3D ENGINES AND SCENE GRAPHS

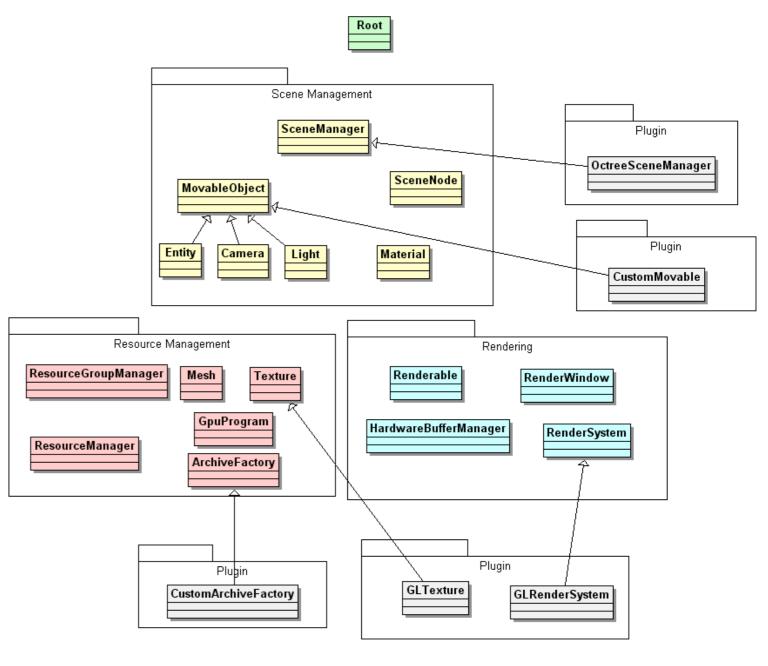
CS354R DR SARAH ABRAHAM

3D GRAPHICS ENGINES

What is a 3D graphics engine and what should it include?

3D ENGINES

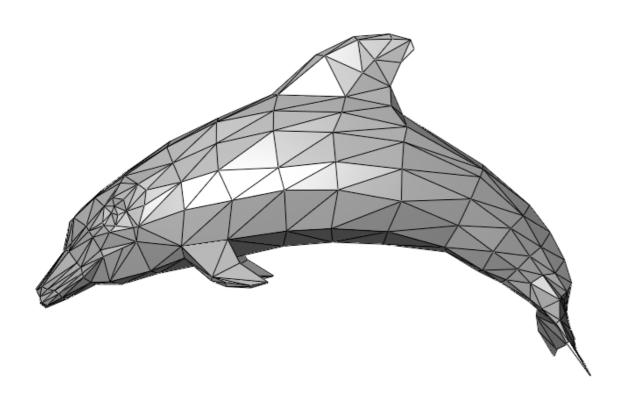
- Handles functionality related to graphics and rendering
- The "graphics" part of a game engine

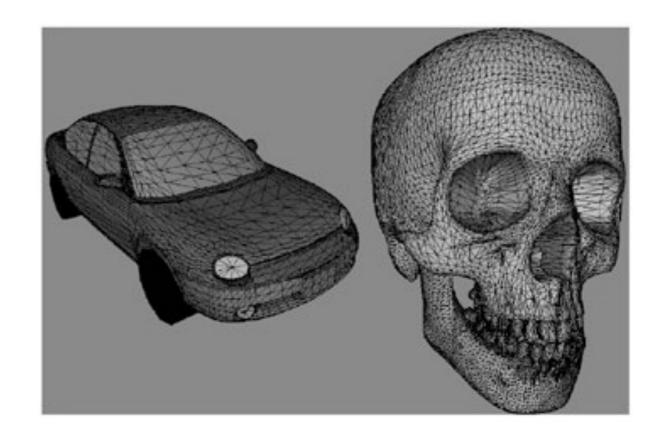


Ogre 1.9 Core class structure

WHAT ARE THE OBJECTS?

- Geometry polygon (triangle, quad) meshes
 - Vertices form edges
 - Edges form faces





OBJECTS OF INCREASING COMPLEXITY...



Monster Hunter World

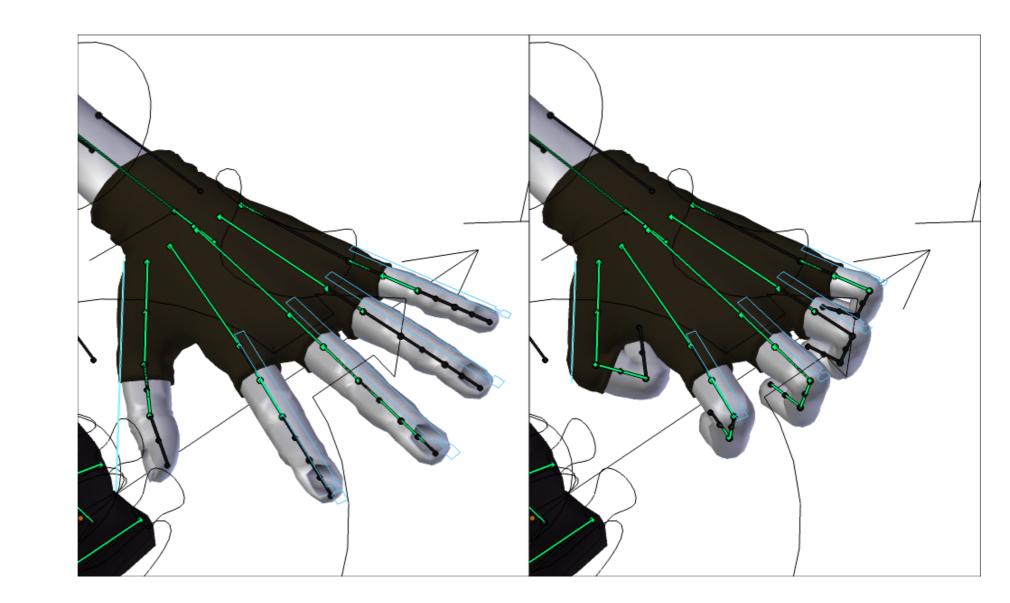
HIERARCHICAL MODELING

- Ways character can move:
 - Move the whole character wrt the world
 - Move legs, arms, head wrt body
 - Move hands wrt arms
 - Move upper vs. lower arm
 - Same for legs



THE HIGHER LEVEL (3D MODELED OBJECTS)

- Modeling
- Rigging
- Skinning
- Animating



Wikipedia (Skeletal Animation)

THE LOWER LEVEL (SYMBOLS AND INSTANCES)

- Most graphics APIs support a few geometric **primitives**:
 - Spheres
 - Cubes
 - Triangles
- These symbols are instanced using an instance transformation.

TRANSFORMATION REPRESENTATION

We can represent a 2D point, p = (x, y), in the plane as a column vector: $\begin{bmatrix} x \end{bmatrix}$

• We can represent a 2-D transformation M by a matrix:

 $\mathbf{M} = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$

If p is a column vector, M goes on the left:

 $\mathbf{p}' = \mathbf{M}\mathbf{p}$ $\begin{bmatrix} x'\\ y' \end{bmatrix} = \begin{bmatrix} a & b\\ c & d \end{bmatrix} \begin{bmatrix} x\\ y \end{bmatrix}$

2D TRANSFORMATIONS

Here's all you get with a 2x2 transformation matrix M:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

So:

$$x' = ax + by$$
$$y' = cx + dy$$

IDENTITY

- Suppose we choose a = d = 1, b = c = 0:

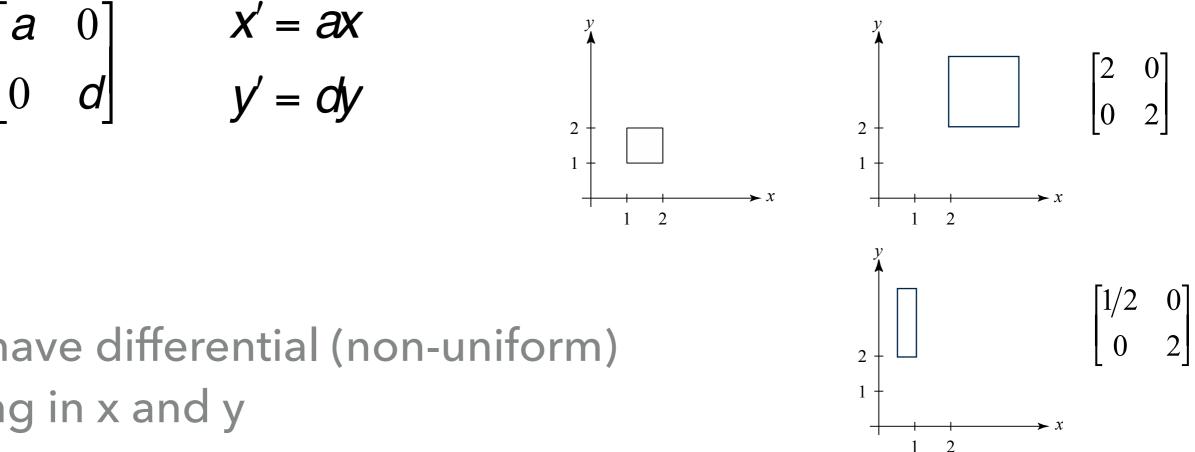
Doesn't move the point at all

SCALING

- Suppose b = c = 0, but let a and d take on any positive value
- Gives a scaling matrix:

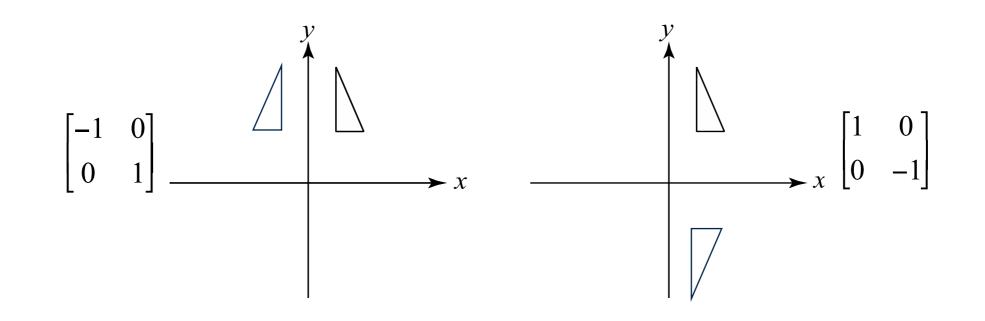
$$\begin{bmatrix} a & 0 \\ 0 & d \end{bmatrix} \qquad \begin{array}{l} \mathbf{X}' = \mathbf{A}\mathbf{X} \\ \mathbf{Y}' = \mathbf{A}\mathbf{Y} \end{array}$$

Can have differential (non-uniform) scaling in x and y



REFLECTION

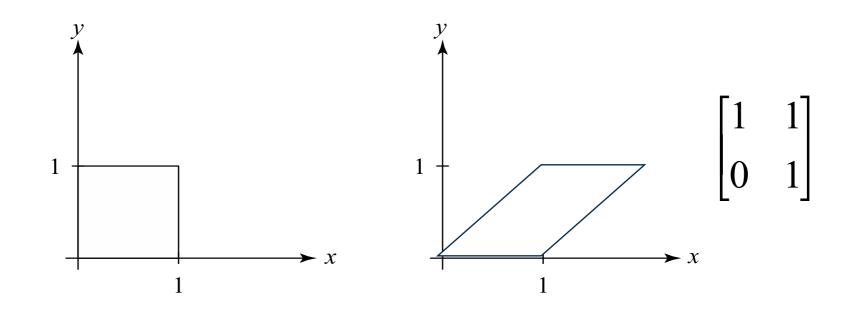
- Suppose b = c = 0, but either a or d goes negative
- Consider:



SHEAR

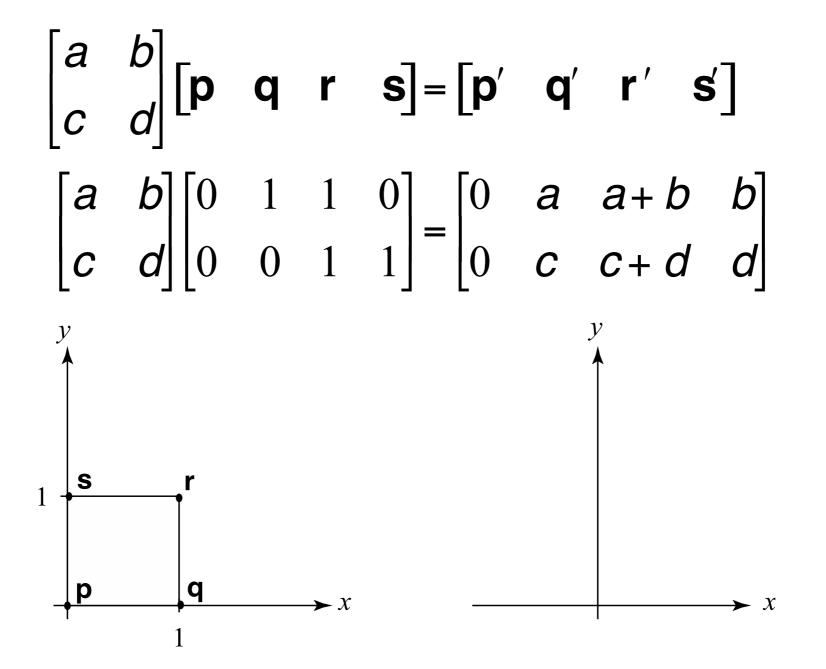
Now leave a = d = 1 and experiment with b $\begin{bmatrix} 1 & b \\ 0 & 1 \end{bmatrix} \qquad \begin{array}{l} x' = x + by \\ y' = y \end{array}$

Consider:



EFFECT ON UNIT SQUARE

A general 2 x 2 transformation M on the unit square:

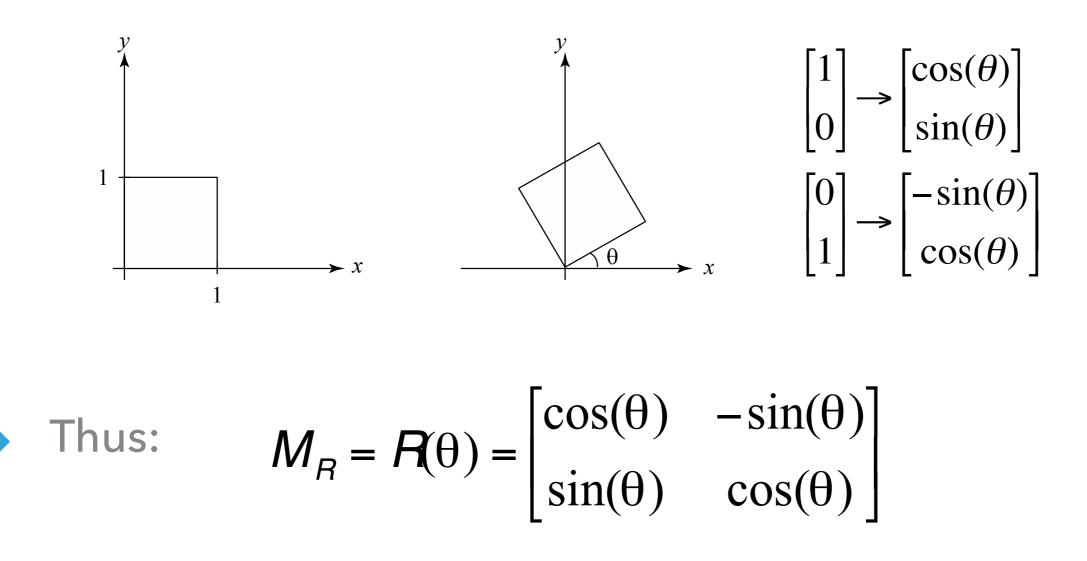


OBSERVATIONS

- Origin invariant under M
- M can be determined just by knowing how the corners (1,0) and (0,1) are mapped
- a and d give x- and y-scaling
- b and c give x- and y-shearing

ROTATION

From our observations of the effect on the unit square, the matrix for "rotation about the origin":



LINEAR TRANSFORMATIONS

The unit square observations suggest the 2x2 matrix transformation is representing a point in a new coordinate system:

$$\mathbf{b}' = \mathbf{M}\mathbf{p}$$
$$= \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$
$$= \begin{bmatrix} \mathbf{u} & \mathbf{v} \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$
$$= \mathbf{x} \cdot \mathbf{u} + \mathbf{v} \cdot \mathbf{v}$$

- where u = [a c]^T and v = [b d]^T are vectors that define a new basis for a linear space.
- The transformation to this new basis (a.k.a., change of basis) is a linear transformation.

LIMITATIONS OF THE 2X2 MATRIX

- A 2x2 linear transformation matrix allows:
 - Scaling
 - Rotation
 - Reflection
 - Shearing

What important operation does that leave out?

AFFINE TRANSFORMATIONS

- In order to incorporate the idea that both the basis and the origin can change, we augment the linear space u, v with an origin t.
- Note that while **u** and **v** are basis vectors, the origin **t** is a point.
- We call **u**, **v**, and **t** (basis and origin) a **frame** for an **affine space**.
- > Then, we can represent a change of frame as:

$$\mathbf{p}' = \mathbf{X} \cdot \mathbf{u} + \mathbf{y} \cdot \mathbf{v} + \mathbf{t}$$

> This change of frame is also known as an **affine transformation**.

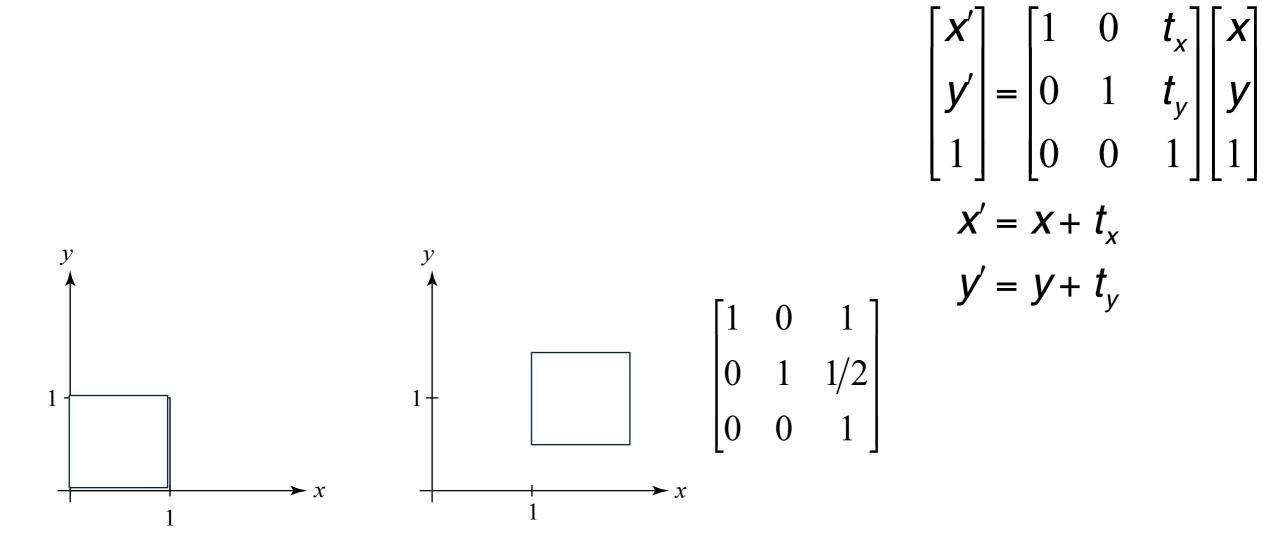
HOMOGENEOUS COORDINATES

- To represent transformations among affine frames, we can loft the problem up into 3-space, adding a third component to every point:
- Note that:
 - ► [a c 0]^T and [b d 0]^T represent vectors
 - $[t_x t_y 1]^T$, $[x y 1]^T$ and $[x' y' 1]^T$ represent points.

 $\mathbf{p}' = \mathbf{M}\mathbf{p}$ $= \begin{vmatrix} a & b & t_x \\ C & d & t_y \\ 0 & 0 & 1 \end{vmatrix} \begin{vmatrix} x \\ y \\ y \end{vmatrix}$ $= \begin{bmatrix} \mathbf{u} & \mathbf{v} & \mathbf{t} \end{bmatrix} \begin{vmatrix} y \end{vmatrix}$ $= \mathbf{X} \cdot \mathbf{U} + \mathbf{Y} \cdot \mathbf{V} + 1 \cdot \mathbf{t}$

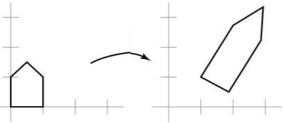
HOMOGENEOUS COORDINATES

This allows us to perform translation as well as the linear transformations as a matrix operation: $p' = M_T p$

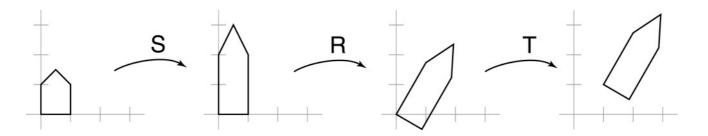


USE A SERIES OF TRANSFORMATIONS

• A particular geometric instance is transformed by one combined transformation matrix:



But it's convenient to build this single matrix from a series of simpler transformations:

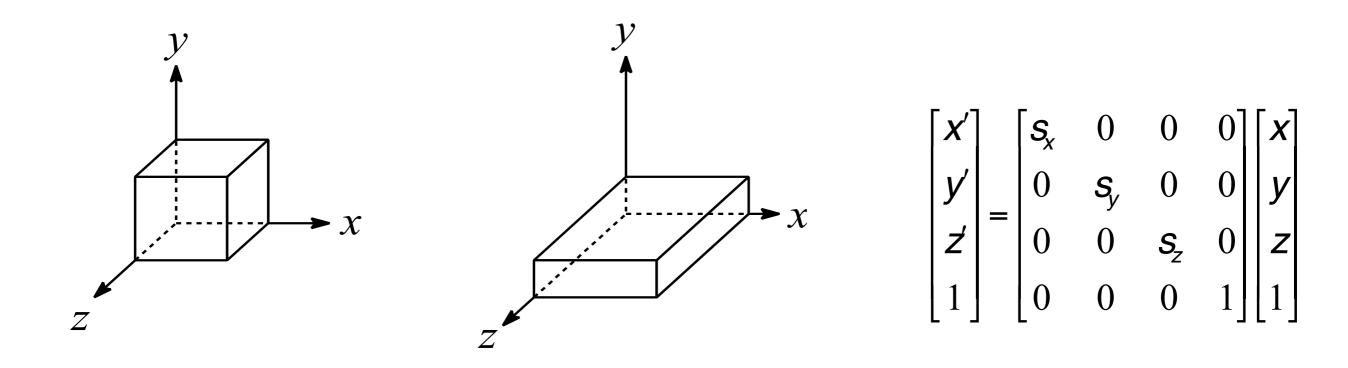


• We have to be careful about how we think about composing these transformations.

(Mathematical reason: Transformation matrices don't commute under matrix multiplication!)

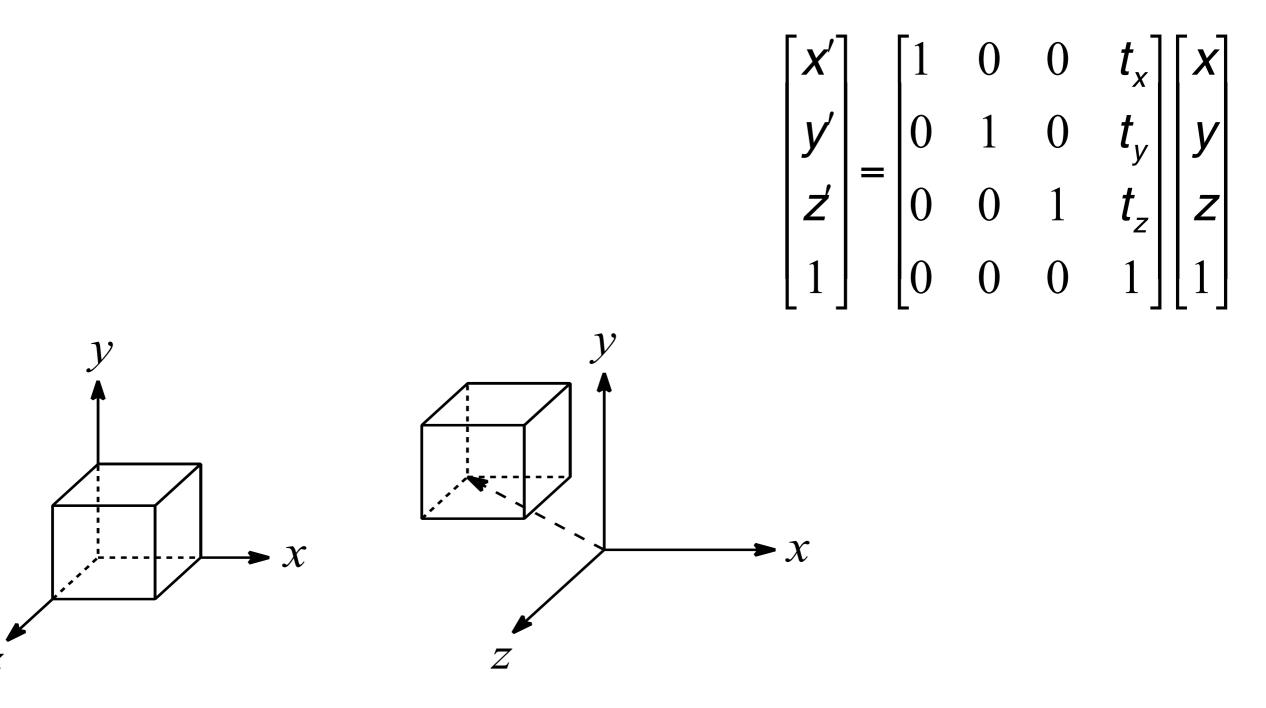
SCALING IN 3D

Some of the 3-D transformations are just like the 2-D ones.
For example, scaling:



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TRANSLATION IN 3D

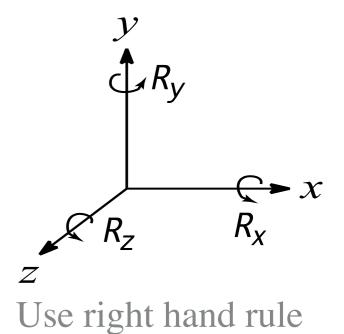


Z

ROTATION IN 3D

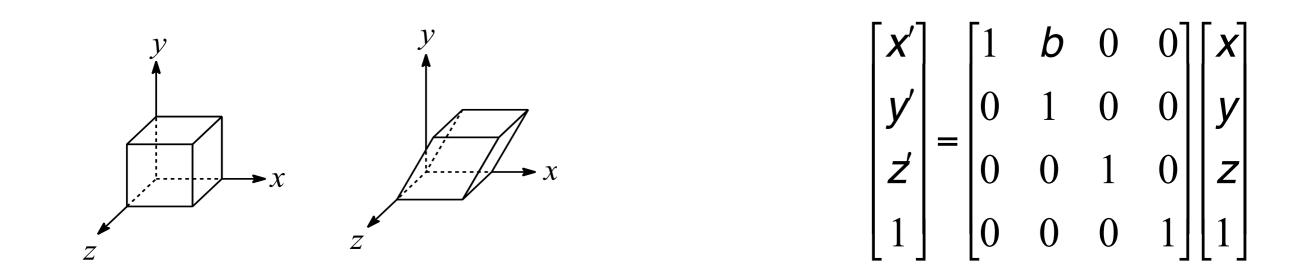
Rotation now has more possibilities in 3D:

$$R_{\chi}(\theta) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(\theta) & -\sin(\theta) & 0 \\ 0 & \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
$$R_{\chi}(\theta) = \begin{bmatrix} \cos(\theta) & 0 & \sin(\theta) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(\theta) & 0 & \cos(\theta) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
$$R_{z}(\theta) = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 & 0 \\ \sin(\theta) & \cos(\theta) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



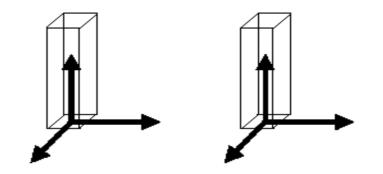
SHEARING IN 3D

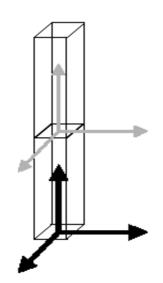
Shearing is also more complicated. Here is one example:

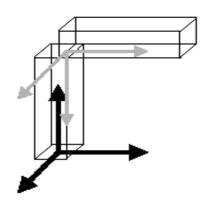


We call this a shear with respect to the x-z plane.

COMBINING TRANSFORMATIONS AND PRIMITIVES

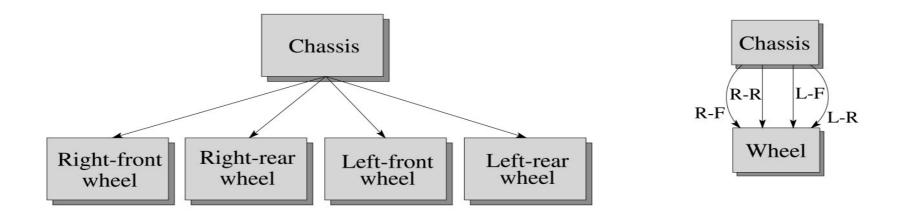






HIERARCHICAL MODELING

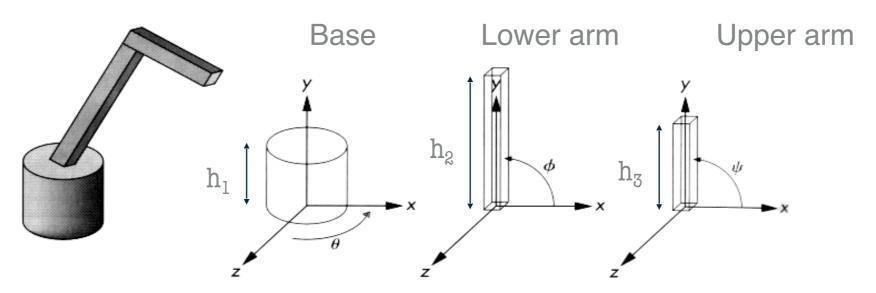
Hierarchical models can be composed of instances using trees or DAGs:



- Edges contain geometric transformations
- Nodes contain geometry (and possibly drawing attributes)

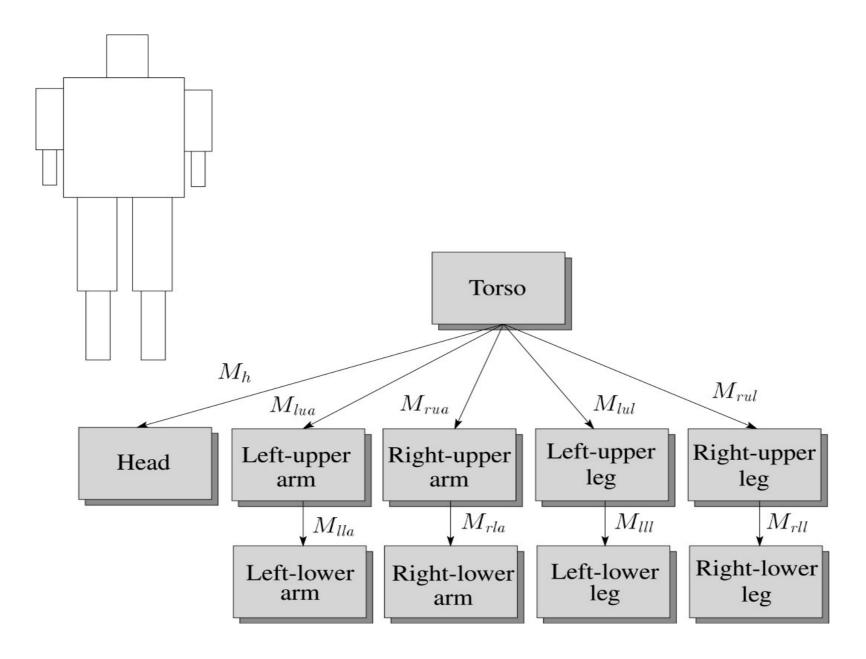
3D EXAMPLE: A ROBOT ARM

- Consider this robot arm with 3 degrees of freedom:
 - > Base rotates about its vertical axis by $\boldsymbol{\theta}$
 - Lower arm rotates in its xy-plane by φ
 - Upper arm rotates in its *xy*-plane by ψ
- How might we draw the tree for the robot arm?



A COMPLEX EXAMPLE: HUMAN FIGURE

What's the most sensible way to traverse this tree?



HUMAN FIGURE IMPLEMENTATION

torso();

glPushMatrix();

glTranslate(...);

glRotate(...);

head();

glPopMatrix();

glPushMatrix();

glTranslate(...);

glRotate(...);

left_upper_arm();

glPushMatrix();

glTranslate(...);

glRotate(...);

left_lower_arm();

glPopMatrix();

glPopMatrix();

Note: Fixed pipeline OpenGL is outdated but works well for illustrative purposes!

ON OUR WAY TO ANIMATING!



https://youtu.be/vOGhAV-84il?t=1m45s

SCENE GRAPHS

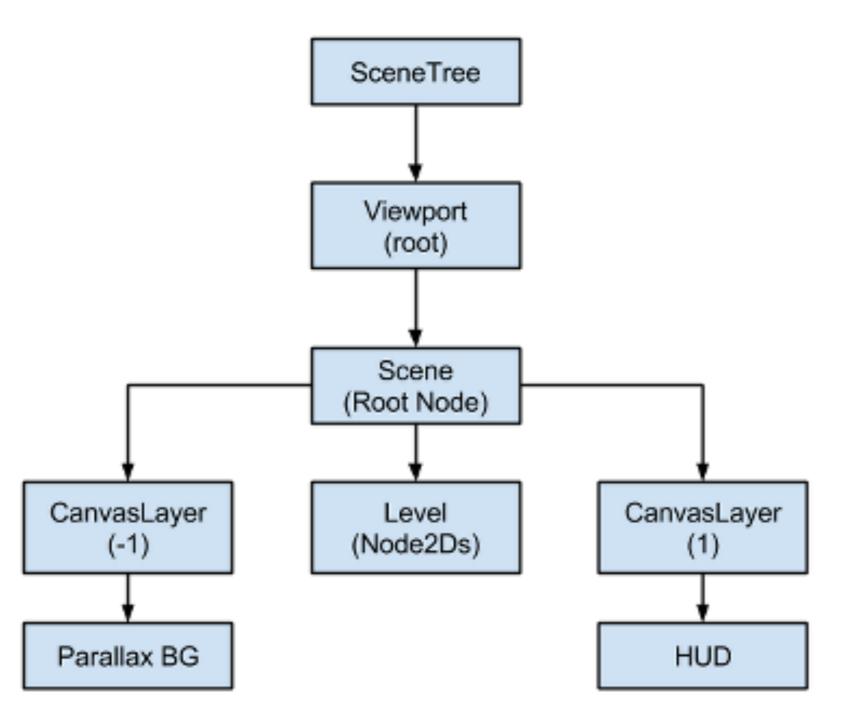
- The idea of hierarchical modeling can be extended to an entire scene, encompassing:

 Scene
- Multiple objects
 Lights
 Camera position
 This is called a scene tree or scene graph

SCENE GRAPHS IN GODOT

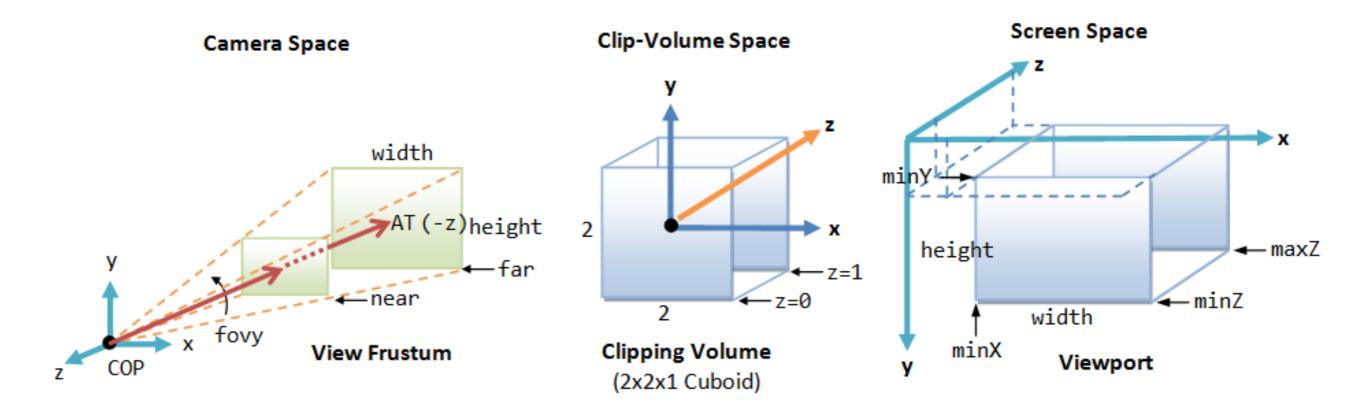
- Godot originally a 2D game engine
 - Added support for 3D in 3.0
- > 2D scene graphs built of CanvasItems
 - Control inherits for GUI items
 - Node2Ds used for 2D scene graphs
- 3D scene graphics built on top of Node3Ds
 - Transform property is 3x4 matrix
 - ▶ 3 Vector 3 properties for translate, rotate, and scale

2D SCENE GRAPH IN GODOT



VIEWPORTS

- Viewports are how scenes are rendered out to a screen
- Allows for easier rendering to multiple screen resolutions



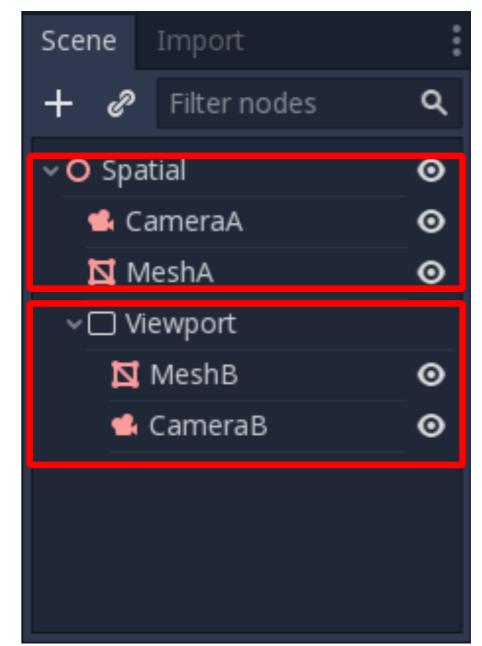
(https://www.ntu.edu.sg/home/ehchua/programming/opengl/CG_Examples.html)

VIEWPORTS IN GAMES

- Game utilize multiple viewports for:
 - Displaying multiple cameras
 - Rendering 2D elements in 3D scenes
 - Rendering to textures
 - etc
- Can add multiple viewports to the scene graphs in Godot
- Viewport Containers help set the outputted viewport size, and connect objects to display with its viewport

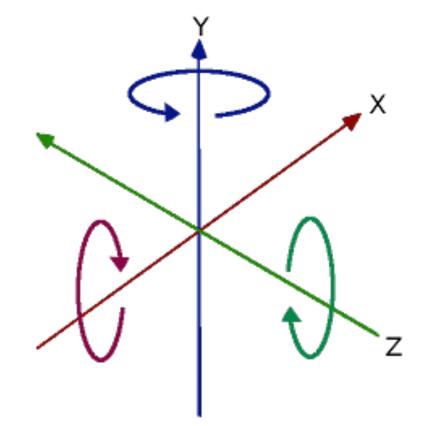
WHAT ABOUT CAMERAS?

- Cameras automatically display on closest parent viewport
 - Only one active camera per viewport
 - Viewport nodes only display objects that are their children
- Must instance the world scene to **both** viewports for displaying splitscreens/ overhead maps/etc



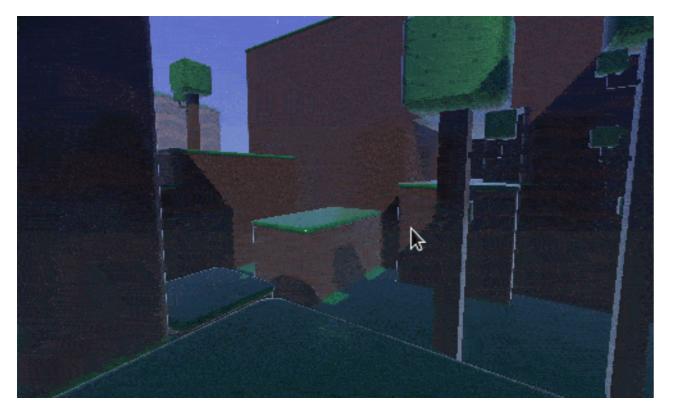
UNDERSTANDING ROTATION

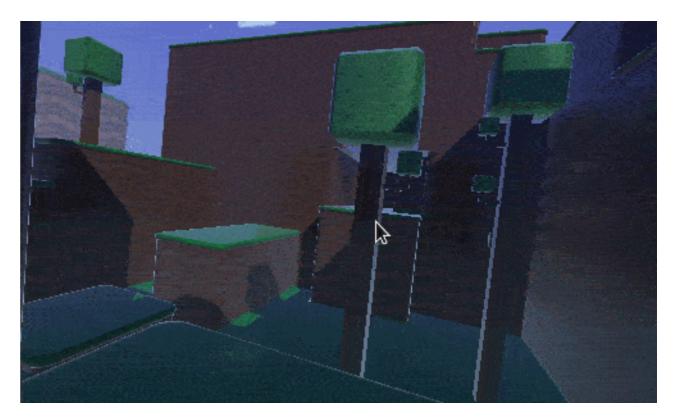
- Euler angles are a common way of representing orientation and rotation
 - Rotations about the x, y, and z axis can be composed to form any arbitrary rotation
 - Yaw (up-axis), pitch (side-axis), and roll (front-axis)
- If any orientation/rotation can be represented, why are Euler angles insufficient?



GIMBAL LOCK

- Gimbal Lock Explained:
 - https://www.youtube.com/watch?v=zc8b2Jo7mno



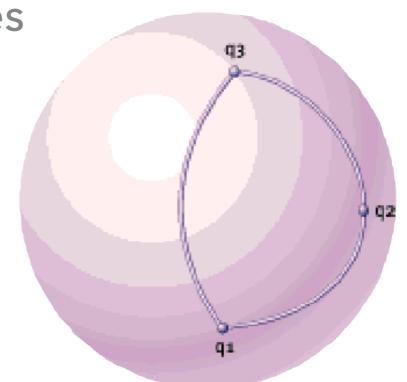


YX rotation

XY rotation

QUATERNIONS

- Mathematical notation for representing object orientation and rotation
- Complex planes rather than Cartesian planes
- Alternative to Euler angles and matrices
- No gimbal lock
- Simpler representation
- Finds closest path



Quaternion Rotation (Gamasutra)

NOTATION

Complex Number Notation:

$$q = w + xi + yj + zk$$

AD Vector Notation:

$$q = [w, v]$$
 where $v = (x, y, z)$

Rotate by angle *θ* about axis \hat{v} :

$$q = \left[\cos\frac{1}{2}\theta, \sin\frac{1}{2}\theta\hat{v} \right]$$

- Can apply Euler rotations using axis-angle notation above
 - Must apply rotations in correct order as quaternion multiplication is not commutative!

QUATERNION INTERPOLATION

- SLERP (Spherical Linear Interpolation)
 - Equation for LERP: $p_t = p_1 + (p_2 p_1)t$
 - Equation for SLERP: $q_t = \frac{sin((1-t)\theta)}{sin(\theta)}q_1 + \frac{sin(t\theta)}{sin(\theta)}q_2$
- SQAD (Spherical and Quadrangle)
 - Smoothly interpolate over a path of rotations (cubic)
 - Defines "helper" quaternion that acts as a control point
- Caveat: when the angular distance between p₁ and p₂ is small, sin(**θ**) approaches zero. Must switch back to LERP.

WORKING WITH ROTATIONS IN GAMES

- Often easier to think of rotations as Euler angles...
- But should convert to quaternions whenever applying rotations/ interpolations!
- One way to do this:
 - 1. Get current and target orientation values as Euler angles
 - 2. Convert Euler angles to quaternions
 - 3. Slerp between current and target quaternion
 - 4. Convert back to Euler angles
- Some overhead but your designers will thank you!

FURTHER READING ON QUATERNIONS

- Understanding Quaternions (Jeremiah van Oosten)
 - http://3dgep.com/understanding-quaternions/
- Rotating Objects Using Quaternions (Nick Bobic)
 - http://www.gamasutra.com/view/feature/131686/ rotating_objects_using_quaternions.php