      # initial input
[5 5 5 5 5]      # distribute pivot across segment
[f f t f t]      # input > pivot?
[5 3 4] [7 6]    # split-and-segment
[5 5 5] [7 7]    # distribute pivot across segment
[t f f] [t f]    # input >= pivot?
[3 4 5] [6 7]    # split-and-segment, done!
```

Sparse Matrix-Vector Multiplication

$$\begin{pmatrix} y_0 \\ y_1 \\ y_2 \end{pmatrix} += \begin{pmatrix} a & 0 & b \\ c & d & e \\ 0 & 0 & f \end{pmatrix} \begin{pmatrix} x_0 \\ x_1 \\ x_2 \end{pmatrix}$$

value = [a,b,c,d,e,f]

index = [0,2,0,1,2,2]

rowPtr = [0,2,5]

$$\text{product} = [x_0a, x_2b, x_0c, x_1d, x_2e, x_2f] \quad (1)$$

$$= [[x_0a, x_2b][x_0c, x_1d, x_2e][x_2f]] \quad (2)$$

$$= [[x_0a + x_2b, x_2b] \\ [x_0c + x_1d + x_2e, x_1d + x_2e, x_2e][x_2f]] \quad (3)$$

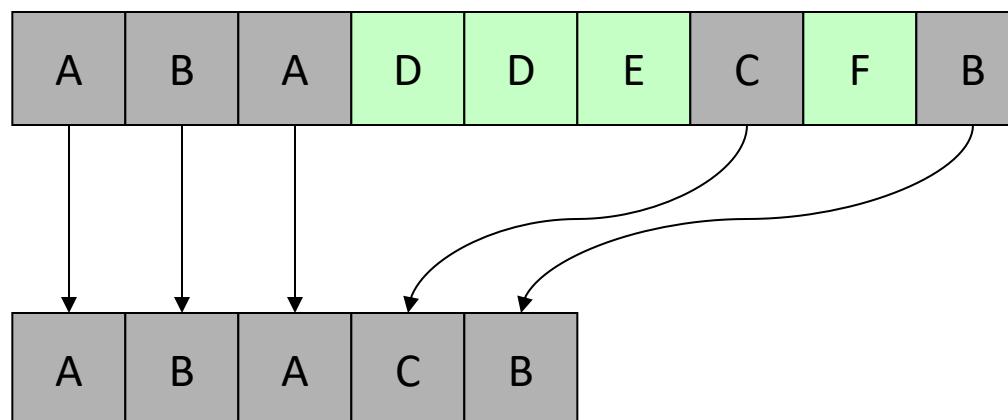
$$y = y + [[x_0a + x_2b, x_0c + x_1d + x_2e, x_2f]] \quad (4)$$

1. The first kernel runs over all entries. For each entry, it sets the corresponding flag to 0 and performs a multiplication on each entry: product = x[index] * value.
2. The next kernel runs over all rows and sets the head flag to 1 for each rowPtr in flag through a scatter. This creates one segment per row.
3. We then perform a backward segmented inclusive sum scan on the e elements in product with head flags in flag.
4. To finish, we run our final kernel over all rows, adding the value in y to the gathered value from products[idx].

Stream Compaction

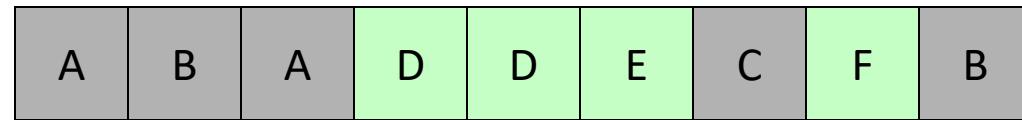
Definition:

- Extracts the ‘interest’ elements from an array of elements and places them continuously in a new array
- Uses:
 - Collision Detection
 - Sparse Matrix Compression



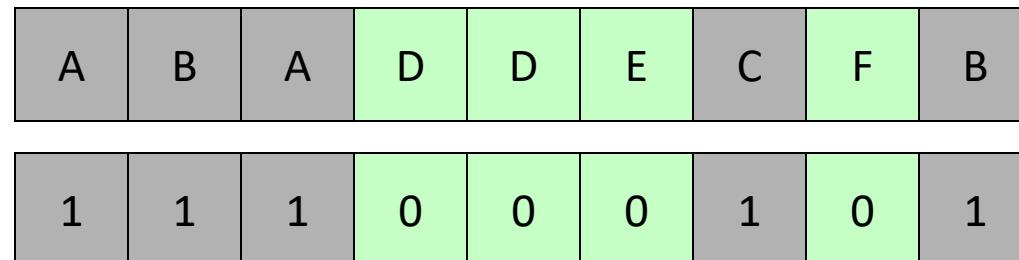
Stream Compaction

Stream Compaction



Input: We want to preserve the gray elements

Stream Compaction



Input: We want to preserve the gray elements
Set a '1' in each gray input

Stream Compaction

A	B	A	D	D	E	C	F	B
1	1	1	0	0	0	1	0	1

Input: We want to preserve the gray elements
Set a '1' in each gray input

0	1	2	3	3	3	3	4	4
---	---	---	---	---	---	---	---	---

Scan

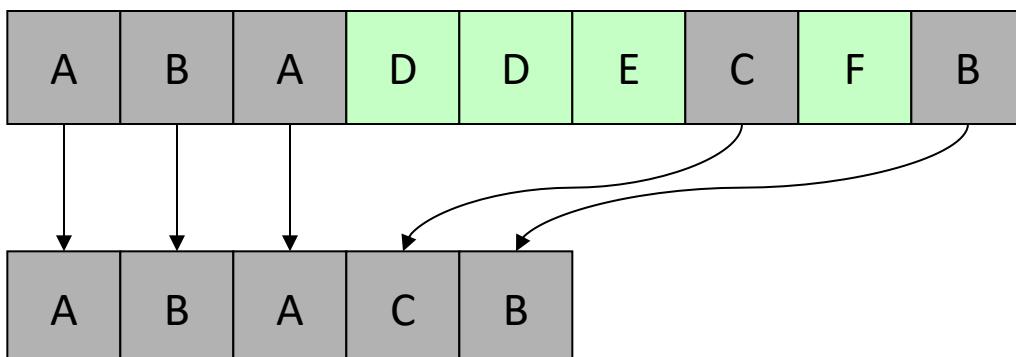
Stream Compaction

A	B	A	D	D	E	C	F	B
1	1	1	0	0	0	1	0	1

Input: We want to preserve the gray elements
Set a '1' in each gray input

0	1	2	3	3	3	3	4	4
---	---	---	---	---	---	---	---	---

Scan



Scatter gray inputs to output using scan result as scatter address

Radix Sort Using Scan

100	111	010	110	011	101	001	000
-----	-----	-----	-----	-----	-----	-----	-----

Input Array

Radix Sort Using Scan

100	111	010	110	011	101	001	000
0	1	0	0	1	1	1	0

Input Array

b = least significant bit

Radix Sort Using Scan

100	111	010	110	011	101	001	000
0	1	0	0	1	1	1	0
1	0	1	1	0	0	0	1

Input Array

b = least significant bit

e = Insert a 1 for all
false sort keys

Radix Sort Using Scan

100	111	010	110	011	101	001	000
0	1	0	0	1	1	1	0
1	0	1	1	0	0	0	1
0	1	1	2	3	3	3	3

Input Array

b = least significant bit

e = Insert a 1 for all
false sort keys

f = Scan the 1s

Radix Sort Using Scan

100	111	010	110	011	101	001	000
0	1	0	0	1	1	1	0
1	0	1	1	0	0	0	1
0	1	1	2	3	3	3	3

Input Array

b = least significant bit

e = Insert a 1 for all
false sort keys

f = Scan the 1s

Total False = $e[n-1] + f[n-1]$

Radix Sort Using Scan

100	111	010	110	011	101	001	000
0	1	0	0	1	1	1	0
1	0	1	1	0	0	0	1
0	1	1	2	3	3	3	3
0-0+4 = 4	1-1+4 = 4	2-1+4 = 5	3-2+4 = 5	4-3+4 = 5	5-3+4 = 6	6-3+4 = 7	7-3+4 = 8

Input Array

b = least significant bit

e = Insert a 1 for all
false sort keys

f = Scan the 1s

Total Falses = e[n-1] + f[n-1]

t = index - f + Total Falses

Radix Sort Using Scan

100	111	010	110	011	101	001	000
0	1	0	0	1	1	1	0
1	0	1	1	0	0	0	1
0	1	1	2	3	3	3	3
0-0+4 = 4	1-1+4 = 4	2-1+4 = 5	3-2+4 = 5	4-3+4 = 5	5-3+4 = 6	6-3+4 = 7	7-3+4 = 8
0	4	1	2	5	6	7	3

Input Array

b = least significant bit

e = Insert a 1 for all
false sort keys

f = Scan the 1s

Total Falses = e[n-1] + f[n-1]

t = index - f + Total Falses

d = b ? t : f

Radix Sort Using Scan

100	111	010	110	011	101	001	000
0	1	0	0	1	1	1	0
1	0	1	1	0	0	0	1
0	1	1	2	3	3	3	3

Input Array

b = least significant bit

e = Insert a 1 for all
false sort keys

f = Scan the 1s

Total Falses = $e[n-1] + f[n-1]$

t = index - f + Total Falses

d = b ? t : f

0-0+4 = 4	1-1+4 = 4	2-1+4 = 5	3-2+4 = 5	4-3+4 = 5	5-3+4 = 6	6-3+4 = 7	7-3+4 = 8
--------------	--------------	--------------	--------------	--------------	--------------	--------------	--------------

0	4	1	2	5	6	7	3
---	---	---	---	---	---	---	---

100	111	010	110	011	101	001	000
-----	-----	-----	-----	-----	-----	-----	-----

100	010	110	000	111	011	101	001
-----	-----	-----	-----	-----	-----	-----	-----

Scatter input using d
as scatter address

Specialized Libraries

- CUDPP: CUDA Data Parallel Primitives Library
 - CUDPP is a library of data-parallel algorithm primitives such as parallel prefix-sum ("scan"), parallel sort and parallel reduction.

CUDPP_DLL CUDPPResult cudppSparseMatrixVectorMultiply(CUDPPHandle *sparseMatrixHandle*,void * *d_y*,const void * *d_x*)

Perform matrix-vector multiply $y = A*x$ for arbitrary sparse matrix A and vector x.

```
CUDPPScanConfig config;  
config.direction = CUDPP_SCAN_FORWARD; config.exclusivity =  
CUDPP_SCAN_EXCLUSIVE; config.op = CUDPP_ADD;  
config.datatype = CUDPP_FLOAT; config.maxNumElements = numElements;  
config.maxNumRows = 1;  
config.rowPitch = 0;  
cudppInitializeScan(&config);  
cudppScan(d_odata, d_idata, numElements, &config);
```

CUFFT

- No. of elements<8192 slower than fftw
- >8192, 5x speedup over threaded fftw
and 10x over serial fftw.

CUBLAS

- Cuda Based Linear Algebra Subroutines
- Saxpy, conjugate gradient, linear solvers.
- 3D reconstruction of planetary nebulae.
 - <http://graphics.tu-bs.de/publications/Fernandez08TechReport.pdf>