

# Tutorial on Online Partial Evaluation

William R. Cook

Department of Computer Science, University of Texas at Austin, USA

Ralf Lämmel

Department of Computer Science, University of Koblenz-Landau, Germany

This paper is a short tutorial introduction to online partial evaluation. We show how to write a simple online partial evaluator for a simple, pure, first-order, functional programming language. In particular, we show that the partial evaluator can be derived as a variation on a compositionally defined interpreter. We demonstrate the use of the resulting partial evaluator for program optimization in the context of model-driven development.

## 1 Introduction

Partial evaluation is a powerful and general optimization technique [5]. It has applications in model-driven development, domain-specific language engineering [4], and generic programming [7]. The C++ template system can be understood as a form of partial evaluation [11]. However, partial evaluation has not been very widely adopted. It has a reputation as an esoteric and complex topic. The challenge, set forth by Futamura in the 1970s [2]—to create an automatic compiler-compiler by partial evaluation—has largely been abandoned; a failure that may taint the entire effort.

These notes introduce partial evaluation by converting an interpreter for a functional language into a simple partial evaluator for the language.<sup>1</sup> The conversion relies on a simple basic idea:

*Allow undefined variables during evaluation.*

*Preserve syntactical phrases if they cannot be evaluated completely.*

A regular interpreter maintains variable bindings in an *environment*. Normally, the environment is required to contain bindings for all variables mentioned in the program—an undefined variable is a fatal error. For example, the evaluation of the expression  $x^n$  only succeeds if both  $x$  and  $n$  are bound to values of types for which exponentiation is defined. Assuming bindings  $x = 2$  and  $n = 3$ , an interpreter evaluates  $x^n$  to 8, but it fails if either  $x$  or  $n$  are not bound.

What would it mean to evaluate  $x^n$  given a *partial* environment that only includes  $n = 3$ ? The result cannot be a number, because the value of  $x$  is not known. If we assume that the value of  $x$  will be known later, then the result can be a new program  $x^3$ . This is called *residual* code, because it is the code that is left over after evaluating parts of the expression. Note that the variable  $n$  does not occur in the residual code. It has been eliminated from the program.

Thus, one way to understand partial evaluation is this: enhance regular evaluation to synthesize residual code when encountering unbound variables in the partial environment. Partial evaluation becomes more complicated when it deals with all the different kinds of expressions that can occur in a program. Consider the following expression:

```
if x>y then (10+y)/x else y
```

---

<sup>1</sup>A code distribution is available from the paper's website: <http://softlang.uni-koblenz.de/ds111>

```

type Prog = ([FDef], Expr)

type FDef = (String, ([String], Expr))

data Val
  = IVal { getInt :: Int }
  | BVal { getBool :: Bool }

data Expr
  = Const { getVal :: Val }
  | Var String
  | Apply String [Expr]
  | Prim Op [Expr]
  | If Expr Expr Expr

data Op = Equal | Add | Sub | Mul

```

Figure 1: Syntax of a simple functional programming language

What does it mean to partially evaluate the given expression in an environment that specifies  $y = 0$  and with no binding for  $x$ ? The result is the residual code `if x>0 then 10/x else 0`. In this case, both branches of the conditional must be partially evaluated, if  $y$  is to be eliminated. This is not the normal evaluation rule for conditionals. As a result, partial evaluation may diverge where regular evaluation would terminate—unless extra effort is made. Also, great care must be taken in the presence of side effects. Consider again the expression given earlier for a partial environment such that  $x = 0$  and with no binding for  $y$ . Partial evaluation is supposed to result in the residual code `if 0>y then error else y`. Note that the division-by-zero error must not be raised during partial evaluation, but it must be delayed so that it is executed at the right point in the residual code—if it is ever exercised. Function calls and recursive definitions also cause complications, which are discussed in the tutorial.

The style of partial evaluator developed here is called an *online* partial evaluator, because it makes decisions about specialization as it goes, based on whatever variables are in the environment at a given point during evaluation [5]. An *offline* partial evaluator performs a static analysis of the program to decide which variables will be considered known and which will be considered unknown. It has been claimed that offline partial evaluation is simpler than online partial evaluation [10]. It can be more difficult to ensure termination in an online setting. In this tutorial, we avoid issues of termination, so this complexity does not arise [9]. Given this restriction, we believe that the online style is simpler to describe, because the partial evaluator can be derived easily from an existing interpreter.

## 2 A Simple Language and Evaluator

Fig. 1 lists the abstract syntax for a simple, pure, first-order, functional programming language. A program consists of a list of function definitions (see type `FDef`) and a main expression. A function definition is tuple of the form  $(f, ([a_1, \dots, a_n], b))$  where  $f$  is the function name,  $a_i$  are formal parameter names, and  $b$  is the body expression of the function. There are the following expression forms: a constant (of type `Val`), a variable, a function application, the application of a primitive operator, and a conditional expression. Evaluation of an expression is supposed to return a value, but it may fail in reply to a dynamic

type error; it may also diverge. Functions are first-order: functions are neither passed as arguments, nor returned as results.

As an example, consider the following exponentiation function written in Haskell:

```
exp(x, n) = if n == 0 then 1 else x * exp(x, n - 1)
```

This function can be encoded in our simple language as follows:

```
exp = (
  "exp", ([ "x", "n" ],
    If (Prim Equal [Var "n", Const (IVal 0)])
      (Const (IVal 1))
      (Prim Mul
        [Var "x",
         Apply "exp" [Var "x", Prim Sub [Var "n", Const (IVal 1)]]]))))
```

The interpreter is a function `eval` that takes a program (i.e., a list of function definitions and a main expression) and returns a value (i.e., a Boolean or an int), or it fails, or it diverges. For instance:

```
> eval ([exp], Apply "exp" [Const (IVal 2), Const (IVal 3)])
8
```

Fig. 2 gives the complete interpreter. The main evaluation function `eval` binds the argument `fdefs` to the list of functions and it invokes the expression-level evaluation function `eval'` on the main expression. Since `eval'` is defined in the scope of `eval`, the function list `fdefs` does not need to be passed on every recursive call. The helper function does take an *environment* `env` that maps variables to values. The environment is initialized to the empty list.

It must be emphasized that this interpreter is in no way special, unusual, or targeted at partial evaluation. One gets this interpreter naturally when using big-step style of operational semantics or direct style of denotational semantics (i.e., compositional, functional semantics) as the guiding principle.

### 3 A Naive Partial Evaluator

Let us start the conversion of the interpreter into a partial evaluator. The partial evaluator should produce the same result as the interpreter when given a complete environment, but it should compute a residual expression when given a partial environment. Let us think of the residual expression as the “rest of the program” that needs to be evaluated once the remaining variables are bound to values. For instance:

```
> peval ([exp], Apply "exp" [Var "x", Const (IVal 3)])

Prim Mul [Var "x",
          Prim Mul [Var "x",
                    Prim Mul [Var "x", Const (IVal 1)]]]
```

Thus, the function `exp` is applied to a specific exponent 3, but the base remains a variable `x`, and the result of partial evaluation represents the expression to compute  $x^3 = x * x * x * 1$ . The partial evaluator derived that expression by applying (unfolding) the recursive definition of `exp` for exponents 3, 2, 1, and 0.

We develop a partial evaluator in two steps. The intermediate version is very simple, but also limited. In fact, it is essentially a systematic inlining transformation. We start from the insight that the type of the top-level function must be changed so that expressions are returned instead of values. Please note that values are trivially embedded into expressions through the constant form of expressions. Thus:

```

type Env = [(String, Val)]

eval :: Prog -> Val
eval (fdefs, main) = eval' main []

where

eval' :: Expr -> Env -> Val

eval' (Const v) env = v

eval' (Var s) env =
  case lookup s env of
    Just v -> v
    Nothing -> error "undefined variable"

eval' (Prim op es) env =
  let rs = [ eval' e env | e <- es ] in
  prim op rs

eval' (If e0 e1 e2) env =
  if getBool (eval' e0 env)
  then eval' e1 env
  else eval' e2 env

eval' (Apply f es) env =
  eval' body env'
  where
    (ss, body) = fromJust (lookup f fdefs)
    env' = zip ss [ eval' e env | e <- es ]

prim Equal [IVal i1, IVal i2] = BVal (i1 == i2)
prim Add [IVal i1, IVal i2] = IVal (i1 + i2)
prim Sub [IVal i1, IVal i2] = IVal (i1 - i2)
prim Mul [IVal i1, IVal i2] = IVal (i1 * i2)

```

Figure 2: An evaluator for Fig. 1

```

-- Interpreter
eval :: Prog -> Val

-- Partial evaluator
peval :: Prog -> Expr

```

Also, our initial, naive development uses the idea that function applications should always be inlined, and hence, we need to be able to apply functions to results of partial evaluation, i.e., to expressions rather than values. Accordingly, the type of environments changes as follows:

```

-- Interpreter
type Env = [(String, Val)]

-- Naive, inlining-oriented partial evaluator
type Env = [(String, Expr)]

```

Fig. 3 gives the complete, naive partial evaluator. Function `peval` generalizes `eval` as follows:

- A *constant* is partially evaluated to itself (just like in the interpreter).
- A *variable* is partially evaluated to the value (constant) according to the variable's binding in the environment (just like in the interpreter), if there is a binding. Otherwise, the variable is partially evaluated to itself. (The interpreter failed in this case.)
- A *primitive* operation is applied to the (partially) evaluated arguments (just like in the interpreter), if these are all values (constants). Otherwise, a primitive operation form of expression is reconstructed from the partially evaluated arguments.
- A *conditional* can be eliminated such that one of the two branches is chosen for recursive (partial) evaluation (just like in the interpreter), if the condition is (partially) evaluated to a value (constant). Otherwise, both branches are partially evaluated, and the conditional is reconstructed.
- A *function application* is partially evaluated just like in the interpreter—modulo the changed environment type. (Alpha renaming should be applied to avoid any name confusion but this is omitted here for brevity.)

The treatment of conditionals and function applications is naive. For example, partial evaluation of a function application may diverge when compared to regular evaluation. Thus:

```
> peval ([exp], Apply "exp" [Const (IVal 2), Var "n"])
```

```

-- Result shown in regular Haskell notation for clarity
if n == 0
  then 1
  else 2 * (if n-1 == 0
            then 1
            else 2 * (if (n-1)-1 == 0 ...))

```

In this example, the function `exp` is applied to a specific base 2, but the exponent remains a variable `n`. Inlining diverges because the recursive case of `exp` is continuously exercised for different argument expressions for the exponent.

```

type Env = [(String, Expr)]

peval :: Prog -> Expr
peval (fdefs, main) = peval' main []

where

peval' :: Expr -> Env -> Expr

peval' (Const v) env = Const v

peval' (Var s) env =
  case lookup s env of
    Just e -> e
    Nothing -> Var s -- return code for variable

peval' (Prim op es) env =
  let rs = [ peval' e env | e <- es ] in
  if all isVal rs
  then Const (prim op (map getVal rs))
  else Prim op rs -- return code for primitive

peval' (If e0 e1 e2) env =
  let r0 = peval' e0 env in
  if isVal r0
  then if getBool (getVal r0)
    then peval' e1 env
    else peval' e2 env
  else (If r0
    (peval' e1 env)
    (peval' e2 env)) -- return code for if

peval' (Apply f es) env =
  peval' body env'
where
  (ss, body) = fromJust (lookup f fdefs)
  env' = zip ss [ peval' e env | e <- es ]

```

Figure 3: The naive partial evaluator

## 4 Proper Program Specialization

Proper treatment of recursive functions requires from us to synthesize *residual programs* instead of just residual expressions based on naive inlining. Hence, our more advanced partial evaluator uses the following type:

```
peval :: Prog -> Prog
```

Also, we return to the original definition of Env, which binds variables to values rather than expressions. The idea is here that the incoming function definitions and the main expression are specialized such that the resulting main expression only refers to specialized function definitions. The same original function definition may be specialized several times depending on the encountered, statically known argument values. For instance:

```
> peval ([exp], Apply "exp" [Var "x", Const (IVal 3)])

([ ("exp'a", ([ "x",
                Prim Mul [Var "x", Apply "exp'b" [Var "x"]]),
                ("exp'b", ([ "x",
                            Prim Mul [Var "x", Apply "exp'c" [Var "x"]]),
                            ("exp'c", ([ "x",
                                        Prim Mul [Var "x", Apply "exp'd" [Var "x"]]),
                                        ("exp'd", ([ "x",
                                                    Const (IVal 1)]))
                            ],
                Apply "exp'a" [Var "x"]
            ])
```

The names of the specialized functions are fabricated from the original name by some qualification scheme. For clarity, the list of function definitions are also shown in plain Haskell:

```
exp'a x = x * exp'b x
exp'b x = x * exp'c x
exp'c x = x * exp'd x
exp'd x = 1
```

Thus, specialized function definitions were inferred for all the inductively encountered values 3, 2, 1, and 0 for the exponent. Thus, subject to a simple inlining optimization, which is not shown here for brevity, we obtain the familiar expression for  $x$  to the power 3.

Let us apply the more advanced, partial evaluator to the diverging example that we faced at the end of the previous section. Function specialization carefully tracks argument lists for which specialization is under way or has been completed. This solves the termination problem.

```
> peval ([exp], Apply "exp" [Const (IVal 2), Var "n"])

(["exp'", ([ "n",
              If (Prim Equal [Var "n", Const (IVal 0)])
                (Const (IVal 1))
                (Prim Mul
                 [Const (IVal 2),
                  Apply "exp'" [Prim Sub [Var "n", Const (IVal 1)]]])
              ],
            Apply "exp'" [Var "n"]
          ])
```

```

type Env = [(String, Val)]

peval :: Prog -> Prog
peval (fdefs, main) = swap (runState (peval' main []) [])

where

peval' :: Expr -> Env -> State [FDef] Expr

peval' (Const v) env = return (Const v)

peval' (Var s) env =
  case lookup s env of
    Just v -> return (Const v)
    Nothing -> return (Var s)

peval' (Prim op es) env = do
  rs <- mapM (flip peval' env) es
  if all isVal rs
  then return (Const (prim op (map getVal rs)))
  else return (Prim op rs)

peval' (If e0 e1 e2) env = do
  r0 <- peval' e0 env
  if isVal r0 then
    if getBool (getVal r0)
    then peval' e1 env
    else peval' e2 env
  else do
    r1 <- peval' e1 env
    r2 <- peval' e2 env
    return (If r0 r1 r2)

```

Figure 4: Monadic partial evaluation

Thus, the original definition of `exp` was specialized such that the argument position for the statically known base is eliminated. Please note that the specialized function is recursive.

The partial evaluator needs to aggregate specialized functions along with recursion into expressions. To this end, we use the state monad in the type of the expression-level function `peval'`. Thus:

```

-- Naive inlining transformation
peval' :: Expr -> Env -> Expr

-- Proper program specialization
peval' :: Expr -> Env -> State [FDef] Expr

```

The cases for all constructs but function application can be adopted from the simpler partial evaluator—except that we need to convert to monadic style, which is a simple, systematic program transformation in itself [6, 1]. See Fig. 4 for the result. That is, recursive calls to `peval'` are not used directly in

reconstructing terms, but their results are bound in the state monad.

It remains to define the case for partial evaluation of function application. We provide an informal specification for this case; please refer to Fig. 5 for the actual implementation:

1. The applied function is looked up and the arguments are evaluated—just like in the interpreter.
2. The partially evaluated arguments are partitioned into static and dynamic ones. Static arguments are values (constants); dynamic arguments leverage other expression forms.
3. The “identity” (the name) of the specialized function derives from the applied function and the static arguments. Here, we assume that values can be compared for equality. This is essential for remembering (say, memoizing) previous function specializations.
4. The body of the specialized function is obtained by partially evaluating the original body in the variable environment of the static variables. The argument list of the specialized function only includes variables for the dynamic positions.
5. The specialized function is ultimately applied to the dynamic arguments. The expression for that application serves as the result of partial evaluation.

Close inspection of Fig. 5 reveals additional details. For the special case of an application with static arguments only (see `if null das then ...`), we switch to the behavior of the interpreter by (partially) evaluating the body of the applied function. Also, in order to deal with recursion, it is important that the specialized function is already added to the state before its body is obtained. To this end, an undefined body is initially registered as a placeholder to be updated later.

## 5 Applications of Partial Evaluation

The exponentiation function is used frequently in discussing partial evaluation. Such simple examples are useful, because they illustrate the basic ideas with as little complication as possible. However, there is not much benefit in partially evaluating simple numeric functions, like exponentiation. Thus the potential benefits of the approach are not highlighted.

One promising application area for partial evaluation is in model-driven development. A *model* is a description of some desired behavior. While it is common practice to *translate* models into code that generates the desired behavior, we consider another approach. A *model interpreter* takes the model as an input and performs the behaviors specified in the model. Using partial evaluation, we can specialize a model interpreter to create a compiled version of a model [2]. To illustrate this technique, we show how to partially evaluate a state machine interpreter written in our simple language. In what follows, we use Haskell code to represent the interpreter, although it can be easily translated into our simple language for interpretation and partial evaluation.

Fig. 6 defines a type for representing state machines, and gives a simple state machine with two states. (We assume deterministic finite automata here.) A state machine is encoded using two Haskell data types for the accept states and the transition table. The double circle on state 2 indicates that it is the accept state.

Fig. 7 gives a Haskell version of a simple interpreter for state machines. The interpreter takes the current state, the accept states, the transition table, and a sequence of input labels. It returns true if the machine consumes all input and ends in an accept state.

To translate the interpreter into our simple language, additional data structures and primitive operators must be added to the language, to represent pairs and lists as well as maybes. These changes are left as an exercise for the reader. The lookup and `elem` function must also be written.

```

peval' (Apply s es) env = do
  -- Look up function.
  let (ss, body) = fromJust (lookup s fdefs)

  -- Partially evaluate arguments.
  rs <- mapM (flip peval' env) es

  -- Determine static and dynamic arguments.
  let z = zip ss rs
      sas = [ (s, getVal r) | (s, r) <- z, isVal r ]
      das = [ (s,v) | (s,v) <- z, not (isVal v) ]

  if null das then

    -- Inline completely static applications.
    peval' body sas

    -- Otherwise these applications make their contexts dynamic.
  else do

    -- Fabricate name from static variables.
    let s' = s ++ show (hashString (show sas))

    -- Specialize each "name" just once.
    fdefs <- get
    when (isNothing (lookup s' fdefs)) (do

      -- Create placeholder for memoization.
      put (fdefs ++ [(s', undefined)])

      -- Partially evaluate function body.
      e' <- peval' body sas

      -- Replace placeholder by actual definition.
      modify (update (const (map fst das, e')) s'))

    -- Return application of specialized function.
    return (Apply s' (map snd das))

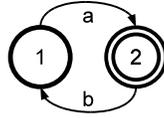
```

Figure 5: Partial evaluation of function application

```

type State = Int
type Label = Char
type Transitions = [(State, [(Label, State)])]
type Accept = [State]

```



```

transitions = [(1, [( 'a', 2)]),
               (2, [( 'b', 1)])]
accept = [2]

```

Figure 6: Types for state machines and example

```

run :: State -> Accept -> Transitions -> [Label] -> Bool
run current accept transitions [] = current `elem` accept
run current accept transitions (l:ls) =
  case lookup l (fromJust (lookup current transitions)) of
    Nothing -> False
    Just next -> run next accept transitions ls

```

Figure 7: Haskell interpreter for state machines

```

run1 ls = if null ls
  then False
  else if head ls == 'a'
    then run2 (tail ls)
    else False

run2 ls = if null ls
  then True
  else if head ls == 'b'
    then run1 (tail ls)
    else False

```

Figure 8: Desired output from partial evaluation

The desired result from partially evaluating the state machine interpreter on the state machine in Fig. 6 is given in Fig. 8. The accept states and the transition table are no longer present as data structures—thereby promising an aggressive optimization. However, when our partial evaluator is applied to the program in Fig. 6 (appropriately encoded in our simple language), specialization fails to eliminate the data structures for accept states and transition table. The problem is this expression:

```
lookup current transitions
```

```

run :: State -> Accept -> Transitions -> [Label] -> Bool
run s accept transitions ls =
  if null ls
  then s 'elem' accept
  else runNext (lookup s transitions) accept transitions ls

runNext s accept transitions ls =
  if null s
  then False
  else if (head ls) == fst (head s)
    then run (snd (head s)) accept transitions (tail ls)
    else runNext (tail s) accept transitions ls

```

Figure 9: State machine interpreter with binding time improvements

In this call, the current variable is *dynamic* during partial evaluation, although `transitions` is static. Given a dynamic input, the result of `lookup current transitions` is always dynamic (that is, unknown) even though the result is a list of transitions which is static information in the program. Thus, partial evaluation stops prematurely.

This is a well-known problem in partial evaluation: when static and dynamic information are tangled together, the static information is lost and partial evaluation stops. In such cases, it is necessary to rewrite the program so that it works better with the partial evaluator. Such rewrites are known as “binding time improvements” [5]. There is a huge body of work on this problem, but our example provides a simple illustration. The improvement pattern we need can be described with the following pseudo code. Our current program works by looking up the dynamic key in a static table, then processing the result:

```

let v = lookup table key in
  process v

```

Instead, we must iterate over the static table, and compare its keys to the dynamic key, and then process the value, if it matches:

```

for (k,v) in table do
  if k == key then
    process v

```

A partial evaluator can unroll this loop such that `v` is static in the call `process v` and partial evaluation will continue. In our functional language, we do not use any loop construct, but we use recursion instead. Fig. 9 gives a rewritten version of the state machine interpreter with the binding time improvement. This version is also more directly translatable to our simple language, because it does not use pattern matching.

## 6 Further Reading

These tutorial notes are only a quick introduction to the idea of partial evaluation. There are many sources for further reading. We recommend Jones, Gomard and Sestoft’s book on partial evaluation [5] and John Hatcliff’s detailed course material [3] as a good place to start. Both are available online.

## 7 Conclusion

This introduction merely hints at a number of important questions and issues. For example, our partial evaluator does not always terminate. Ensuring termination is a complex problem, but it is also possible to leave it to the programmer to avoid termination problems. Controlling partial evaluation is an important area of research [8]. A partial evaluator can fail to specialize desired parts of a program (as illustrated in the last section), or it can generate huge amounts of code without any practical benefit. Is it possible to automatically refactor programs so that programs will work better with partial evaluation? Dealing with imperative effects (e.g., mutable variables and input/output) is also a significant problem. We hope that this tutorial will encourage more researchers to investigate and apply partial evaluation in their work.

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