Thinking like a computer scientist means more than being able to program a computer. It requires thinking at multiple levels of abstraction.
— Jeannette M. Wing

Java's Math class

<table>
<thead>
<tr>
<th>Method name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Math.abs(value)</td>
<td>absolute value</td>
</tr>
<tr>
<td>Math.ceil(value)</td>
<td>moves up to ceiling</td>
</tr>
<tr>
<td>Math.floor(value)</td>
<td>moves down to floor</td>
</tr>
<tr>
<td>Math.log10(value)</td>
<td>logarithm, base 10</td>
</tr>
<tr>
<td>Math.max(value1, value2)</td>
<td>larger of two values</td>
</tr>
<tr>
<td>Math.min(value1, value2)</td>
<td>smaller of two values</td>
</tr>
<tr>
<td>Math.pow(base, exp)</td>
<td>base to the exp power</td>
</tr>
<tr>
<td>Math.random()</td>
<td>random double between 0 and 1</td>
</tr>
<tr>
<td>Mathrint(value)</td>
<td>Round int, nearest whole number</td>
</tr>
<tr>
<td>Math.sqrt(value)</td>
<td>square root</td>
</tr>
<tr>
<td>Math.sin(value)</td>
<td>sine/cosine/tangent of an angle in radians</td>
</tr>
<tr>
<td>Math.cos(value)</td>
<td></td>
</tr>
<tr>
<td>Math.tan(value)</td>
<td></td>
</tr>
<tr>
<td>Math.toDegrees(value)</td>
<td>convert degrees to radians and back</td>
</tr>
<tr>
<td>Math.toRadians(value)</td>
<td></td>
</tr>
</tbody>
</table>

Constant | Description
---|---
Math.E   | 2.7182818...
Math.PI  | 3.1415926...

静的 methods in other Classes

- Java includes 8 primitive data types
  - byte, short, int, long, float, double, char, boolean
- The Java Standard Library includes thousands of other data types, classes
  - System, String, Graphics, Color, ...
- The Math class contains static methods for common mathematical operations (for which an operator does not exist in Java)
- Call those methods: Math.<MethodName>
  
  Math.pow(2, 5);

No output?

- Simply calling these methods produces no visible result.
  
  Math.pow(3, 4); // no output

- Math method calls use a Java feature called return values that cause them to be treated as expressions.

- The program runs the method, computes the answer, and then "replaces" the call with its computed result value.

  Math.pow(3, 4); // no output
  81.0; // no output

- To see the result, we must print it or store it in a variable.

  double result = Math.pow(3, 4);
  System.out.println(result); // 81.0
Calling Math methods

Math.methodName(parameters)

Examples:

double squareRoot = Math.sqrt(121.0);
System.out.println(squareRoot); // 11.0

int absoluteValue = Math.abs(-50);
System.out.println(absoluteValue); // 50
System.out.println(Math.min(3, 7) + 2); // 5

The Math methods do not print to the console.
– Each method produces ("returns") a numeric result.
– The results are used as expressions (printed, stored, etc.).

Why return and not print?

– It might seem more useful for the Math methods to print their results rather than returning them. Why don't they?

Answer: Returning is more flexible than printing.
– We can compute several things before printing:

double pow1 = Math.pow(3, 4);
double pow2 = Math.pow(10, 6);
System.out.println("Powers are " + pow1 + " and " + pow2);

– We can combine the results of many computations:

double k = 13 * Math.pow(3, 4) + 5 - Math.sqrt(17.8);

Return

• return: To send out a value as the result of a method.
  – The opposite of a parameter:
    • Parameters send information in from the caller to the method.
    • Return values send information out from a method to its caller.
      – A call to the method can be used as part of an expression.

Clicker 1

What is output by the following code?

double a = -1.9;
double b = 2.25;
System.out.print( Math.floor(a) + " " + Math.ceil(b) + " " + a);

A. 3.0
B. -2.0 3.0 -2.0
C. -1.0 3.0 -1.0
D. -1 3 -1.9
E. -2.0 3.0 -1.9
Math questions

- Evaluate the following expressions:
  - Math.abs(-1.23)
  - Math.pow(3, 2)
  - Math.pow(10, -2)
  - Math.sqrt(121.0) - Math.sqrt(256.0)
  - Math.ceil(6.022) + Math.floor(15.9994)
  - Math.abs(Math.min(-3, -5))

- Math.max and Math.min can be used to bound numbers.
  - Consider an int variable named age.
  - What statement would replace negative ages with 0?
  - What statement would cap the maximum age to 40?

Quirks of real numbers

- Some Math methods return double or other non-int types.
  - int x = Math.pow(10, 3); // ERROR: incompat. types

- Some double values print poorly (too many digits).
  - double result = 1.0 / 3.0;
  - System.out.println(result); // 0.3333333333333333

- The computer represents doubles in an imprecise way.
  - System.out.println(0.1 + 0.2);
  - Instead of 0.3, the output is 0.30000000000000004

Type casting

- **type cast**: A conversion from one type to another.
  - To promote an int into a double for floating point division
  - To truncate a double from a real number to an integer

- Syntax:
  - `(type) expression`

- Examples:
  - double result = (double) 19 / 5; // 3.8
  - int result2 = (int) result; // 3
  - int x = (int) Math.pow(10, 3); // 1000

More about type casting

- Type casting has high precedence and only casts the item immediately next to it.
  - double x = (double) 1 + 1 / 2; // 1.0
  - double y = 1 + (double) 1 / 2; // 1.5

- You can use parentheses to force evaluation order.
  - double average = (double) (a + b + c) / 3;

- A conversion to double can be achieved in other ways.
  - double average = 1.0 * (a + b + c) / 3;
Returning a value from a method

```java
public static type name(parameters) {
    statements;
    ...
    return expression;
}
```

Example:

```java
// Returns the slope of the line between the given points.
public static double slope(int x1, int y1, int x2, int y2) {
    double dy = y2 - y1;
    double dx = x2 - x1;
    return dy / dx;
}
```

```java
slope(5, 11, 1, 3) returns 2.0
```

Clicker 2

- Have we (in CS312, before today) used a method that returns a value in lecture?
  A. No
  B. Yes, a few times
  C. Yes, hundreds of time
  D. Lecture?? What lecture?
  E. Maybe?

Return examples

```java
// Converts degrees Fahrenheit to Celsius.
public static double fToC(double degreesF) {
    double degreesC = 5.0 / 9.0 * (degreesF - 32);
    return degreesC;
}
```

```java
// Computes triangle hypotenuse length given its side lengths.
public static double hypotenuse(int a, int b) {
    double c = Math.sqrt(a * a + b * b);
    return c;
}
```

- You can shorten the examples by returning an expression:

```java
public static double fToC(double degreesF) {
    return 5.0 / 9.0 * (degreesF - 32);
}
```

Common error: Not storing

- a return statement DOES NOT send a variable's name back to the calling method.

```java
public static void main(String[] args) {
    slope(0, 0, 6, 3);
    System.out.println("The slope is " + result);
    // ERROR: result not defined
}
```
Fixing the common error

- Instead, returning sends the variable's value back.
  - The returned value must be stored into a variable or used in an expression to be useful to the caller.

```java
public static void main(String[] args) {
    double s = slope(0, 0, 6, 3);
    System.out.println("The slope is " + s);
}

public static double slope(int x1, int x2, int y1, int y2) {
    double dy = y2 - y1;
    double dx = x2 - x1;
    double result = dy / dx;
    return result;
}
```

Clicker 3

- What is the output of the following code?

```java
int x = 5;
int y = 7;
System.out.print(m(x, y) + " " + x + " " + m(y, x));

public static int m(int x, int y) {
    x += 2;
    System.out.print(x + " ");
    y -= 2;
    return x * y;
}
```

A. 7 9 35 5 27
B. 7 7 35 7 27
C. 7 5 9 27 35
D. 35 7 5 9 27
E. None of A - D are correct

Exercise

- In physics, the displacement of a moving body represents its change in position over time while accelerating.
  - Given initial velocity \( v_0 \) in m/s, acceleration \( a \) in m/s\(^2\), and elapsed time \( t \) in s, the displacement of the body is:
    - Displacement = \( v_0 \cdot t + \frac{1}{2} \cdot a \cdot t^2 \)

Write a method displacement that accepts \( v_0 \), \( a \), and \( t \) and computes and returns the change in position.

- example: displacement(3.0, 4.0, 5.0) returns 65.0

Exercise solution

```java
public static double displacement(
    double v0, double a,
    double t) {
    double d = v0 * t + 0.5
    * a * Math.pow(t, 2);
    return d;
}
```
Exercises

- write a method to
  - return the int average of 3 ints
  - return the double average of 3 ints
  - return the average of a given number of rolls of 2 six sided dice
  - calculate and return N factorial (N!).
  - return the number of seconds in a given number of years.
  - return the Nth digit of a given integer.
  - return the distance between two points.

Exercise

- If you drop two balls, which will hit the ground first?
  - Ball 1: height of 600m, initial velocity = 25 m/sec downward
  - Ball 2: height of 500m, initial velocity = 15 m/sec downward

- Write a program that determines how long each ball takes to hit the ground (and draws each ball falling).
  - Total time is based on the force of gravity on each ball.
  - Acceleration due to gravity ≈ 9.81 m/s², downward
  - Displacement = \( v_0 t + \frac{1}{2} a t^2 \)

Ball solution

```java
// Simulates the dropping of two balls from various heights.
import java.awt.*;
public class Balls {
    public static void main(String[] args) {
        DrawingPanel panel = new DrawingPanel(600, 600);
        Graphics g = panel.getGraphics();
        int ball1x = 100, ball1y = 0, v01 = 25;
        int ball2x = 200, ball2y = 100, v02 = 15;

        // draw the balls at each time increment
        for (double t = 0; t <= 10.0; t = t + 0.1) {
            g.setColor(Color.GRAY);
            panel.fillRect(0, 0, 600, 600);
            g.setColor(Color.RED);
            double disp1 = displacement(v01, t, 9.81);
            g.fillOval(ball1x, ball1y + (int) disp1, 10, 10);
            double disp2 = displacement(v02, t, 9.81);
            g.fillOval(ball2x, ball2y + (int) disp2, 10, 10);
            panel.sleep(50); // pause for 50 ms
        }
    }
}
```