



This young bird closely resembles its parents which are about a third larger. The white flecks on the face are mallophaga eggs. Most bird lice taxa found on Hoatzins are unique to this host.  
© 2009 Photo and Comment by [Petroglyph](http://www.flickr.com/photos/20113115@N00/)  
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# New methods for inferring species trees in the presence of incomplete lineage sorting

Tandy Warnow

The University of Illinois



# Avian Phylogenomics Project

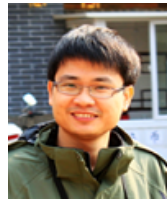
Erich Jarvis,  
HHMI



MTP Gilbert,  
Copenhagen



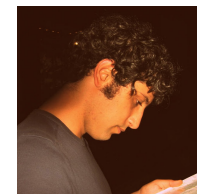
G Zhang,  
BGI



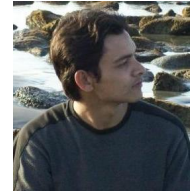
T. Warnow  
UT-Austin



S. Mirarab  
UT-Austin



Md. S. Bayzid,  
UT-Austin



Plus many many other people...

- Approx. 50 species, whole genomes
- 8000+ genes, UCEs

## Challenges:

- Massive gene tree conflict consistent with incomplete lineage sorting
- Maximum likelihood estimation on a million-site genome-scale alignment

In press

# 1kp: Thousand Transcriptome Project

G. Ka-Shu Wong  
U Alberta



J. Leebens-Mack  
U Georgia



N. Wickett  
Northwestern



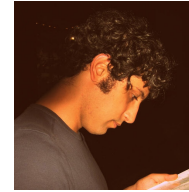
N. Matasci  
iPlant



T. Warnow,  
UIUC



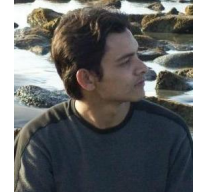
S. Mirarab,  
UT-Austin



N. Nguyen,  
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Plus many many other people...

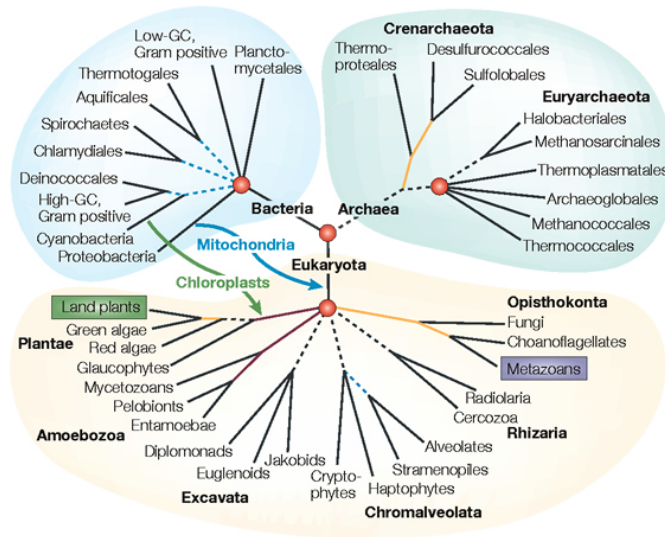
- Plant Tree of Life based on transcriptomes of ~1200 species
- More than 13,000 gene families (most not single copy)

## Challenges:

- Massive gene tree conflict consistent with incomplete lineage sorting
- Multiple sequence alignment of >100,000 sequences (with lots of fragments!)

In press

# The Tree of Life: *Multiple* Challenges

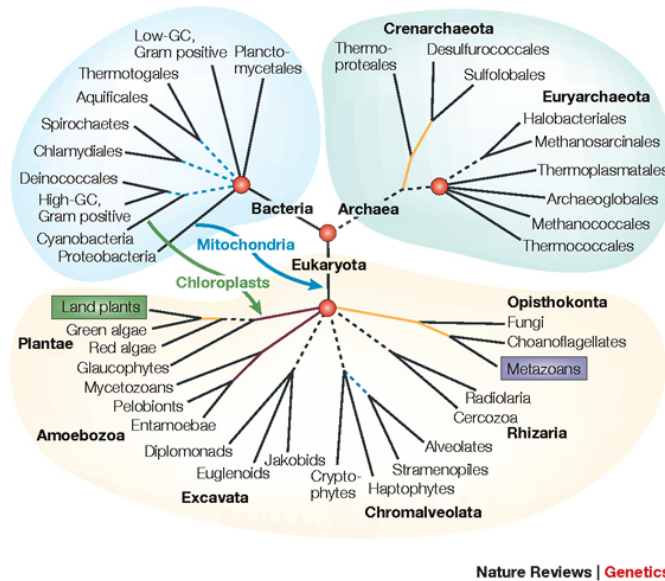


Large datasets:  
100,000+ sequences  
10,000+ genes  
“BigData” complexity

Large-scale statistical phylogeny estimation  
Ultra-large multiple-sequence alignment  
Estimating species trees from incongruent gene trees  
Supertree estimation  
Genome rearrangement phylogeny  
Reticulate evolution  
Visualization of large trees and alignments  
Data mining techniques to explore multiple optima



# The Tree of Life: *Multiple* Challenges



Large datasets:  
100,000+ sequences  
10,000+ genes  
“BigData” complexity

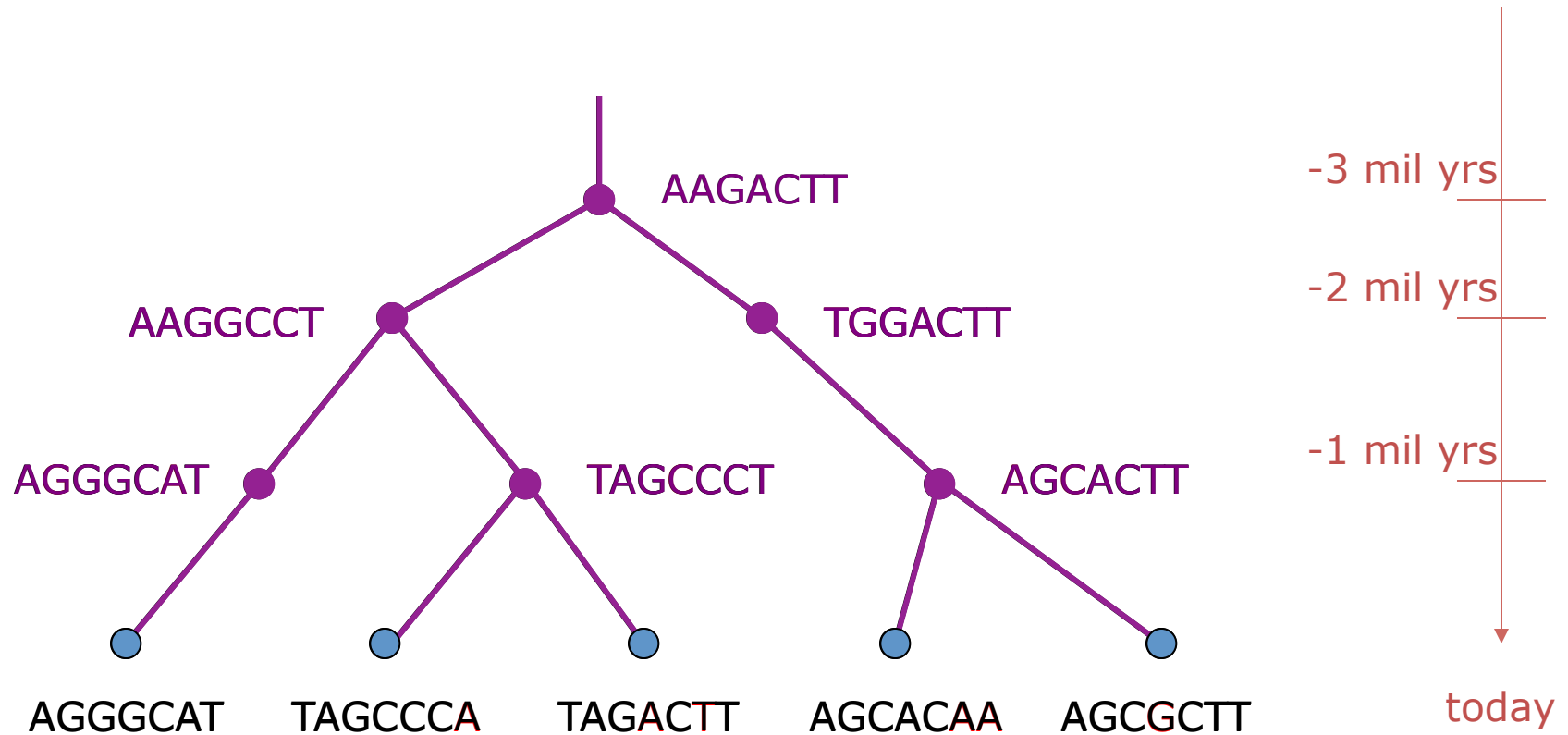
Large-scale statistical phylogeny estimation  
Ultra-large multiple-sequence alignment  
[Estimating species trees from incongruent gene trees](#)  
Supertree estimation  
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Reticulate evolution  
Visualization of large trees and alignments  
Data mining techniques to explore multiple optima

This talk

# This talk

- Statistical gene tree estimation
  - Models of evolution
  - Identifiability and statistical consistency
  - Absolute fast converging methods
- Statistical species tree estimation
  - Gene tree conflict due to incomplete lineage sorting
  - The multi-species coalescent model
  - Identifiability and statistical consistency
  - New methods for species tree estimation
    - Statistical Binning (in press)
    - ASTRAL (Bioinformatics 2014)
  - The challenge of gene tree estimation error

# DNA Sequence Evolution (Idealized)



# Markov Model of Site Evolution

Simplest (Jukes-Cantor, 1969):

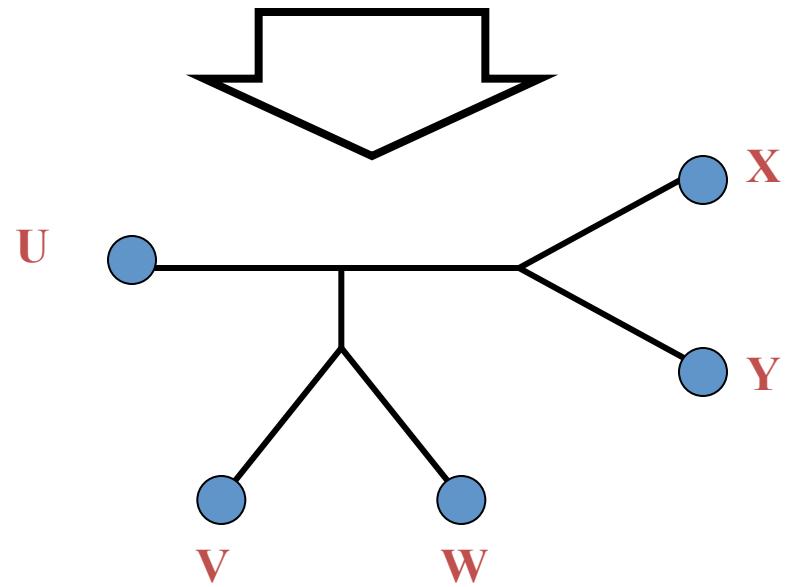
- The model tree  $T$  is binary and has substitution probabilities  $p(e)$  on each edge  $e$ .
- The state at the root is randomly drawn from  $\{A, C, T, G\}$  (nucleotides)
- If a site (position) changes on an edge, *it changes with equal probability to each of the remaining states.*
- The evolutionary process is Markovian.

The different sites are assumed to evolve independently and identically down the tree (with rates that are drawn from a gamma distribution).

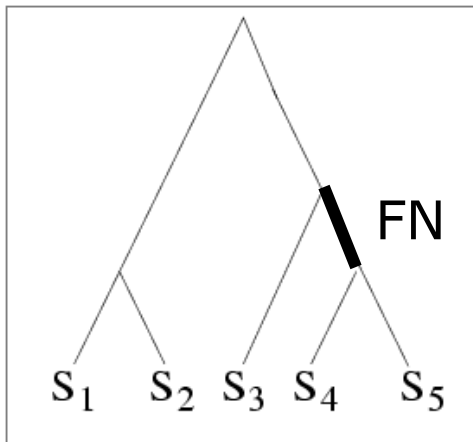
More complex models (such as the General Markov model) are also considered, often with little change to the theory.



U AGGTCA      V AGATTA      W AGACTA      X TGGACA      Y TGCGACT



# Quantifying Error



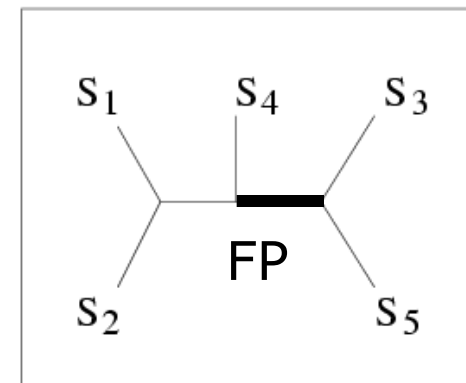
TRUE TREE

S <sub>1</sub>	ACAATTAGAAC
S <sub>2</sub>	ACCCTTAGAAC
S <sub>3</sub>	ACCATTCCAAC
S <sub>4</sub>	ACCAGACCAAC
S <sub>5</sub>	ACCAGACCGGA

DNA SEQUENCES

FN: false negative  
(missing edge)  
FP: false positive  
(incorrect edge)

**50% error rate**

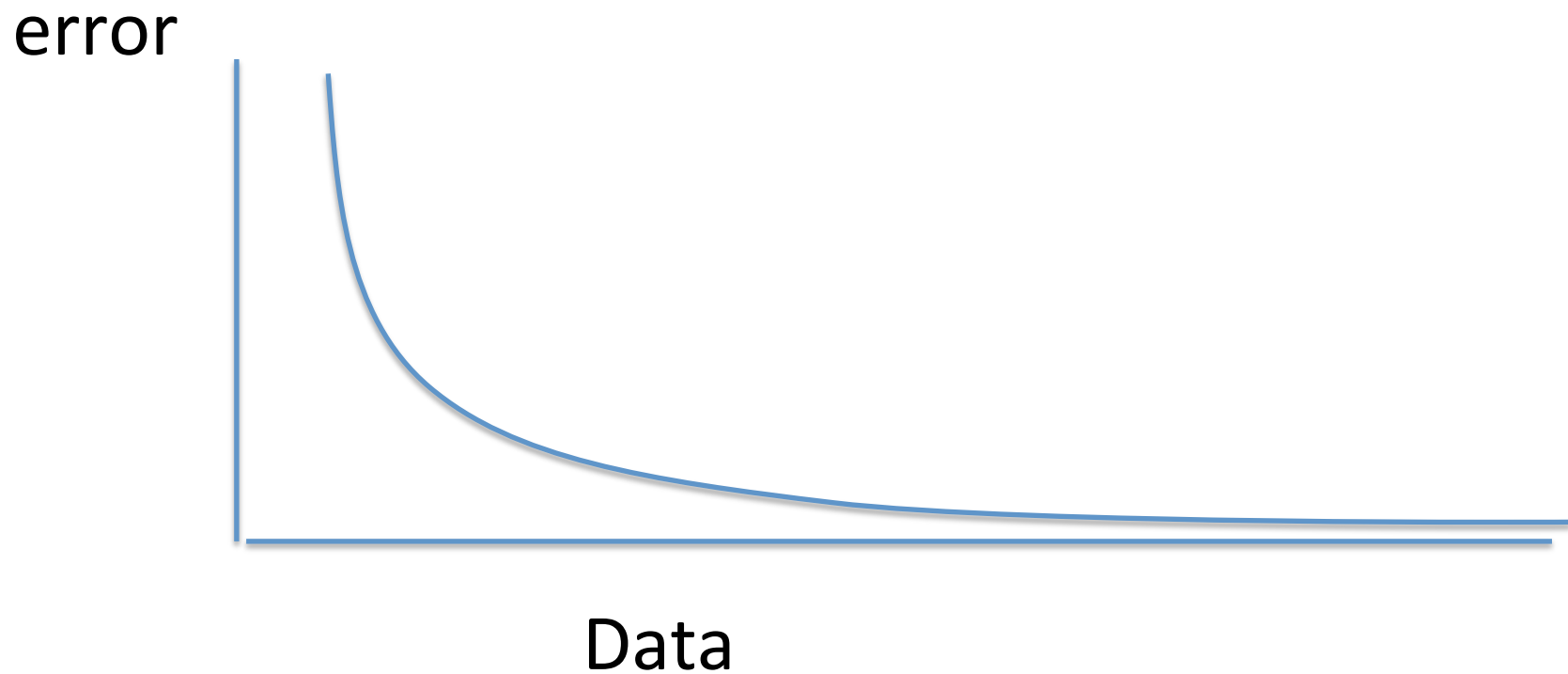


INFERRED TREE

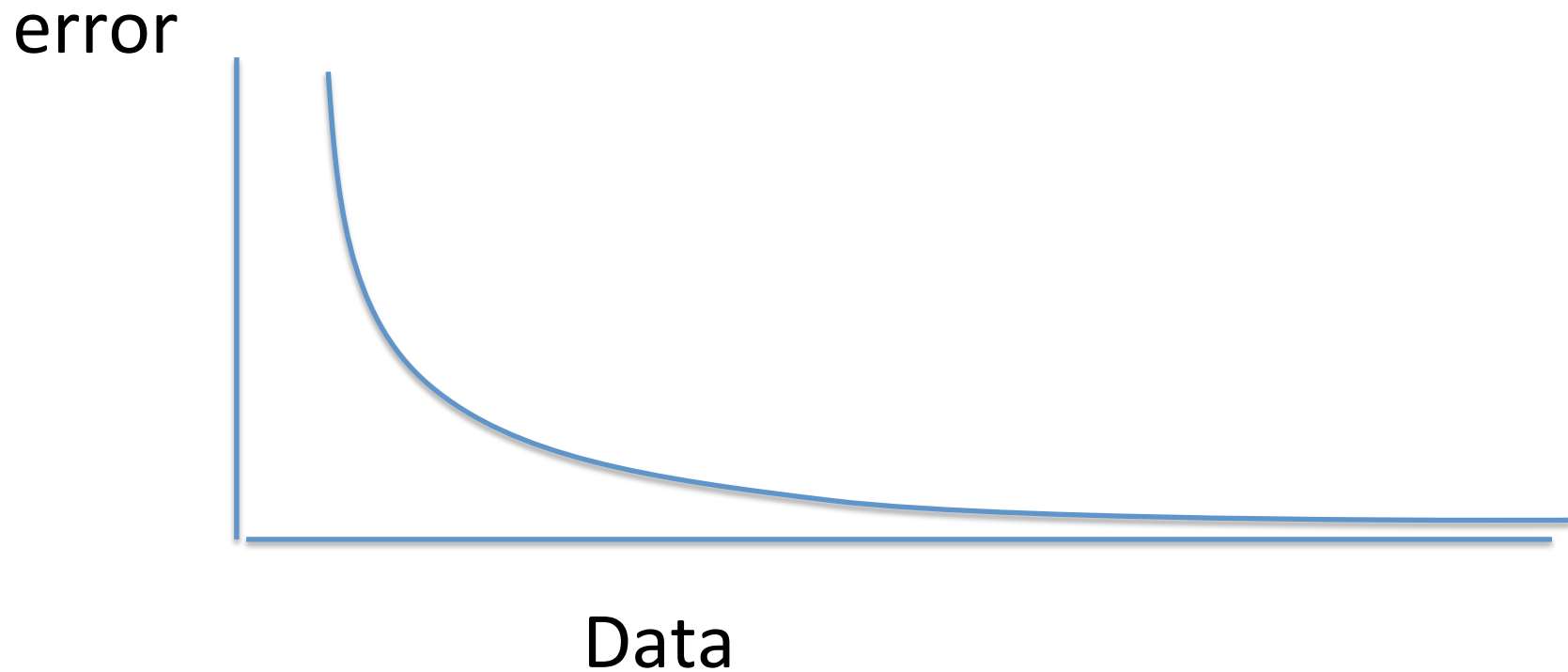
# Questions

- Is the model tree **identifiable**?
- Which estimation methods are **statistically consistent** under this model?
- **How much data** does the method need to estimate the model tree correctly (with high probability)?
- What is the **computational complexity** of an estimation problem?

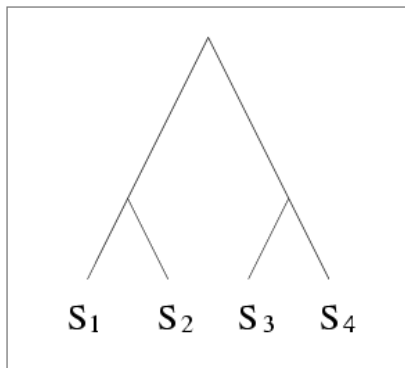
# Statistical Consistency



# Statistical Consistency



Data are sites in an alignment

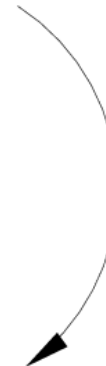


TRUE TREE

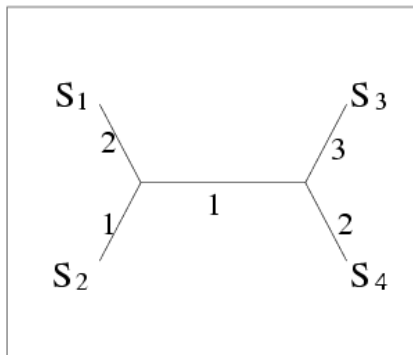


S <sub>1</sub>	ACAATTAGAAC
S <sub>2</sub>	ACCCTTAGAAC
S <sub>3</sub>	ACCATTCCAAC
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DNA SEQUENCES



STATISTICAL  
ESTIMATION  
OF PAIRWISE  
DISTANCES



INFERRED TREE

METHODS  
SUCH AS  
NEIGHBOR  
JOINING

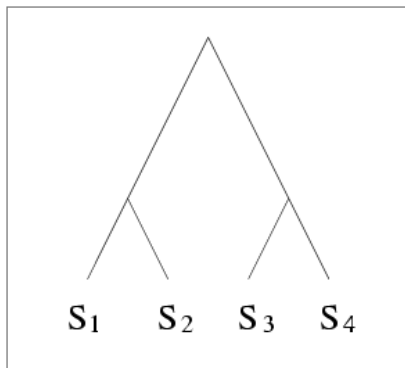


	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>
S <sub>1</sub>	0	3	6	5
S <sub>2</sub>		0	5	4
S <sub>3</sub>			0	5
S <sub>4</sub>				0

DISTANCE MATRIX

Neighbor Joining (and many other distance-based methods) are statistically consistent under Jukes-Cantor





TRUE TREE

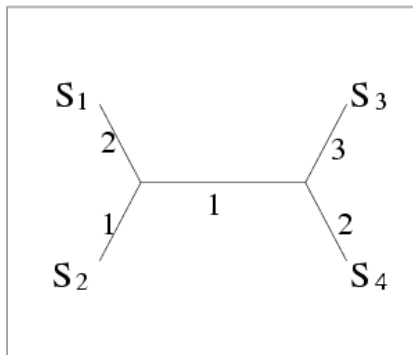


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DNA SEQUENCES



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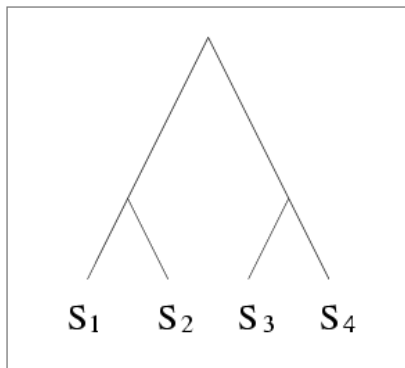


	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>
S <sub>1</sub>	0	3	6	5
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S <sub>3</sub>			0	5
S <sub>4</sub>				0

DISTANCE MATRIX

**Additive matrices satisfy the  
“Four Point Condition”**

**Neighbor Joining (and many other distance-based methods) are statistically consistent under Jukes-Cantor**



TRUE TREE



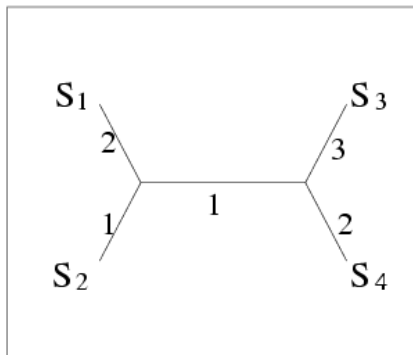
S <sub>1</sub>	ACAATTAGAAC
S <sub>2</sub>	ACCCTTAGAAC
S <sub>3</sub>	ACCATTCCAAC
S <sub>4</sub>	ACCAGACCAAC

DNA SEQUENCES

**Four Point Method:**  
**Construct tree AB|CD**  
**If  $AB+CD < \min\{AC+BD, AD+BC\}$**



STATISTICAL  
ESTIMATION  
OF PAIRWISE  
DISTANCES



INFERRED TREE

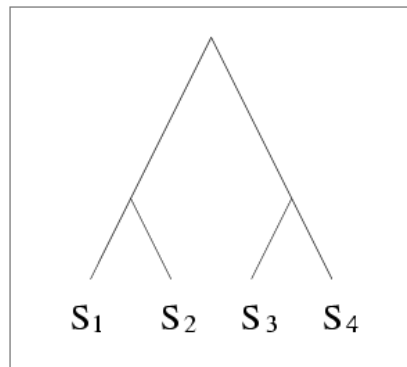
METHODS  
SUCH AS  
NEIGHBOR  
JOINING



	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>
S <sub>1</sub>	0	3	6	5
S <sub>2</sub>		0	5	4
S <sub>3</sub>			0	5
S <sub>4</sub>				0

DISTANCE MATRIX

Neighbor Joining (and many other distance-based methods) are statistically consistent under Jukes-Cantor



TRUE TREE



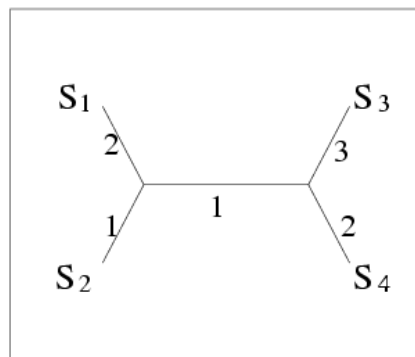
S <sub>1</sub>	ACAATTAGAAC
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DNA SEQUENCES

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STATISTICAL  
ESTIMATION  
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METHODS  
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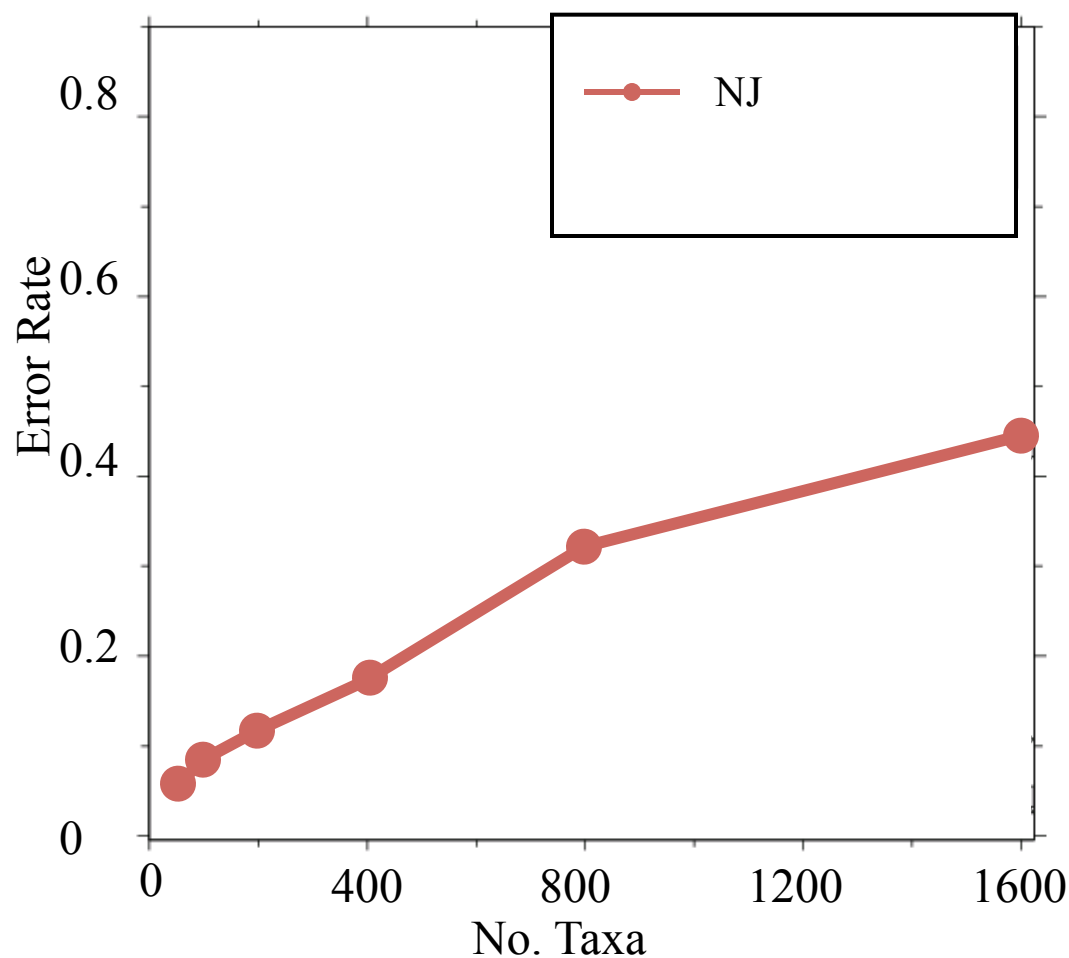
	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>
S <sub>1</sub>	0	3	6	5
S <sub>2</sub>		0	5	4
S <sub>3</sub>			0	5
S <sub>4</sub>				0

DISTANCE MATRIX

**Constructing larger trees:**  
**(1) Compute quartet trees using FPM**  
**(2) Determine if the quartet trees are “compatible”; if so, return the tree on which they agree. Else Return FAIL.**

Neighbor Joining (and many other distance-based methods) are statistically consistent under Jukes-Cantor

# Neighbor Joining on large diameter trees

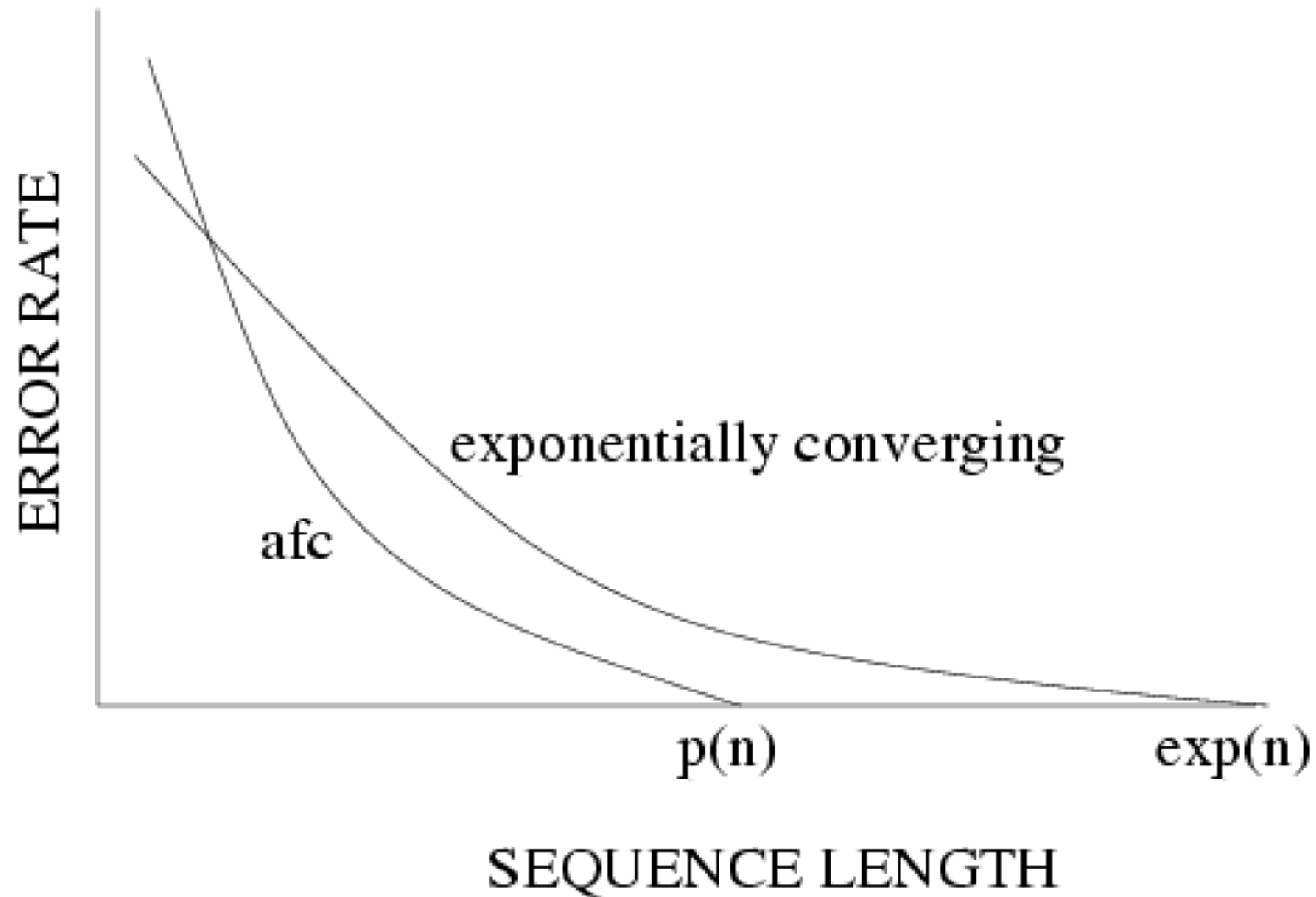


Simulation study based upon fixed edge lengths, K2P model of evolution, sequence lengths fixed to 1000 nucleotides.

Error rates reflect proportion of incorrect edges in inferred trees.

*[Nakhleh et al. ISMB 2001]*

# Statistical consistency, exponential convergence, and absolute fast convergence (afc)



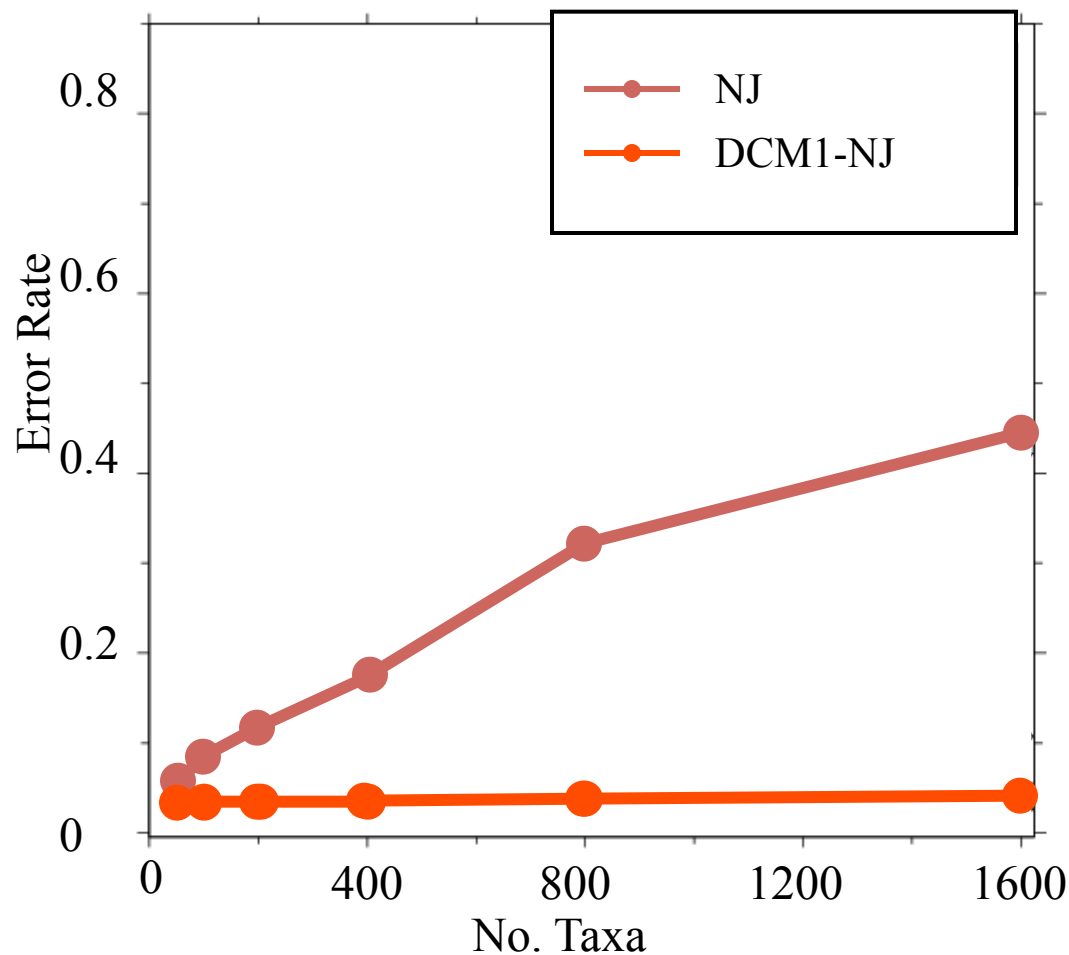
# Fast-converging methods (and related work)

- 1997: Erdos, Steel, Szekely, and Warnow (ICALP).
- 1999: Erdos, Steel, Szekely, and Warnow (RSA, TCS);  
Huson, Nettles and Warnow (J. Comp Bio.)
- 2001: Warnow, St. John, and Moret (SODA);  
Nakhleh, St. John, Roshan, Sun, and Warnow (ISMB)  
Cryan, Goldberg, and Goldberg (SICOMP);  
Csuros and Kao (SODA);
- 2002: Csuros (J. Comp. Bio.)
- 2006: Daskalakis, Mossel, Roch (STOC),  
Daskalakis, Hill, Jaffe, Mihaescu, Mossel, and Rao (RECOMB)
- 2007: Mossel (IEEE TCBB)
- 2008: Gronau, Moran and Snir (SODA)
- 2010: Roch (Science)



# DCM1-boosting distance-based methods

*[Nakhleh et al. ISMB 2001]*



Theorem (Warnow et al., SODA 2001): DCM1-NJ converges to the true tree from **polynomial length** sequences. Hence DCM1-NJ is afc.

**Proof: uses chordal graph theory and probabilistic analysis of algorithms**

# Questions

- Is the model tree **identifiable**?
- Which estimation methods are **statistically consistent** under this model?
- **How much data** does the method need to estimate the model tree correctly (with high probability)?
- What is the **computational complexity** of an estimation problem?

# Answers?

- We know a lot about which site evolution models are **identifiable**, and which methods are **statistically consistent**.

# Answers?

- We know a lot about which site evolution models are identifiable, and which methods are statistically consistent.
- Some polynomial time afc methods have been developed, and we know a little bit about the sequence length requirements for standard methods.

# Answers?

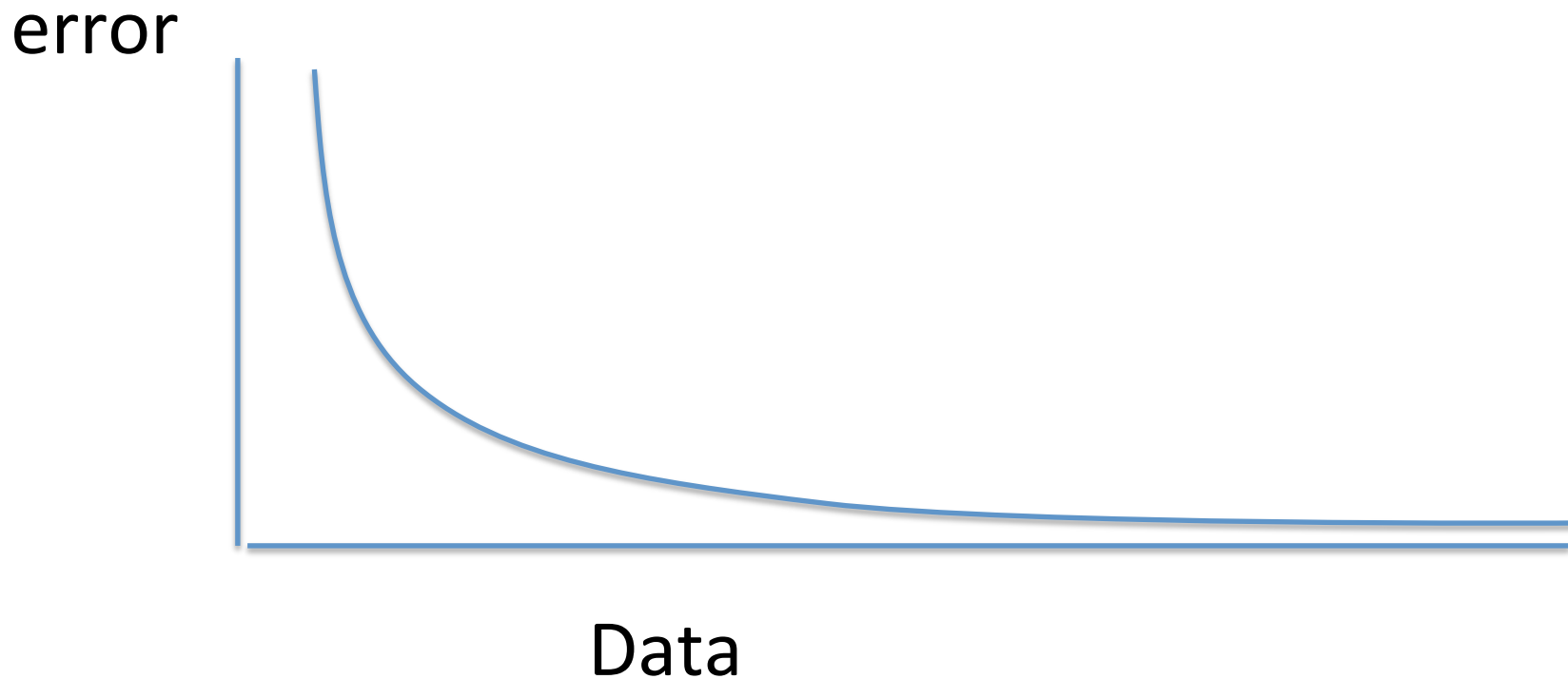
- We know a lot about which site evolution models are identifiable, and which methods are statistically consistent.
- Some polynomial time afc methods have been developed, and we know a little bit about the sequence length requirements for standard methods.
- Just about everything is NP-hard, and the datasets are big.

# Answers?

- We know a lot about which site evolution models are identifiable, and which methods are statistically consistent.
- Some polynomial time afc methods have been developed, and we know a little bit about the sequence length requirements for standard methods.
- Just about everything is NP-hard, and the datasets are big.
- Extensive studies show that even the best methods produce gene trees with some error.

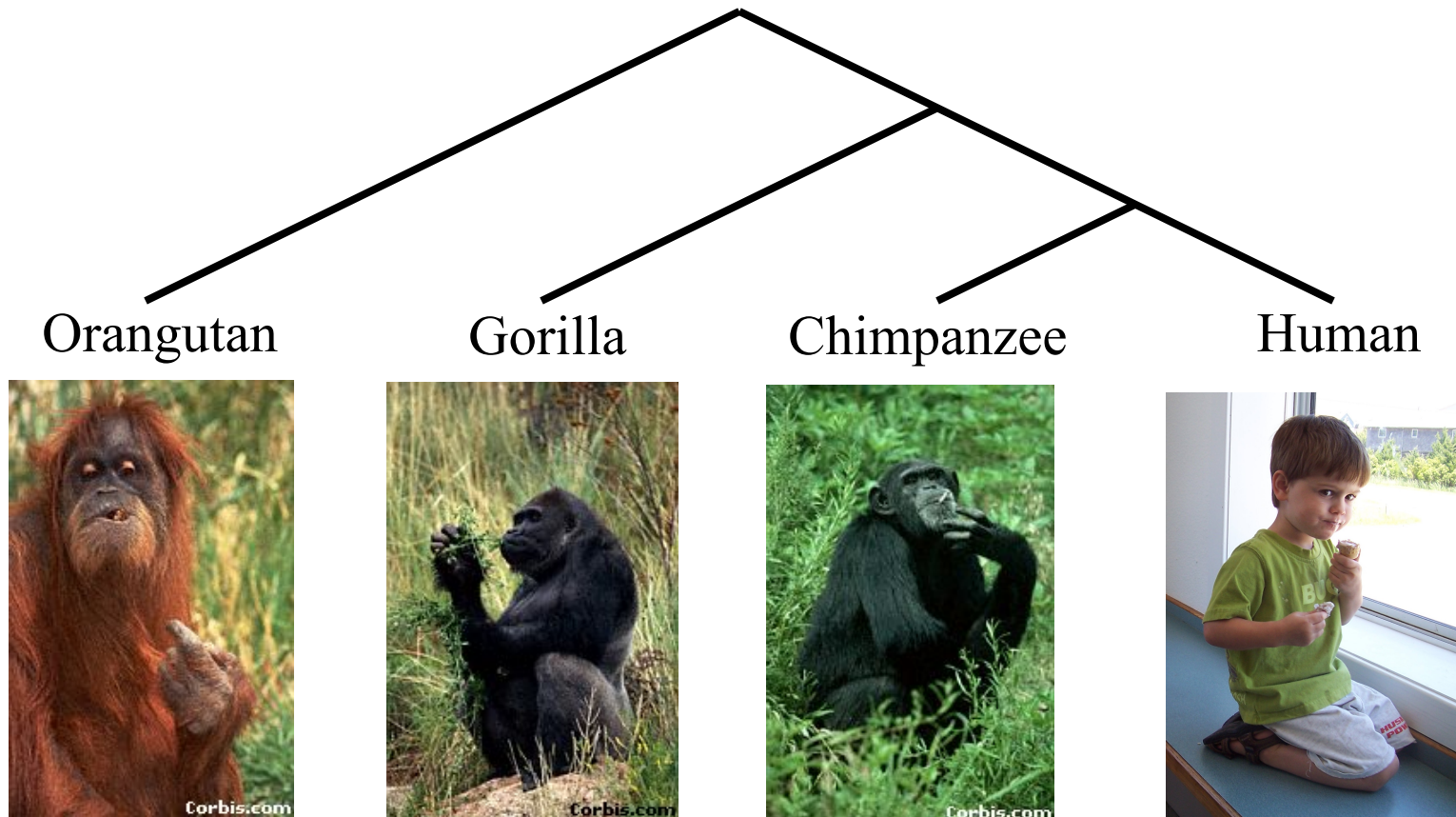


# In other words...



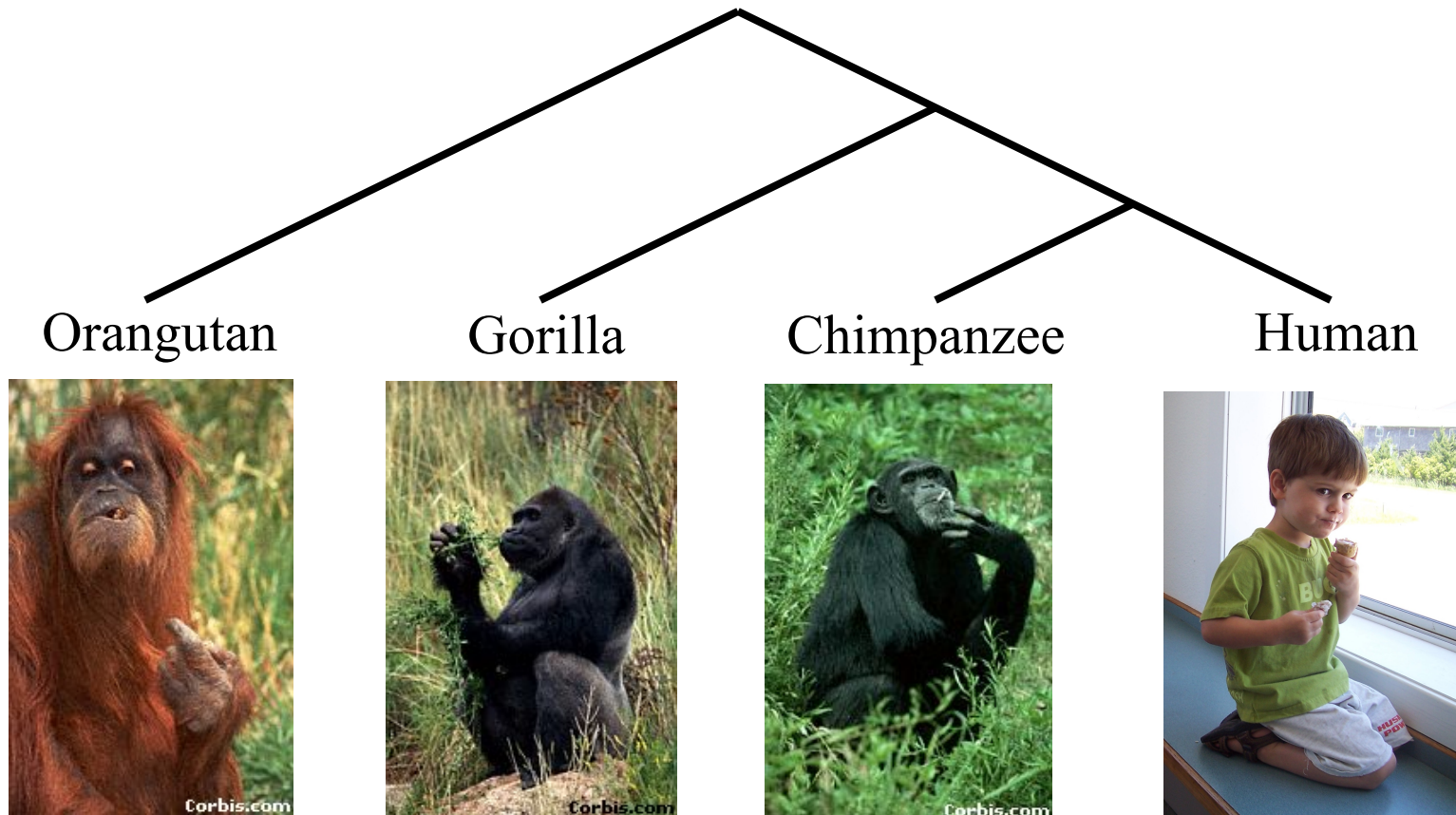
Statistical consistency doesn't guarantee accuracy w.h.p. unless the sequences ***are long enough.***

# Phylogeny (evolutionary tree)



*From the Tree of the Life Website,  
University of Arizona*

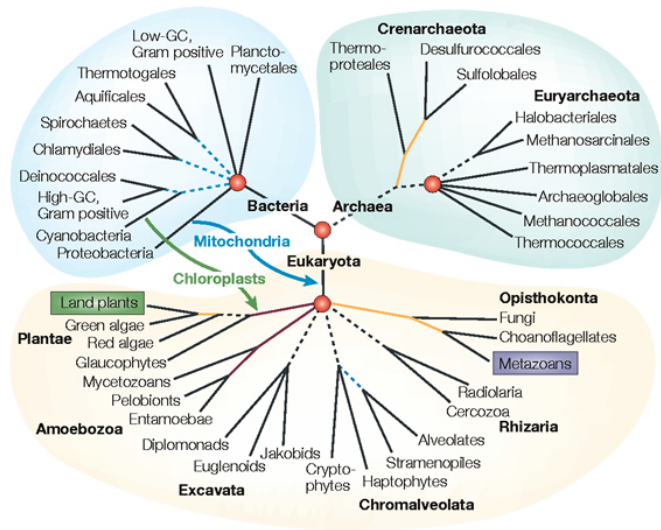
# Sampling multiple genes from multiple species



*From the Tree of the Life Website,  
University of Arizona*

# Phylogenomics

(Phylogenetic estimation from whole genomes)



Nature Reviews | Genetics



# Using multiple genes

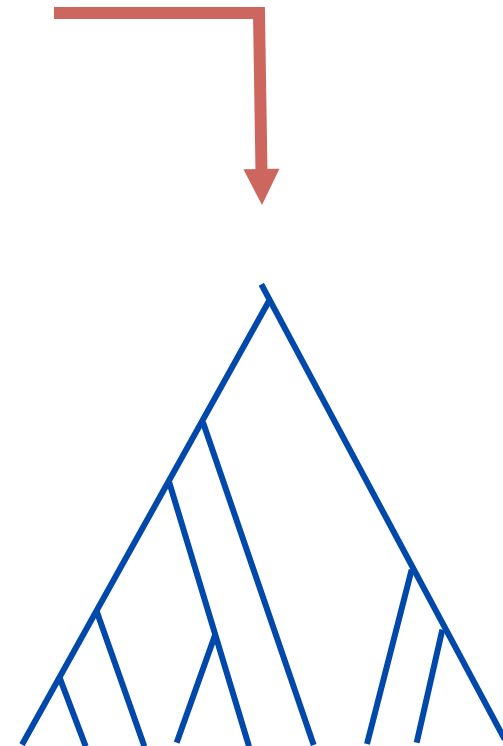
	gene 1
$S_1$	TCTAATGGAA
$S_2$	GCTAAGGGAA
$S_3$	TCTAAGGGAA
$S_4$	TCTAACGGAA
$S_7$	TCTAATGGAC
$S_8$	TATAACGGAA

	gene 2
$S_4$	GGTAACCCTC
$S_5$	GCTAAACCTC
$S_6$	GGTGACCATC
$S_7$	GCTAAACCTC

	gene 3
$S_1$	TATTGATACA
$S_3$	TCTTGATACC
$S_4$	TAGTGATGCA
$S_7$	TAGTGATGCA
$S_8$	CATTCATACC

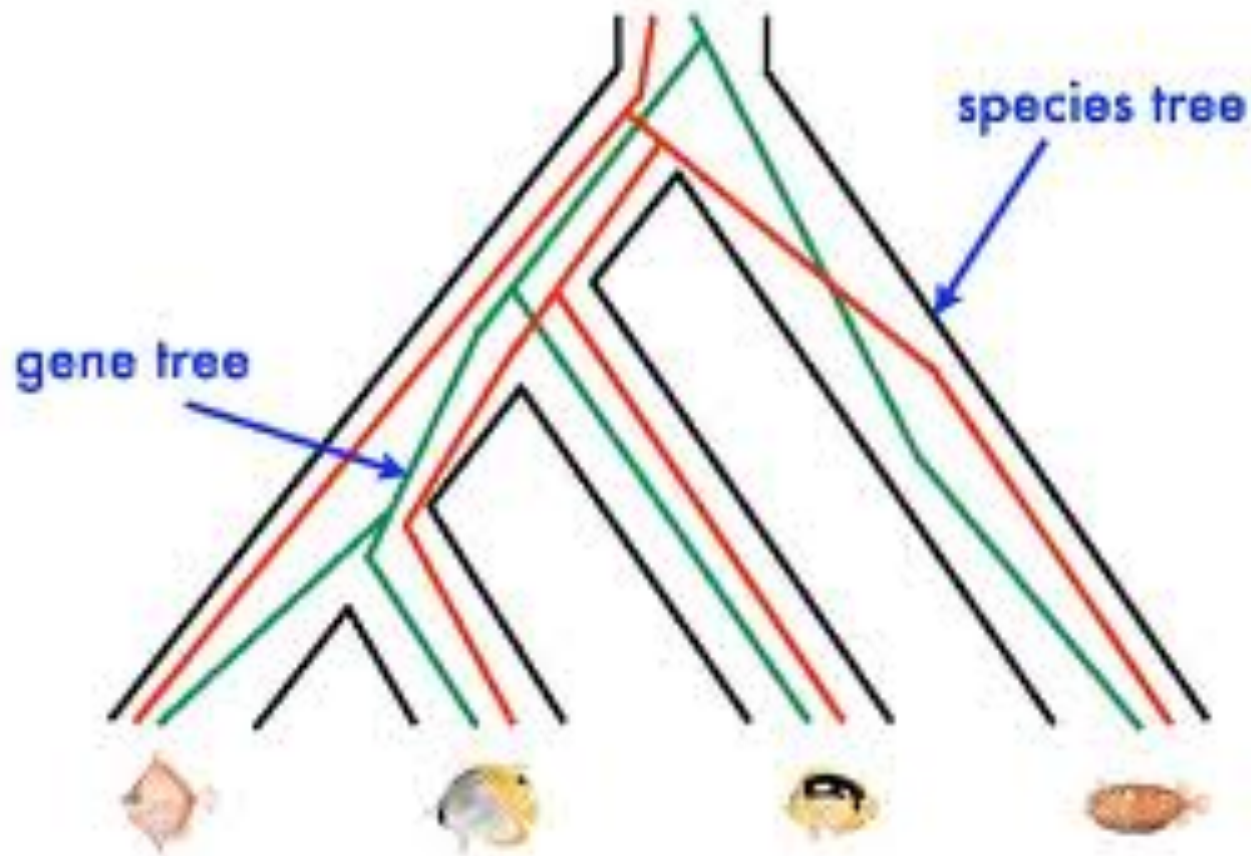
# Concatenation

	gene 1	gene 2	gene 3
S <sub>1</sub>	TCTAATGGAA	??????????	TATTGATACA
S <sub>2</sub>	GCTAAGGGAA	??????????	??????????
S <sub>3</sub>	TCTAAGGGAA	??????????	TCTTGATACC
S <sub>4</sub>	TCTAACGGAA	GGTAACCCTC	TAGTGATGCA
S <sub>5</sub>	??????????	GCTAAACCTC	??????????
S <sub>6</sub>	??????????	GGTGACCATC	??????????
S <sub>7</sub>	TCTAATGGAC	GCTAAACCTC	TAGTGATGCA
S <sub>8</sub>	TATAACGGAA	??????????	CATTCATACC





Red gene tree  $\neq$  species tree  
(green gene tree okay)



# Avian Phylogenomics Project

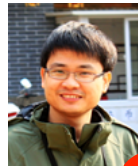
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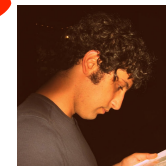
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Plus many many other people...

- Approx. 50 species, whole genomes
- 8000+ genes, UCEs
- Gene sequence alignments computed using SATé (Liu et al., Science 2009 and Systematic Biology 2012)



# 1KP: Thousand Transcriptome Project



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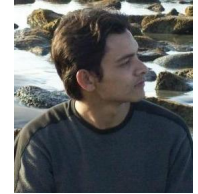
T. Warnow,  
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UT-Austin



N. Nguyen,  
UT-Austin



Md. S. Bayzid  
UT-Austin

- 1200 plant transcriptomes
- More than 13,000 gene families (most not single copy)
- Multi-institutional project (10+ universities)
- iPLANT (NSF-funded cooperative)
- Gene sequence alignments and trees computed using SATe (Liu et al., Science 2009 and Systematic Biology 2012)

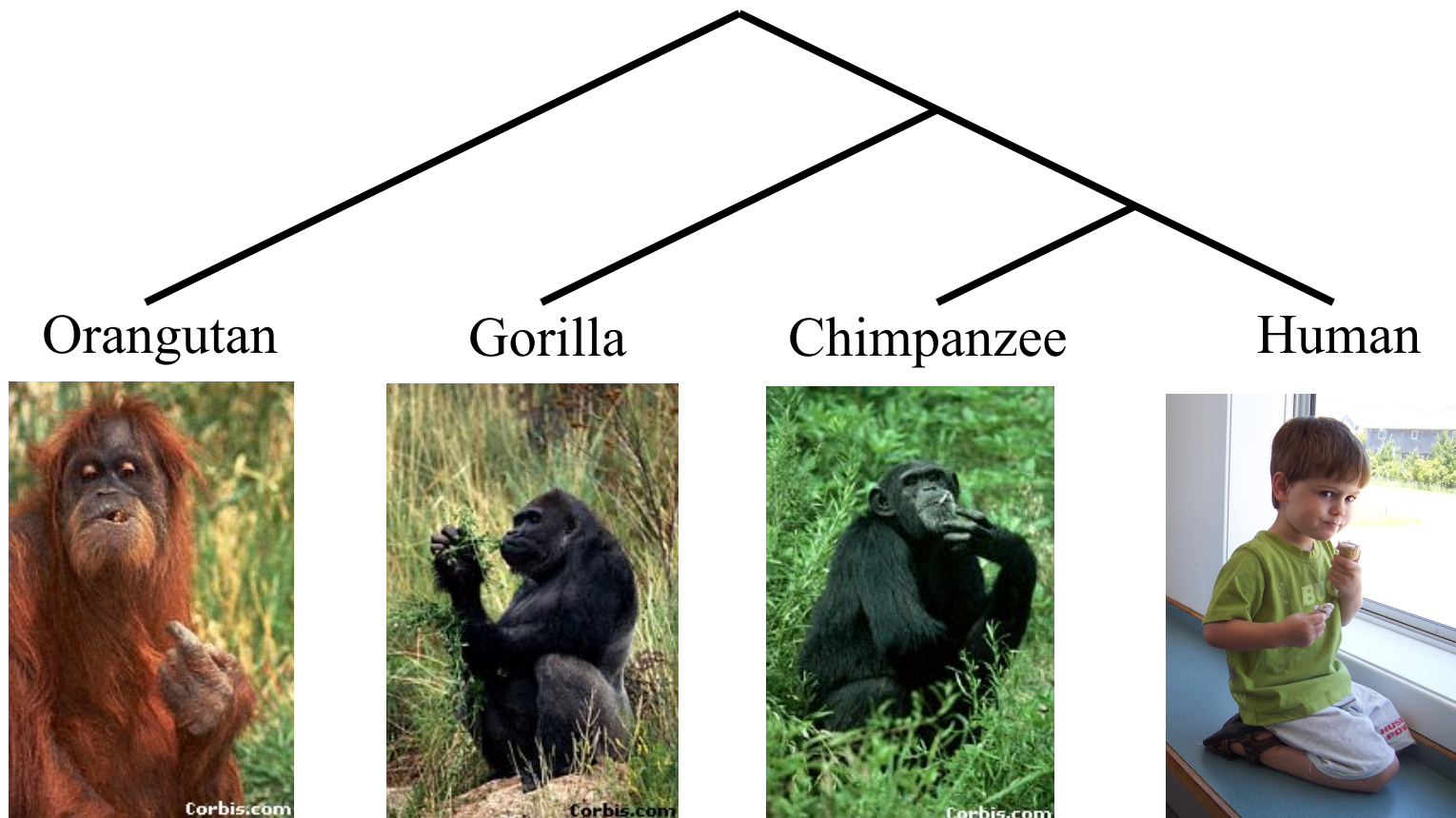
# Gene Tree Incongruence

- Gene trees can differ from the species tree due to:
  - Duplication and loss
  - Horizontal gene transfer
  - Incomplete lineage sorting (ILS)

# Incomplete Lineage Sorting (ILS)

- 1000+ papers in 2013 alone
- Confounds phylogenetic analysis for many groups:
  - Hominids
  - Birds
  - Yeast
  - Animals
  - Toads
  - Fish
  - Fungi
- There is substantial debate about how to analyze phylogenomic datasets in the presence of ILS.

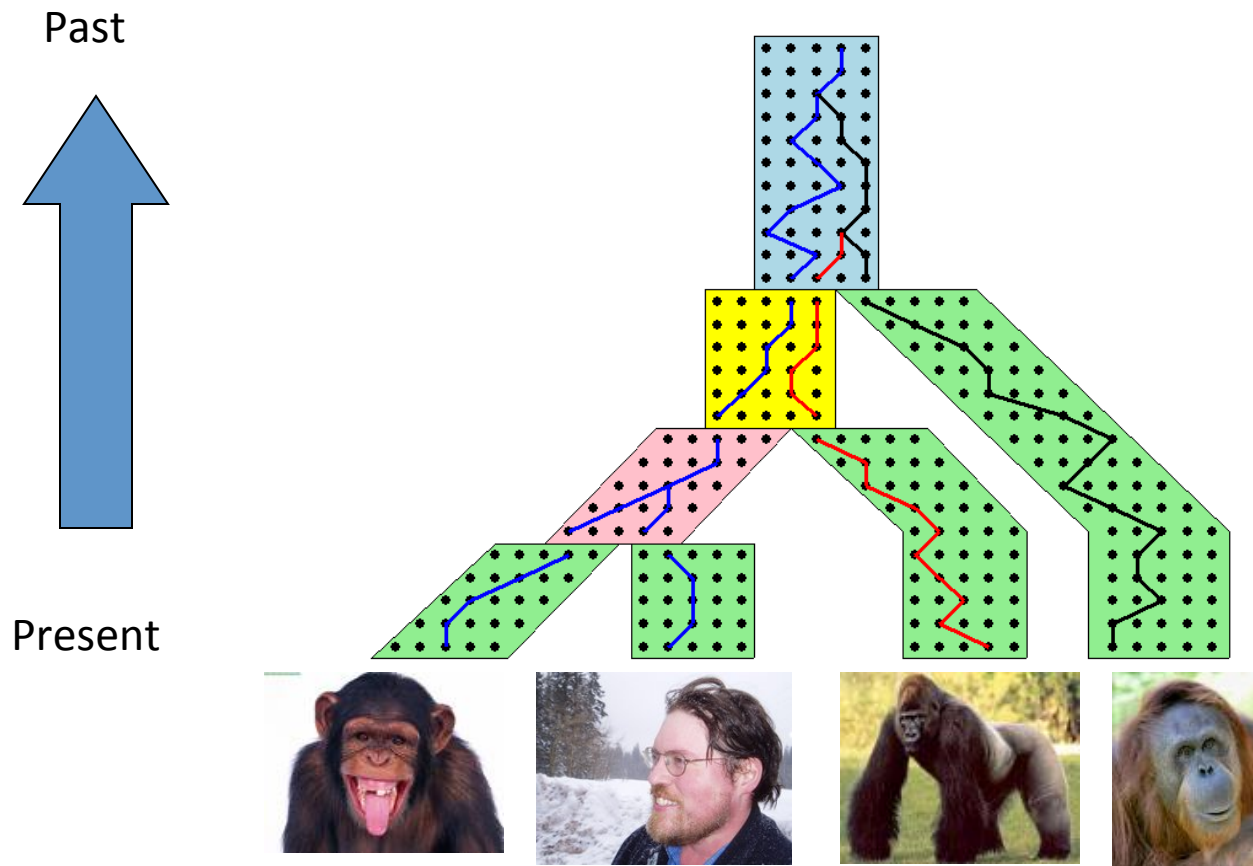
# Species tree estimation: difficult, even for small datasets!



*From the Tree of the Life Website,  
University of Arizona*

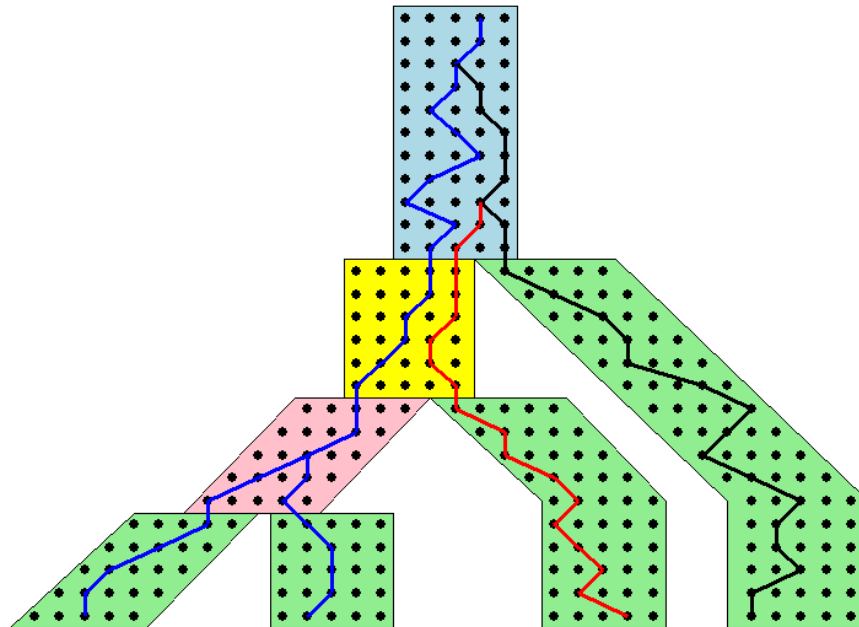
# The Coalescent

Courtesy James Degnan



# Gene tree in a species tree

Courtesy James Degnan

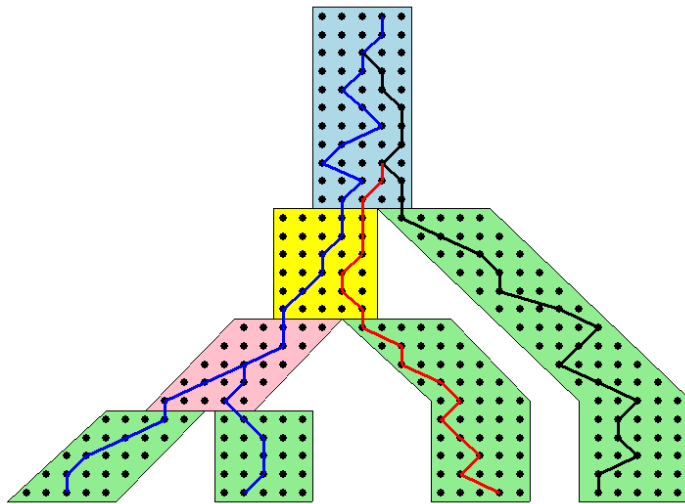


# Lineage Sorting

- Population-level process, also called the “Multi-species coalescent” (Kingman, 1982)
- Gene trees can differ from species trees due to short times between speciation events or large population size; this is called “Incomplete Lineage Sorting” or “Deep Coalescence”.

## Key observation:

Under the multi-species coalescent model, the species tree defines a *probability distribution on the gene trees, and is identifiable from the distribution on gene trees*

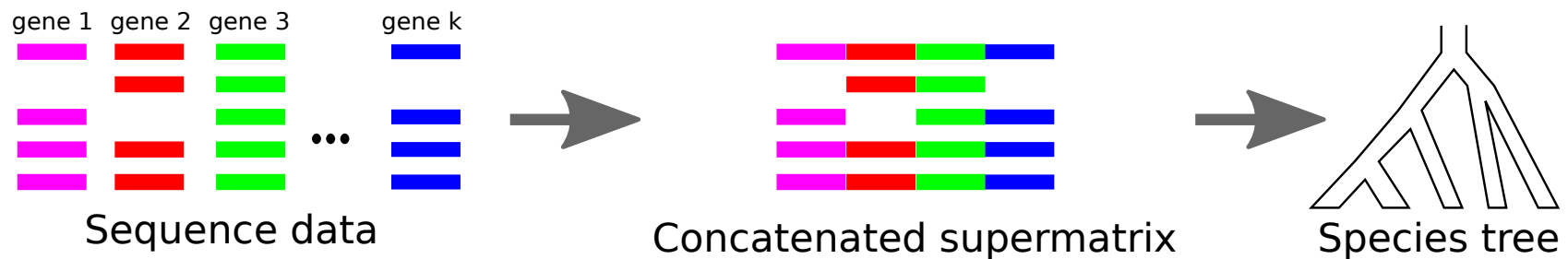


Courtesy James Degnan

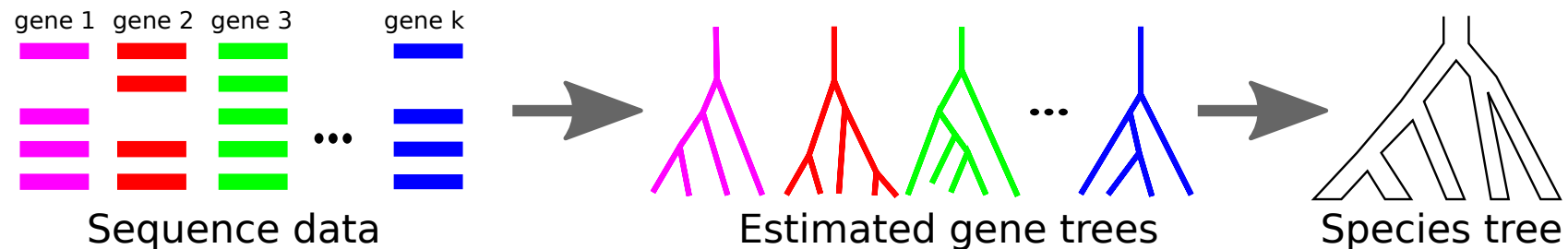


# Species tree estimation

**1- Concatenation:** statistically inconsistent (Roch & Steel 2014)

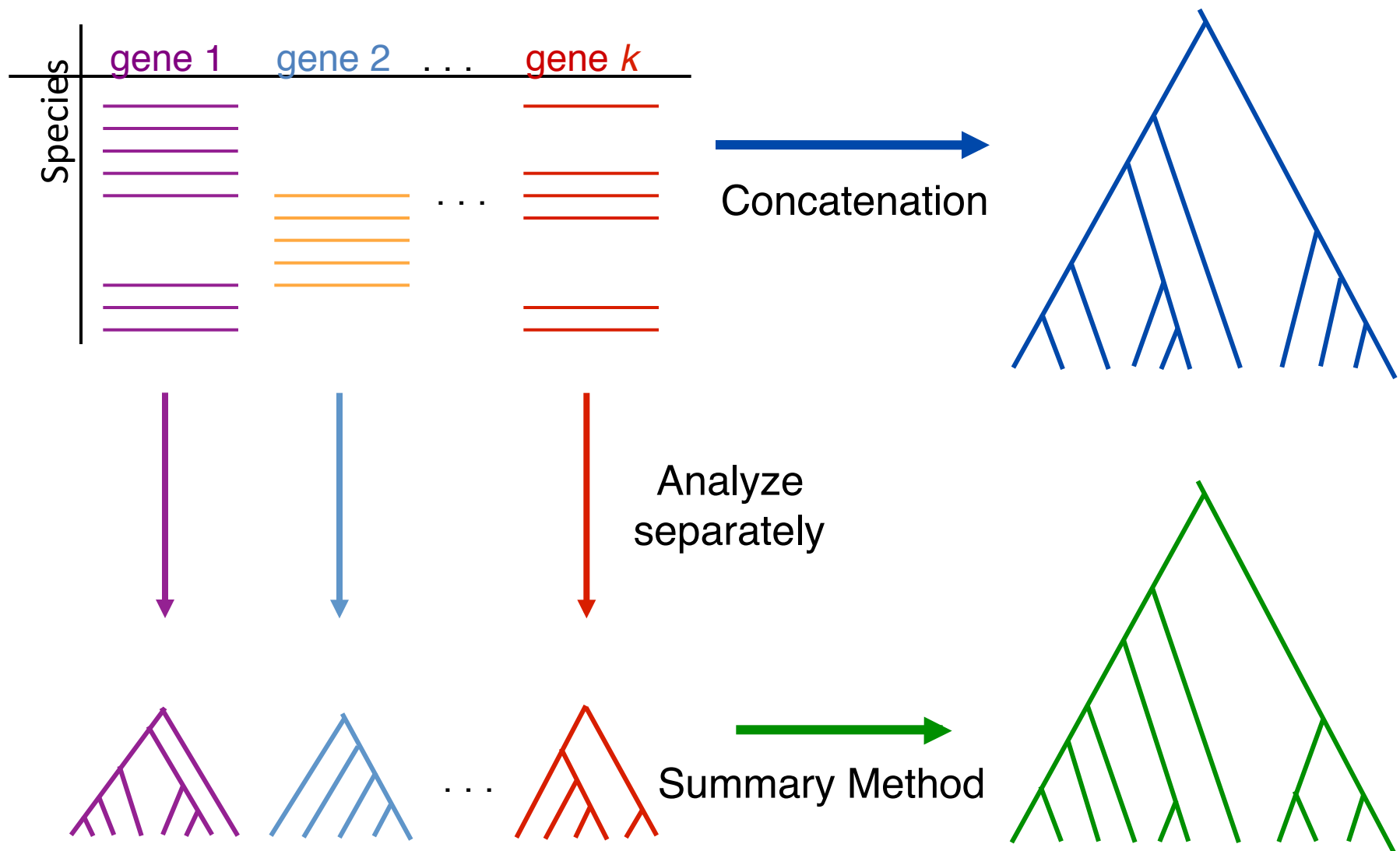


**2- Summary methods:** can be statistically consistent



**3- Co-estimation methods:** too slow for large datasets

# Two competing approaches



# How to compute a species tree?



# How to compute a species tree?



Techniques:

Most frequent gene tree?

Consensus of gene trees?

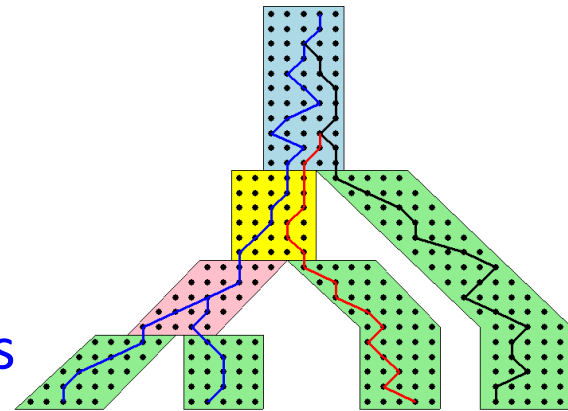
Other?



Under the multi-species coalescent model, the species tree defines a probability distribution on the gene trees

Courtesy James Degnan

Theorem (Degnan et al., 2006, 2009):  
Under the multi-species coalescent model, for any three taxa A, B, and C, the **most probable rooted gene tree** on {A,B,C} is identical to the rooted species tree induced on {A,B,C}.

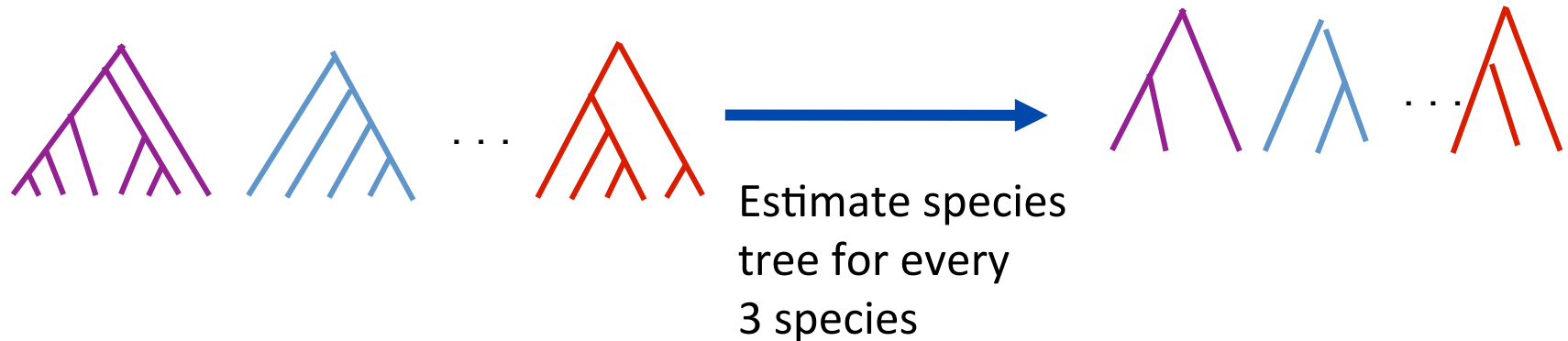


# How to compute a species tree?



Theorem (Degnan et al., 2006, 2009):  
Under the multi-species coalescent model, for any three taxa A, B, and C, the **most probable rooted gene tree** on  $\{A, B, C\}$  is identical to the rooted species tree induced on  $\{A, B, C\}$ .

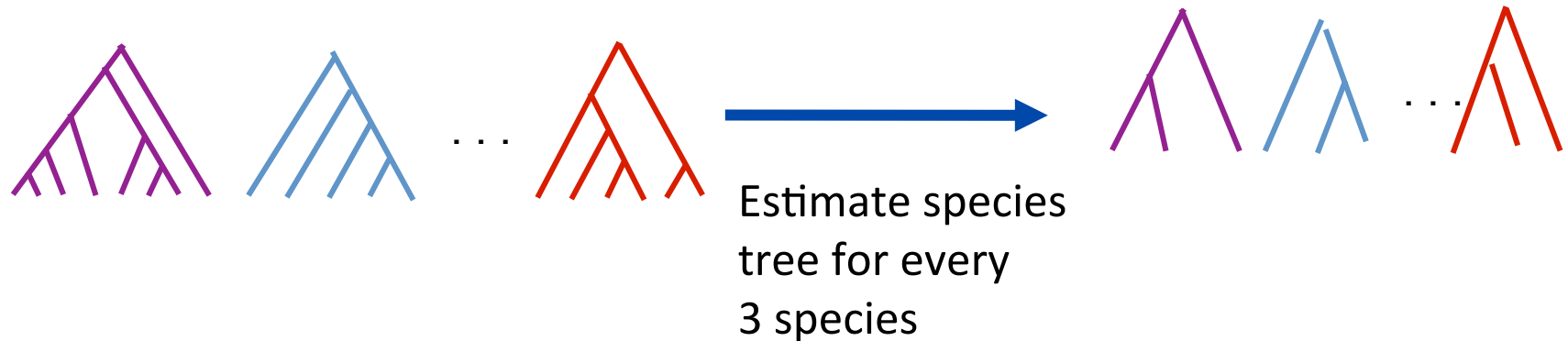
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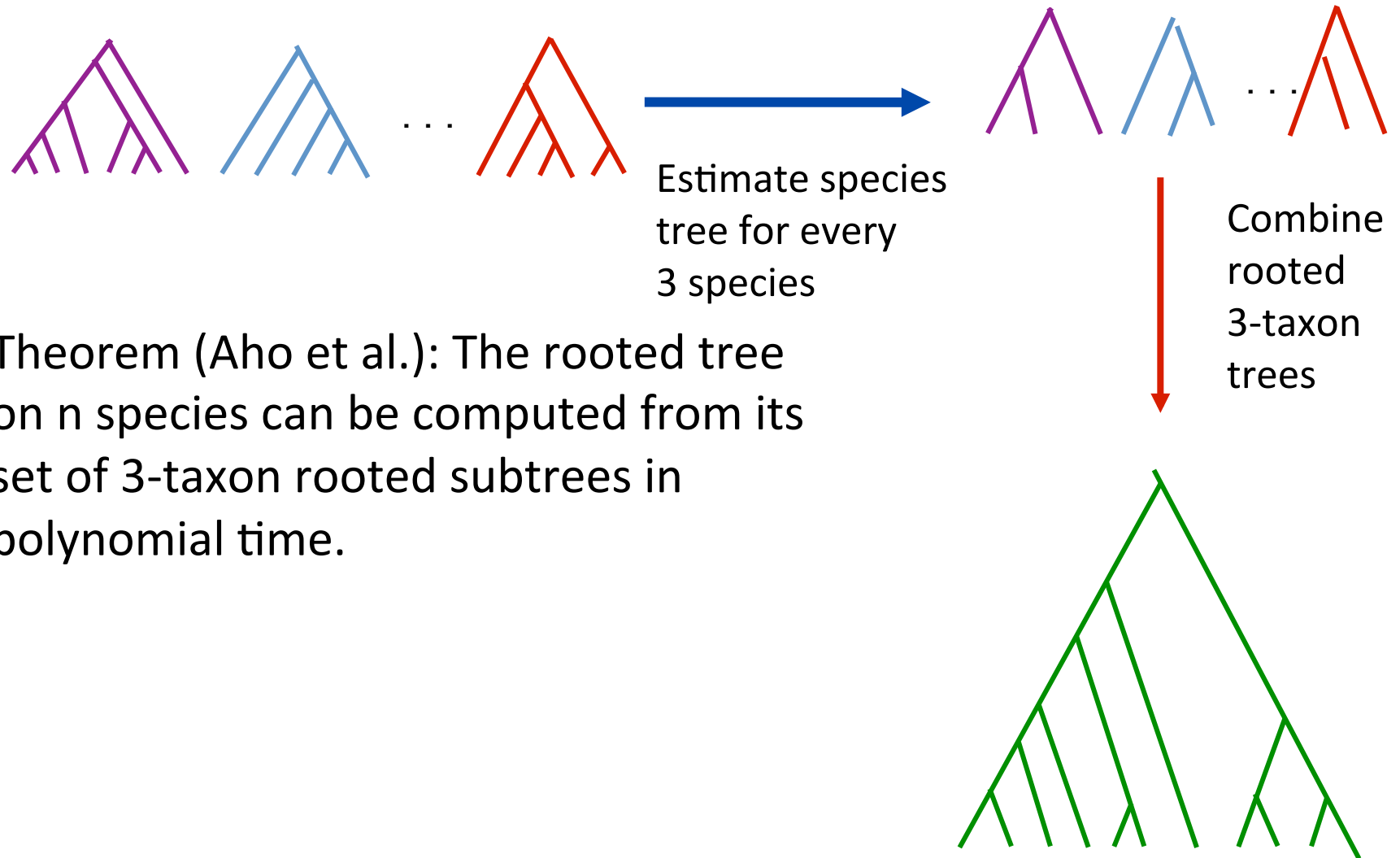
# How to compute a species tree?



Theorem (Aho et al.): The rooted tree on  $n$  species can be computed from its set of 3-taxon rooted subtrees in polynomial time.

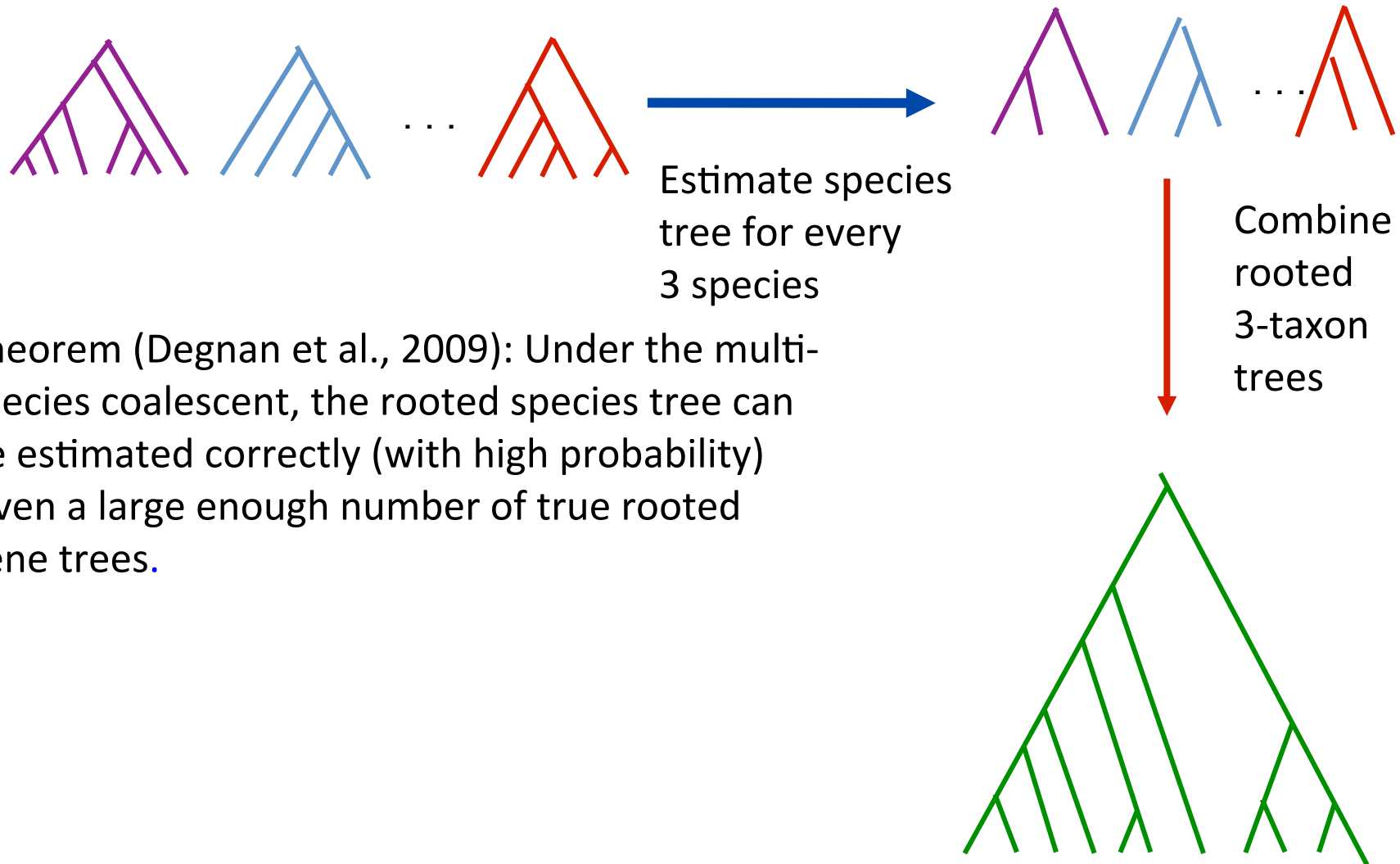


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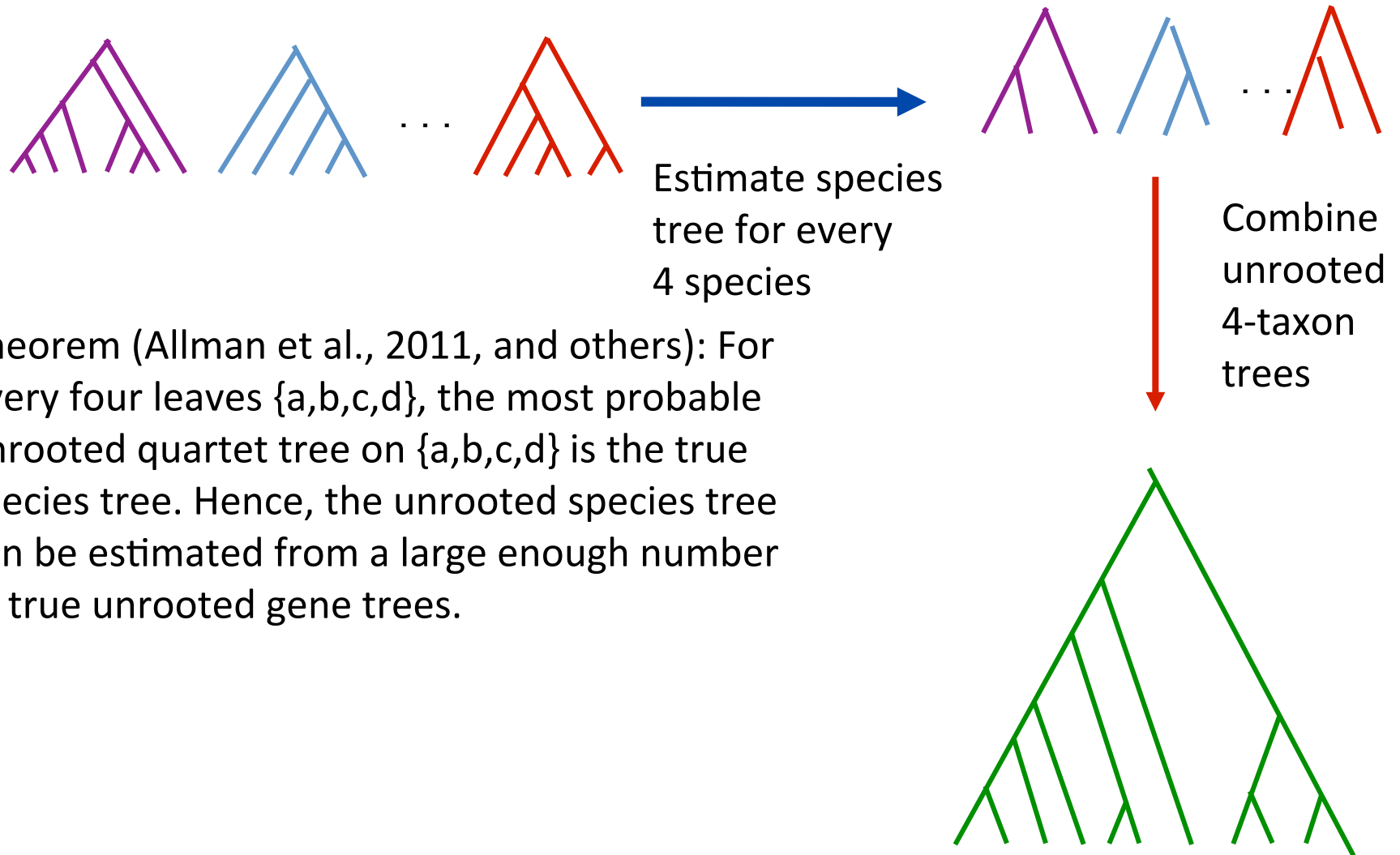
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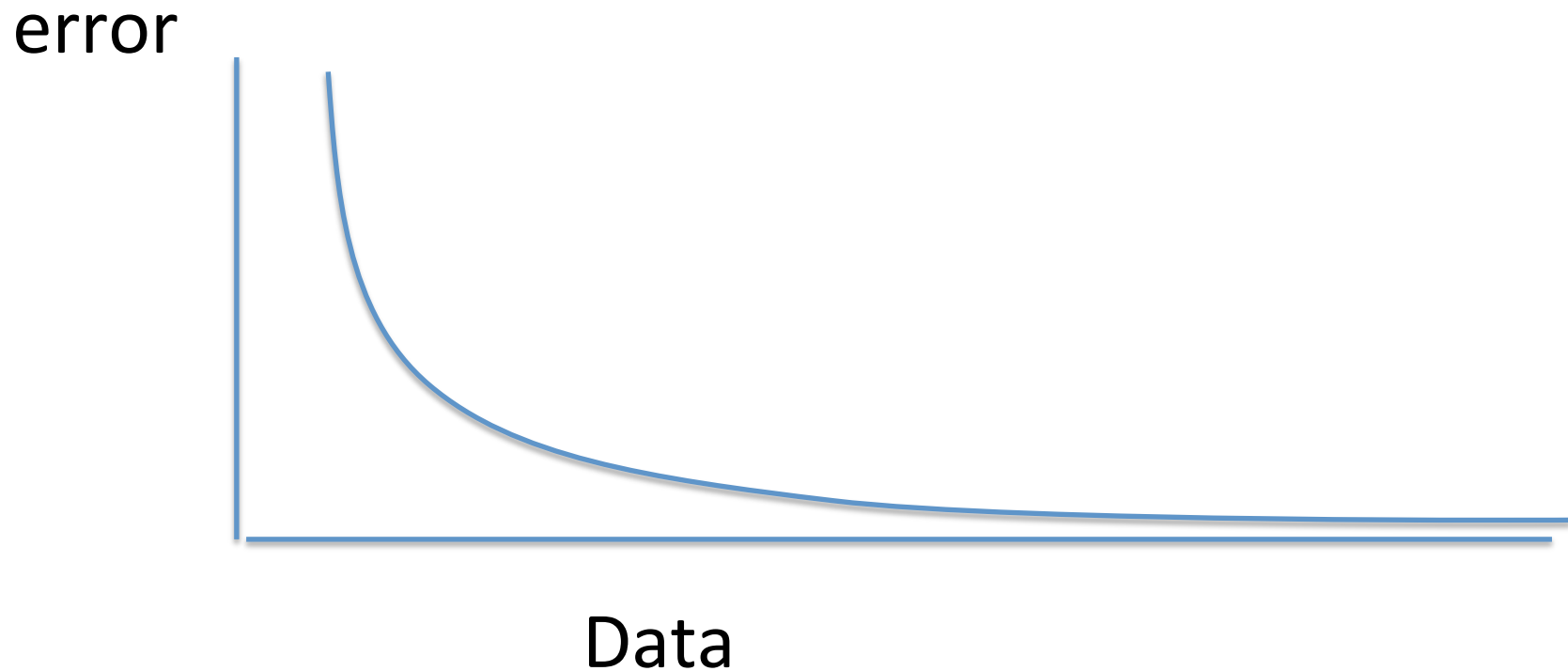
Theorem (Degnan et al., 2009): Under the multi-species coalescent, the rooted species tree can be estimated correctly (with high probability) given a large enough number of true rooted gene trees.

# How to compute a species tree?



Theorem (Allman et al., 2011, and others): For every four leaves  $\{a,b,c,d\}$ , the most probable unrooted quartet tree on  $\{a,b,c,d\}$  is the true species tree. Hence, the unrooted species tree can be estimated from a large enough number of true unrooted gene trees.

# Statistical Consistency

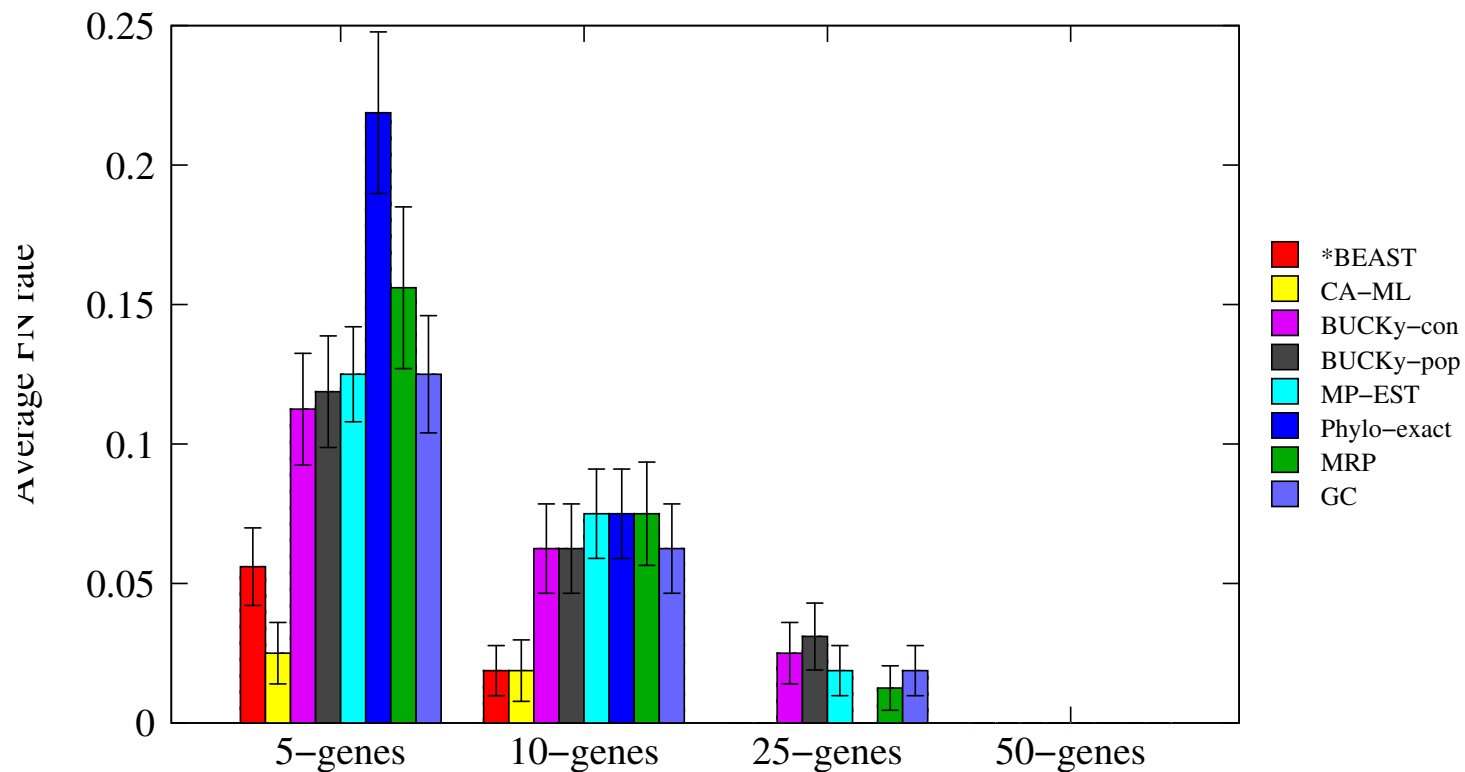


Data are gene trees, presumed to be randomly sampled true gene trees.

# Statistically consistent under ILS?

- **MP-EST** (Liu et al. 2010): maximum likelihood estimation of rooted species tree – YES
- BUCKy-pop (Ané and Larget 2010): quartet-based Bayesian species tree estimation –YES
- MDC – NO
- Greedy – NO
- Concatenation under maximum likelihood - NO
- MRP (supertree method) – open

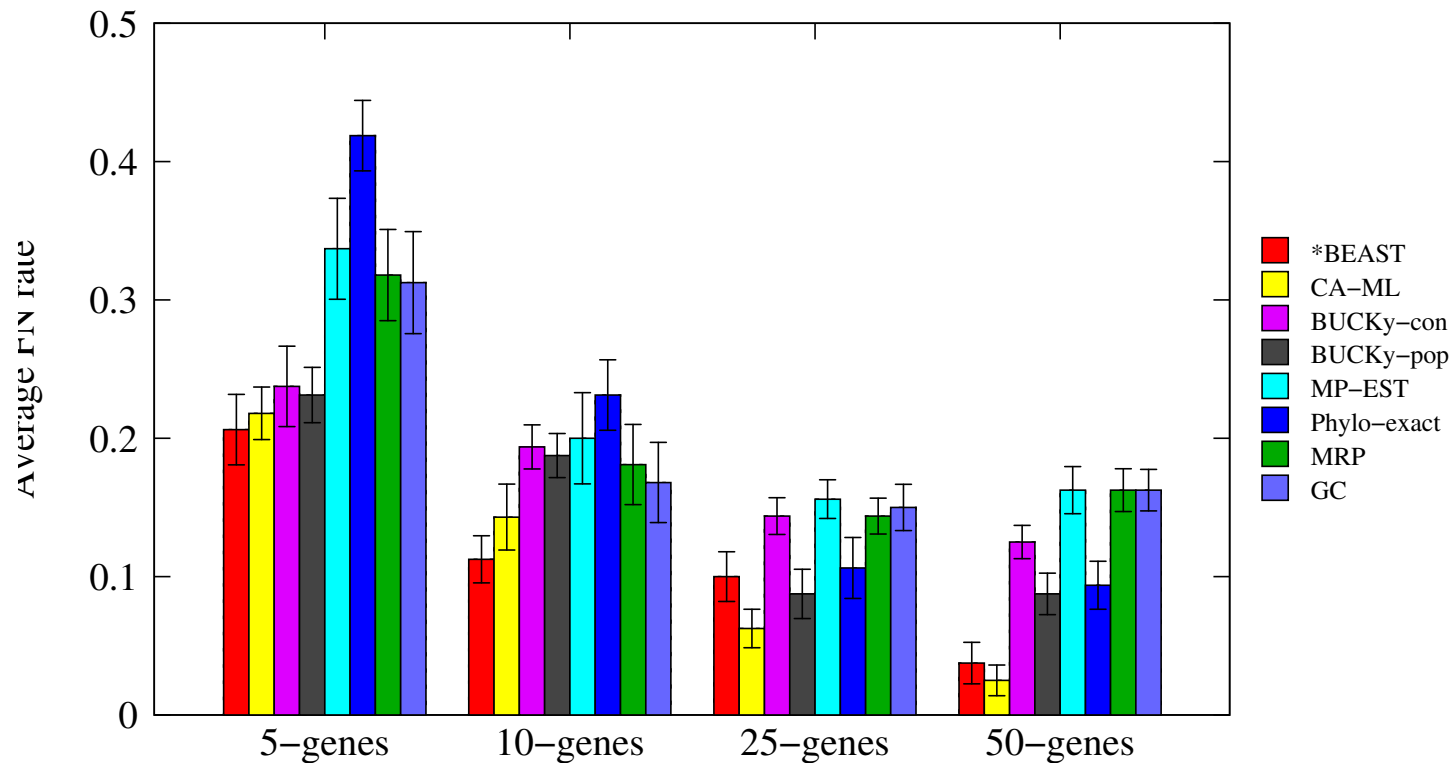
# Results on 11-taxon datasets with weak ILS



**\*BEAST** more accurate than summary methods (MP-EST, BUCKy, etc)  
CA-ML: concatenated analysis) most accurate

Datasets from Chung and Ané, 2011  
Bayzid & Warnow, Bioinformatics 2013

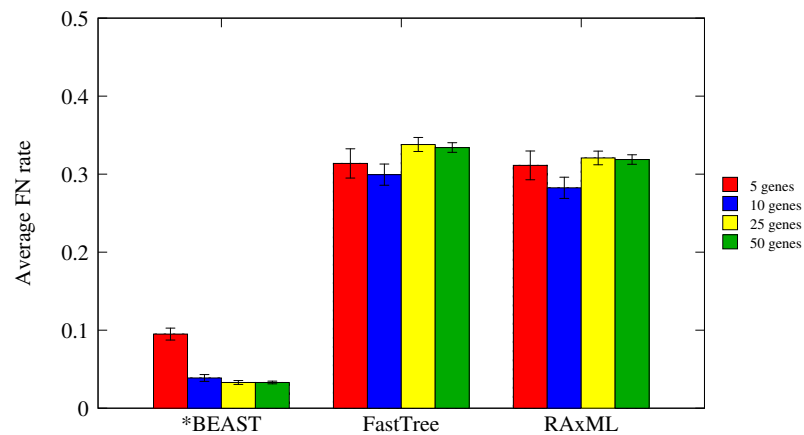
# Results on 11-taxon datasets with strongILS



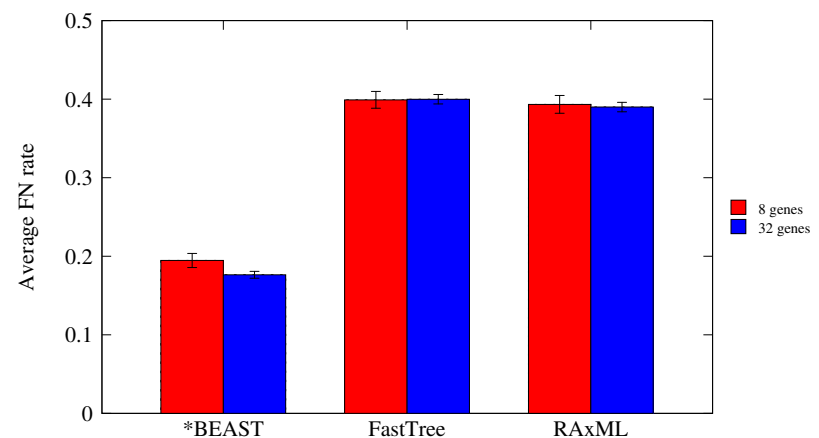
**\*BEAST** more accurate than summary methods (MP-EST, BUCKy, etc)  
CA-ML: (concatenated analysis) also very accurate

Datasets from Chung and Ané, 2011  
Bayzid & Warnow, Bioinformatics 2013

## \*BEAST co-estimation produces more accurate gene trees than Maximum Likelihood



11-taxon weakILS datasets



17-taxon (very high ILS) datasets

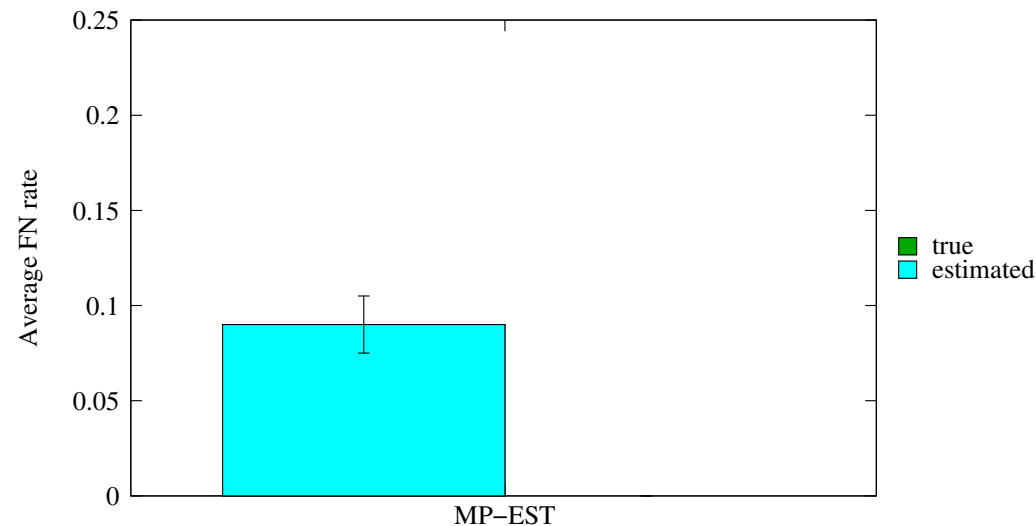
11-taxon datasets from Chung and Ané, Syst Biol 2012

17-taxon datasets from Yu, Warnow, and Nakhleh, JCB 2011

Bayzid & Warnow, Bioinformatics 2013



# Impact of Gene Tree Estimation Error on MP-EST



MP-EST has **no error on true gene trees**, but  
MP-EST has **9% error on estimated gene trees**

Datasets: 11-taxon strongILS conditions with 50 genes

Similar results for other summary methods (MDC, Greedy, etc.).

# Problem: poor gene trees

- Summary methods combine estimated gene trees, not true gene trees.

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- The individual gene sequence alignments in the 11-taxon datasets have poor phylogenetic signal, and result in poorly estimated gene trees.
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**TYPICAL PHYLOGENOMICS PROBLEM:**  
many poor gene trees

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- The individual gene sequence alignments in the 11-taxon datasets have poor phylogenetic signal, and result in poorly estimated gene trees.
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# Addressing gene tree estimation error

- Get better estimates of the gene trees
- Restrict to subset of estimated gene trees
- Model error in the estimated gene trees
- Modify gene trees to reduce error
- Develop methods with greater robustness to gene tree error

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  - ASTRAL. Bioinformatics 2014 (Mirarab et al.)
  - Statistical binning. In press (Mirarab et al.)

# Avian Phylogenomics Project

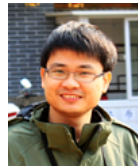
E Jarvis,  
HHMI



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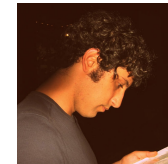
G Zhang,  
BGI



T. Warnow  
UT-Austin



S. Mirarab  
UT-Austin



Md. S. Bayzid,  
UT-Austin



- Approx. 50 species, whole genomes
  - 8000+ genes, UCEs
  - Gene sequence alignments computed using SATé (Liu et al., Science 2009 and Systematic Biology 2012)
- Plus many many other people...

**Species tree estimated using Statistical Binning with MP-EST  
In press**



# 1KP: Thousand Transcriptome Project



G. Ka-Shu Wong  
U Alberta



J. Leebens-Mack  
U Georgia



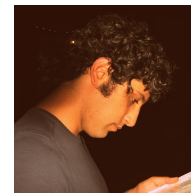
N. Wickett  
Northwestern



N. Matasci  
iPlant



T. Warnow,  
UT-Austin



S. Mirarab,  
UT-Austin



N. Nguyen,  
UT-Austin



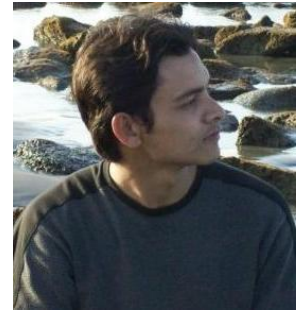
Md. S. Bayzid  
UT-Austin

- 1200 plant transcriptomes
  - More than 13,000 gene families (most not single copy)
  - Gene sequence alignments and trees computed using SATe (Liu et al., Science 2009 and Systematic Biology 2012)
- Plus many other people...

**Species tree estimated using ASTRAL (Bioinformatics, 2014)**  
**In press**



# Statistical binning



Input: estimated gene trees with bootstrap support, and minimum **support threshold  $t$**

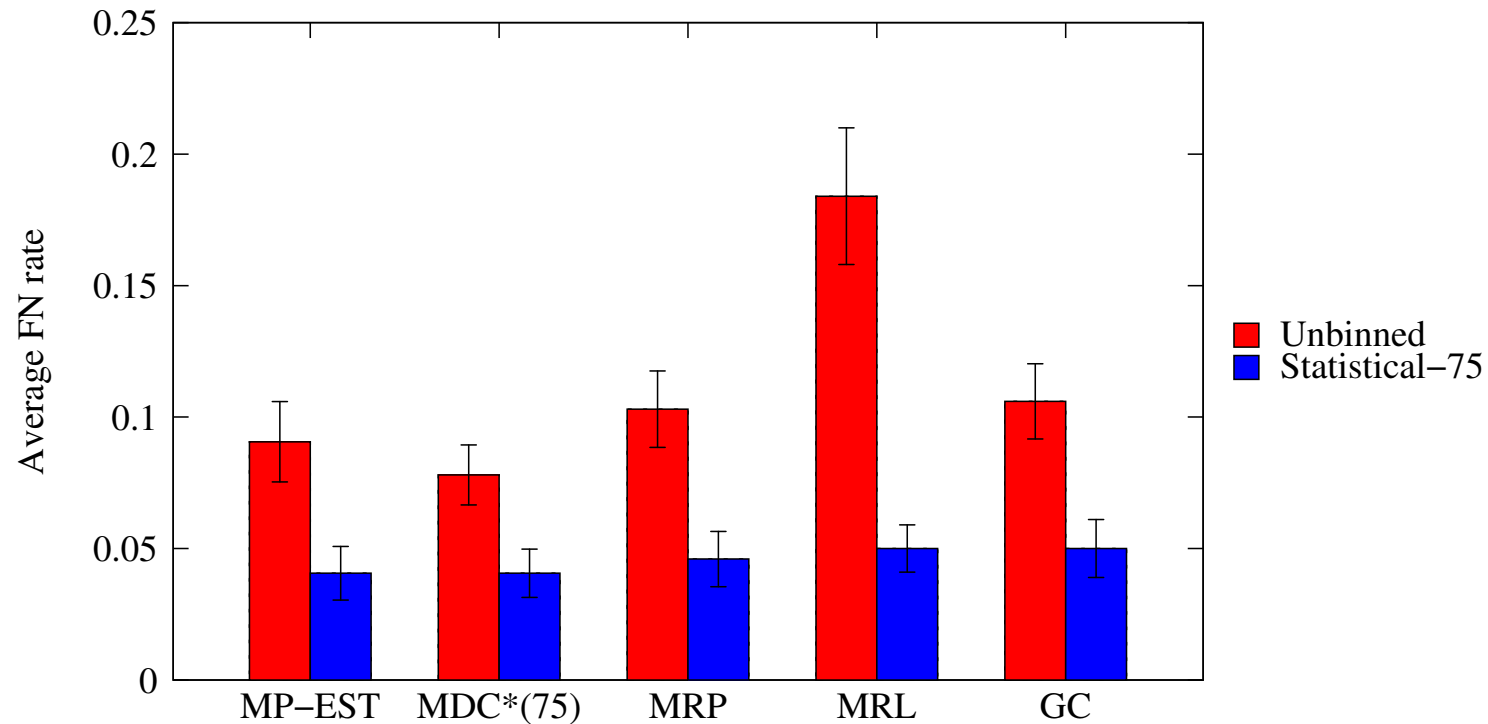
Step 1: partition of the estimated gene trees into sets, so that no two gene trees in the same set are strongly incompatible, and the sets have approximately the same size.

Step 2: estimate “supergene” trees on each set using concatenation (maximum likelihood)

Step 3: combine supergene trees using coalescent-based method

**Note: Step 1 requires solving the NP-hard “balanced vertex coloring problem”, for which we developed a good heuristic (modified 1979 Brelaz algorithm)**

# Statistical binning vs. unbinned

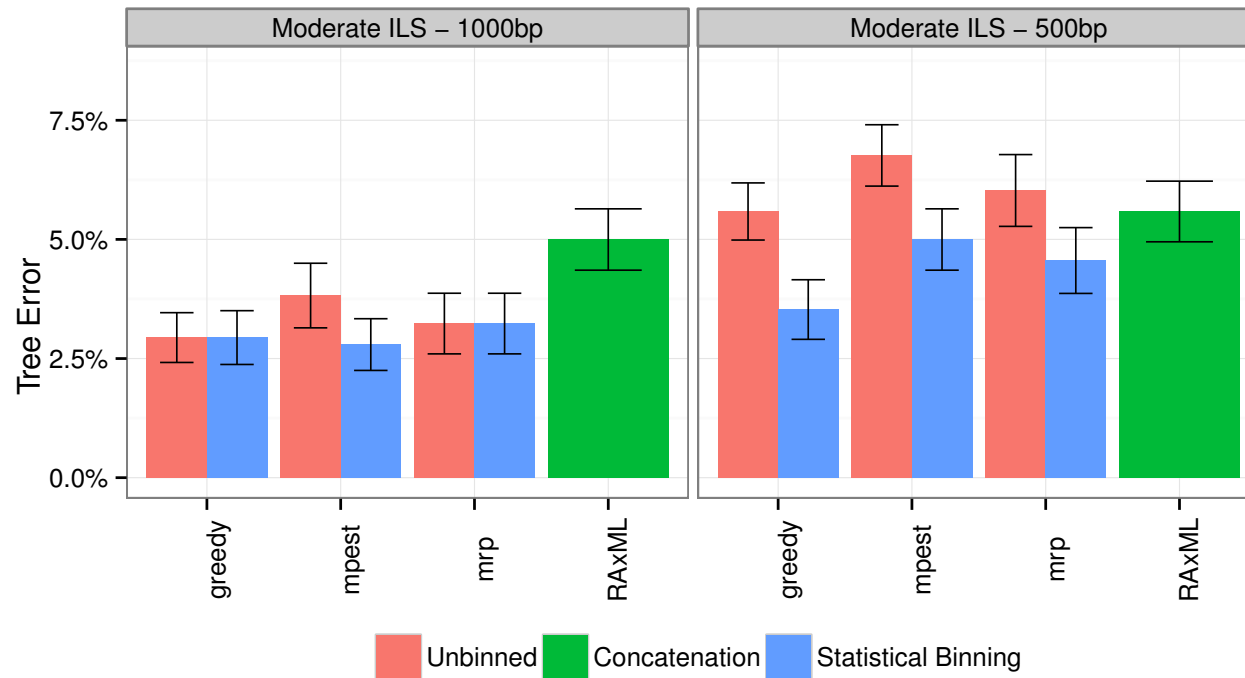


Mirarab, et al., to appear (Science 2014)

Binning produces bins with approximate 5 to 7 genes each

Datasets: 11-taxon strongILS datasets with 50 genes, Chung and Ané, Systematic Biology

# Mammalian Simulation Study



## Observations:

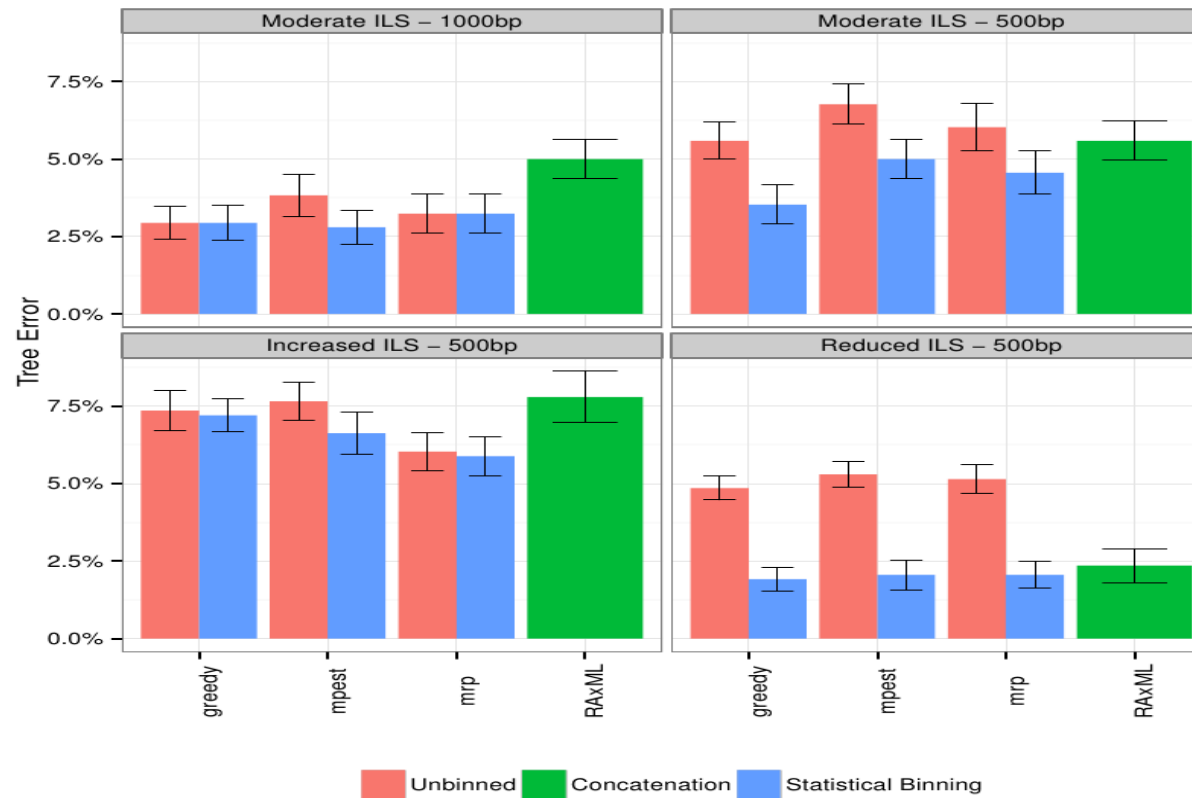
Binning can improve accuracy, but impact depends on accuracy of estimated gene trees and phylogenetic estimation method.

Binned methods can be more accurate than RAxML (maximum likelihood), even when unbinned methods are less accurate.

Data: 200 genes, 20 replicate datasets, based on Song et al. PNAS 2012

Mirarab et al., to appear

# Mammalian simulation



## Observation:

Binning can improve summary methods, but amount of improvement depends on method, amount of ILS, number of gene trees, and gene tree estimation error.

MP-EST is statistically consistent; Greedy and Maximum Likelihood are not; unknown for MRP.  
Data (200 genes, 20 replicate datasets) based on Song et al. PNAS 2012

# ASTRAL

- Accurate Species Trees Algorithm
- Mirarab et al., ECCB 2014 and Bioinformatics 2014
- Statistically-consistent estimation of the species tree from unrooted gene trees

# ASTRAL's approach

- Input: set of unrooted gene trees  $T_1, T_2, \dots, T_k$
- Output: Tree  $T^*$  maximizing the total quartet-similarity score to the unrooted gene trees

Theorem:

- An exact solution to this problem would be a statistically consistent algorithm in the presence of ILS

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- Output: Tree  $T^*$  maximizing the total quartet-similarity score to the unrooted gene trees

Theorem:

- An exact solution to this problem is NP-hard

Comment: unknown computational complexity  
if all trees  $T_i$  are on the same leaf set



# ASTRAL's approach

- Input: set of unrooted gene trees  $T_1, T_2, \dots, T_k$  and set  $X$  of bipartitions on species set  $S$
- Output: Tree  $T^*$  maximizing the total quartet-similarity score to the unrooted gene trees, subject to  $\text{Bipartitions}(T^*)$  drawn from  $X$

Theorem:

- An exact solution to this problem is achievable in polynomial time!

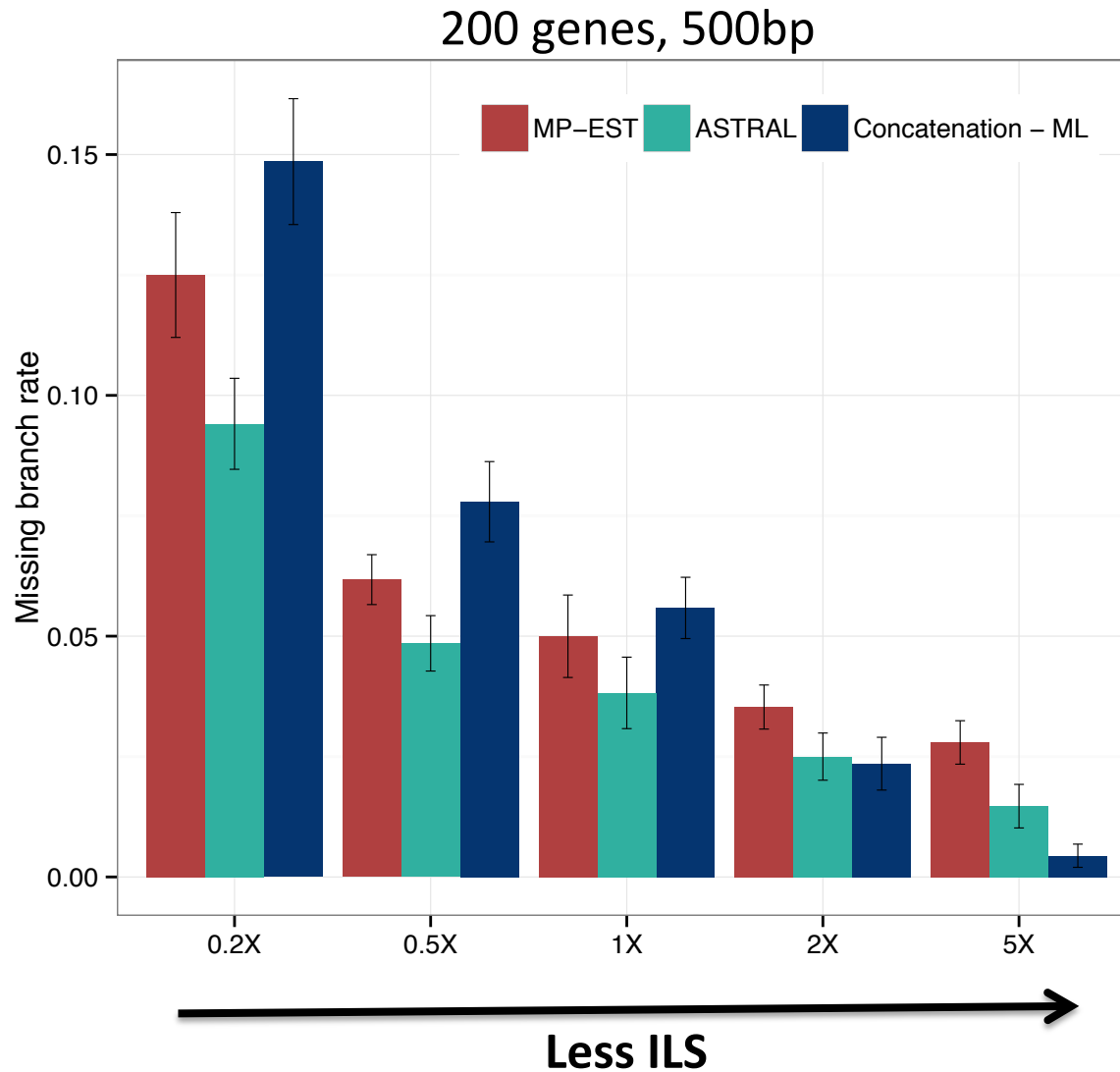
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## Theorem:

- Letting  $X$  be the set of bipartitions from the input gene trees is statistically consistent and polynomial time.

# ASTRAL vs. Concatenation



# Basic Question

- Is it possible to estimate the species tree with high probability given a large enough set of estimated gene trees, each with some non-zero probability of error?



## Partial answers

Theorem (Roch & Warnow, in preparation): If gene sequence evolution obeys the strong molecular clock, then statistically consistent estimation is possible – even where all gene trees are estimated based on a single site.



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Theorem (Roch & Warnow, in preparation): If gene sequence evolution obeys the strong molecular clock, then statistically consistent estimation is possible – even where all gene trees are estimated based on a single site.

Proof (sketch): Under the multi-species coalescent model, the most probable rooted triplet gene tree on  $\{a,b,c\}$  is the true species tree for  $\{a,b,c\}$ , and this remains true (when the molecular clock holds) *even for triplet gene trees estimated on a single site*.



# When molecular clock fails

- Without the molecular clock, the estimation of the species tree is based on quartet trees.



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- Without the molecular clock, the estimation of the species tree is based on quartet trees.
- Although the most probable quartet tree is still the true species tree, this is *no longer true for estimated quartet trees – except for very long sequences.*
- *No positive results established for any of the current coalescent-based methods in use!*

# Summary

## Gene tree estimation under Markov models of evolution:

- Absolute fast converging (afc) methods: true trees from polynomial length sequences.

## Coalescent-based species tree estimation:

- Gene tree estimation error impacts species tree estimation.
- Statistical binning (in press) improves coalescent-based species tree estimation from multiple genes, used in Avian Tree (in press).
- ASTRAL (Bioinformatics, 2014) more robust to gene tree estimation error, used in Plant Tree (in press).
- Identifiability in the presence of gene tree estimation error? Yes under the strong molecular clock, very limited results otherwise.
- New questions about statistical inference, focusing on the impact of input error.

# Computational Phylogenetics

Interesting combination of different mathematics and computer science:

- statistical estimation under Markov models of evolution
- mathematical modelling
- graph theory and combinatorics
- machine learning and data mining
- heuristics for NP-hard optimization problems
- high performance computing

Testing involves massive simulations

# Acknowledgments



PhD students: Siavash Mirarab\* and Md. S. Bayzid\*\*  
Sebastien Roch (Wisconsin) – work began at IPAM (UCLA)

**Funding:** Guggenheim Foundation, Packard, NSF, Microsoft Research New England, David Bruton Jr. Centennial Professorship, TACC (Texas Advanced Computing Center), and GEBCO.

**TACC** and UTCS computational resources

\* Supported by HHMI Predoctoral Fellowship

\*\* Supported by Fulbright Foundation Predoctoral Fellowship

## Bin-and-Conquer?

1. Assign genes to “bins”, creating “supergene alignments”
2. Estimate trees on each supergene alignment using maximum likelihood
3. Combine the supergene trees together using a summary method

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## Variants:

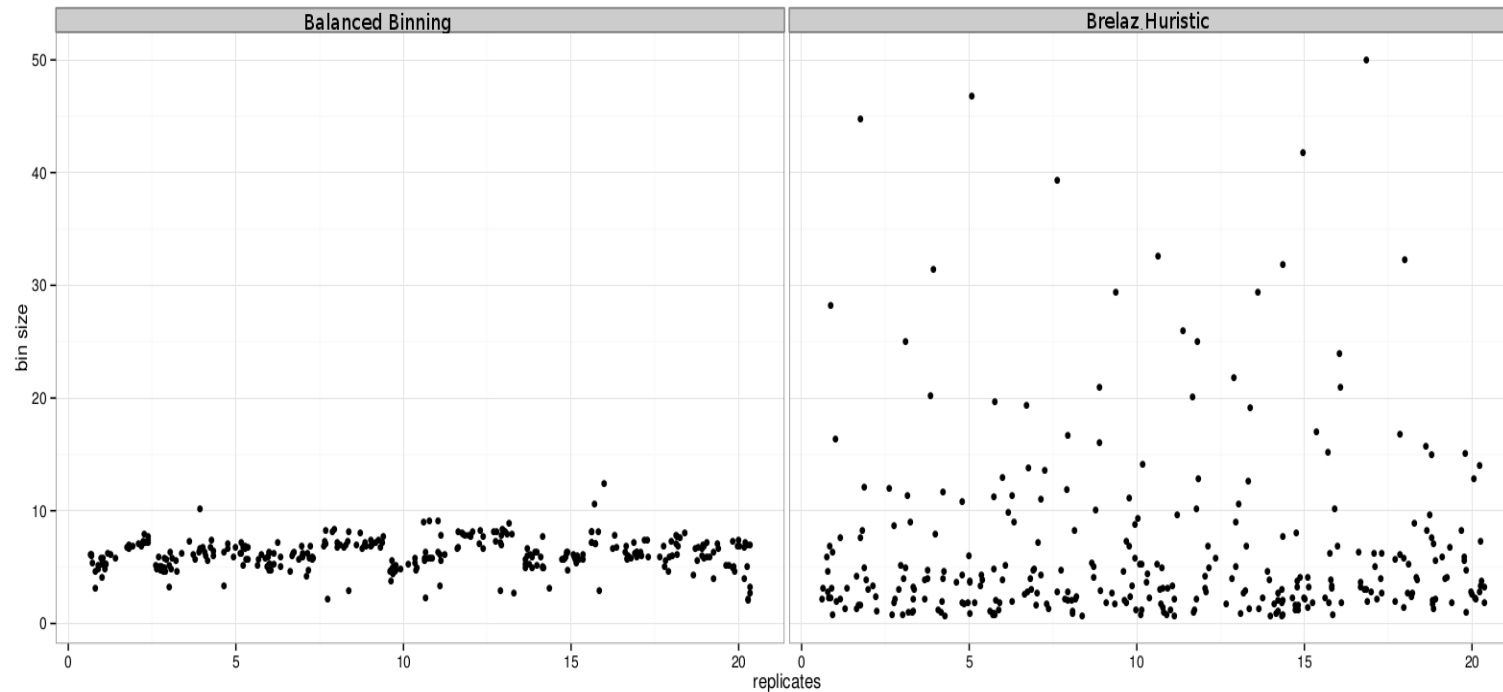
- Naïve binning (Bayzid and Warnow, Bioinformatics 2013)
- Statistical binning (Mirarab, Bayzid, and Warnow, to appear, Science)

# Statistical binning

Input: estimated gene trees with bootstrap support, and minimum support threshold  $t$

Output: partition of the estimated gene trees into sets, so that no two gene trees in the same set are strongly incompatible.

# Balanced Statistical Binning



Mirarab, Bayzid, and Warnow, in preparation  
Modification of Brelaz Heuristic for minimum vertex coloring.



# Avian Phylogenomics Project

E Jarvis,  
HHMI



MTP Gilbert,  
Copenhagen



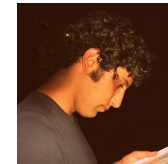
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Gene Tree Incongruence

Plus many many other people...

# Avian Phylogeny

- GTRGAMMA Maximum likelihood analysis (RAxML) of 37 million basepair alignment (exons, introns, UCEs) – highly resolved tree with near 100% bootstrap support.
- More than 17 years of compute time, and used 256 GB. Run at HPC centers.

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- Unbinned MP-EST on 14000+ genes: highly incongruent with the concatenated maximum likelihood analysis, poor bootstrap support.

# Avian Simulation – 14,000 genes

- **MP-EST:**
  - Unbinned ~ 11.1% error
  -
- **Greedy:**
  - Unbinned ~ 26.6% error
  -
- 8250 exon-like genes (27% avg. bootstrap support)
- 3600 UCE-like genes (37% avg. bootstrap support)
- 2500 intron-like genes (51% avg. bootstrap support)

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- **MP-EST:**
  - Unbinned ~ 11.1% error
  - Binned ~ 6.6% error
- **Greedy:**
  - Unbinned ~ 26.6% error
  - Binned ~ 13.3% error
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- More than 17 years of compute time, and used 256 GB. Run at HPC centers.
- Unbinned MP-EST on 14000+ genes: highly incongruent with the concatenated maximum likelihood analysis, poor bootstrap support.
- Statistical binning version of MP-EST on 14000+ gene trees – highly resolved tree, largely congruent with the concatenated analysis, good bootstrap support

# To consider

- Binning *reduces the amount* of data (number of gene trees) but can improve the accuracy of individual “supergene trees”. The response to binning differs between methods. Thus, there is a **trade-off between data quantity and quality**, *and not all methods respond the same to the trade-off*.
- We know very little about the **impact of data error** on methods. **We do not even have proofs of statistical consistency in the presence of data error.**



# Other recent related work

- ASTRAL: statistically consistent method for species tree estimation under the multi-species coalescent (Mirarab et al., Bioinformatics 2014)
- DCM-boosting coalescent-based methods (Bayzid et al., RECOMB-CG and BMC Genomics 2014)
- Weighted Statistical Binning (Bayzid et al., in preparation) – statistically consistent version of statistical binning

# Other Research in my lab

Method development for

- Supertree estimation
- Multiple sequence alignment
- Metagenomic taxon identification
- Genome rearrangement phylogeny
- Historical Linguistics

Techniques:

- Statistical estimation under Markov models of evolution
- Graph theory and combinatorics
- Machine learning and data mining
- Heuristics for NP-hard optimization problems
- High performance computing
- Massive simulations

# Research Agenda

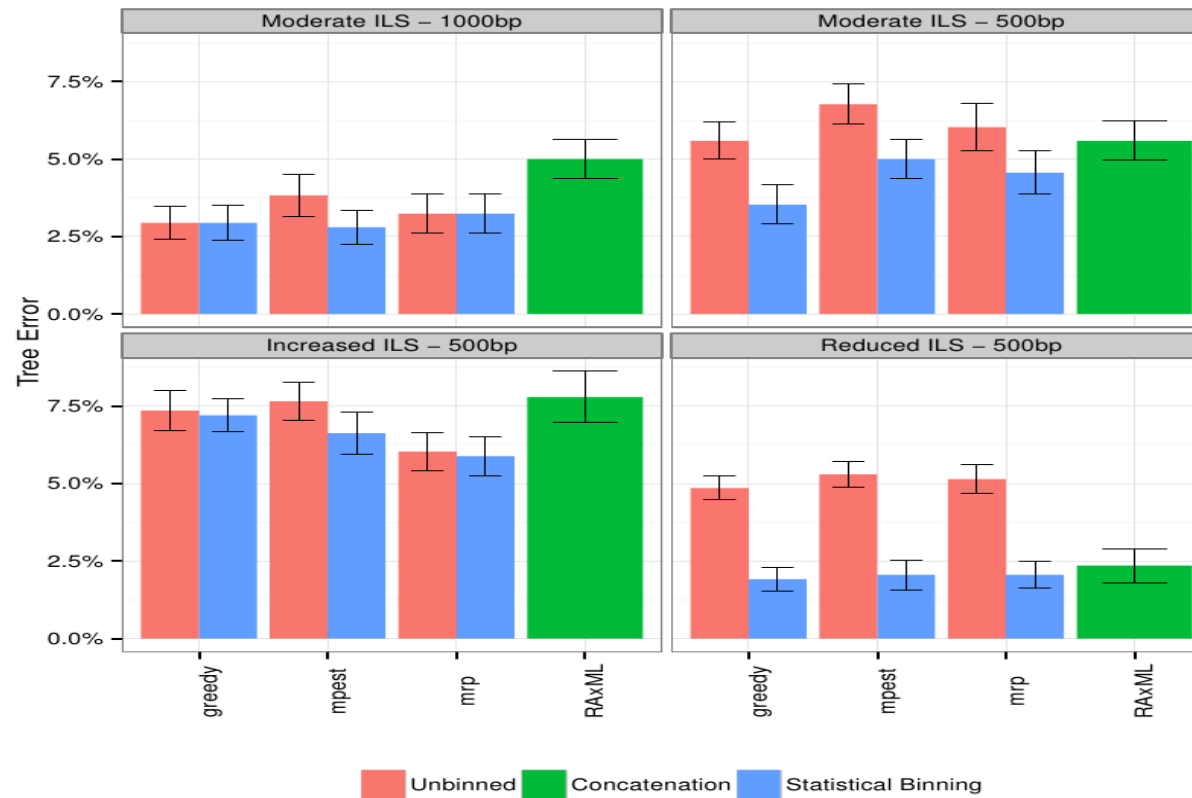
Major scientific goals:

- Develop **methods** that produce more accurate alignments and phylogenetic estimations for *difficult-to-analyze datasets*
- Produce **mathematical theory** for statistical inference under complex models of evolution
- Develop **novel machine learning techniques** to boost the performance of classification methods

Software that:

- Can run efficiently on *desktop* computers on large datasets
- Can analyze ultra-large datasets (100,000+) using multiple processors
- Is freely available in *open source* form, with biologist-friendly GUIs

# Mammalian simulation



Observation:

Binning can improve summary methods, but amount of improvement depends on: method, amount of ILS, and accuracy of gene trees.

MP-EST is statistically consistent in the presence of ILS; Greedy is not, unknown for MRP And RAxML.

Data (200 genes, 20 replicate datasets) based on Song et al. PNAS 2012

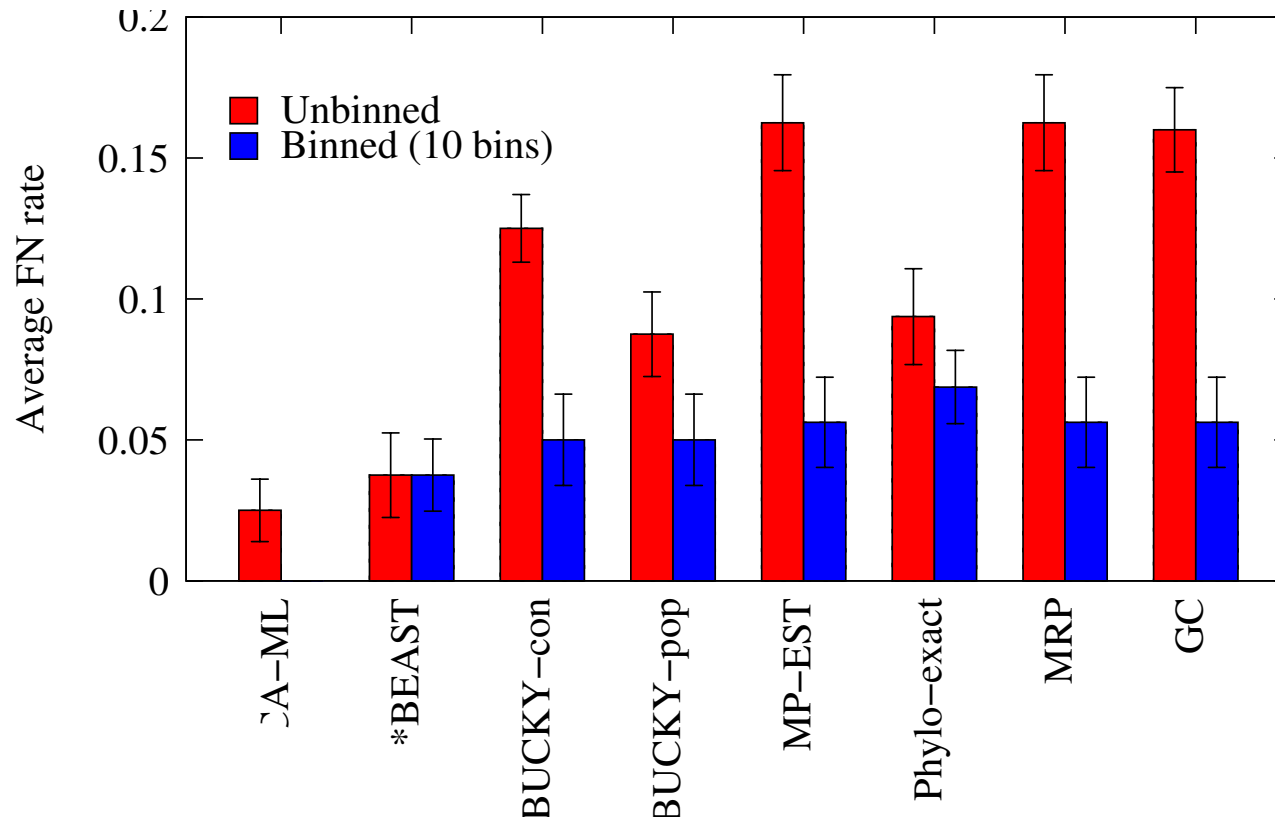
# Statistically consistent methods

**Input:** Set of estimated gene trees or alignments, one (or more) for each gene

**Output:** estimated species tree

- **\*BEAST** (Heled and Drummond 2010): Bayesian co-estimation of gene trees and species trees given sequence alignments
- **MP-EST** (Liu et al. 2010): maximum likelihood estimation of rooted species tree
- **BUCKy-pop** (Ané and Larget 2010): quartet-based Bayesian species tree estimation

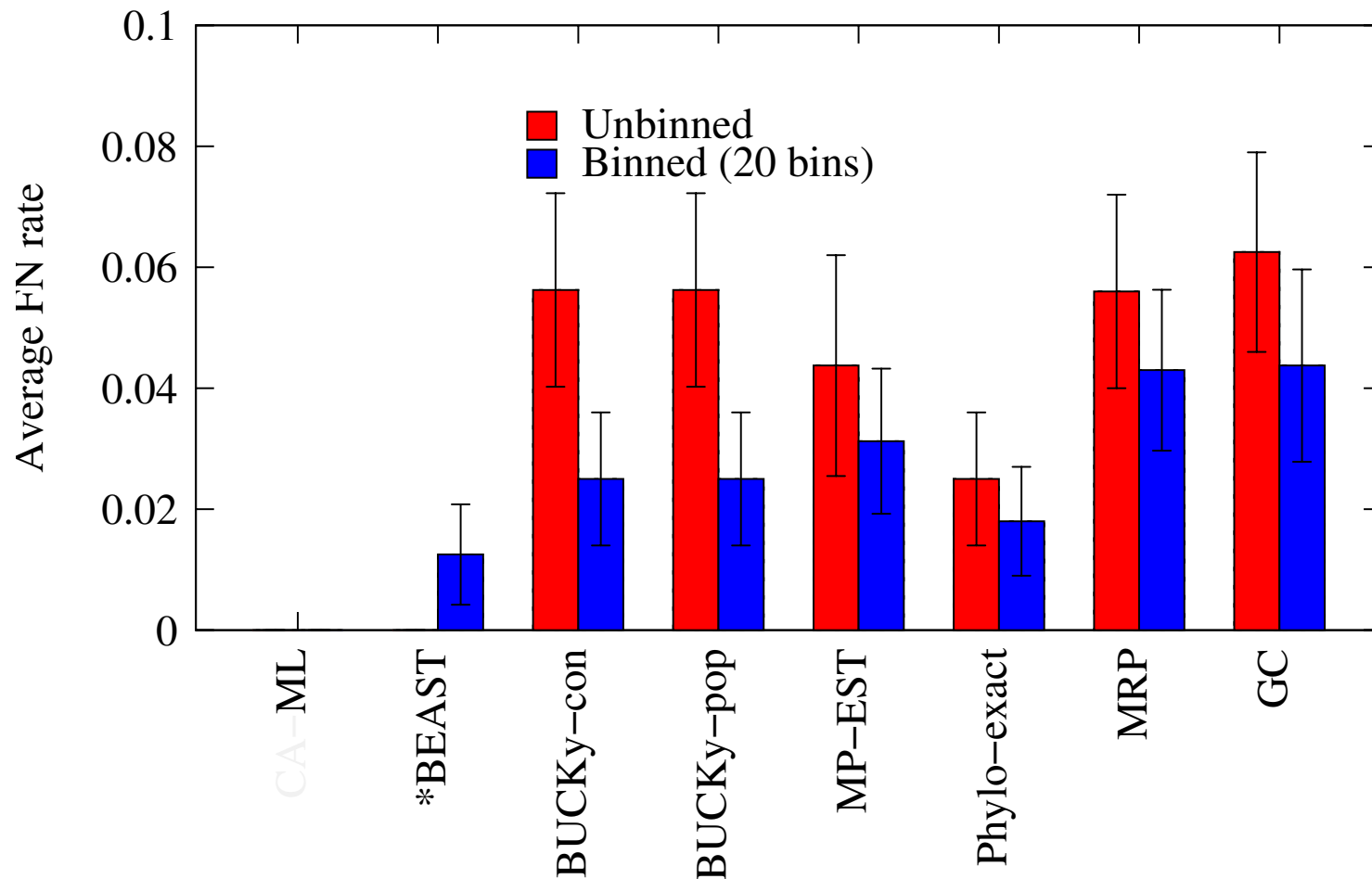
# Naïve binning vs. unbinned: 50 genes



Bayzid and Warnow, Bioinformatics 2013

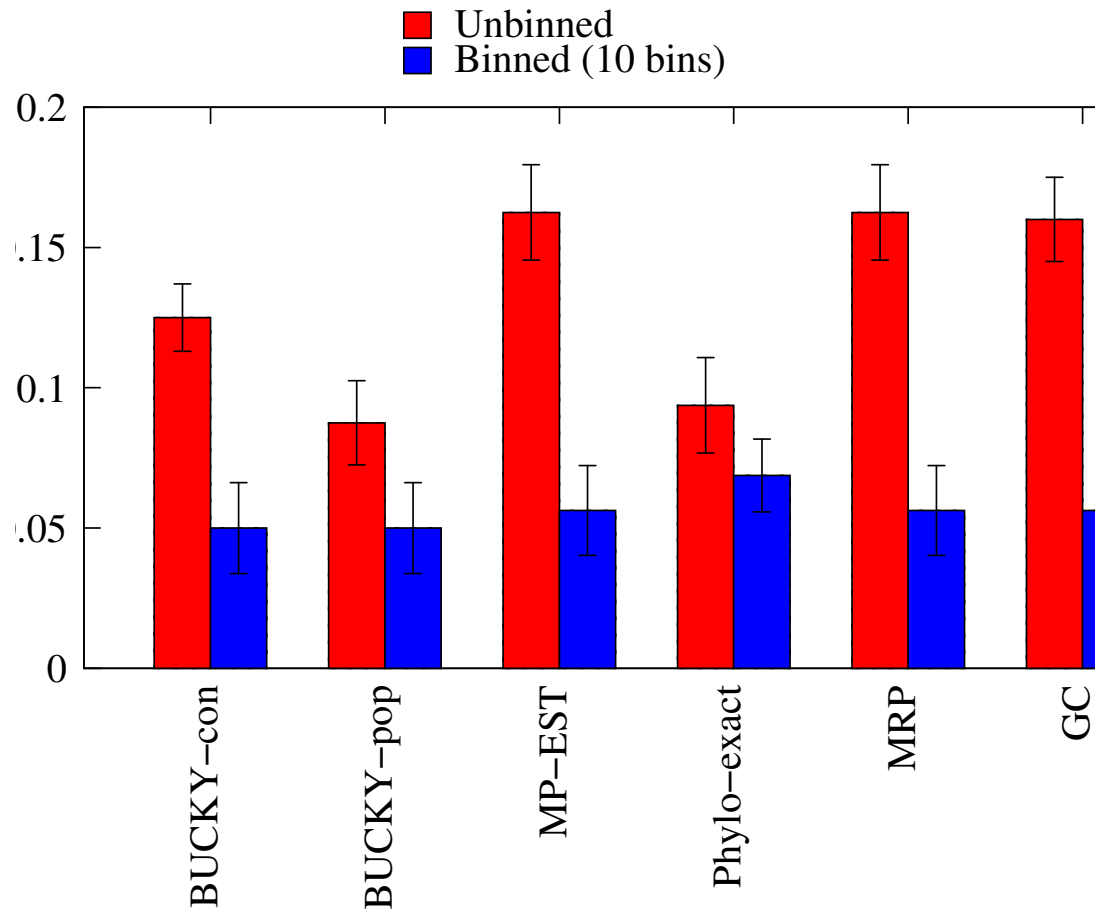
11-taxon strongILS datasets with 50 genes, 5 genes per bin

# Naïve binning vs. unbinned, 100 genes



\*BEAST did not converge on these datasets, even with 150 hours.  
With binning, it converged in 10 hours.

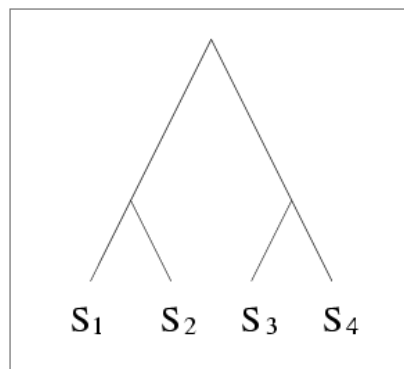
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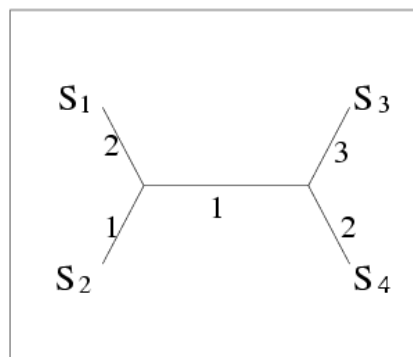


TRUE TREE

S<sub>1</sub> ACAATTAGAAC  
 S<sub>2</sub> ACCCTTAGAAC  
 S<sub>3</sub> ACCATTCCAAC  
 S<sub>4</sub> ACCAGACCAAC

DNA SEQUENCES

STATISTICAL  
ESTIMATION  
OF PAIRWISE  
DISTANCES



INFERRED TREE

METHODS  
SUCH AS  
NEIGHBOR  
JOINING

	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>
S <sub>1</sub>	0	3	6	5
S <sub>2</sub>		0	5	4
S <sub>3</sub>			0	5
S <sub>4</sub>				0

DISTANCE MATRIX

Neighbor Joining (and many other distance-based methods) are statistically consistent under Jukes-Cantor